



A Practical Guide for Pricing Equity Swap



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Summary

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- The Use of Equity Swap
- Valuation
- Practical Guide
- A Real World Example



Equity Swap

Equity Swap Introduction

- *An equity swap is an OTC contract between two parties to exchange a set of cash flows in the future. Normally one party pays the return based on capital gains and dividends realized on an equity security and the other party pays the return based on a floating interest rate plus a spread.*
- *The party receiving the equity returns gains exposure to the performance of the reference equity without actually owning the equity; hence this instrument can be used to obtain a leveraged exposure.*
- *On the other hand, the party receiving payments based on the reference rate receives protection against a loss in the value of the underlying equity.*
- *Unlike other swap types, the equity swap notional resets on each cash flow reset date, depending on the performance of the underlying asset.*



Equity Swap

The Use of Equity Swap

- Equity swaps allow parties to potentially benefit from returns of an equity security without the need to own its shares.
- A party enters an equity swap with the objective of either obtaining return exposure or hedge existing equity risk for a period of time.
- An equity swap can be used to transfer both the credit risk and the market risk of an underlying asset.
- Equity swaps can be also used to avoid transaction costs (including Tax), to avoid locally based dividend taxes, limitations on leverage (notably the US margin regime) or to get around rules governing the particular type of investment that an institution can hold.
- Equity swaps can make investment barriers vanish and help an investor create leverage.



Equity Swap

Valuation

- There are two legs in an equity swap: an equity leg and a floating interest leg.
- The payoff for both legs could be set at every reset date or at maturity; or could be one side at maturity and the other at every reset date.
- The price of the swap is the difference between the present values of both legs' cash flows. In other words, the present value of swap is net of present value of "equity leg" and "money market leg".



Equity Swap

Valuation (Cont)

- The present value of the equity leg is given by

$$PV_{equity}(t) = N \sum_{i=1}^n \left[\frac{S_i - S_{i-1}}{S_{i-1}} \right] D_i$$

where

t – the valuation date

N – the notational principal amount

i – the i^{th} cash flow from 1 to n

$D_i = D(t, T_i)$ – the discount factor

$S_i = [S - PV_i(D)]e^{r_i(T_i-t)}$ - the equity forward price

S – the equity spot price at valuation date

$PV_i(D) = \sum_{t < \tau < T_i} d_{\tau} e^{-r_{\tau}(\tau-t)}$ - the present value of all dividends between t and T_i

d_{τ} – the discrete dividend paid at τ where $t \leq \tau \leq T$

r_i – the continuously compounded interest rate from t to T_i



Equity Swap

Valuation (Cont)

- The present value of the floating interest rate leg can expressed as

$$PV_{floating}(t) = N \sum_{i=1}^m (F_i + s) \tau_i D_i$$

where

t – the valuation date

N – the notational principal amount

i – the i^{th} cash flow (swaplet) from 1 to n

$\tau_i = \tau(T_{i-1}, T_i)$ – the accrual period (T_{i-1}, T_i) of the i^{th} cash flow.

$D_i = D(t, T_i)$ – the discount factor

$F_i = \frac{1}{\tau_i} \left(\frac{D_{i-1}}{D_i} - 1 \right)$ - the simply compounded forward rate

s - the floating spread



Equity Swap

Valuation (Cont)

- The present value of the equity swap from the equity receiver perspective is given by

$$PV(t) = PV_{equity}(t) - PV_{floating}(t)$$



Equity Swap

Practical Guide

- We consider discrete dividends only as described in the equity future note.
- To value an equity swap, you need to generate cash flows first, based on the start time, end time and payment frequency of the leg, plus calendar (holidays), business convention (e.g., modified following, following, etc.) and whether sticky month end.
- Second, an interest rate curve needs to be constructed via the most liquid interest rate instruments.
- Then, you need to compute equity forward prices correctly by accounting for all discrete dividends. This is a key factor for all equity related valuation.
- Accrual period is calculated according to the start date and end date of a cash flow plus day count convention
- Forward rate is continuously compounded rather than other compounding types



Equity Swap

A Real World Example

Equity Leg		Interest Rate Leg	
Currency	USD	Currency	USD
Initial Price	164.38	Leg Type	Float
Start Date	2/15/2017	Day Count	dcAct360
Maturity Date	8/15/2017	Notional	4931400
Shares	30000	PayReceive	Receive
Notional	4931400	Start Date	2/15/2017
PayReceive	Pay	Maturity Date	8/15/2017
Payment Frequency	1M	Payment Frequency	1M
Underlying	737446807=	Spread	0.0075
		Index Definition	
		Index Day Count	dcAct360
		Index Tenor	1M
		Index Type	LIBOR



Thank You

You can find more details at

<http://www.finpricing.com/lib/EqSwap.html>