# Statistical Inference Course Project

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## **Project Description**

This project investigates the exponential distribution in R and compares it with the Central Limit Theorem. The exponential distribution can be simulated in R with  $\mathbf{rexp(n,lambda)}$  where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda. Set  $\mathbf{lambda} = \mathbf{0.2}$  for all of the simulations. You will investigate the distribution of mean of 40 exponentials. Note that you will need to do  $\mathbf{1000}$  simulations.

This report covers the following objectives:

- 1. Show the sample mean and compare it to the theoretical mean of the distribution.
- 2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.
- 3. Show that the distribution is approximately normal.

### Simulation Criteria and Results

Parameters for Simulation

```
set.seed(110)
sim_cnt <-1000
lambda <-0.2
n<-40</pre>
```

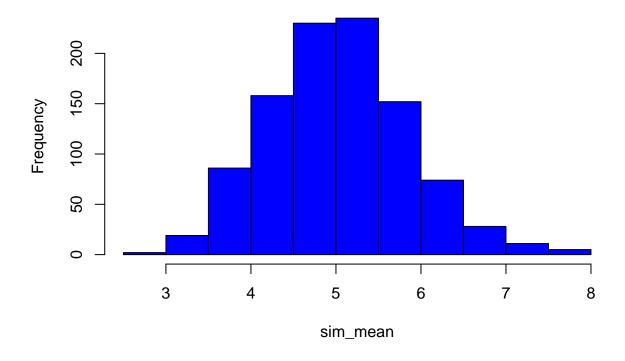
Generate 1000 samples of 40 exponentials

```
sim_mean<-NULL
for(i in 1:1000){
    sim_mean<-c(sim_mean,mean(rexp(n,lambda)))
}</pre>
```

The histogram of the mean of 1000 samples

```
hist(sim_mean,col="blue")
```

# Histogram of sim\_mean



The **mean** of 1000 sample means

mean(sim\_mean)

## [1] 5.034976

The  $standard\ deviation$  of 1000 sample means

sd(sim\_mean)

## [1] 0.8185278

The **variance** of 1000 sample means

var(sim\_mean)

## [1] 0.6699878

### Comparing sample mean to the theoretical mean

The theoretical mean  $=\frac{1}{\lambda}=\frac{1}{0.2}=5$ .

From the above simulation, the estimate value of the mean of the 1000 sample means is 5.0349765. The value is very close to theoretical mean, with a difference of only 0.0349765.

### Comparing sample variance to the theoretical variance

The population standard deviation =  $\frac{1}{lambda}$ .

Theoretical variance of sample mean  $=\frac{(\frac{1}{lambda})^2}{n}$ 

Therefore, theoretical variance of sample mean  $=\frac{5^2}{40}=0.625$ 

Slight different between the variance of sample means (from simulation) and theoretical variance of sample mean, that is 0.6699878 - 0.625 = 0.0449878

