OCR Oxford Cambridge and RSA		
day June 20XX – Mornin	g/Afternoon	
A Level Further Mathematics A Y543 Mechanics		
SAMPLE MARK SCHEME		
		Duration: 1 hour 30 minutes
MAXIMUM MARK 75		
	This document consists of 12 pages	

Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓and ≭	Ĭ
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in	Meaning
mark scheme	
E1	Mark for explaining a result or establishing a given result
	Mark for explaining a result of establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
dep*	
-	Mark dependent on a previous mark, indicated by *
cao	Mark dependent on a previous mark, indicated by * Correct answer only
cao oe	Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent
cao oe rot	Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated
cao oe rot soi	Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied
cao oe rot soi www	Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working
cao oe rot soi www AG	Mark dependent on a previous mark, indicated by * Correct answer only Or equivalent Rounded or truncated Seen or implied Without wrong working Answer given

2. Subject-specific Marking Instructions for A Level Further Mathematics A

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

М

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are imblied and full credit must be given.
- The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

 Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for g. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

	Questio	n	Answer	Marks	AO	Guidan	ce
1	(i)			M1	1.1	Differentiating one term of v correctly	
			$\mathbf{a} = \frac{\mathrm{d}\mathbf{v}}{\mathrm{d}t} = 2t\mathbf{i} - \frac{10}{(2t+1)^2}\mathbf{j}$	A1	1.1		
			$\mathbf{F} = m\mathbf{a} = 4t\mathbf{i} - \frac{20}{(2t+1)^2}\mathbf{j}$	A1FT	3.3	FT their a	
				[3]			
1	(ii)			M1	3.4	Attempt at scalar product	OR
							M1 at $t = 4$
			$\mathbf{F.v} = 4t \left(t^2 - 3\right) - \frac{100}{\left(2t + 1\right)^3}$	A1	1.1		$\mathbf{A1 F} \cdot \mathbf{v} = \left(16\mathbf{i} - \frac{20}{81}\mathbf{j}\right) \cdot \left(13\mathbf{i} + \frac{5}{9}\mathbf{j}\right)$
			Power is 208 W	A1	1.1	207.86282	
				[3]			
1	(iii)		$T = \frac{1}{2} \left(\frac{1}{2} \right)^2 + \frac{25}{2}$	B1	3.4		OR
			$T = \frac{1}{2}m\mathbf{v} \cdot \mathbf{v} = (t^2 - 3)^2 + \frac{25}{(2t+1)^2}$				B1 for value of T at 2 or 4
				M1	1.1	T(4)-T(2)	M1 $T(4) - T(2)$
			Work done is 167 J	A1	1.1	167.308642	
				[3]			

	Questio	on	Answer	Marks	AO	Guidance		
2	(i)			M1	3.3	Attempt at conservation of energy		
			$\frac{1}{10800x^2}$	A1	1.1	GPE term(s)	GPE is Gravitational Potential	
			$75g(6.2) + \frac{1}{2}(75)(2)^2 = 75g(1.2 - x) + \frac{10800x^2}{2(1.2)}$	A1	1.1	KE term	Energy	
				A1	1.1	EPE term	KE is Kinetic Energy	
							EPE is Elastic Potential Energy	
			$300x^2 - 49x - 255 = 0$	E1	2.1	www; AG must show intermediate		
						step		
				[5]				
2	(ii)		x = -0.8438977 < 0 so not valid	B1	2.3	The negative value of x must be seen		
						and not given as a final answer		
			x = 1.01	B1	3.4		1.007231	
				[2]				
2	(iii)		e.g. $g = 9.8$ is not precise enough, use $g = 9.81$	E1	3.5b	For one assumption and a sensible		
			e.g. the army recruit is not a particle, model as a	E1	3.5c	refinement		
			rigid body					
			e.g. the mat is not a single spring, model as					
			multiple springs					
				[2]				
3	(i)			M1	3.3	Integrating one term of F correctly		
			$I = \int t^2 + 3e^t dt = \frac{1}{3}t^3 + 3e^t$	A1	1.1			
				A1	1.1	BC	182.1277	
			$I = \int_0^4 F dt = \frac{55}{3} + 3e^4 = 182$, so impulse is 182 N s	AI	1.1	BC	182.1277	
				[3]				
3	(ii)		$2(v-5) = \frac{55}{3} + 3e^4$	M1	3.4	Use of $I = mv - mu$		
			Speed is 96.1 ms ⁻¹	A1	1.1		96.0638	
			1	[2]				

	Questio	n	Answer		AO	Guidance	
4	(i)			M1	3.3	Attempt at conservation of mechanical	
						energy	
			$35g(5) - \frac{1}{2}(35)v^2 = \dots$	A1	1.1	PE term on lhs	
			_	A1	1.1	KE term on rhs	
			$35g(7-4\cos\theta)$	A1	1.1		
			$v^2 = 4g(2\cos\theta - 1)$	E1	2.1	www; AG must show an intermediate	
						step	
				[5]			
4	(ii)		When $\theta = 0^{\circ}$, $v_H = 2\sqrt{g}$	B1	3.3		6.260990
			$\left v_V^2 = 2g(3) \right $	B1	3.3		
			, 3()	M1	3.4	Use of either $v^2 = v_V^2 + v_H^2$ or	
						,	
						$\tan \theta = \frac{v_V}{v_H}$	
			$v = 9.90$ so speed is $9.90 \mathrm{m s^{-1}}$	A1	1.1		9.8994949
			$\theta = 50.8^{\circ}$ below the horizontal	A1	1.1		50.768479
				[5]			
4	(iii)		Tension when $\theta = 60^{\circ}$ is $17.5g$ N	B1	1.1	May appear anywhere in answer	
			_	*M1	3.1b	Attempt to use N2L radially with	N2L is Newton's second law
						$a = \frac{v^2}{r}$	
			$T - 35g\cos\theta = \frac{35}{4} \left(4g \left(2\cos\theta - 1 \right) \right)$	A1	1.1		
				dep*	1.1a	Substituting $3 \times \text{their}(T)$ into their	
				M1		N2L attempt and solving for θ	
			$\theta = 33.6^{\circ}$	A1	1.1	BC	33.55730
				[5]			

	Overtic		Angwon	Marks	AO	Guidan	
<u> </u>	Questio		Answer			Guidan	ce I
5	(i)	(a)	$m\frac{\mathrm{d}v}{\mathrm{d}t} = -mg - \left(-6mv + mv^2\right)$	B1	3.3		
			$\frac{\mathrm{d}t}{\mathrm{d}v} = -\frac{1}{v^2 - 6v + 9.8}$	M1	1.1	Divide by <i>m</i> and rearrange	
			$= -\frac{1}{(v-3)^2 - 9 + 9.8} = -\frac{1}{(v-3)^2 + 0.8}$	E1	2.1	AG Completing the square in the denominator	
				[3]			
5	(i)	(b)	$t = -\int \frac{dv}{(v-3)^2 + 0.8}$	M1	3.1a	Separation of variables	
			$(v-3)^2 + 0.8$				
			$t_1 = -\int_{8.25}^{0} \frac{\mathrm{d}v}{(v-3)^2 + 0.8}$, and	B1	3.4	Using the limits correctly at least once	
			$t_2 = -\int_{8.75}^{0} \frac{\mathrm{d}v}{\left(v - 3\right)^2 + 0.8}$				
			$t_1 = 2.9997903$	A1	1.1	BC	Or use
							$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \left(\frac{x}{a} \right)$
			$t_2 = 3.0159247$	A1	1.1	BC	
			2.9997 $< t < 3.0159$ so <i>B</i> 's model for the vast majority of speeds in the interval $(8.5 \pm 0.25) \text{m s}^{-1}$ does produce a value of <i>t</i>	E1	2.2b	Indication that the non-exact nature of the initial speed leads to a result that is likely to be correct	
			greater than 3 so it is extremely likely (but not certain) that B 's model is consistent with the time recorded by A .				
				[5]			

	Question		Answer		AO	Guidance
5	(ii)		e.g. student C's claim is incorrect as they have assumed that the differential equation for the motion of the particle is the same in both directions	B1	2.2a	For explaining that the differential equation of motion is not the same in each direction
			In fact the differential equation for when the particle is falling is given by $mg - (-6mv + mv^2) = m\frac{dv}{dt}$	B1	2.3	For either this corrected model or stating that the two forces in the vertical direction are now acting in opposite directions
			$-\int_{0}^{1} \frac{1}{(v-3)^{2}-18.8} \mathrm{d}v$	B1	3.3	
				[3]		

	Questi	on	Answer	Marks	AO	Guidance
6	(i)			*M1	3.4	Attempt at use of conservation of
						linear momentum
			$2.5u\cos\theta - 3u\cos\theta = -2.5v_1\cos\alpha + 3v_2\cos\beta$	A1	1.1	
				*M1	3.4	Attempt at use of restitution equation,
						must be correct way round
			$-v_1\cos\alpha - v_2\cos\beta = -e(u\cos\theta + u\cos\theta)$	A1	1.1	Must be consistent with the directions
						used for conservation of linear
				i na		momentum
			$u \sin \theta = v_1 \sin \alpha \text{ and } u \sin \theta = v_2 \sin \beta$	*B2	1.1a	B1 for one correct
					1.1a	
				dep*	3.1b	Solving simultaneous equations by
				M1		eliminating v_1 and v_2 use of
						$\tan X = \frac{\sin X}{\cos X}$
			$\tan \beta = \frac{11 \tan \theta}{10e - 1}$	E1	2.1	www; AG
			10e-1			
				[8]		
6	(ii)		$10e - 1 = 0 \Rightarrow e = \frac{1}{10}$	*M1	2.2a	Setting the denominator of $\tan \beta$
						equal to 0 and obtaining a value for <i>e</i>
			$\tan \alpha = \frac{11 \tan \theta}{}$	B1	3.1b	
			$\tan \alpha = \frac{1}{1+12e}$			
			$\tan 50 = \frac{11\tan \theta}{1 + 12/10}$	dep*	3.1b	Substituting their e and $\alpha = 50^{\circ}$ and
			$\frac{\tan 30}{1+12/10}$	M1		solving for θ
			$\theta = 13.4^{\circ}$	A1	1.1	13.40634 BC
				[4]		

	Questio	nn l	Answer	Marks	AO	Guida	ace
7	(i)	1	Migner	M1	1.2	Attempt to integrate to find area	Limits not required for M mark
			$A = \int_0^{\ln 32} e^{0.8x} dx = \frac{75}{4}$	A1	1.1	BC BC	$ [1.25e^{0.8x}]_0^{\ln 32} $
			$A\overline{x} = \int_0^{\ln 32} x e^{0.8x} dx$	M1 A1	3.1a 1.1	Use integration by parts Correctly applied to end of first stage	
			$= \left[1.25xe^{0.8x}\right]_0^{\ln 32} - 1.25 \int_0^{\ln 32} e^{0.8x} dx$ $= \left[1.25xe^{0.8x} - 1.5625e^{0.8x}\right]_0^{\ln 32}$	A1	1.1		
			= $(20\ln 32 - 25) - (0 - 1.5625) \Rightarrow \overline{x} =$	M1	1.1	Using correct limits and $\overline{x} = \frac{A\overline{x}}{x}$	
			$\overline{x} = \frac{16}{3} \ln 2 - \frac{5}{4}$	E1	2.1	www; AG	
				[7]			
7	(ii)			M1	2.1	For $\dots \frac{1}{2} \int y^2 dx$ and attempt to	
			$A\overline{y} = \frac{1}{2} \int_0^{\ln 32} (e^{0.8x})^2 dx = \frac{1275}{16}$	A1	1.1	integrate BC	$\frac{1}{2} \left[\frac{e^{1.6x}}{1.6} \right]_0^{\ln 32}$
			$\overline{y} = \frac{17}{4}$ oe	A1	1.1		
				[3]			
7	(iii)			M1	3.1a	Table of values idea to get an equation/expression	
				M1	2.1	Attempt at $cv(\overline{x}) = (8)(16)(\ln 32) - cv(A\overline{x})$	
			$\overline{X}(16\ln 32 - \frac{75}{4}) = (8)(16)(\ln 32) - (\frac{17}{4} \times \frac{75}{4})$	A1FT	1.1	,	
			$\overline{X} = 9.92$	A1	1.1	9.915779	
				[4]			

Assessment Objectives (AO) Grid

Question	AO1	AO2	AO3(PS)	AO3(M)	Total
1(i)	2	(3)	- 0	1	3
1(ii)	2	0	0	1	3
1(iii)	2	79	()	1	3
2(i)	3	1	0	1	5
2(ii)	U	1	U	1	2
2(iii)	(1)	0	0	2	2
3(i)	2	0	()	1	3
3(ii)	1	[3]	- 0	1	2
4(i)	3	1	0	1	5
4(ii)	2	(3)	10:	3	5
4(iii)	4	Q.	1	0	5
5(i)(a)	1	1	0	1	3
5(i)(b)	2	1	1	1	5
5(ii)	(I)	1	0	2	3
6(i)	4	1	1	2	8
6(ii)	1	1	2	0	4
7(i)	5	1	1	- b	7
7(ii)	2	1	0	0	3
7(iii)	2	1	1	Or .	4
Totals	38	11	7	19	75

PS = Problem Solving M = Modelling

Summary of Updates

Date	Version	Change
October 2019	2	Amendments to the front cover rubric instructions to candidates





A Level Further Mathematics A Y543 Mechanics

Printed Answer Booklet

Version 2

Date – Morning/Afternoon

Time allowed: 1 hour 30 minutes

You must have:

- · Question Paper Y543 (inserted)
- Formulae A Level Further Mathematics A

You may use:

· a scientific or graphical calculator



First name		
Last name		
Centre number	Candidate number	

INSTRUCTIONS

- The Question Paper will be found inside the Printed Answer Booklet.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- · Answer all the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet. Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question.
- The acceleration due to gravity is denoted by g m s⁻². Unless otherwise instructed, when a numerical value is needed, use g = 9.8

INFORMATION

- You are reminded of the need for clear presentation in your answers.
- The Printed Answer Booklet consists of 12 pages. The Question Paper consists of 8 pages.



1(i)	
1(ii)	

3

1(iii)	
-	
-	

PLEASE DO NOT WRITE IN THIS SPACE

2(i)	
A (11)	
2(ii)	

2(iii)	
2(1)	
3(i)	
3(ii)	
3(11)	

4(i)	
4(ii)	
4(11)	
	(answer space continued on next page)

4(ii)	(continued)
4(iii)	
1	

5(i)(a)	
5(i)(b)	

	(answer space continued on next page)
6(i)	
5(ii)	

6(i)	(continued)
6(ii)	

7(i)	
7(ii)	

7(iii)	

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