

Modelling dynamic electric vehicle routing problem with heterogeneity and uncertainty

Abstract

With more and more serious issues like air pollution and traffic noise in transport sector, a fast growing number of electric vehicles has been used for various purpose in road transport, including urban freight transport. To promote the usage of electric vehicle in urban freight transport, this study investigates the dynamic vehicle routing problem with consideration of heterogeneous vehicle types and mixed-type charging facilities, as well as multiple uncertain factors in real operation. It is a challenge to incorporate charging activity into the routing plan since the availability of charging station and the travel time en-route are stochastic. The decision-maker needs to assign the right vehicle type to a certain route with minimized total time to implement the routing plan. An adaptive solution approach based on multiple scenario approach and two heuristics is developed to solve the proposed model. To validate the proposed model and test the solution approach, multiple numerical experiments are conducted based on a benchmark dataset.

Keywords Electric vehicle routing problem, Heterogeneous electric vehicles, Mixed-type charging, Uncertainty, Dynamic approach, Multiple scenario approach

1 Introduction

Although road urban freight transport may cause various issues, such as traffic congestion, traffic noise, air pollution, energy consumption, and high logistics costs, it remains the primary mode of urban freight transport. The use of electric vehicles (EVs) has emerged as a promising solution to reducing such environmental and sustainable concerns. It is evident that EVs operate more silently than conventional vehicles, and they could help reduce traffic emission significantly. Nevertheless, how to run EVs efficiently and economically under various features and limitations associated with EV, for instance, limited driving range, limited load capacity, long charging time and the scarcity of charging station (CS), is a challenge to address before they can be used for freight transport widely.

To promote the integration and operation of EVs for freight transport, several models of electric vehicle routing problem (EVRP) have been proposed during the past few years. As optimization decision models seek to represent real-life problems, research on EVRP has introduced several variants. One of them is the heterogeneous EVRP (HEVRP). Logistics companies usually hold a fleet of diverse EVs with different acquisition cost, capacity, driving range, and energy consumption. Therefore, fleet management, i.e. selecting the right EV for a certain transportation request, is highly important. In HEVRP, it is considered that EVs differ in their capacity, battery size, and purchasing cost. Another variant of the EVRP is the stochastic EVRP (SEVRP). In real life, one or more inputs of the problem are often uncertain, and the developments in the area of algorithms and the area of information technologies, e.g. development of intelligent transportation systems (ITS), have rendered possible to freight providers the use of real-time data on the management of their operations.

That is, VRP can now be solved dynamically, i.e. on real-time manner.

Although a diversity of EVRP models have been proposed with consideration of various factors and constraints, several key factors associated with EVs are missing, and more importantly the relationship among various factors lacks exploration.

In this paper, we introduce a model for the dynamic heterogeneous electric vehicle routing problem (DHEVRP) with consideration of heterogeneity and uncertainty. This model aims to address multiple challenges associated with EV operation in an adaptive way, i.e. sequential decision-making. Heterogeneity comes from multiple types of EVs with different loading capacity, battery capacity and energy consumption, as well as various charging rates at different CSs. Three sources of uncertainty are considered: travel time, charging station availability,

and waiting time at a CS. Travel time is considered stochastic due to traffic congestion. For example, travel time is usually larger at peak hours than at non-peak hours along the same route. We assume that each CS has a probability of being available, and in case of CS is fully occupied, a stochastic waiting time will be imposed for the EV in queue. Moreover, both time window and service time are considered for each customer. Penalty cost/time will be charged if delivery occurs out of the time window. The objective function of the DHEVRP consists of en-route time and on-demand charging time. En-route includes travel time, service time, and penalty cost/time for early or late delivery whereas on-demand charging time is a function of availability of CS, waiting time at CS, charging rate, remaining and expected battery levels. To solve this problem, we proposed a dynamic solution method in which the time horizon is divided into intervals. The goal is to design a solution for how to serve customers and when/where recharge the EV within the next time interval, using both deterministic and stochastic information about the inputs. The solution method is developed based on the Multiple Scenario Approach (MSA) (Bent & Hentenryck 2004) and uses two heuristics for solving the scenarios.

To our best knowledge, it is the first study to consider both heterogeneous EVs and on-demand charging in EVRP, and both considerations are quite practical and important in real-life EVRP. In the literature, most parameters in EVRP were either given as fixed or considered as stochastic and separate from each other. In this study, we aim to explore the connection among multiple parameters to develop interlinked conditions. For example, in our proposed model, we consider charging time as a function of a series of parameters, like remaining battery level, charging rate, and so on. Rather than fully charged setting in most studies, we consider on-demand charging, i.e. top-up charges, based on the adaptive route plan, which makes the charging strategy more flexible and economical. Last but not the least, different cases will be tested based on benchmark networks to validate the DEHVRP model and prove the efficiency of the proposed solution method.

The structure of the paper is as follows. In the next section, a review research on EVRP is briefly presented. In Section 3, the mathematical formulation of the problem is shown. The proposed solution approach is introduced in Section 4 followed by the description of the dataset in Section 5. In Section 6, we define the different cases used in the experiments. The computational results are displayed in Section 7, and the work is concluded in Section 8.

2 Literature Review

In this work, we cover two categories of the electric vehicle routing problem. A brief description of these classes together with examples of works that have investigated them are presented as follows.

The first class is the HEVRP. Companies usually hold a fleet of diverse electric vehicles regards to, for instance, driving range. The fleet management, i.e. selecting the right EV for a certain transportation request, is highly important when the fleet of electric vehicles is heterogeneous. This class has been proposed to represent this situation. The HEVRP may, therefore, include many types of electric vehicles which can differ in capacity, battery capacity, energy battery consumption, charge level, and fixed cost. To the best of our knowledge only Hiermann et al. (2016) and Penna et al. (2016) have approached the HEVRP. Hiermann et al. (2016) studied the HEVRP with capacity constraints, time windows, service times, and charging stations. In this problem, each customer has a specific demand, a duration of the service, and must be serviced within its time window. It was assumed that the EVs vary in their transportation capacity, battery size, and purchasing costs. The authors proposed a mixed integer programming (MIP) formulation whose objective function minimizes not only the acquisition costs but also total traveled distance. Two solution algorithms were used to solve the model, branch & bound (B&B) solver and a hybrid one. The hybrid heuristic combines an adaptive large neighbourhood search (ALNS) together with an embedded local search (LS) and a labeling procedure. Since there is no benchmark dataset available for this problem, they created one based on the modified Solomon instances of Schneider et al. (2014) and the description of the vehicle type categories of Liu & Shen (1999). Hiermann et al. (2016) extended these vehicle types to include energy consumption, battery size, and recharging rate. Computational results on the benchmark dataset showed that the proposed ALNS was able to find optimal solutions for all small instances, whereas for the other instances it found solutions within small gaps to the best known solutions. They also performed a sensitivity analysis to demonstrate the benefit of considering a fleet of heterogeneous vehicles. Penna et al. (2016) investigated the very same problem but proposed a different solution approach. The proposed solution approach is a hybrid heuristic (HILS), which incorporates a Set Partitioning (SP) model to an Iterated Local Search (ILS). The performance of the proposed solution approach

was evaluated on the benchmark instances created by Hiermann et al. (2016). The numerical results indicated that the performance of the HILS was similar to the ALNS. That is to say, HILS was able to find optimal solutions for various instances and solutions with small gap to the optimal solutions. Although Hiermann et al. (2016) and Penna et al. (2016) considered electric vehicles with different battery energy consumption and charging rates, it was assumed in both studies that the electric vehicles are always charged to full capacity every time a vehicle reaches a charging station.

The second class is the SEVRP. In contrast to the assumptions of the classical EVRP, in the real world one or more of the elements of the EVRP are uncertain. The inputs of the EVRP that have been assumed to be stochastic are customer presence (Shi et al. 2019), demands (Lu & Wang 2019), travel time (Shao et al. 2017), energy consumption (Pelletier et al. 2019), and charging station availability (Sweda et al. 2017). Because of the importance of the time frame in the decision-making process, the SEVRP can be examined from two perspectives: static or dynamic. From a static perspective, the goal is to calculate a robust a-priori solution that undergoes minor changes during its execution to manage the fluctuations in the uncertain inputs. From a dynamic perspective, the aim is to design a route plan in an online way reporting to every vehicle what to do next. For this reason, the SEVRP can be classified either as static and stochastic EVRP (SSEVRP) or dynamic and stochastic EVRP (DSEVRP). In the SSEVRP decisions are made at the planning phase and define actions which are implemented at the execution phase, whereas in the DSEVRP decisions are made as soon as a new event occurs. In the latter, route plans are reoptimized at predefined stages with respect to both the current condition of the system and the available stochastic information. To the best of our knowledge only Bi & Tang (2019) and Lu & Wang (2019) have investigated the stochastic EVRP from a dynamic perspective. Bi & Tang (2019) considered the dynamic electric vehicle routing problem with battery charging and discharging and stochastic travel time and stochastic demands. The authors considered a single EV and designed a Markov decision process (MDP) model which incorporates an analytical battery model to better capture the discharging and charging pattern of the EVs. To solve this model, a hybrid rollout algorithm (HRA) which combines a pre-planning strategy and a rollout algorithm was developed. They used data of a logistics company in Singapore and the charging network of the country to generate several instances of the DSEVRP. The historical traffic data necessary in the pre-planning strategy is collected via Google Map Distance Matrix API. While the performance of the HRA was compared with that of a hybrid policy iteration (HPI) and hybrid base heuristic (HBH), the performance of the analytical battery model was compared to a linear approximation (LP) model. HRA calculated solutions that were little worse than HPI and HBH solutions in all small instances but it outperformed them in large instances. The simulation results also indicated that the analytical model outperformed the LP model. Lu & Wang (2019) approached the dynamic capacitated electric vehicle routing problem (DCEVRP) with stochastic customers and stochastic demands by transforming the problem into a series of static problems. For solving the series of static problems, they introduced a bi-strategy based optimization algorithm (BSOA) which reoptimizes the route plan every time a new customer appears. The authors adapted static instances from literature to compare the proposed solution algorithm with an ant colony optimization (ACO) algorithm and an exact method. The result experiments showed that both BSOA and ACO were able to find optimal solutions for most of the instances. Nonetheless, BSOA required less computational time than the exact method and ACO.

In this work, we combine the two classes of EVRP described before and introduce the DHEVRP. Therefore, in this model, different types of EV are available and uncertainties are present, and the problem is solved using a dynamic approach. The EVs distinguish based on capacity, battery capacity, energy battery consumption, and charging rate. The sources of uncertainty are: travel time, charging station availability, and waiting time at a CS. Stochastic charging station availability means that each CS has a probability of being available. If the CS is available, the EV is promptly recharged, otherwise stochastic waiting time will be imposed. On-demand charging time is defined as the whole period an EV remains at the CS, and it is considered as a function of the parameters: availability of CS, waiting time at CS, energy consumption rate, charging rate, remaining and target battery level. The remaining battery level is calculated based on the initial battery level and en-route energy consumption. The latter is a function of the travel distance and energy consumption rate. The target battery level of an EV is determined based on the estimation of energy consumption on the remainder of its route. That is to say, instead of recharging the battery from empty-to-full, top-up chargings are done. The battery is charged to a level so that the EV is able to attend the remaining customers and return to the depot. Historical data on the stochastic inputs is available, and the decision-making process is divided into several stages. The first stage is called planning stage. In this stage, we use the stochastic information about the inputs

to calculate the so-called a-priori route plan. After that, the a-priori route plan is reoptimized every time a new event occurs. An event happens when the true value of any of the stochastic inputs is disclosed. Figure 1 illustrates the difference between the stages for a single EV (route) when the true values of the stochastic travel times are revealed. At the beginning of a work day ($t = 0$), an EV starts to execute its route in accordance to the a priori route plan (represented in gray). The a priori route plan was designed in the previous day considering the known inputs, e.g. customers' locations, and the expected values of the uncertain inputs. In the next stage ($t = t_e$), the battery energy is consumed as the EV follows its route. Based on the a priori route plan, the EV should consume one unit of battery power as it travels from depot to customer 1 and one unit from customer 1 to customer 2. Although the traffic was normal (black arrow), i.e. normal travel time, and one unit of battery was thus used from depot to customer 1, the traffic was congested (red arrow), i.e. higher travel time, from customer 1 to customer 2 and two units of battery were used by the EV. Therefore, instead of being charged after attending customer 3 as planned in the a priori route plan, the EV must move to a different CS right after serving customer 2. Once all the stochastic travel times are revealed, the final route plan can be seen at $t = t_f$.

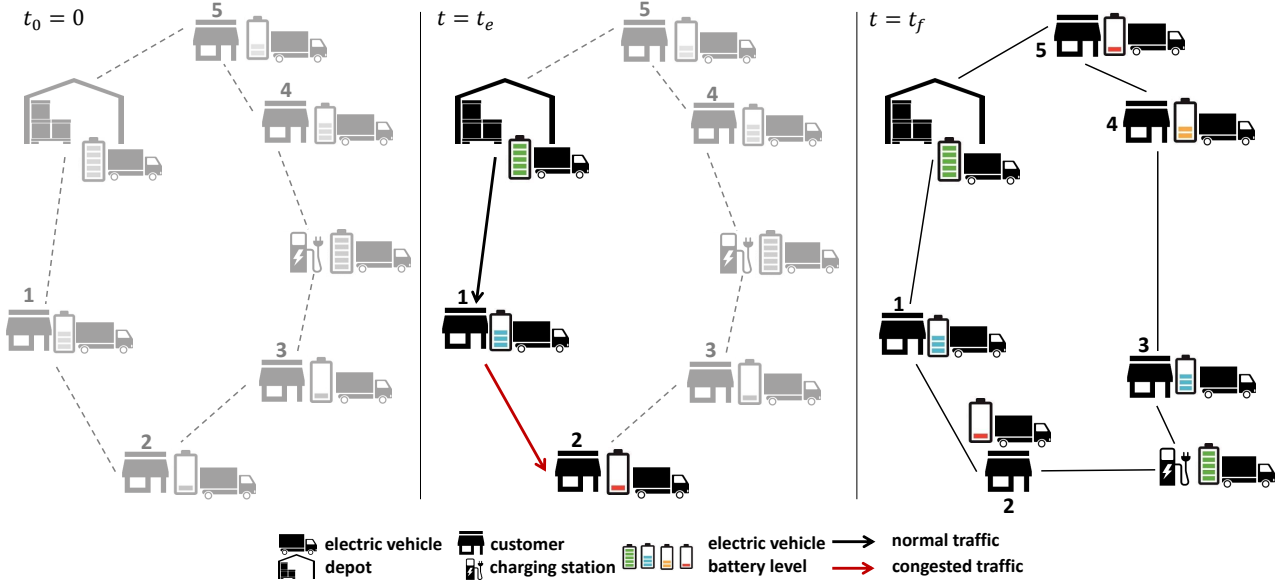


Figure 1: Example of the Dynamic electric vehicle routing problem under uncertainties

3 Static heterogeneous electric vehicle routing problem under uncertainties

As mentioned before, the DHEVRP can be studied from two perspectives. In this study, we adopt a dynamic approach for dealing with the problem. We divide the time horizon in a number of stages such that the number of stages is equal to the number of times a new event occurs. At each stage, we define an static DHEVRP with the deterministic inputs and stochastic inputs. Thus, the objective of this section is to formally introduce the static DHEVRP. We first provide the definitions and notations together with some assumptions used in the model. After that, we introduce the mathematical formulation of the static problem.

3.1 Problem description

The goal of the DHEVRP is to find a route plan to attend a set of customers with a given heterogeneous vehicle fleet while minimizing acquisition costs, total travel times, and charging times. This problem is represented on a fully connected directed graph $G = (N, A)$, where $N = (0, 1, 2, 3 \dots n)$ is the set of nodes and $A = \{(i, j) | i, j \in N, i \neq j\}$ is the set of arcs. Therefore, there are $|A| = n \cdot (n - 1)$ arcs in the graph. The set of nodes is partitioned into a set of customers $C = (0, 1, 2, 3 \dots c)$ and a set of dummy nodes E' , i.e. $N = C \cup U'$, where U' contains multiple charging stations of $U = (u_1, u_2, u_3, \dots u_u)$. Let n_0 and n_{n+1} represent the start and end depot nodes, respectively. For simplicity, we defined N_0 as the set of nodes with the start depot node and N_{n+1} as the set of nodes with the end depot node. $N_{0,n+1}$ portrays $N \cup \{n_0, n_{n+1}\}$. We also adopt this notation for the sets C and U' (Hiermann et al. 2016).

Since the availability of each charging station $i \in E$ is uncertain, we represented it by a stochastic variable Λ_i , i.e. $\Lambda_i : \Gamma_i \rightarrow \mathbb{R}_0^+ \forall i \in N$ with sampling spaces Γ_i . When a vehicle arrives at node i and the station is available, then $\Lambda_i = 1$. In this case, the vehicle is promptly recharged. If the station is not available, i.e. $\Lambda_i = 0$, the vehicle has to wait a time interval w_i until the charging station turns available. This time interval is also uncertain, i.e. $w_i : \alpha_i \rightarrow \mathbb{R}_0^+ \forall i \in N$ with sampling space α_i .

The deterministic amount of goods that has to be delivered to (or/and collected at) customer $i \in C$ is denoted as customer demand and is given by d_i , therefore, $d_0 = 0$. Each node $i \in N$ has a time window $[e_i, l_i]$ and a service time s_i . The true start of the service time is stored in τ_i .

There is a fleet of $K = \{1, 2, \dots, k\}$ types of electric vehicles. For each vehicle type k , the variable g^k expresses the charging rate (time/energy unit) and the variable e^k expresses the battery energy consumption rate (energy unit/kilometre). The maximum capacity of vehicle type k is defined as Q^k , and q_i^k displays the current load of a vehicle type k in node i . The maximum energy capacity of vehicle type k is represented by Y^k , and y_i^k displays the remaining battery energy level of vehicle type k at node i . The remaining battery energy level is also uncertain and it is thus represented by $y_i^k : \vartheta_i^k \rightarrow \mathbb{R}_0^+ \forall i \in N, \forall k \in K$ with sampling spaces ϑ_i^k . It is worth mentioning that the time spent by EV type k at a CS, that is $s_i, \forall i \in Q$, depends on the charging rate g^k of vehicle type k , its maximum energy capacity Y^k , and battery energy level of the vehicle when it reaches node $y_i^k, i \in R$, i.e. $s_i = g^k(Y^k - y_i^k)$.

If a EV type travels from i to j , the remaining battery level at customer y_j^k is calculated based on the battery level at node i and en-route energy consumption. We follow the work of Felipe et al. (2014) and assume that the en-route energy consumption (expressed in KWh per km) is proportional to the distance c_{ij} traveled through a given coefficient energy consumption e^k for EV type k .

The target battery level of an EV is determined based on the estimation of energy consumption on the remainder of its route. That is to say, instead of recharging the battery from empty-to-full, top-up chargings are done. The battery is charged to a level so that the EV is able to attend the remaining customers and return to the depot.

EXPLAIN HERE HOW MUCH THE BATTERY IS CHARGED AT ANY CS

Each arc $i, j \in A$ has two variables c_{ij} and t_{ij}^k associated with it. c_{ij} is the distance between the nodes i and j , and t_{ij}^k represents the travel time spent by vehicle type k in arc i, j . Travel times is represented by a stochastic variable, that is $t_{ij} : \Omega_{ij} \rightarrow \mathbb{R}_0^+ \forall i, j \in N$ with sampling spaces Ω_{ij} .

Note that an instance of the problem is defined by a complete weighted graph $G = (N, A, (c_{ij}, t_{ij}^k))$ together with the $|K|$ types of electric vehicles. α^k is defined as the acquisition cost of vehicle type k . The decision variables x_{ij}^k indicate whether or not vehicle type k travels from node i to node j . A solution $z = \{r_1, r_2, r_3, r_k\}$ to the DHEVRP, i.e. a route plan, consists of k routes. The total time is expressed by $J(z)$. A feasible route r_k is performed by one electric vehicle of type k which leaves the depot with a fully charged battery, serves a subset $B = \{i_1, i_2, \dots, i_b\} \subseteq C$ of customers, whose total demand does not exceed Q^k , recharges its battery at a charging station $u \in U'$ if necessary, and returns to the depot, i.e. $r_k = (n_0, \gamma_1^k, \gamma_2^k, u_u^k, \dots, \gamma_b^k, n_{n+1})$.

3.2 Mathematical model

The static DHEVRP is presented as a three-index mixed integer programming model:

$$\min_z J(z) := \min \sum_{k \in K} \sum_{i \in N_0, j \in N_{n+1}, i \neq j} E[t_{ij}^k] x_{ij}^k + \sum_{i \in U'} E[s_i] + \sum_{i \in U'} E[w_i | \Lambda_i = 0] \quad (1)$$

$$\text{s.t.} \sum_{k \in K} \sum_{j \in N_{n+1}, i \neq j} x_{ij}^k = 1, \quad \forall i \in C \quad (2)$$

$$\sum_{k \in K} \sum_{j \in N_{n+1}, i \neq j} x_{ij}^k \leq 1, \quad \forall i \in R' \quad (3)$$

$$\sum_{i \in N_{n+1}, i \neq j} x_{ji}^k - \sum_{i \in N_0, i \neq j} x_{ij}^k = 0, \quad \forall j \in N, \forall k \in K \quad (4)$$

$$e_j \leq E[\tau_j] \leq l_j, \quad \forall j \in N_{0,n+1} \quad (5)$$

$$E[\tau_i] + (E[t_{ij}] + s_i) x_{ij}^k - l_0(1 - x_{ij}^k) \leq E[\tau_j], \quad \forall k \in K, \forall i \in C_0, \forall j \in N_{n+1}, i \neq j \quad (6)$$

$$E[\tau_i] + E[t_{ij}^k] x_{ij}^k + g^k(Y^k - y_i^k) - (l_0 + g^k Y^k)(1 - x_{ij}^k) \leq E[\tau_j], \quad \forall K \in K, \forall i \in U', \forall j \in N_{n+1}, i \neq j \quad (7)$$

$$q_j^k \leq q_i^k - d_i x_{ij}^k + Q^k(1 + x_{ij}^k), \quad \forall k \in K, \forall i \in N_0, \forall j \in N_{n+1}, i \neq j \quad (8)$$

$$0 \leq q_j^k \leq Q^k, \quad \forall k \in K, \forall j \in N_{0,n+1} \quad (9)$$

$$0 \leq y_j^k \leq y_i^k - (E[e^k]d_{ij})x_{ij}^k + Y^k(1 - x_{ij}^k), \quad \forall k \in K, \forall i \in C, \forall j \in N_{n+1}, i \neq j \quad (10)$$

$$0 \leq y_j^k \leq Y^k - (E[e^k]d_{ij})x_{ij}^k, \quad \forall k \in K, \forall i \in U'_0, \forall j \in N_{n+1}, i \neq j \quad (11)$$

$$y_0^k = Y^k \quad \forall k \in K \quad (12)$$

$$x_{ij}^k \in \{0, 1\} \quad \forall i \in N_0, j \in N_{n+1}, i \neq j, \forall k \in K \quad (13)$$

This is a minimization problem with an objective function (1) that consists of XXXX terms. The XXXX and XXXX terms are the total travel time and the total charging time, respectively. According to Montoya et al. (2017), by including the sum of the charging time in the objective function, one can capture better the impact of charging operations. The XXXX term counts the total waiting time at charging stations. This is particular important when the availability of charging stations is uncertain and the vehicles have, therefore, to wait before being recharged. Constraints (2) assure that each customer is visited by one incoming and one outgoing vehicle. Constraints (3) mean that a charging station is visited at most once and that it does not necessary need to be visited by a vehicle. Flow conservation is guaranteed by constraints (4). Constraints (5) ensure that the start time of a service τ_i at a node i has to be within its time window. Constraints (6) and (7) track the start time of a service and show the difference between customers and charging stations nodes regards service times. If the previous node is either a customer or the depot, constraints (6) consider the service time, while constraints (7) consider the charging time if the previous node is a charging station. The charging time of vehicle type k is calculated based on its charging rate g^k , its maximum energy capacity Y^k , and its remaining battery level when it arrives at the charging station i (y_i^k). Constraints (8) guarantee that the demand of every customer is satisfied. Vehicle capacity restrictions are expressed by constraints (9). Constraints (10) and (11) not only trace the battery level of the vehicle type k based on its energy consumption as it tours arc i, j and its maximum energy capacity but also secure that its remaining battery level is always positive in any node. Constraints (12) secure that the battery level of any vehicle is full at the depot. Finally, the domain of the decision variables is defined by constraints (13).

4 Solution approach

In this section, we describe the proposed solution approach. Our approach is based on the MSA. The key idea behind MSA is to continuously generate and solve scenarios. In MSA, online decisions are made according to a distinguished plan which evolves over time (Bent & Hentenryck 2004). Figure 2 displays a high level flow diagram of the proposed solution approach. It contains mainly five stages. These stages are described in the next sections.

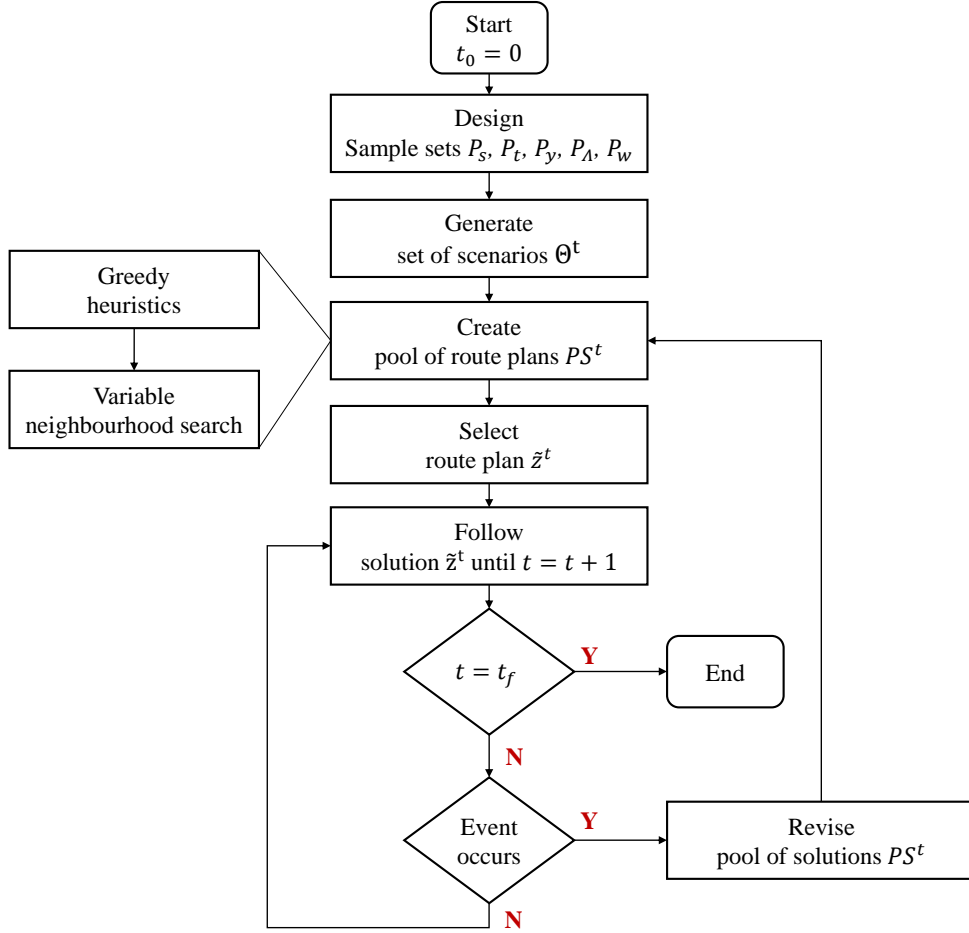


Figure 2: A dynamic approach for the DHEVRP

4.1 Stage 1: sample sets design

In the first stage, we obtain one set of samples of each stochastic input by using Monte Carlo sampling and the probability distributions that model the uncertain input. Thus, five sample sets are generate

$$P_s = \{p_s^m = (s_1^m, s_2^m, s_3^m \dots, s_c^m) \mid m = 0, \dots, \beta\}, \quad (14)$$

$$P_t = \{p_t^m = (t_{01}^m, t_{02}^m, t_{03}^m \dots, t_{n(n-1)}^m) \mid m = 0, \dots, \beta\}, \quad (15)$$

$$P_y = \{p_y^m = (y_0^{1,m}, y_0^{2,m}, y_0^{3,m} \dots, y_0^{k,m}) \mid m = 0, \dots, \beta\}, \quad (16)$$

$$P_\Lambda = \{p_\Lambda^m = (\Lambda_1^m, \Lambda_2^m, \Lambda_3^m \dots, \Lambda_r^m) \mid m = 0, \dots, \beta\}, \quad (17)$$

$$P_w = \{p_w^m = (w_1^m, w_2^m, w_3^m \dots, w_r^m) \mid m = 0, \dots, \beta\}. \quad (18)$$

Sets (14), (15), (16), (17), and (18) represent service time, travel time, remaining battery energy level, availability of CS, and waiting time at CS sample set, respectively. A service time sample p_s^m defines one value for s_i , $\forall i \in C$. Thus, $|p_s^m| = |C|$. In the case of the travel time sample set, a sample p_t^m specifies one value for t_{ij} , $\forall i, j \in A$, $i \neq j$. Hence, $|p_t^m| = |A|$. The number of elements in p_y^m differs at **Step 1** and **Step 4**. At $t_0 = 0$, all vehicles in the fleet are located at the depot ($i = 0$), and there has not been en-route energy consumption. Therefore, one sample p_y^m defines one value of battery energy level for each vehicle type k , i.e. $|p_y^m| = |K|$. We consider two cases for the battery energy level at $t_0 = 0$. These cases are described in **Section 6**. On the other hand, at **Step 4**, EVs have visited different customers, so $|p_y^m| = k \cdot |C|$. Sample p_Λ^m determines one probability for each CS, while p_w^m states one value for w_i , $\forall i \in R$. Thus, $|p_\Lambda^m|, |p_w^m| = |R|$. We consider three cases for the availability of CS, and consequently waiting time at CS. These cases are also described in **Section 6**.

4.2 Stage 2: set of scenarios generation

In the second stage, the set of scenarios $\Theta^t = (\theta_1^t, \theta_2^t, \dots, \theta_\beta^t)$ is created. Each scenario is generated by randomly selecting one sample in every sample set, e.g. $\theta_{64}^t = (p_s^{50}, p_t^4, p_y^{10}, p_\Lambda^{33}, p_w^{27}, N, A)$. All the scenarios in Θ^t have the same set of nodes N and set of arcs A . That is to say, every scenario is a deterministic instance of the stochastic problem.

4.3 Stage 3: pool of solutions creation

In the third stage, all β scenarios in the set Θ^t are solved, creating the pool of solutions $PS^t = (z_1^t, z_2^t, \dots, z_\beta^t)$. Since every scenario in the set is a deterministic instance of the DHEVRP, we can make use of well-established heuristics to solve them. We adopt two heuristics to solve all the scenarios, a greedy algorithm and a randomized variable neighbourhood search (VNS). These heuristics are explained as follows.

The greedy algorithm is used to calculate the initial solution. Its pseudocode is displayed in **Algorithm 1**. In this method, a customer $i \in C$ is allocated to the EV route r^k that has traveled time $J(r^k)$ closer to the time window of the request $[e_i; l_i]$ (Step 5). A customer's request is only added to a route when feasibility can be maintained with respect to remaining battery energy level y_i^k and EV capacity q_i^k . If customer i cannot be added to route r^k because of battery energy level feasibility (Step 6), the CS $u_j \in U'$ with lowest sum of the distance to the current customer c_{ij} plus waiting time w_j is inserted in the EV route (Step 8). This CS is then removed from the list of available CS (Step 10). Since we do not adopt fully charged setting, one has to decide how much to recharge when the EV stops at the CS. As explained before, in this paper we follow that the decision on how much to recharge the battery of any EV at any CS is based on the rest of the customers to be attend by this EV. Nevertheless, this procedure is impracticable at this stage. The initial route plan is being constructed, and not all the customers have, therefore, been assigned to the EVs. We thus create three scenarios that will guide this decision during the creation of the initial route plan. These scenarios are described in **Section 6**. If customer i cannot be allocated to route r^k due to capacity feasibility (Step 13), the EV returns to the depot and it is removed from the list of available EVs (Step 16). The greedy method repeats these steps until all the customers are designated to EV routes. The solution outputted by the greedy method z_g is improved by the VNS.

We implement a VNS modified from the VNS proposed by Mladenović & Hansen (1997). The pseudocode of the VNS is displayed in **Algorithm 2**. VNS requires the determination of three components: shaking procedure, local search procedure, and stopping criteria. For the shaking procedure, a list of neighbourhood structure must be define. The list of neighbourhood structures $M = \{m_1, m_2, m_3, \dots, m_{max}\}$ is a finite set of neighbourhood structures whose $m_1(z')$, for instance, is the set of solutions in the 1st neighbourhood of the solution z' . To define a neighbourhood of the solution z a combination of operators must be specified. We create a list of four operators $O = \{o_1, o_2, o_3, o_4\}$. The o_1 (1-0 exchange move) operator removes a customer from its original route and inserts it after other in a different route. The o_2 (1-1 exchange move) operator swaps two customers in the same route, whereas the o_3 (2-opt move) operator swaps two customers in different routes. The o_4 (CROSS-exchange) (Taillard et al. 1997) operator exchanges two arcs of different routes. All operators are used to determine the set of neighbourhood structures M . We use the randomized variable neighborhood descent (RVND) method (Hansen et al. 1997) as the local search procedure and define the number of iterations ($iterMax = 1000$) without improvement on the current solution as the stop criteria. VNS starts by generating a neighbour z^a of the incumbent solution z' at random from the k^{th} neighbourhood ($z^a \in m_k(z')$). Following, the local procedure is applied to improve the solution z^a . In order to do so, the RVND uses a list of neighbourhood structures $V = \{v_1, v_2, v_3, \dots, v_{max}\}$. First, one neighbourhood structure is randomly selected (Step 8). After that, the best solution in this neighbourhood structure z^b is found by using the strategy first improvement (Step 9). If z^b is better than the solution z^a (Step 10), then z^b is returned as the best solution. If not, this neighborhood structure is removed from the list (Step 14). This procedure is executed until the list V becomes empty. If the best solution found in the local procedure is not better than the incumbent solution z' , VNS starts again with a new neighbourhood structure. These steps are repeated until the stop criteria is met.

Algorithm 1 Greedy algorithm

INPUT: N, A, K **OUTPUT:** z_g

```
1: Initialize  $r^k$ 
2:  $G \leftarrow C, H \leftarrow U', I \leftarrow K, z_g = \emptyset, \gamma_1^k = 0$  and  $J(r^k) = 0 \forall k \in K, position = 1$ 
3: while  $G \neq \emptyset$  do
4:    $position = position + 1$ 
5:   Select customer  $i \in C$  and EV type  $k \in K$  based on  $[e_i; l_i]$  and  $J(r^k)$ 
6:   if  $y_i^k \leq 0$  then
7:     Compute  $c_{\gamma_{(position-1)j}}$  and  $w_j \forall j \in H$ 
8:     Select  $u_j \in U$  with lowest  $c_{\gamma_{(position-1)j}} + w_j$ 
9:     Allocate  $u_j$  to  $r^k, J(r^k) = J(r^k) + c_{\gamma_{(position-1)j}} + w_j$ 
10:     $H \leftarrow H \setminus \{u_j\}$ 
11:    Recharge battery of EV  $k$  according to chosen scenario
12:  else if then
13:    if  $q_i^k \leq 0$  then
14:      Go to the depot,  $\gamma_{position} \leftarrow 0, position \leftarrow 0$ 
15:      Add route  $r^k$  to route plan  $z_g$ 
16:       $I \leftarrow I \setminus \{k\}$ 
17:    else if then
18:      Allocate customer  $i$  to  $r^k, \gamma_{position} \leftarrow i, J(r^k) = J(r^k) + c_{(\gamma_{position-1})\gamma_{position}}$ 
19:       $G \leftarrow G \setminus \{i\}$ 
20:    end if
21:  end if
22: end while
```

4.4 Stage 4: route plan selection

In this stage, we select the solution to be followed by the electric vehicles to attend all the customers. After the pool of route plans is created, the route plan with the smallest objective function (1) value \tilde{z}^t is selected out of the pool PS^t at each time t . The route plan \tilde{z}^t is then followed by the electric vehicles until a new event occurs.

4.5 Stage 5: solution pool revision

When an event occurs the pool of solutions must be revised. The possible events are described in the following. Although each event is solely explained, many of them can happen at the same time.

- **Electric vehicle arrival at customer.** When an electric vehicle type k arrives at customer $j \in C$ coming from node $i \in N$, the true values of two stochastic inputs are disclosed: travel time and remaining battery energy level.
- **Electric vehicle arrival at charging station.** Apart from the true values of the travel time and remaining battery level, the real availability of the CS is also revealed when an EV type k arrives at charging station $i \in U$ coming from customer $i \in C$.
- **Electric vehicle departure from a charging station.** The true values of both the waiting time w_i and the charging time s_i are disclosed when an EV departs from a charging station $i \in U$.

The pool P^t is updated by removing the route plans that are incompatible with the current system status. For instance, if route plan \tilde{z}^t specifies that EV type k must proceed to customer j after visiting customer i , but the event **electric vehicle arrival at customer** i shows that the remaining battery level is not enough to reach customer j , all solutions in P^t that determine the arrival at j after i are deleted from the pool. Since the solution approach always keeps β solutions in the pool at each time t , the same amount of deleted solutions must be created. For updating the pool, first the sample sets and then the set of scenarios Θ^t must be updated,

Algorithm 2 Variable neighbourhood search

INPUT: z_g, N, A, K **OUTPUT:** z

```
1: Initialize  $M, O, V$ 
2:  $z_{best} \leftarrow z_g, z' \leftarrow z_g$ 
3: while  $iterMax \leq 1000$  do
4:    $k \leftarrow 1$ 
5:   for  $k = 1$  to  $max$  do
6:     Generate a solution  $z^a$  of  $z'$  at random in  $m_k(z)$ 
7:     while  $V \neq \emptyset$  do
8:        $l \leftarrow U[1; |V|]$ 
9:       Find the best solution  $z^b$  in  $v_l(z^a)$  via descendent method
10:      if  $J(z^b) \leq J(z^a)$  then
11:         $z^a \leftarrow z^b$ 
12:         $z_{best} \leftarrow z^a$ 
13:      else if then
14:         $V \leftarrow V \setminus \{v_l\}$ 
15:      end if
16:    end while
17:    if  $J(z') \leq J(z_{best})$  then
18:       $z_{best} \leftarrow z'$ 
19:       $iterMax = iterMax + 1$ 
20:       $k = k + 1$ 
21:    else if then
22:       $z' \leftarrow z_{best}$ 
23:    end if
24:  end for
25:   $z \leftarrow z_{best}$ 
26: end while
```

i.e. the solution approach return to **Stage 1**. It is important to mention that the stochastic inputs that have been disclosed before t do not need to be sampled again in **Stage 1** at time t .

5 Dataset design

We evaluate the performance of our solution approach in set of instances adapted from the dataset of Solomon (1987). We also compare our dynamic solution approach with a static solution approach in terms of quality of the solutions and computational time. Our dataset contains 56 instances. The inputs number of nodes N , customer locations C , demands d_i , travel times t_{ij}^k , and service times s_i are taken from these instances. For the representation of the uncertain travel times, we assume that the values defined in the Solomon's instances represent the expected values, and we randomly generate the variances. The same procedure is followed for the customer service times.

For creating the fleet of heterogeneous electric vehicles, we select some of the EVs described in NSR Compilation report (2013). Because this report does not present the charging rates of the EVs, we have to generate them. According to (Montoya et al. 2017), for a battery capacity of 22 kWh, the minimum charging time is 0.50 h, i.e. $g^k = 0.02$. Therefore, we randomly generate the charging rates in $[0.02; 0.06]$. The details of the vehicles are displayed in Table 1.

Name	Q^k (kg)	Y^k (kWh)	e^k (kWh/km)	g^k (h/kWh)
German E-Cars Pantos	1.000	38,60	0,25	0.05
Citroën Berlingo	500	23,50	0,22	0.03
Mercedes Vito E-CELL	900	36,00	0,22	0.04
Renault Kangoo Z.E.	595	22,00	0,17	0.02
Renault Kangoo Rapid Maxi Z. E.	650	22,00	0,18	0.02
Smith Electric Newton Edison	3.500	36,00	0,30	0.04
Smith Electric Newton Newton	2.800	40,00	0,80	0.05
Aixam Mega Multitruck	500	60,00	0,22	0.06

Table 1: Specifications of the available electric vehicles

For selecting the number of charging stations $|R|$, we adopt $|R| = \lfloor 0,1 \cdot |N| \rfloor$. We locate charging stations at randomly drawn nodes and one additional station at the depot. For the representation of the charging station availability and consequent waiting times, we create three scenarios. These scenarios are described in **Section 6**.

6 Cases configuration

6.1 Scenarios based on charging strategy at construction of initial route plan

charge to 1 (100%) every time an EV stops at a CS charge to 0.75 (75%) every time an EV stops at a CS charge to 0.50 (50%) every time an EV stops at a CS

6.2 Scenarios based on charging station availability

For the representation of the charging station availability, we create three scenarios. In *Scenario A.1*, the CS are always available and have long waiting times. The waiting times (hours) are assumed to be uniform distributed $w_i \sim U[1, 50; 2, 50]$. In *Scenario A.2*, the CS are available half of the time and have $w_i \sim U[1, 00; 1, 50]$. In *Scenario A.3*, the charging stations are less likely to be available but have shorter waiting times ($w_i \sim U[1, 50; 2, 50]$).

6.3 Scenarios based on initial setup

INITIAL BATTERY ENERGY LEVEL ($t = 0$) all values in the samples in the set of battery energy level are equal to 1 in the *Scenario B.1*. In *Scenario B.2*, for initializing the set of battery energy level samples, we randomly generate the values in $[0.5; 1]$ for each electric vehicle in the fleet, i.e. $y_0^k \sim U[0.5; 1] \forall k \in K$

Two types of scenarios. In the first scenario (*Scenario B.1*), the vehicles leave the depots with their batteries fully charged, whereas in the second scenario (*Scenario B.2*), the batteries are not fully charged when the vehicles leave the depot.

7 Computational results

8 Conclusions

Acknowledgements

Conflict of Interest

The authors declare that there is no conflict of interest regarding the publication of this paper.

References

- Bent, R. & Hentenryck, P. V. (2004), ‘Scenario-based planning for partially dynamic vehicle routing with stochastic customers’, *Operations Research* **52**(6), 977–987.
- Bi, X. & Tang, W. K. S. (2019), ‘Logistical planning for electric vehicles under time-dependent stochastic traffic’, *IEEE Transaction on Intelligent Transportation System* **20**(10), 3771–3781.
- Felipe, A., Ortuño, M. T., Righini, G. & Tirado, G. (2014), ‘A heuristic approach for the green vehicle routing problem with multiple technologies and partial recharges’, *Transportation Research Part E: Logistics and Transportation Review* **71**, 111–128.
- Hansen, P., Mladenović, N., Brimberg, J. & Moreno Pérez, J. A. M. (1997), Variable neighborhood search, in M. Gendreau & J. Potvin, eds, ‘Handbook of Metaheuristics’, 2 edn, Springer, chapter 3, pp. 61–87.
- Hiermann, G., Puchinger, J., Ropke, S. & Hartl, R. F. (2016), ‘The electric fleet size and mix vehicle routing problem with time windows and recharging stations’, *European Journal of Operational Research* **252**(3), 995–1018.
- Liu, F. H. & Shen, S. Y. (1999), ‘The fleet size and mix vehicle routing problem with time windows’, *Journal of the Operational Research Society* **50**(7), 721–732.
- Lu, J. & Wang, L. (2019), A bi-strategy based optimization algorithm for the dynamic capacitated electric vehicle routing problem, in ‘Proceedings of the IEEE Congress on Evolutionary Computation’, New Zealand.
- Mladenović, N. & Hansen, P. (1997), ‘Variable neighbourhood search’, *Computers & Operations Research* **24**(11), 1097–1100.
- Montoya, A., Guéret, C., Mendoza, J. E. & Villegas, J. G. (2017), ‘The electric vehicle routing problem with nonlinear charging function’, *Transportation Research Part B: Methodological* **103**, 87–110.
- NSR Compilation report (2013), ‘Comparative analysis of european examples of schemes for freight electric vehicles’, http://e-mobility-nsr.eu/fileadmin/user_upload/downloads/info-pool/E-Mobility_-_Final_report_7.3.pdf. Accessed: 11-24-2019.
- Pelletier, S., Jabali, O. & Laporte, G. (2019), ‘The electric vehicle routing problem with energy consumption uncertainty’, *Transportation Research Part B: Methodological* **126**, 225–255.

- Penna, P. H. V., Afsar, H. M., Prins, C. & Prodhon, C. (2016), 'A hybrid iterative local search algorithm for the electric fleet size and mix vehicle routing problem with time windows and recharging stations', *IFAC-PapersOnLine* **49**(12), 955–960.
- Schneider, M., A., S. & Goeke, D. (2014), 'The electric vehicle-routing problem with time windows and recharging stations', *Transportation Research Part B: Methodological* **48**, 465–694.
- Shao, S., Guan, W., Ran, B., He, Z. & Bi, J. (2017), 'Electric vehicle routing problem with charging time and variable travel time', *Mathematical Problems in Engineering* pp. 1–13.
- Shi, j., Gao, Y., Wang, W., Yu, N. & Ioannou, P. (2019), 'Operating electric vehicle fleet for ride-hailing services with reinforcement learning', *IEEE Transactions on Intelligent Transportation Systems* pp. 1–13.
- Solomon, M. (1987), 'Algorithms for the vehicle routing and scheduling problems with time windows', *Operations Research* **35**(2), 254–65.
- Sweda, T. M., Dolinskaya, I. S. & Klabjan, D. (2017), 'Adaptive routing and recharging policies for electric vehicles', *Transportation Science* **51**(4), 1031–1386.
- Taillard, E., Badeau, P., Gendreau, M., Guertin, F. & Potvin, J. (1997), 'A tabu search heuristic for the vehicle routing problem with soft time windows', *Transportation Science* **31**(2), 101–195.