

## **Text Instructions**

# 1. Annotations and abbreviations

Annotation in scoris	Meaning
✓and <b>×</b>	·
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
	Meaning
mark scheme	
	Mark for explaining a result or establishing a given result
mark scheme	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *
mark scheme E1	Mark for explaining a result or establishing a given result
mark scheme E1 dep*	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *
mark scheme E1 dep* cao	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *  Correct answer only
mark scheme E1 dep* cao oe	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *  Correct answer only  Or equivalent
mark scheme E1 dep* cao oe rot	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *  Correct answer only  Or equivalent  Rounded or truncated
mark scheme E1 dep* cao oe rot soi	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *  Correct answer only  Or equivalent  Rounded or truncated  Seen or implied  Without wrong working  Answer given
mark scheme E1 dep* cao oe rot soi www	Mark for explaining a result or establishing a given result Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working
mark scheme E1 dep* cao oe rot soi www AG	Mark for explaining a result or establishing a given result  Mark dependent on a previous mark, indicated by *  Correct answer only  Or equivalent  Rounded or truncated  Seen or implied  Without wrong working  Answer given

### 2. Subject-specific Marking Instructions for AS Level Further Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

#### м

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

#### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

#### В

Mark for a correct result or statement independent of Method marks.

#### Ε

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep\*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

  Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- if in any case the scheme operates with considerable unfairness consult your Team Leader.

	Questic	n	Answer	Marks	AO	Guidan	ice
1			$\mathbf{DR}$ $\alpha + \beta = -2, \ \alpha\beta = 5$	B1	1.2		Allow alternative methods e.g. using complex roots or substituting $x = \sqrt{y}$
			$\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta,  \alpha^2\beta^2 = (\alpha\beta)^2$	M1	1.1a	Both used, must be seen	
			$\Rightarrow p = 6, q = 25$	A1	1.1		
				[3]			
2	(i)		DR				
			$z_1^* z_2 = (3-2i)(-1-i) = -3 + 2i - 3i + 2i^2$	M1	1.1	Find conjugate, then multiply out brackets	Working must be seen
			=-5-i	A1	1.1		
				[2]			
2	(ii)		DR	M1	1.1	Multiply by $\frac{-1+i}{-1+i}$	Must be seen
			$\frac{z_1 + 2z_2}{z_2} = \frac{3 + 2i - 2 - 2i}{-1 - i} = \frac{1}{-1 - i} \cdot \frac{-1 + i}{-1 + i}$			-1+i	
			$= \frac{-1+i}{2} = -\frac{1}{2} + \frac{1}{2}i$	A1	1.1		
				[2]			

	Questio	on .	Answer	Marks	AO	Guidan	ce
3	(i)		$\mathbf{AB} = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix} \begin{pmatrix} -1 & 2 \\ 2 & -1 \end{pmatrix} = \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$	M1	1.1	Or BC	OR M1 $A^{-1} = \frac{1}{1-4} \begin{pmatrix} 1 & -2 \\ -2 & 1 \end{pmatrix}$
			So $\mathbf{AB} = 3\mathbf{I}$ and $m = 3$	E1 [2]	1.1		$= \frac{1}{-3} \begin{pmatrix} 1 & -2 \\ -2 & 1 \end{pmatrix} = \frac{1}{3} \mathbf{B}$ E1 So $\mathbf{AB} = 3\mathbf{AA}^{-1} = 3\mathbf{I}$ and $m = 3$
3	(ii)		(2 0 0)	B1	1.1	BC	OR
			$\mathbf{C}\mathbf{D} = \begin{bmatrix} 2 & 3 & 3 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$ so $\mathbf{C}^{-1} = \frac{1}{2}\mathbf{D}$ and $k = \frac{1}{2}$	E1	2.2a		B1 $\mathbf{C}^{-1} = \begin{pmatrix} -2 & 4 & -1 \\ -2.5 & 4.5 & -0.5 \\ 1.5 & -2.5 & 0.5 \end{pmatrix}$ BC E1 so $\mathbf{C}^{-1} = \frac{1}{2}\mathbf{D}$ and $k = \frac{1}{2}$
2	(***)			[2] M1	1.1a	D-44:-1:-4:44	
3	(iii)		$\mathbf{EF} = \begin{pmatrix} k & k^2 \\ 3 & 0 \end{pmatrix} \begin{pmatrix} 2 \\ k \end{pmatrix} = \begin{pmatrix} 2k + k^3 \\ 6 \end{pmatrix}$ $\Rightarrow \begin{pmatrix} 2k + k^3 \\ 6 \end{pmatrix} = \begin{pmatrix} -2k \\ 6 \end{pmatrix}$	M1	2.1	Both multiplications attempted	
			$\Rightarrow 2k + k^3 = -2k$	A1	2.2a		
			k = 0, 2i, -2i	A1	1.1	BC	
			$\mathbf{F} = \begin{pmatrix} 2 \\ 0 \end{pmatrix}, \begin{pmatrix} 2 \\ 2i \end{pmatrix} \text{ or } \begin{pmatrix} 2 \\ -2i \end{pmatrix}$	A1	1.1	www If <b>A0</b> , allow SC1 for one matrix only	
1				[5]			

Question	Answer	Marks	AO	Guidan	ce
4	I	M1	1.1	A circle with centre 3+4i,	Accept the correct minor arc
	Im 1	A1	1.1	passing through origin.	alone
		B1	1.1	A line parallel to y-axis through 1	Accept the correct line segment alone
	. 3+4i  The shaded region is the required locus	B1	1.1	Correct shading and continuous lines	Must state which region is the required locus.
		[4]			

	Questic	on	Answer	Marks	AO	Guidan	ce
5	(i)	/ <del></del>	2.1.2	B1	2.2a	Coordinates of any two images seen	
	(-)		A' is $\left(-\frac{3}{5}, \frac{4}{5}\right)$ , B' is $\left(\frac{1}{5}, \frac{7}{5}\right)$ and C' is $\left(\frac{4}{5}, \frac{3}{5}\right)$	B1	1.1	Coordinates of third image seen;	
				B1	1.1	completely correct labelled diagram,	
					1	must include indication of	
						coordinates	
				[3]		Coordinates	
5	(ii)		(r) $(r)$	M1	1.1	Seen or implied	OR
	()		$\mathbf{M} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix}$		1	Seen of imprior	
							<b>M1</b> $A'\left(\frac{-3}{5}, \frac{4}{5}\right) A (1, 0)$
			G 3 . 4	M1	1.1	At least one seen	(1.2)
			So $-\frac{3}{5}x + \frac{4}{5}y = x$	IVII	1.1	At least one seen	$M1 \Rightarrow \text{ midpoint is } \left(\frac{1}{5}, \frac{2}{5}\right)$
			$And \frac{4}{5}x + \frac{3}{5}y = y$				(5.5)
			Both of which lead to $y = 2x$	E1	2.2a	Must conclude from both equations	$\mathbf{E1} \Rightarrow y = 2x$
			, and the second	[3]		•	
5	(iii)	(a)	$Det \mathbf{M} = -1$	B1	1.1		
	(-11)	()					
				[1]			
<u> </u>	(***)	(a.)		7.4	2.2		
5	(iii)	(b)	It means that area remains the same	B1	2.2a		
			but that the orientation of the image has changed	B1	2.4	Accept 'sense', 'order of labelling'	
			oe			oe	
				[2]			

(	Questic	on	Answer	Marks	AO	Guidar	ice
6	(i)		Let x, y and z be the amount invested in each	B2	1.1	B1 for writing down matrix alone	OR
			$\begin{vmatrix} 1 & 1 & 1 \\ 0.025 & 0.037 & 0.049 \\ 1 & -2 & 0 \end{vmatrix} \begin{pmatrix} x \\ y \\ z \end{vmatrix} = \begin{pmatrix} 2000 \\ 92 \\ 0 \end{pmatrix}$	[2]	3.1b		B2 Let s be the amount invested in the savings account $ \begin{pmatrix} 0.025 & 0.037 & 0.049 \\ 0.025 & 0.037 & 0.049 \end{pmatrix} \begin{pmatrix} 2s \\ s \\ 2000 - 3s \end{pmatrix} = 92 $
6	(ii)		$ \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 & 1 & 1 \\ 0.025 & 0.037 & 0.049 \\ 1 & -2 & 0 \end{pmatrix}^{-1} \begin{pmatrix} 2000 \\ 92 \\ 0 \end{pmatrix} $ $ x = 200, \ y = 100, \ z = 1700 $ so he invests $ £200 \text{ in the current account} $ £100 in the savings account £1700 in the supersaver account	M1	3.1a	Attempt to find $x, y, z$ BC  Interpret in context	M1 by multiplying out and solving for $s$ .  A1 $s = 100$ so he invests £200 in the current account £100 in the savings account £1700 in the supersaver account
6	(iii)		The 92 in part (ii) should be $92 \pm 0.5$ , therefore giving a range of answers for each account	[2] E1 E1	3.1b 3.2b		

# Y531 Mark Scheme June 20XX

(	Questio	on Answer	Marks	AO	Gui	dance
7		f(5) = 0	M1	3.1a	DR	
		$\Rightarrow f(x) = (x-5)(x^2 + bx + c)$	A1	2.4		OR M1 divide
		(				$x^3 - 13x^2 + 65x - 125$ by
						(x-5)
		$\Rightarrow f(x) = (x-5)(x^2 - 8x + 25)$	<b>B</b> 1	1.1		A1 obtain
		(1 3)(1 3)(1 3)				$(x-5)(x^2-8x+25)$
		Attempt to solve their quadratic	M1	2.1		
		$x = 4 \pm 3i$	<b>A1</b>	1.1	FT	
		The roots are 5, 4+3i and 4–3i				
		Attempt to find moduli	M1	3.1a		
		5  = 5				
		$ 4+3i  = \sqrt{4^2+3^2} = 5$	A1	1.1	FT	
		$ 4+3i  = \sqrt{4^2 + 3^2} = 5$ $ 4-3i  = \sqrt{4^2 + 3^2} = 5$	A1	1.1	FT	
		Distance from origin for all roots is 5 units,	E1	2.4	FT	
		so all roots lie on $ z  = k$ , where $k=5$				
			[9]			

	Question	Answer	Marks	AO	Guidar	ıce
8		Let $n = 4$ , then	B1	2.1	Basis case for proof by induction	
		$4! = 24$ and $2^4 = 16$ so $4! > 2^4$ Assume true for $n = r$	M1	2.1	Assumption	
		$r! > 2^r$ for $r \ge 4$ Then for $n = r + 1$ $(r+1)! = (r+1) \times r! > (r+1) \times 2^r$ by assumption	M1	1.1	Add next statement	
		Since $r+1>2$ , $(r+1)\times 2^r > 2\times 2^r = 2^{r+1}$ so $(r+1)!>2^{r+1}$	E1	2.2a	Sufficient working to establish true for $r+1$	Must state that $r+1>2$ oe
		If true for $r$ then true for $r+1$ . Hence, given basis case, the statement is true for all positive integers.	E1	2.4	Clear conclusion for induction process	A <i>formal</i> proof is required for full marks Accept other <i>complete</i> methods
			[5]			
9	(i)	$-1 \times -2 + 2 \times 3 + 1 \times k = 0$	M1	1.1	Attempt the scalar product and set	Allow use of i, j, k notation
		$\Rightarrow k = -4$	A1 [2]	1.1	equal to zero soi	
9	(ii)	Equate x and y coordinates:	M1	3.1a	Use coordinates to find $\mu$ and $\lambda$ .	
		$3 + \lambda = 6 + 2\mu \Rightarrow \lambda - 2\mu = 3$				
		$2 - \lambda = 5 + \mu \Rightarrow \lambda + \mu = -3$				
		$\Rightarrow \mu = -2, \lambda = -1$	A1	1.1		
		Consistent with z coordinates since $7 + 3 \times (-1) = 4$ and $2 - (-2) = 4$	E1	3.1a	Check consistency with third coordinate	
		So the point of intersection is $(2, 3, 4)$	A1	1.1		
			[4]			

	Question	Answer	Marks	AO	Guidar	ice
9	(iii)	The vector product find a mutual perpendicular				OR M1A1
		$\begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 2 \\ 1 \end{pmatrix} - \begin{pmatrix} -2 \\ 7 \end{pmatrix}$	M1	3.1a	Attempt the vector product, by any valid method	$\begin{bmatrix} 1 \\ -1 \\ 3 \end{bmatrix} \begin{pmatrix} 1 \\ a \\ b \end{bmatrix} = 0 \text{ and } \begin{bmatrix} 2 \\ 1 \\ -1 \end{bmatrix} \begin{pmatrix} 1 \\ a \\ b \end{bmatrix} = 0$
		$ \begin{vmatrix} -1 \\ 3 \end{vmatrix} \times \begin{vmatrix} 1 \\ -1 \end{vmatrix} = \begin{vmatrix} 7 \\ 3 \end{vmatrix} $	A1	1.1	BC	$\begin{pmatrix} -1 \\ 3 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = 0$ and $\begin{pmatrix} 1 \\ -1 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} = 0$
		$\begin{pmatrix} 1 \\ 2 \end{pmatrix} = \begin{pmatrix} -2 \\ 7 \end{pmatrix}$	M1	3.1a		<b>A1</b> $1 - a + 3b = 0$ and $2 + a - b = 0$
		$ \begin{vmatrix} a \\ b \end{vmatrix} = \lambda \begin{vmatrix} 7 \\ 3 \end{vmatrix} $				M1 Solve simultaneous equations
		$\lambda = -\frac{1}{2}  a = -3.5, \ b = -1.5$	M1	1.1		-4
		a = -3.5, b = -1.5	A1 [5]	1.1		<b>A1</b> $a = -3.5, b = -1.5$

# Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1	3	-0	0.0	(0)	3
2(i)	2	16	63	i)	2
2(ii)	2	0:		10	2
3(i)	2				2
3(ii)	1	1			2
3(iii)	3	2			5
4	4	16		u(j)	4
5(i)	2	1	10		3
5(ii)	2	1	(0)	10	3
5(iii)(a)	1	100	(1)	, di	1
5(iii)(b)	-0	2	0.0	- 10	2
6(i)	1	0:	1	9	2
6(ii)	1	- O	1		2
6(iii)	- (3)	(5)	2		2
7	4	3	2	- 6	9
8	1	4	ŢŢ.	ė,	5
9(i)	2	(0)	(0)	0	2
9(ii)	2	10	2	45	4
9(iii)	4	1	60	ıξ	5
Totals	37	15	8	0	60

PS = Problem Solving M = Modelling

# **Summary of Updates**

Date	Version	Change
October 2019	2	Amendments to the front cover rubric instructions to candidates

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# **AS Level Further Mathematics A** Y531 Pure Core

**Printed Answer Booklet** 

Version 2

# **Date – Morning/Afternoon**

Time allowed: 1 hour 15 minutes

### You must have:

- · Question Paper Y531 (inserted)
- · Formulae AS Level Further Mathematics A

## You may have:

· a scientific or graphical calculator



First name	
Last name	
Centre number	Candidate number

## **INSTRUCTIONS**

- The Question Paper will be found inside the Printed Answer Booklet.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question
- The acceleration due to gravity is denoted by  $g \text{ m s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use g = 9.8.

## INFORMATION

- · You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 4 pages.

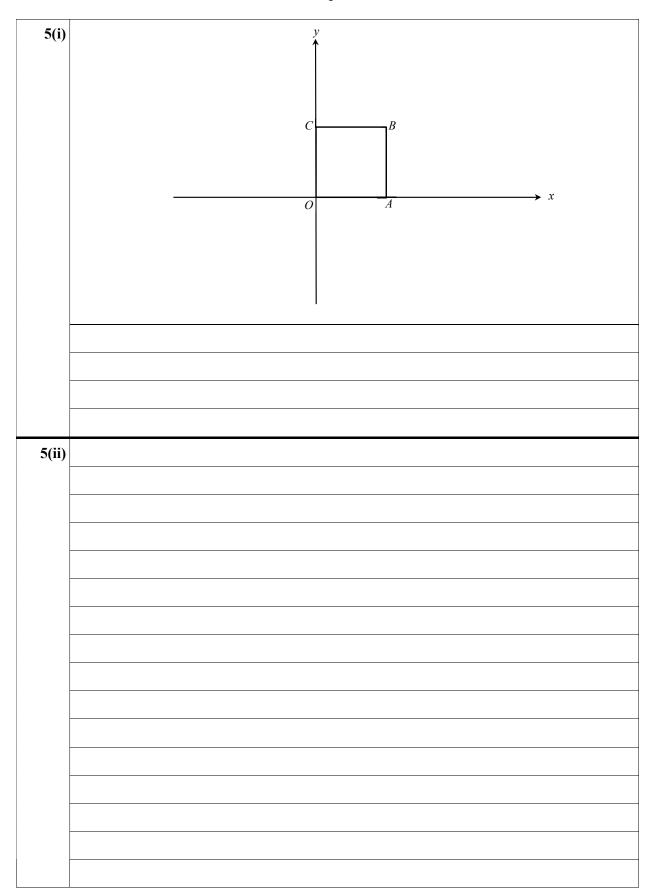


1	
2(i)	
2(ii)	
2(11)	

3(i)	
3(ii)	
3(iii)	
	(answer space continued on next page)

3(iii)	(continued)
4	

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5(iii)(a)	
<b>5(iii)(b)</b>	

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6(i)	
6(ii)	
<i>(</i> (111)	
6(iii)	

7	

8	

9(i)	(i)	
9(ii)	(ii)	

9(iii)	

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