Exam review

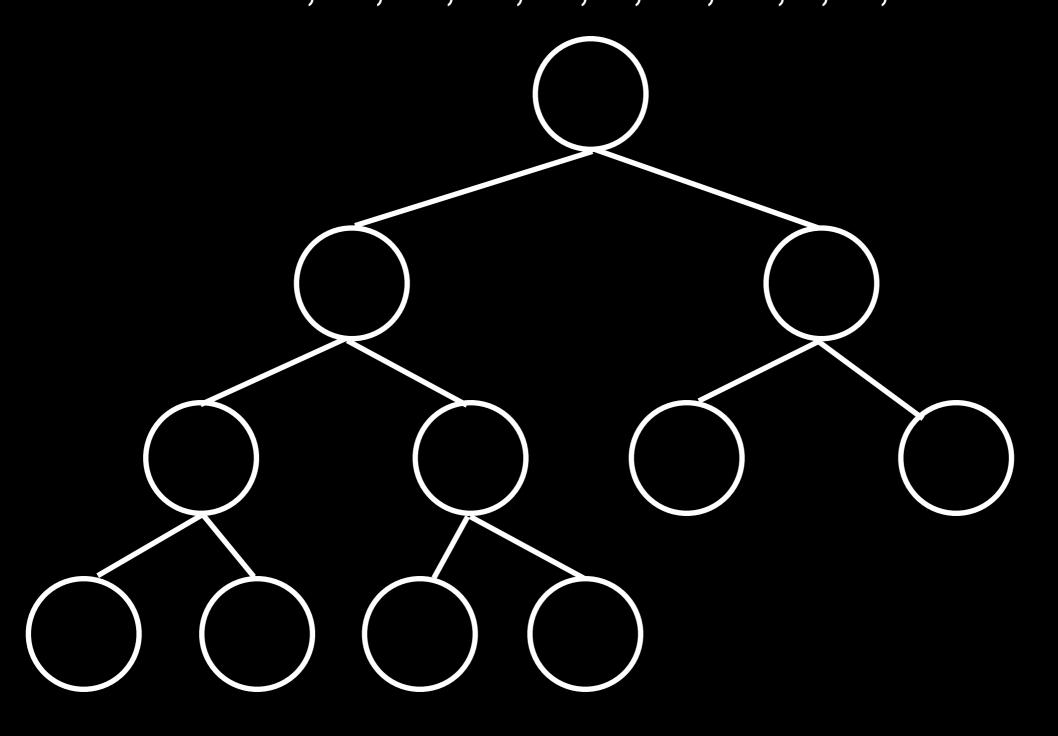
CS 261 Lab #10

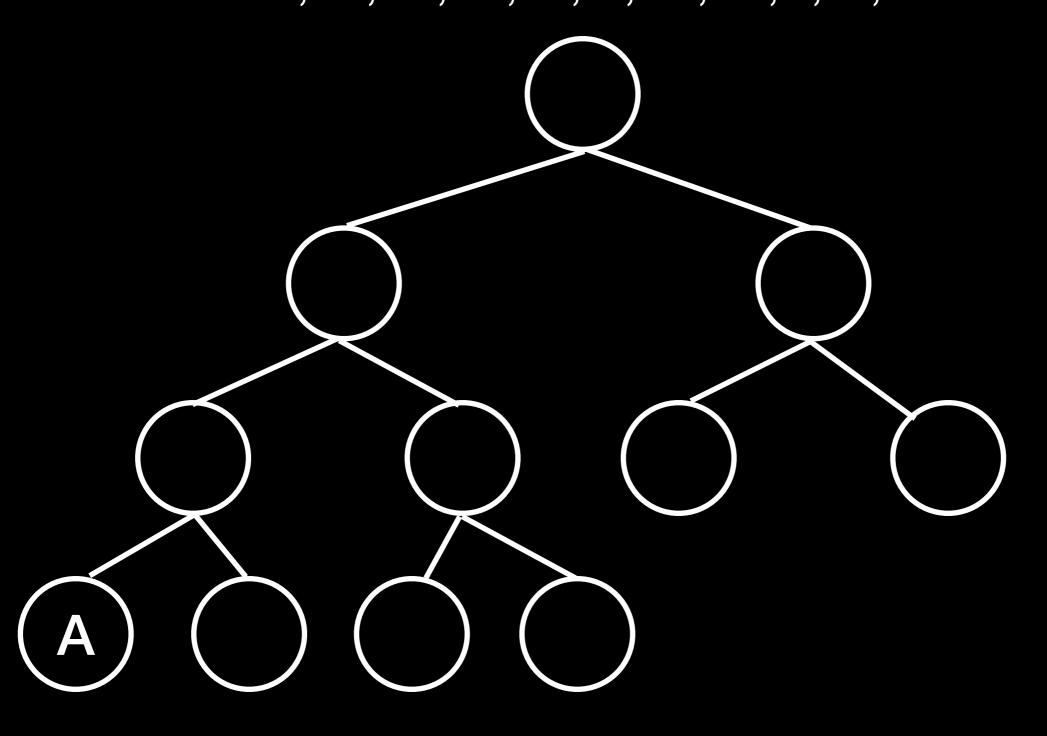


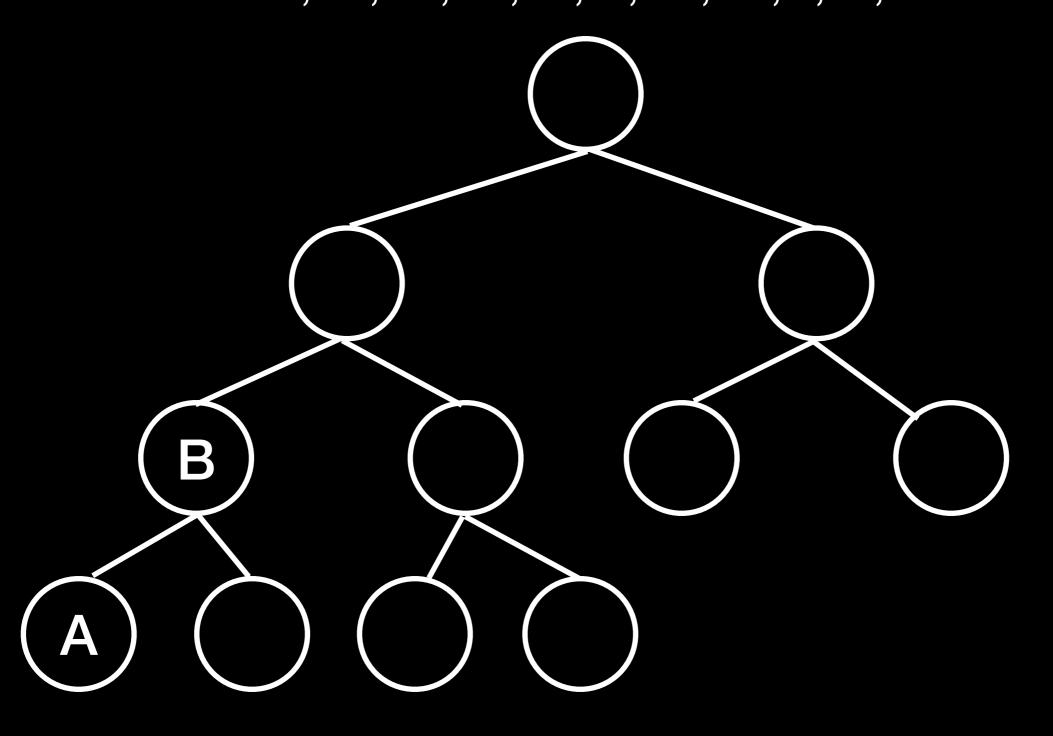
The exam will be **comprehensive** (so don't forget to review the midterm slides!)

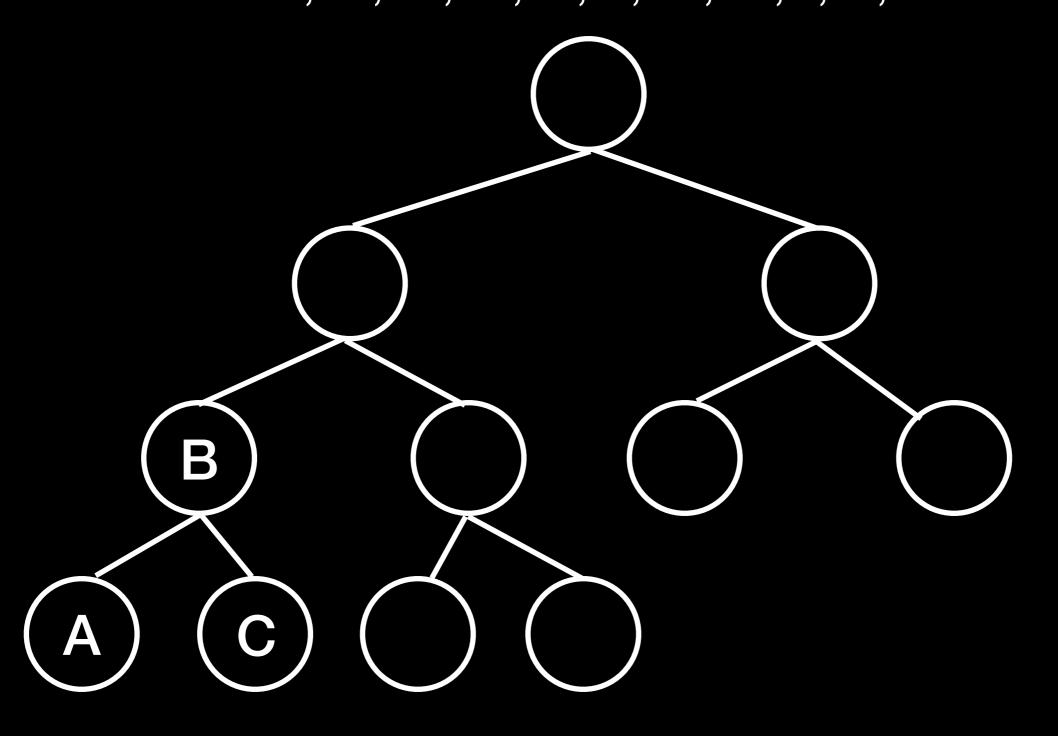
Similar style as midterm (multiple choice, matching, true/false, code)

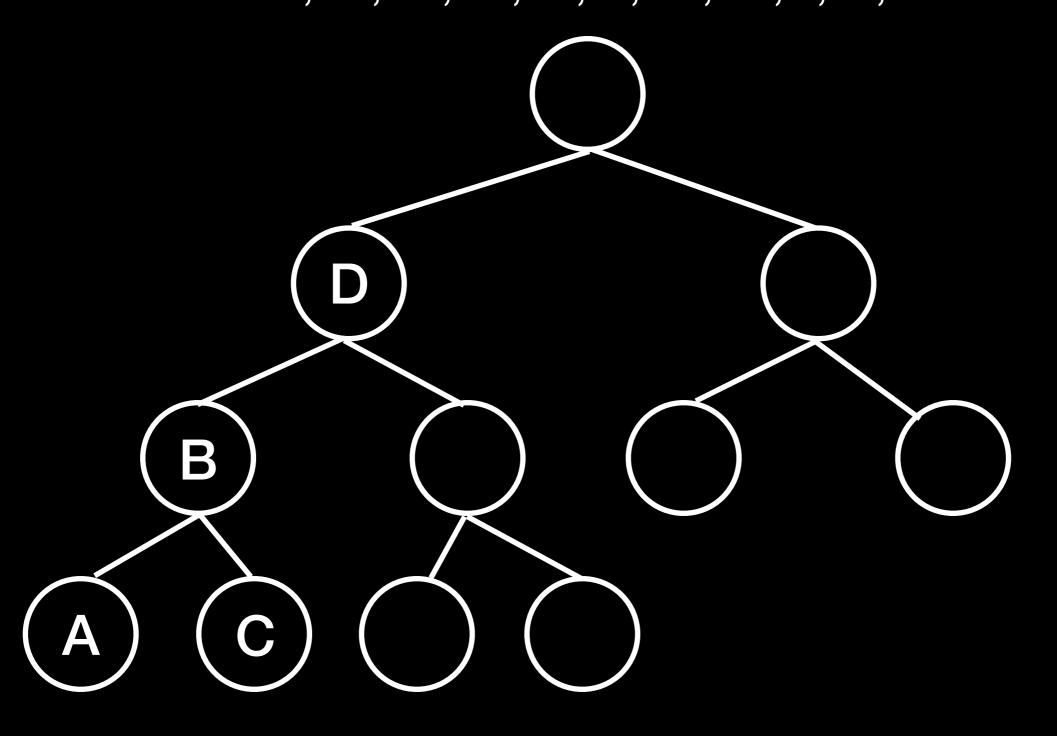
This review will focus on trees, heaps, hash tables, and graphs

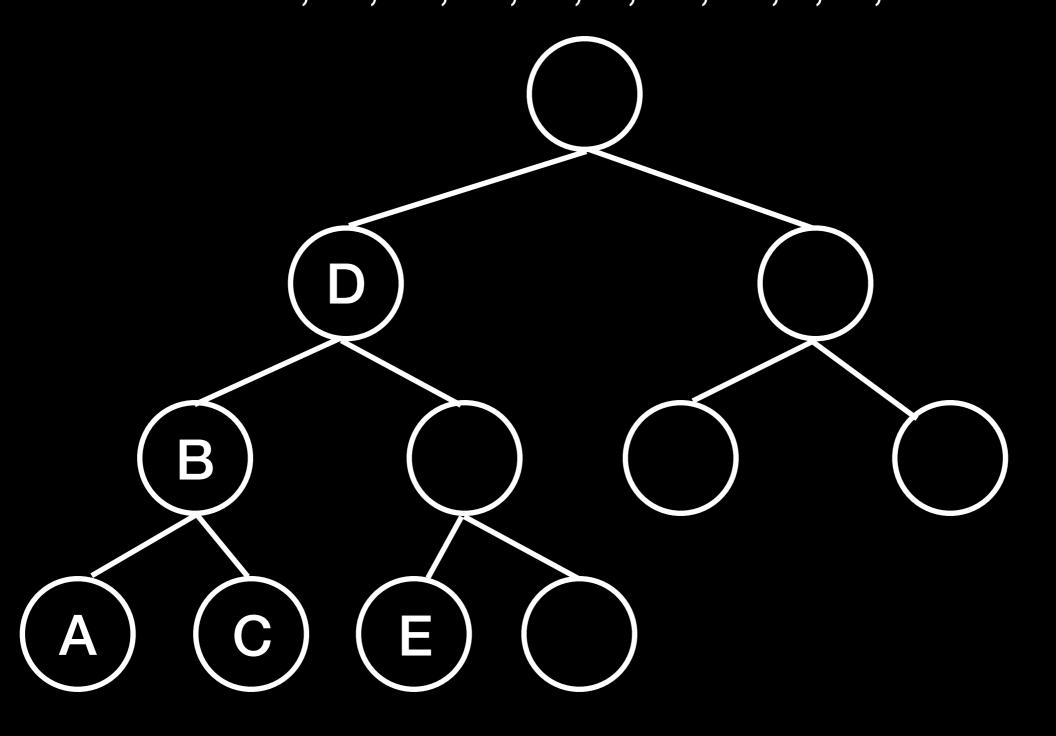


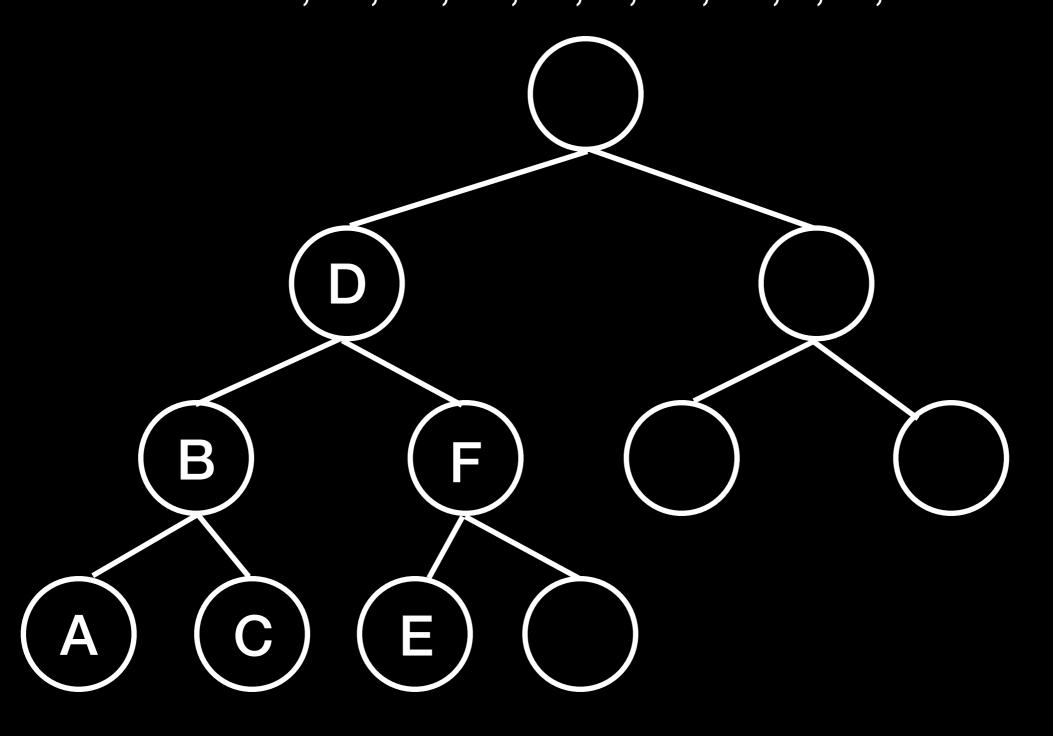


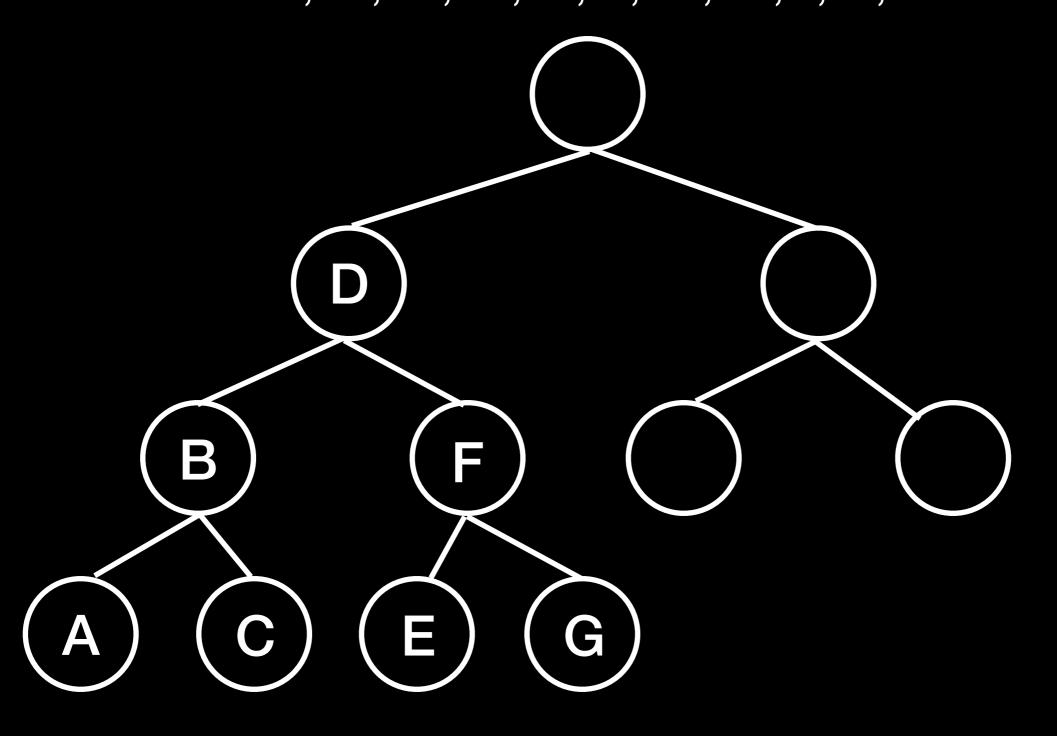


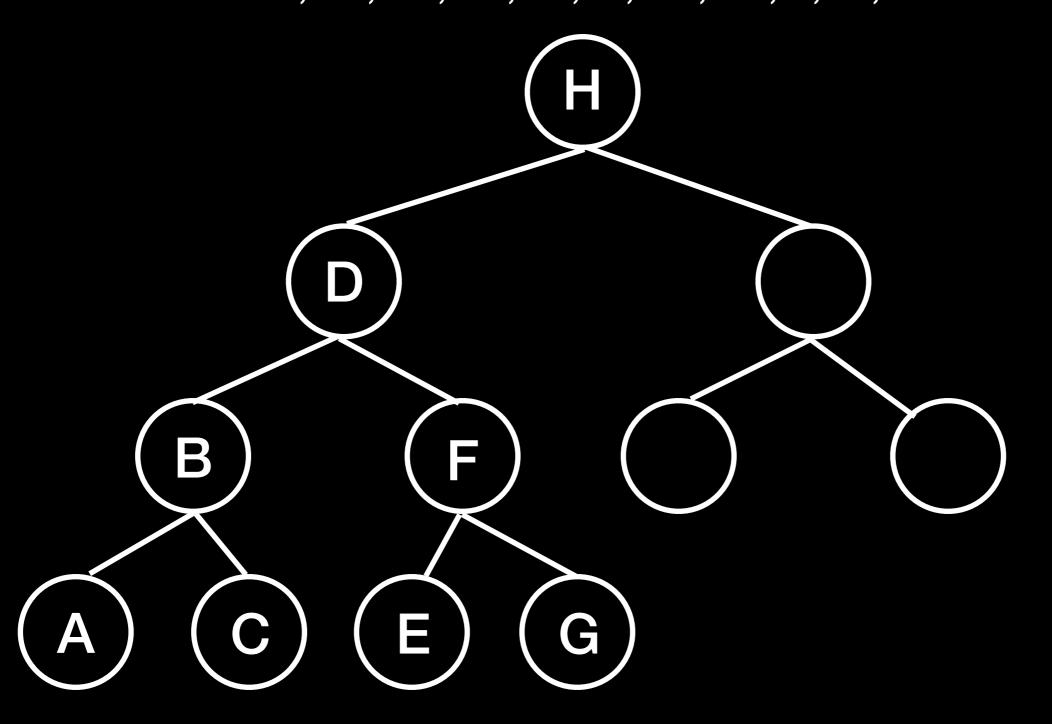


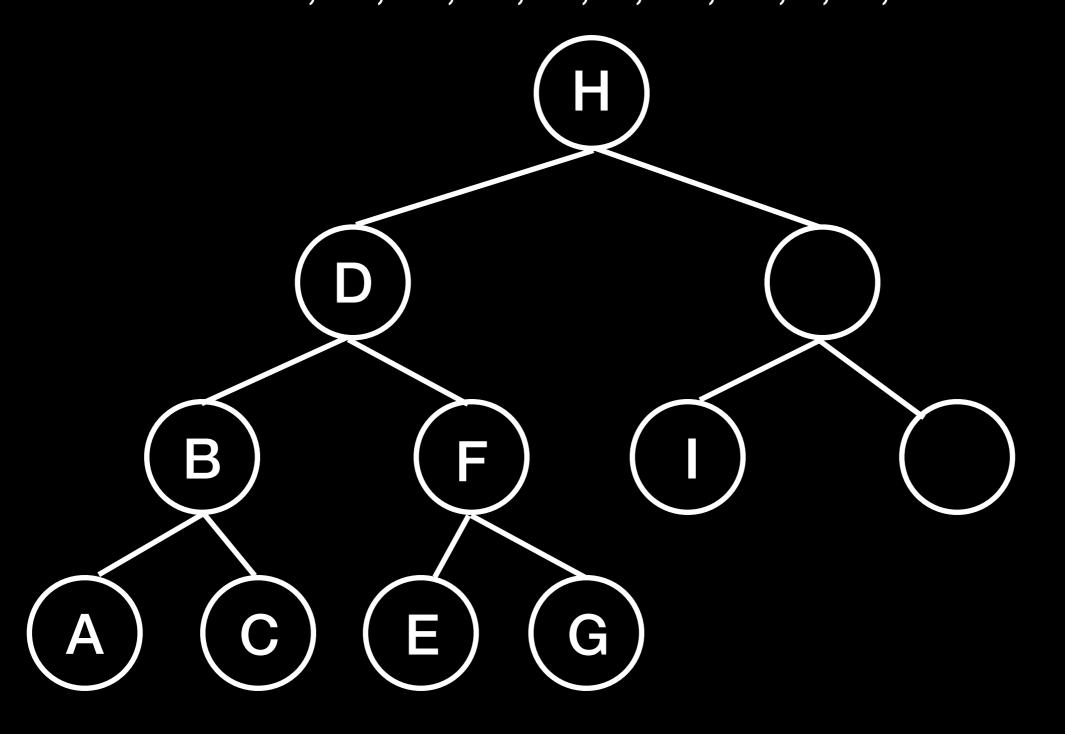


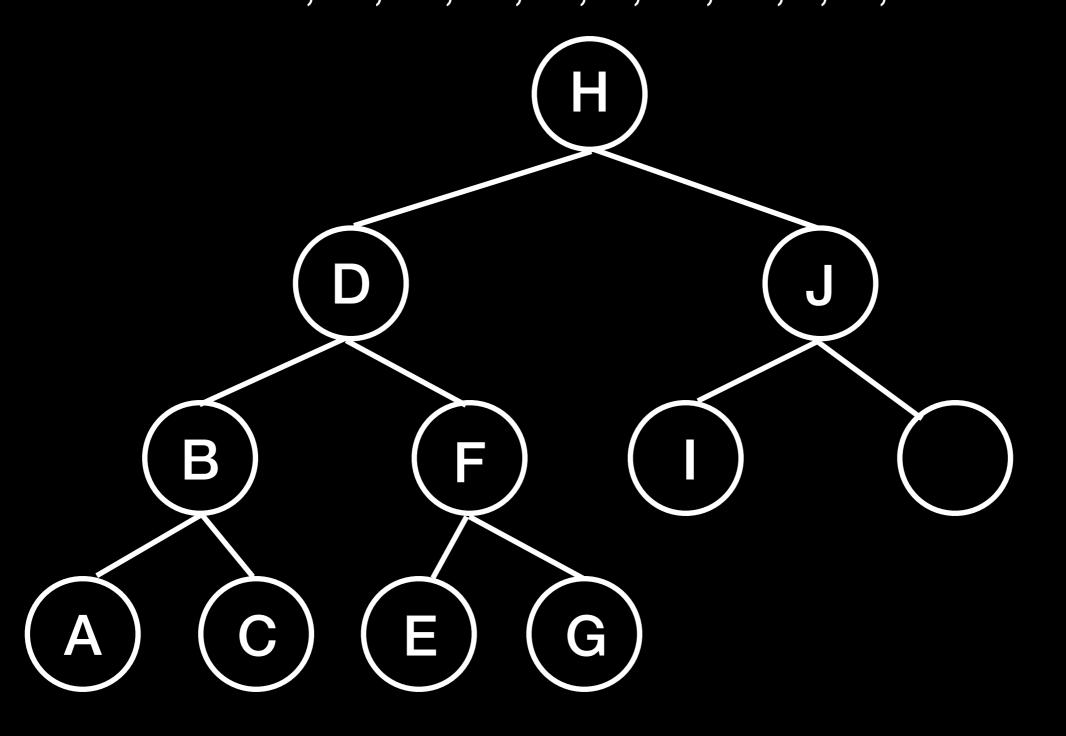


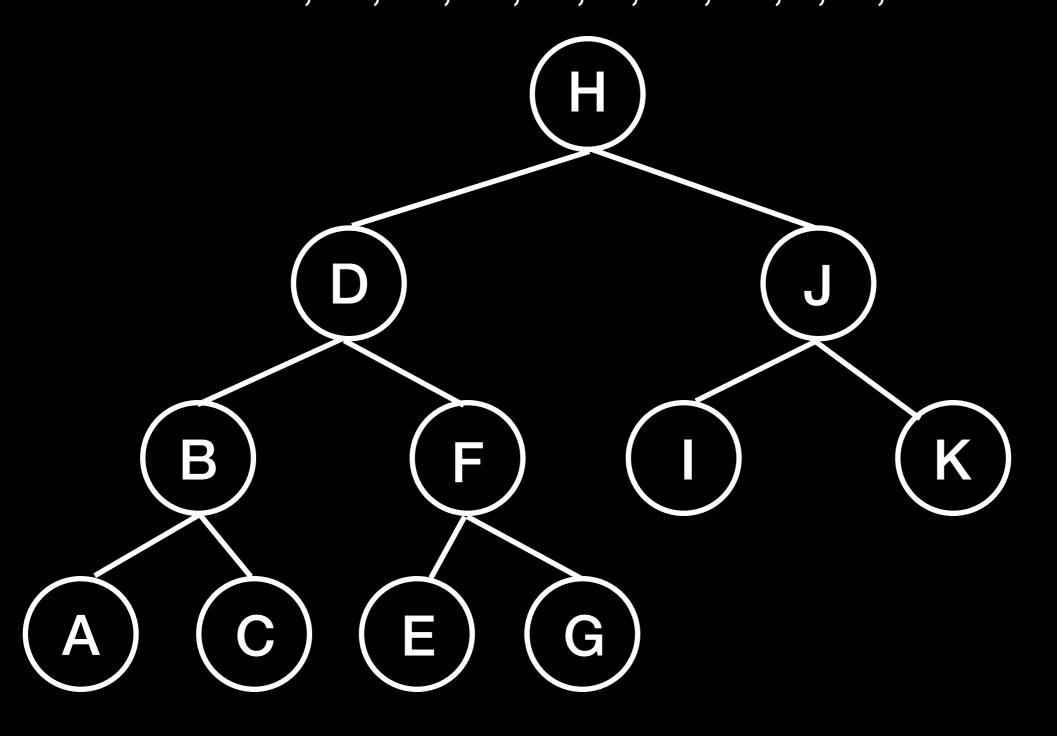


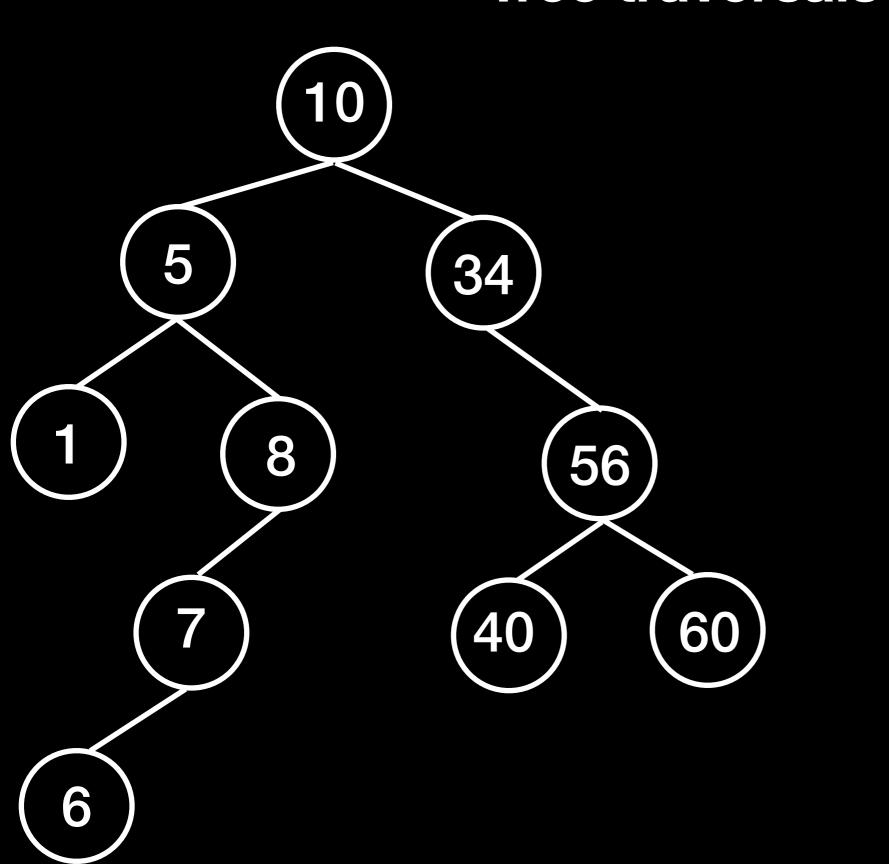


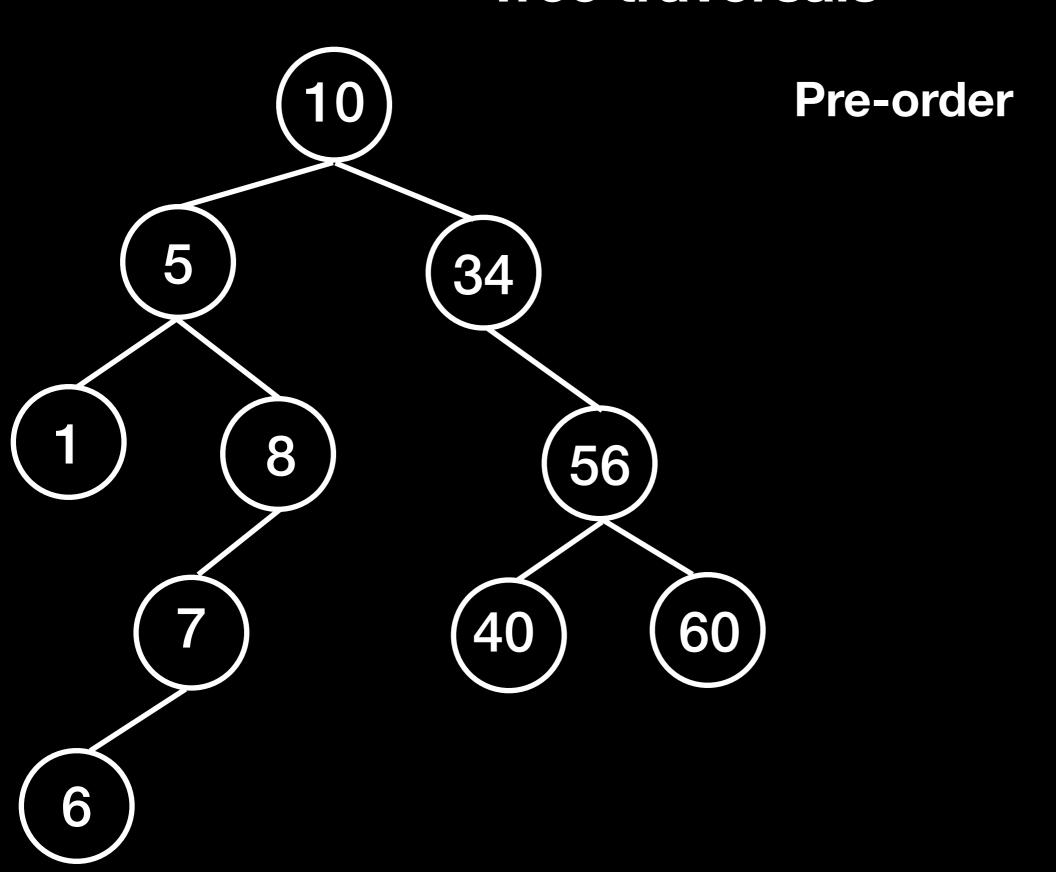


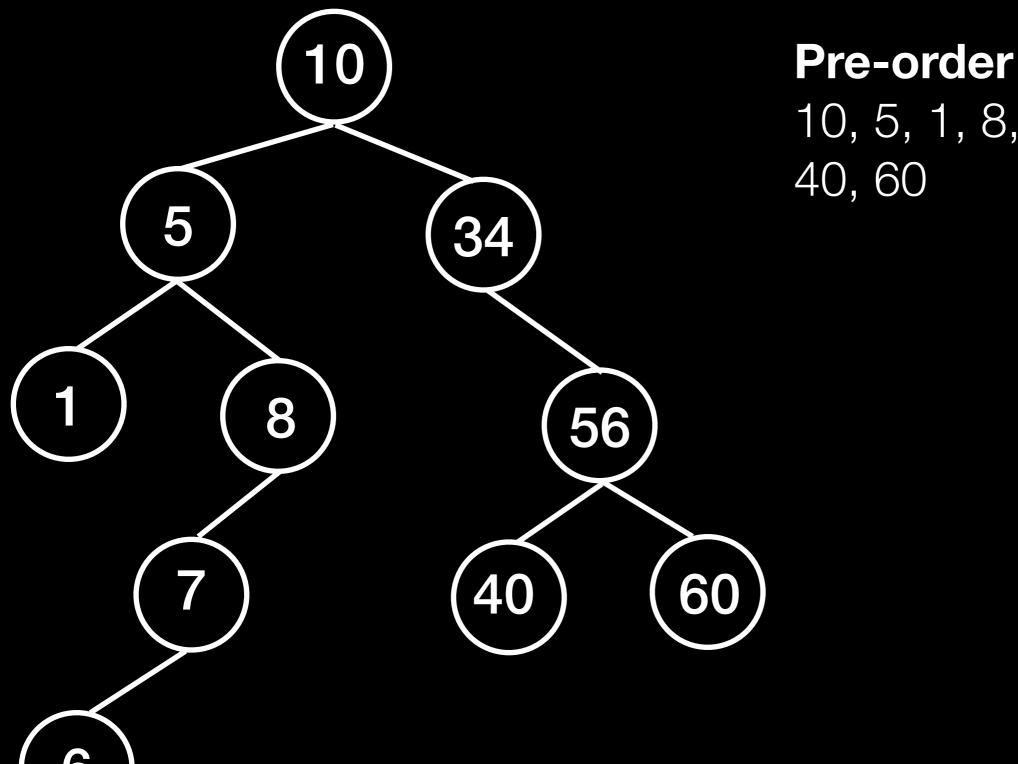




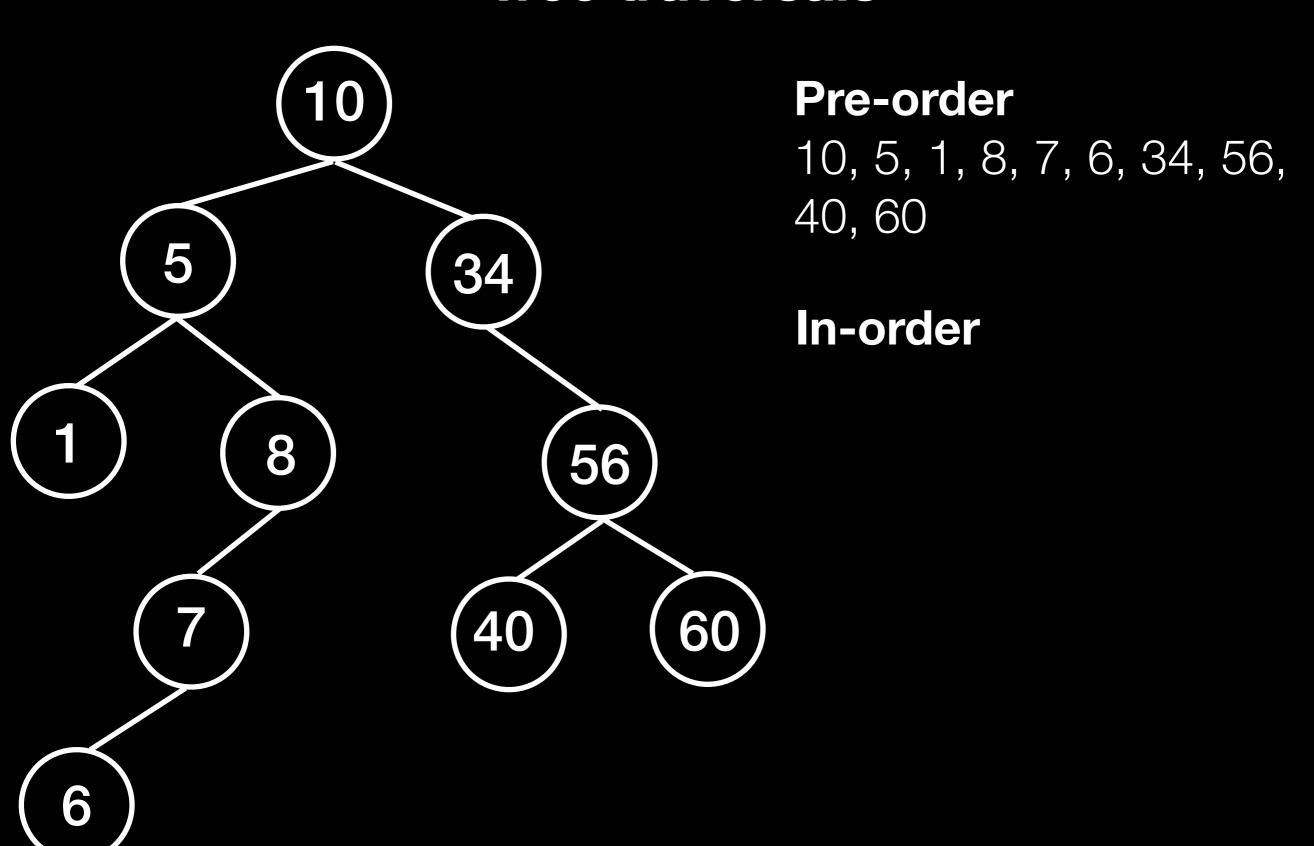


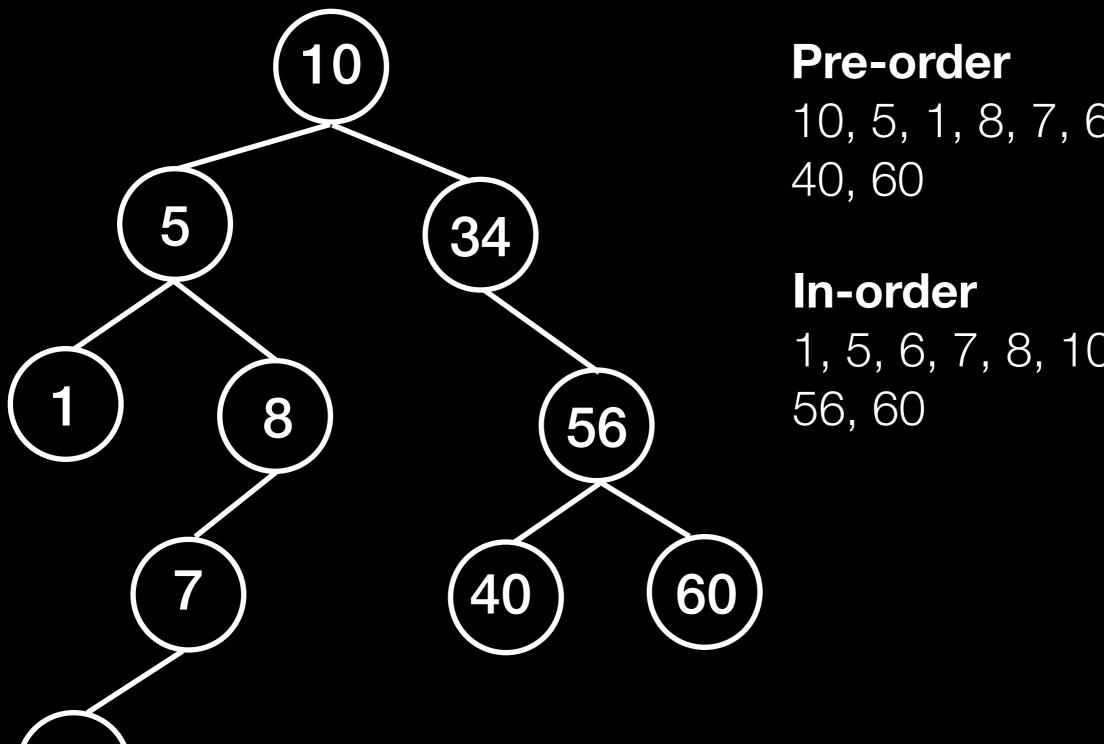






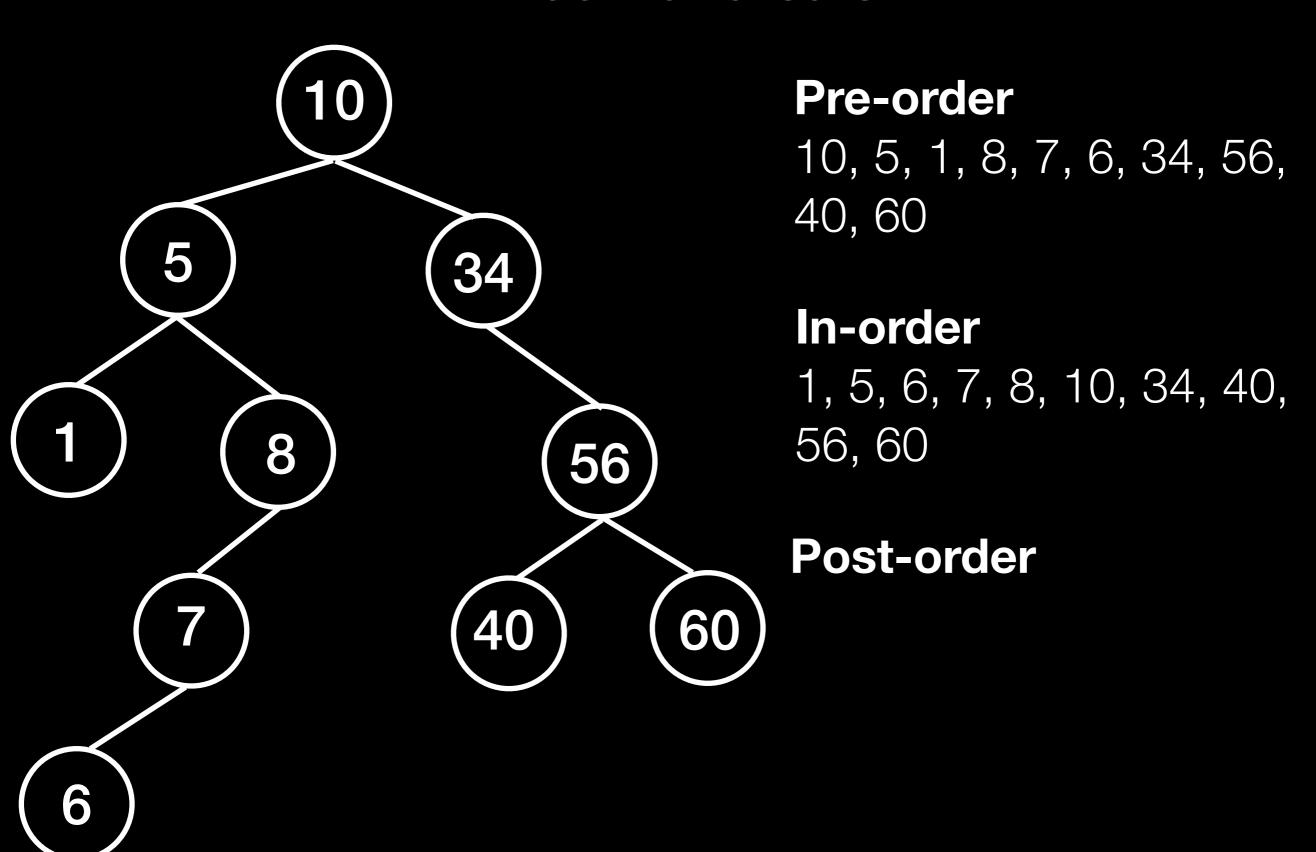
10, 5, 1, 8, 7, 6, 34, 56,

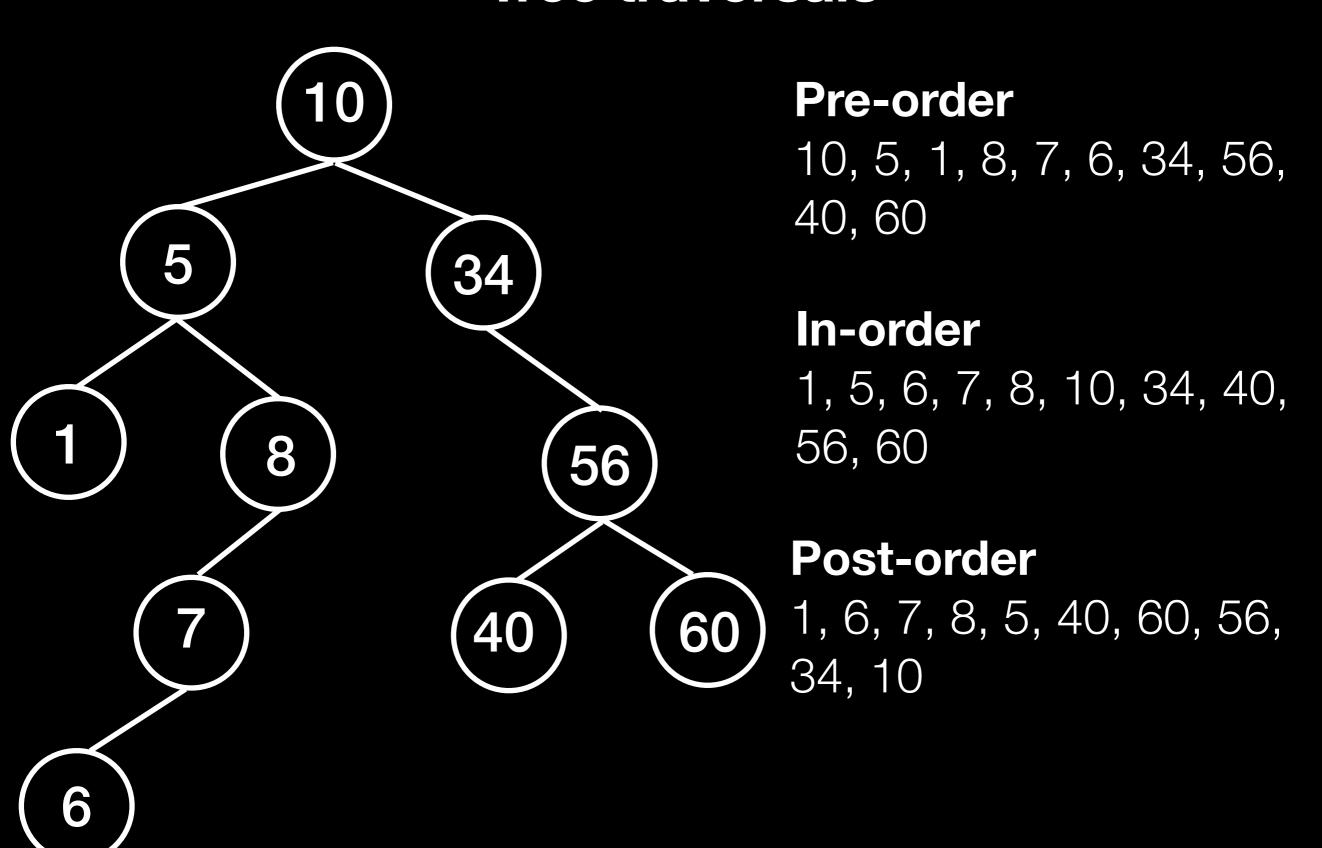


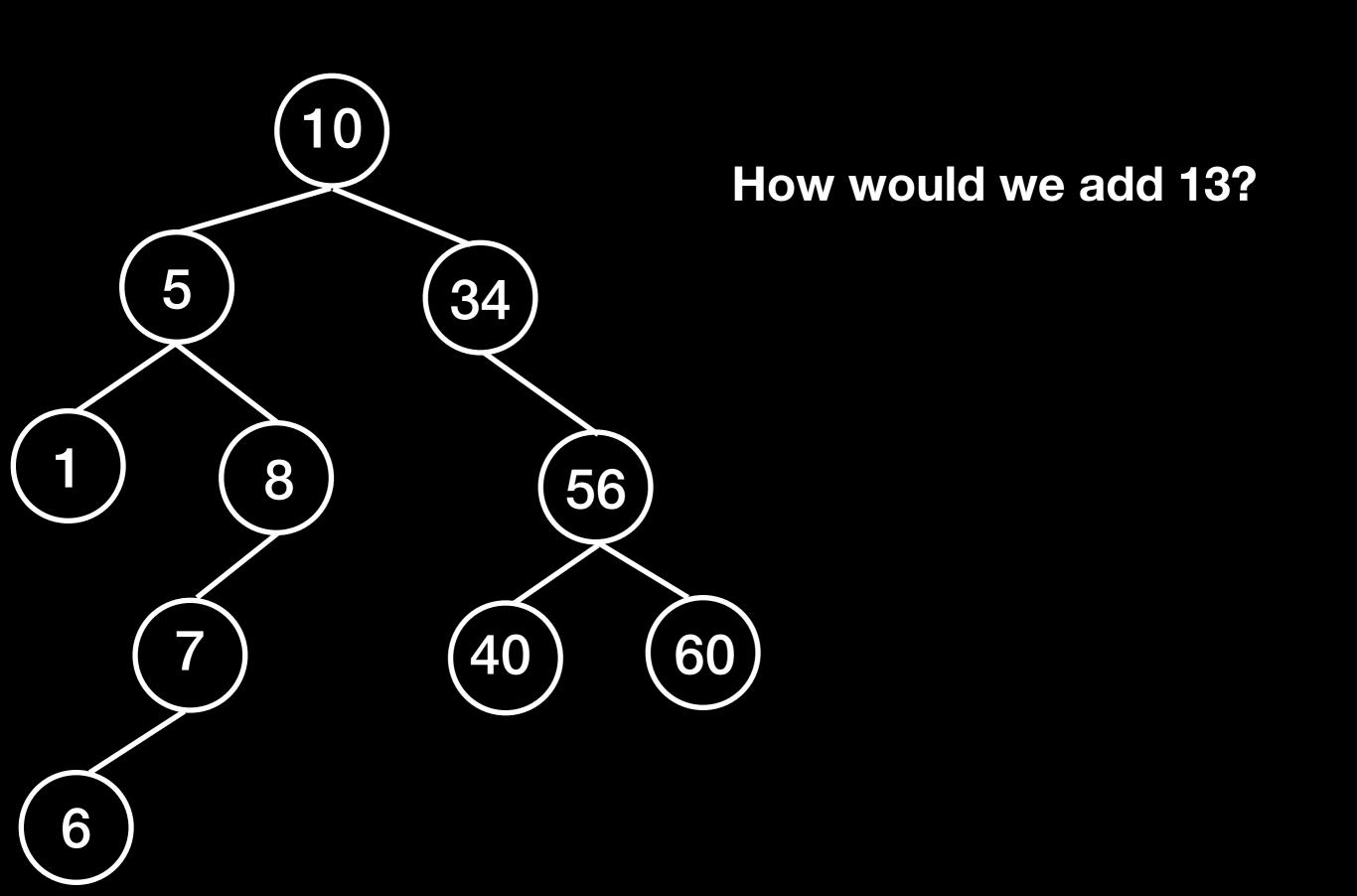


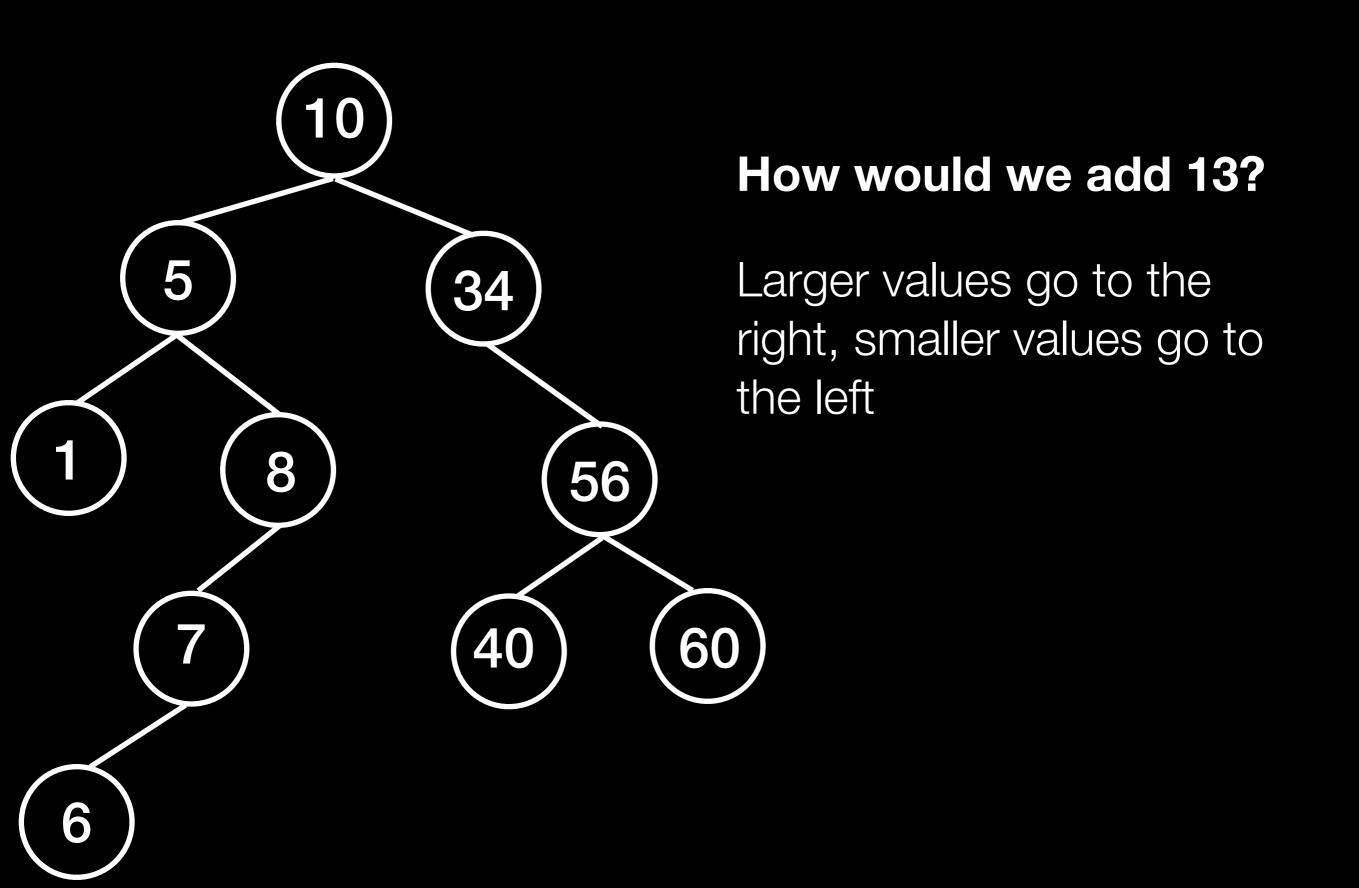
10, 5, 1, 8, 7, 6, 34, 56,

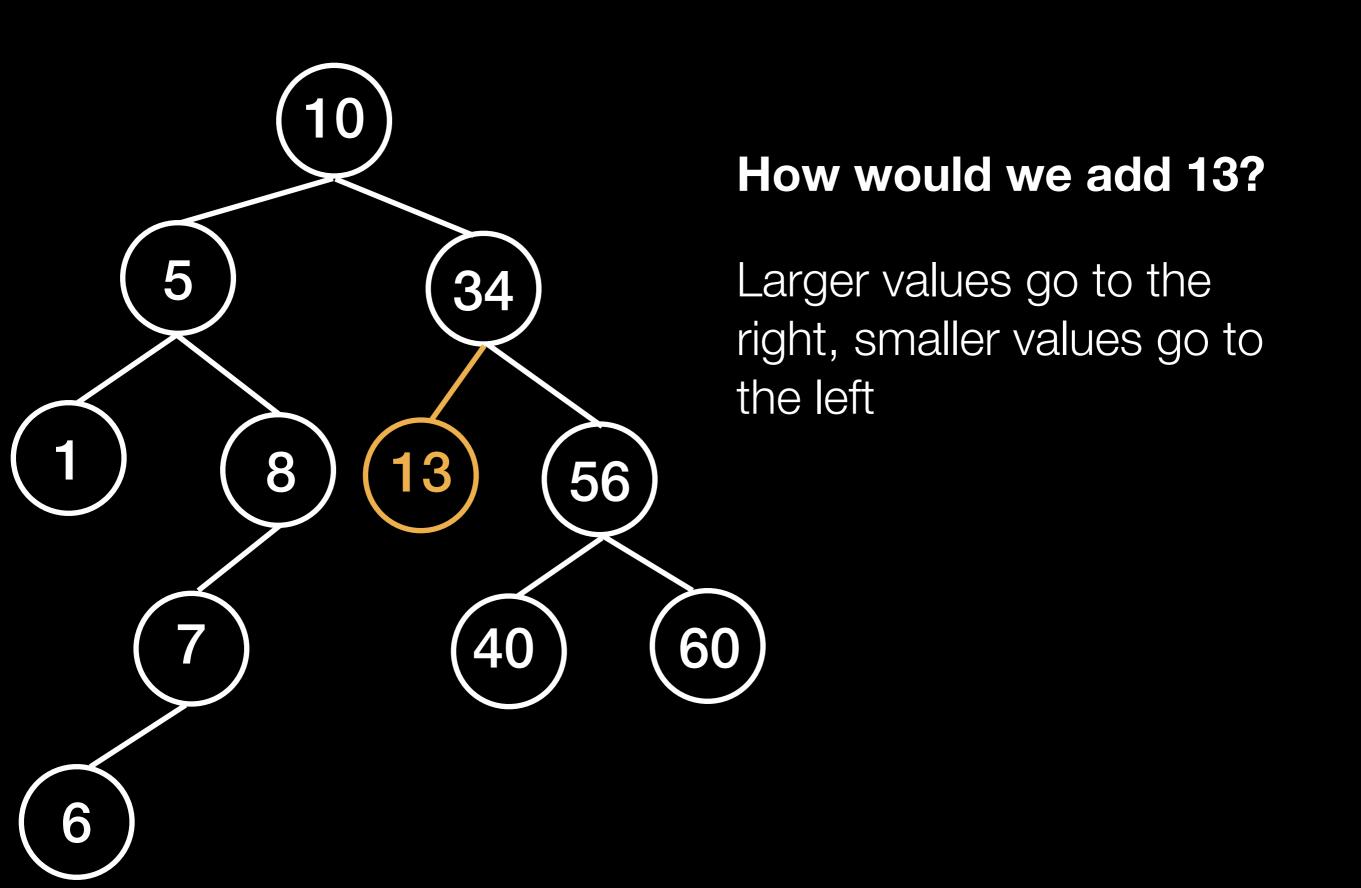
1, 5, 6, 7, 8, 10, 34, 40,

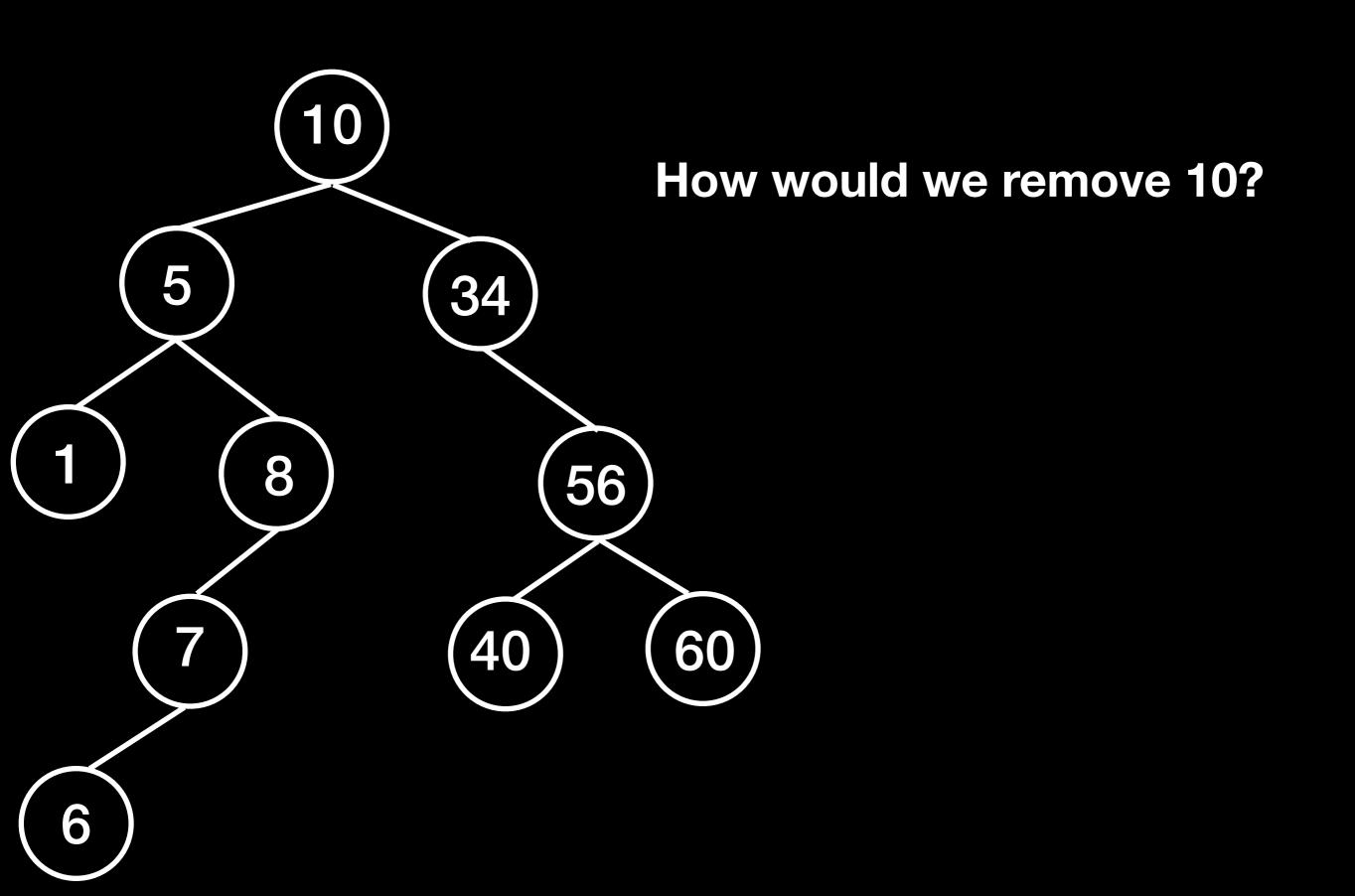


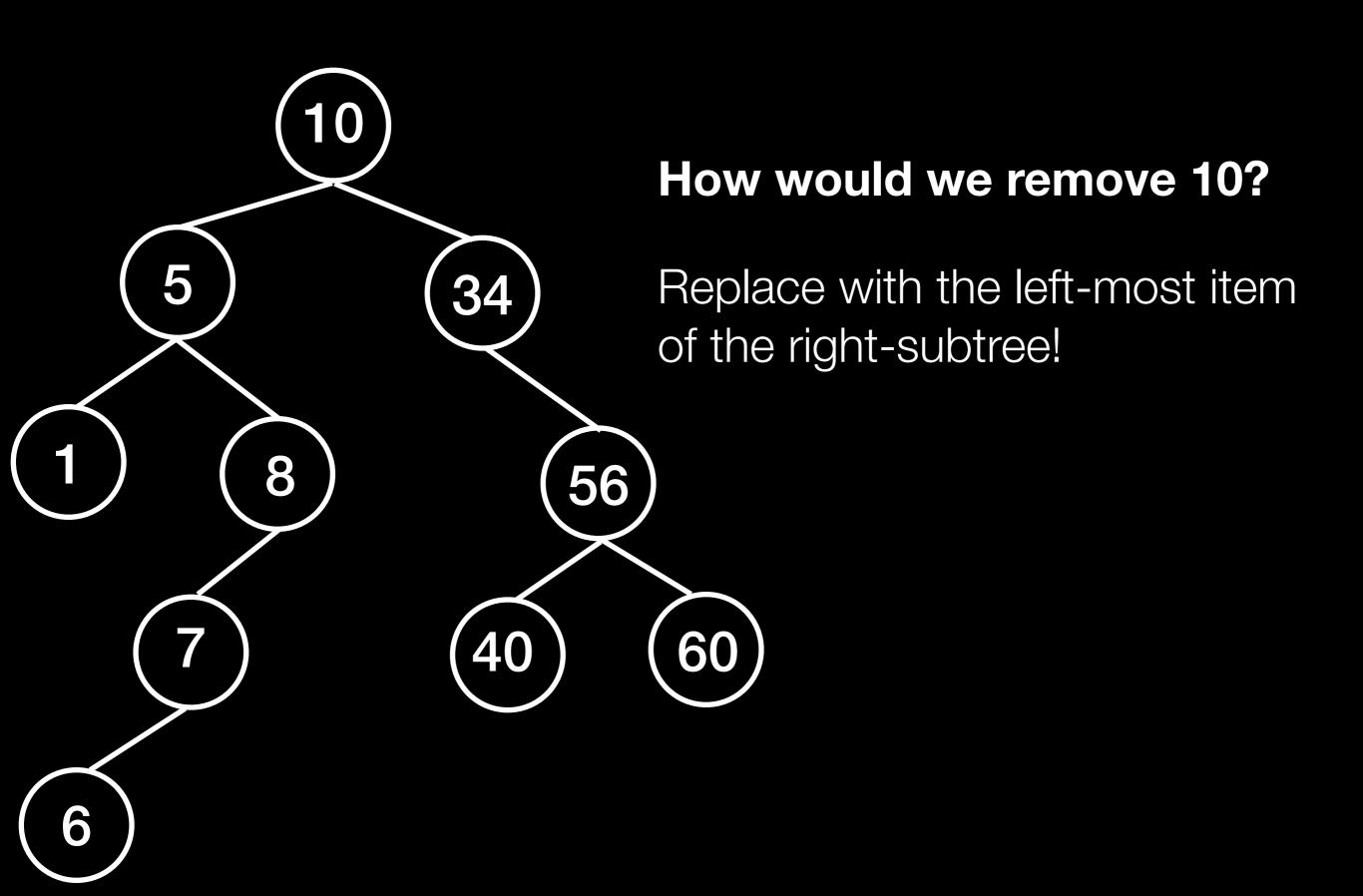


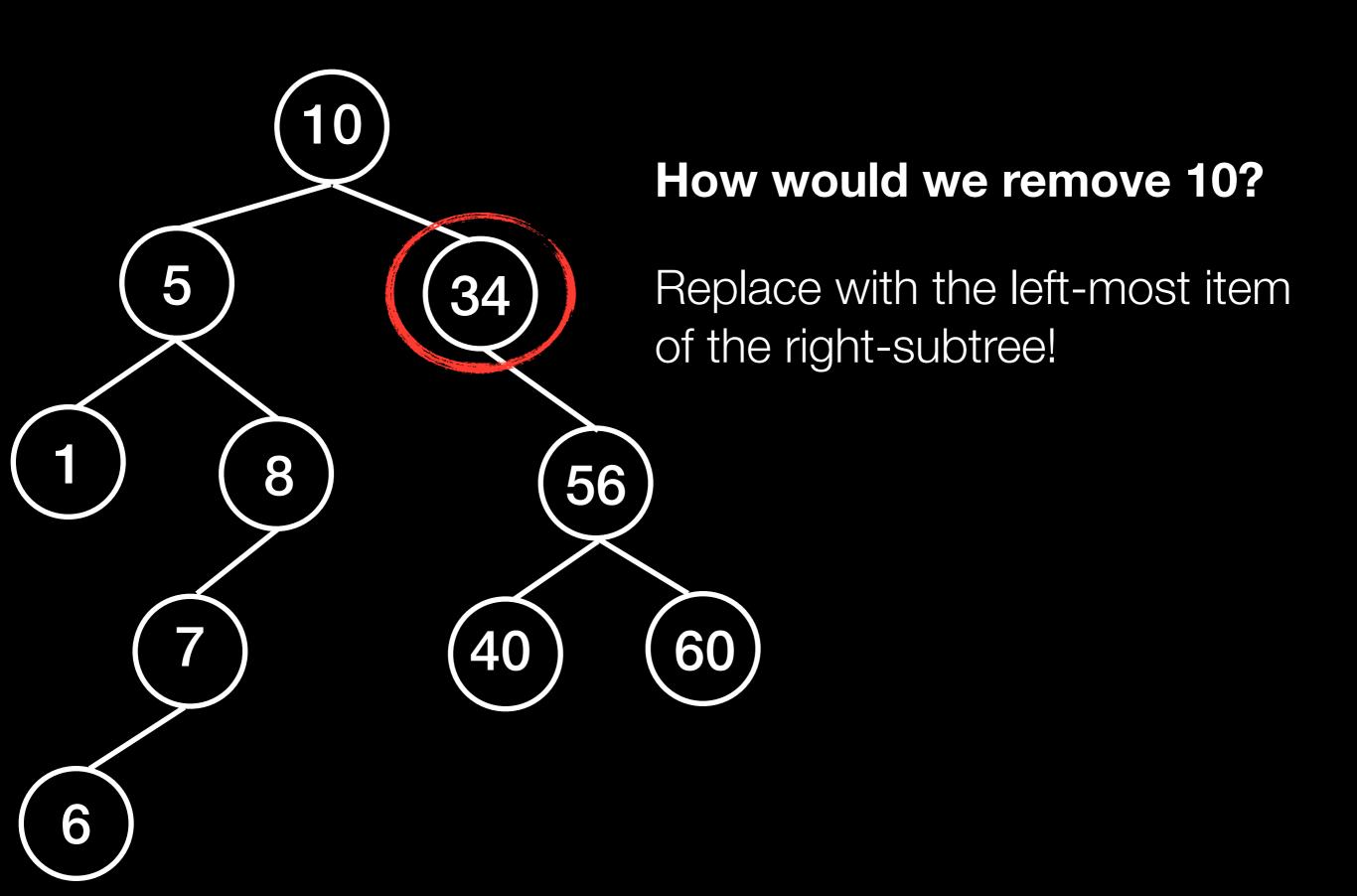


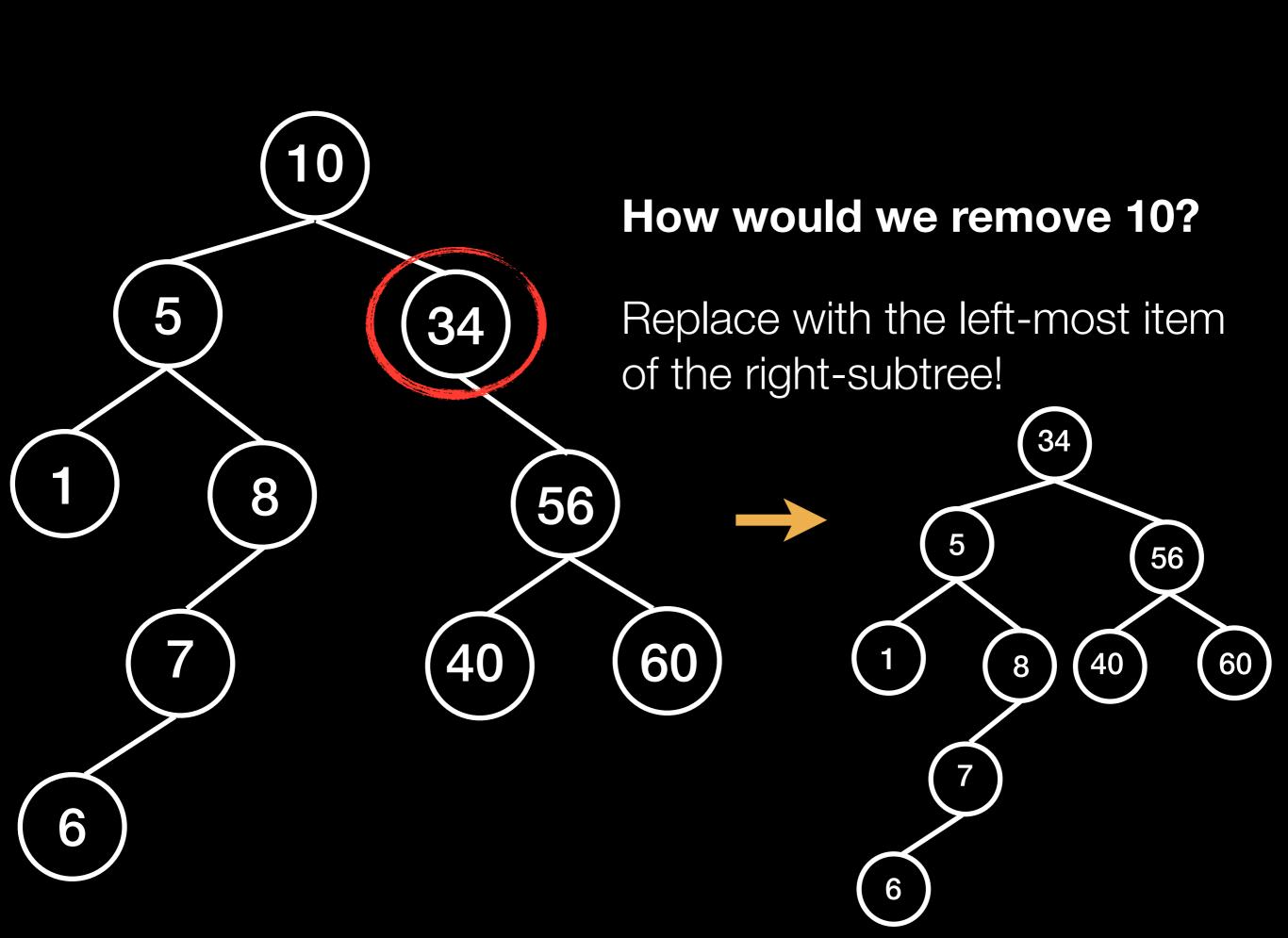












Write a **treeSort** function that takes an array of elements and returns those elements in sorted order. Assume you do not have an iterator (your approach **must be recursive**). You will need a helper function.

Write a **treeSort** function that takes an array of elements and returns those elements in sorted order. Assume you do not have an iterator (your approach **must be recursive**). You will need a helper function.

```
struct AVLTree* newAVLTree();
void addAVLTree(struct AVLTree *tree, TYPE val);
void treeSort (TYPE data[], int n) {
  // WRITE ME
void treeSortHelper(AVLNode *cur, TYPE *data,
int *count) {
  // WRITE ME
```

```
void treeSort(TYPE data[], int size){
  int i;
  int sortIdx = 0;
```

```
void treeSort(TYPE data[], int size){
  int i;
  int sortIdx = 0;

  /* declare an AVL tree */
  struct AVLTree *tree = newAVLtree();
  assert(data != NULL && size > 0);
```

```
void treeSort(TYPE data[], int size){
    int i;
    int sortIdx = 0;
    /* declare an AVL tree */
    struct AVLTree *tree = newAVLtree();
    assert(data != NULL && size > 0);
    /* add elements to the tree */
    for (i = 0; i < size; i++)
        addAVLTree(tree, data[i]);
```

```
void treeSort(TYPE data[], int size){
    int i;
    int sortIdx = 0;
    /* declare an AVL tree */
    struct AVLTree *tree = newAVLtree();
    assert(data != NULL && size > 0);
    /* add elements to the tree */
    for (i = 0; i < size; i++)
        addAVLTree(tree, data[i]);
   /* call the helper function on the root */
   treeSortHelper(tree->root, data, &sortIdx);
```

```
/* *index goes from 0 to size-1 */
void treeSortHelper(AVLNode *cur, TYPE *data,
                     int *index){
   /* In-order traversal: get the left subtree,
      then this node, then the right subtree */
   if (cur != NULL) {
       treeSortHelper(cur->left, data, index);
       data[*index] = cur->val;
       (*index)++;
       treeSortHelper(cur->right, data, index);
```

No, unbalanced trees may have height n

No, unbalanced trees may have height n

Does inserting into an AVL tree with *n* nodes require looking at O(log *n*) nodes?

No, unbalanced trees may have height n

Does inserting into an AVL tree with *n* nodes require looking at $O(\log n)$ nodes?

Yes, because AVL trees are balanced

No, unbalanced trees may have height n

Does inserting into an AVL tree with *n* nodes require looking at $O(\log n)$ nodes?

Yes, because AVL trees are balanced

Does inserting into an AVL tree with *n* nodes require $O(\log n)$ rotations?

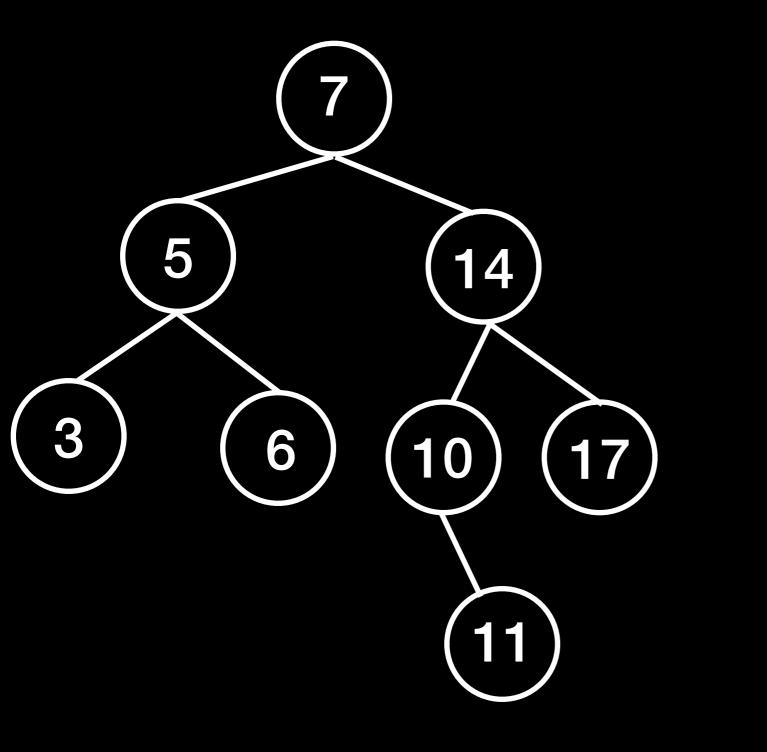
No, unbalanced trees may have height n

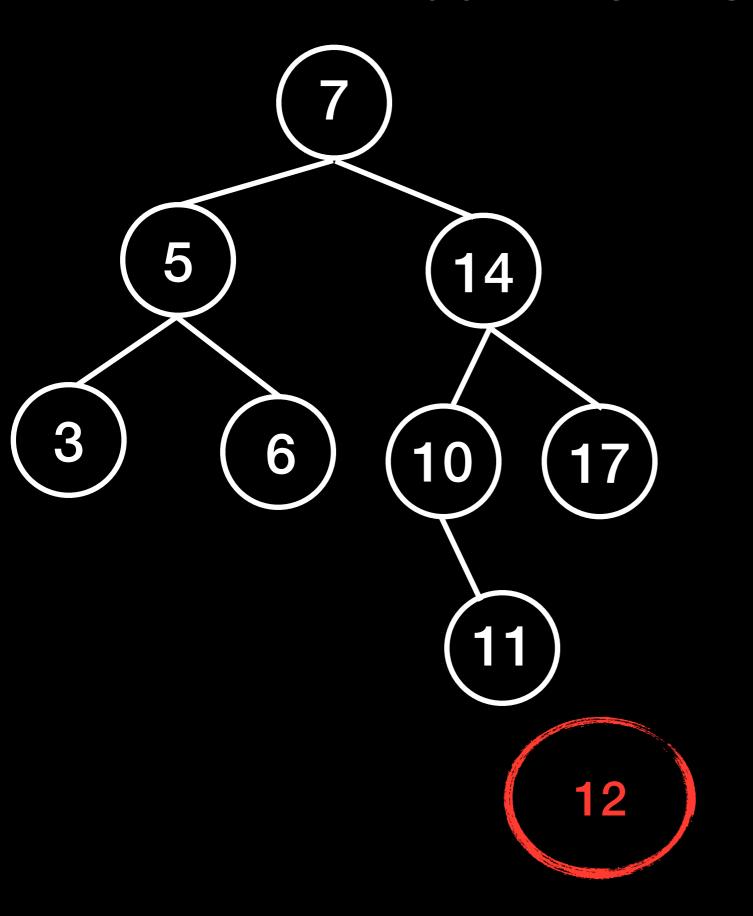
Does inserting into an AVL tree with *n* nodes require looking at $O(\log n)$ nodes?

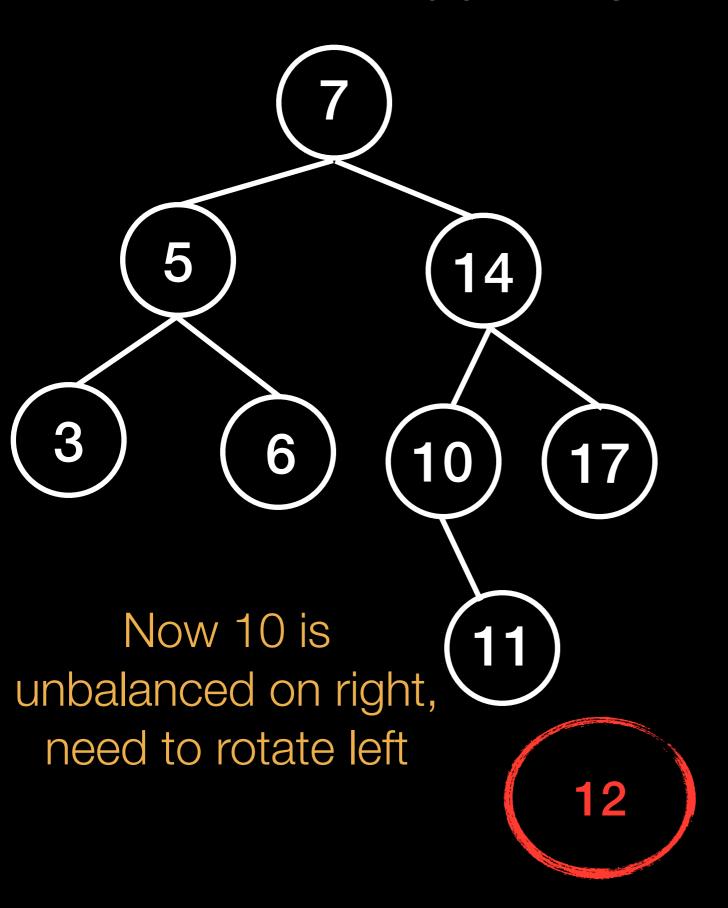
Yes, because AVL trees are balanced

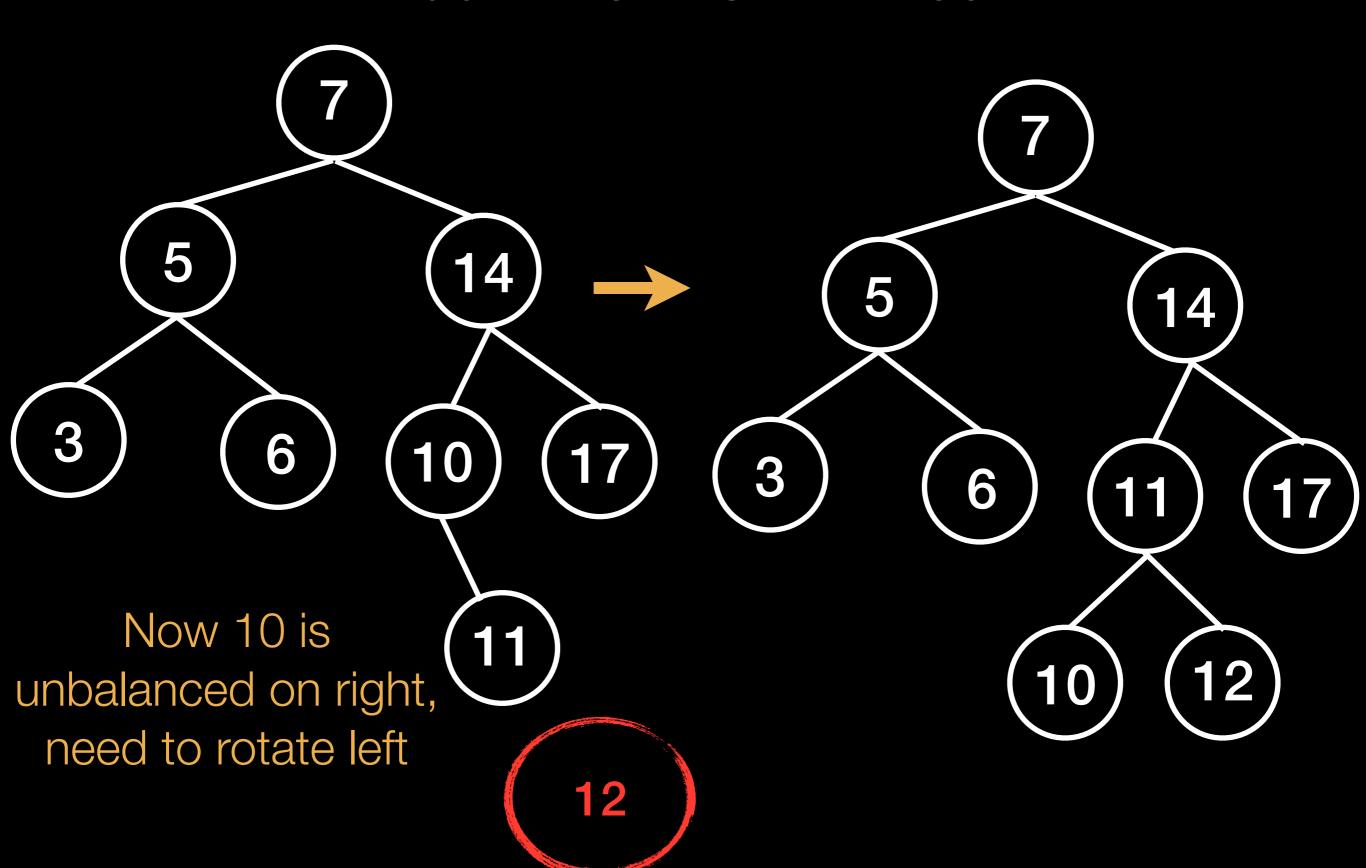
Does inserting into an AVL tree with *n* nodes require $O(\log n)$ rotations?

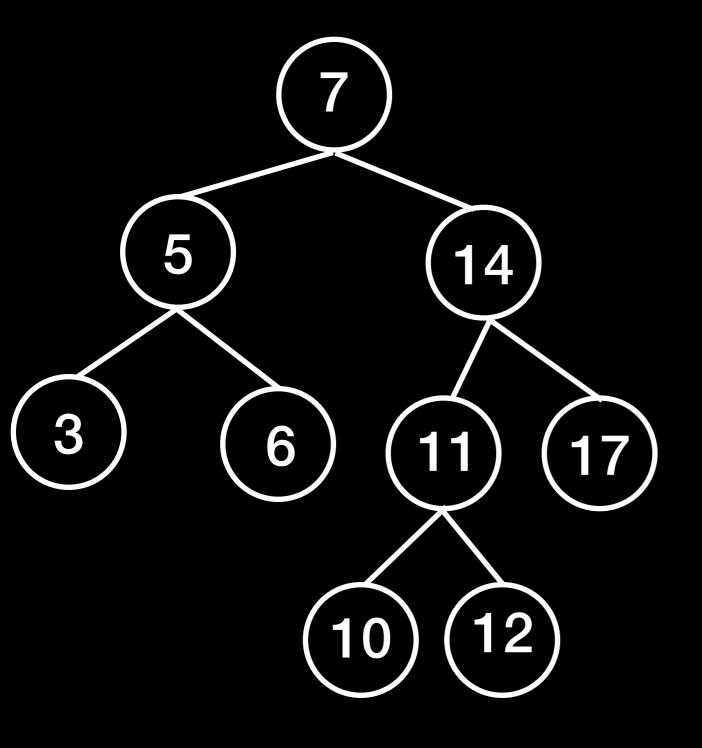
No, we need at most 2 rotations

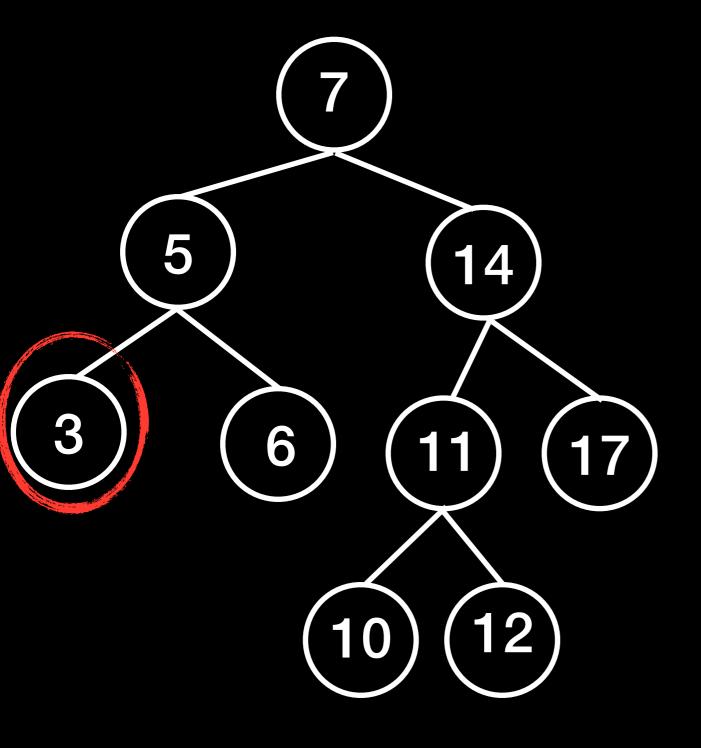


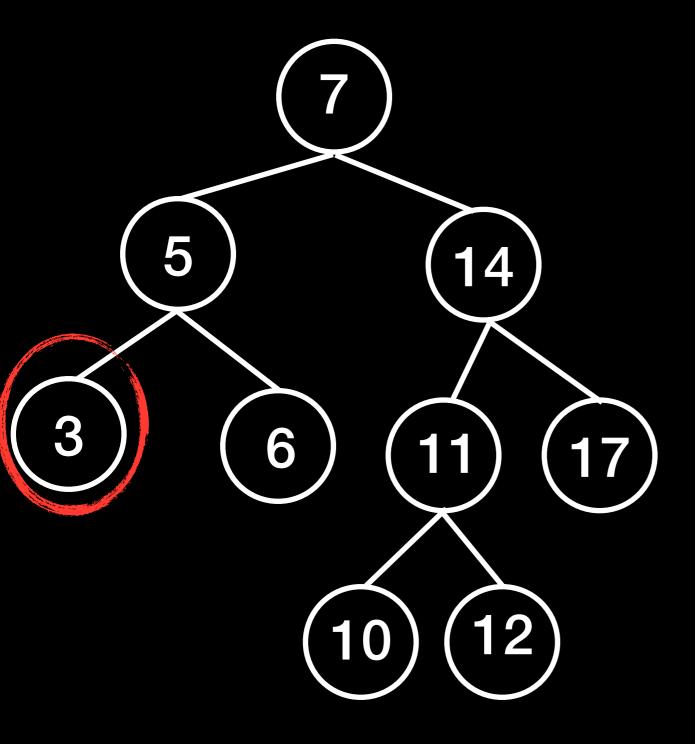




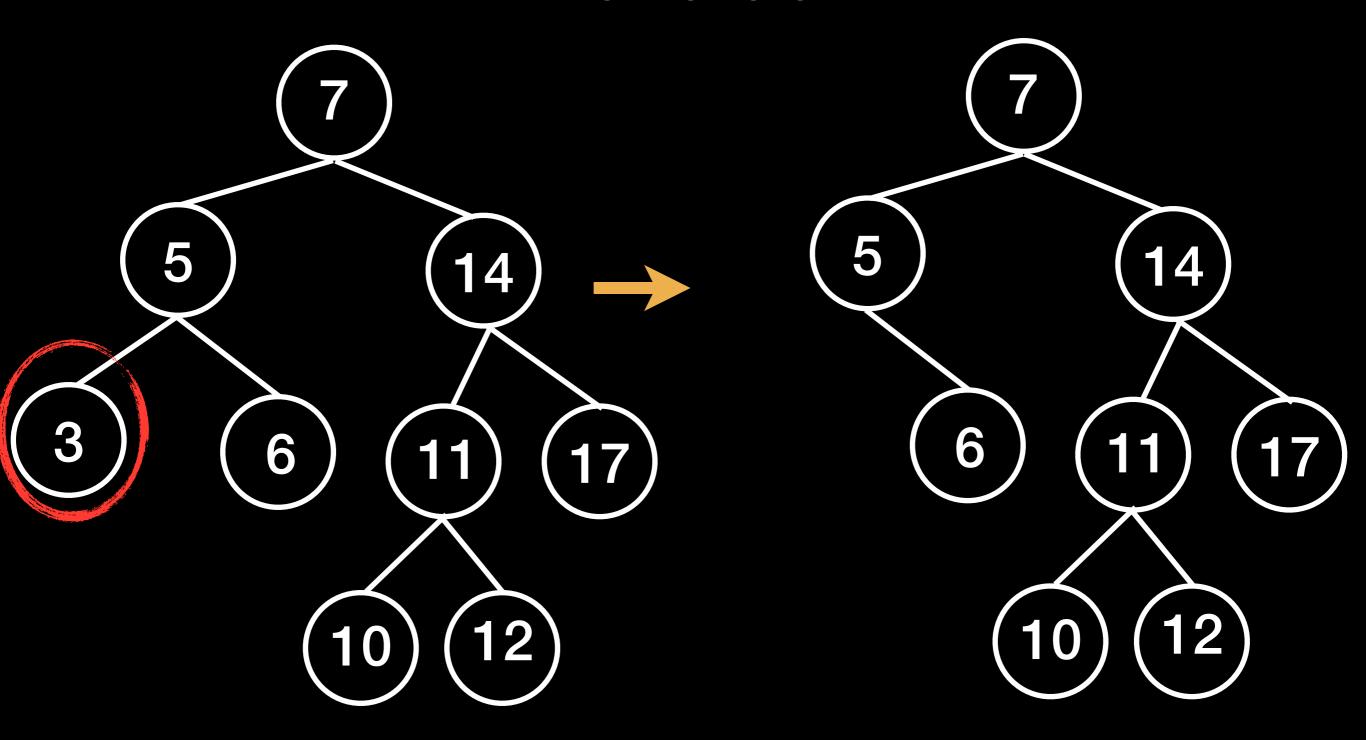




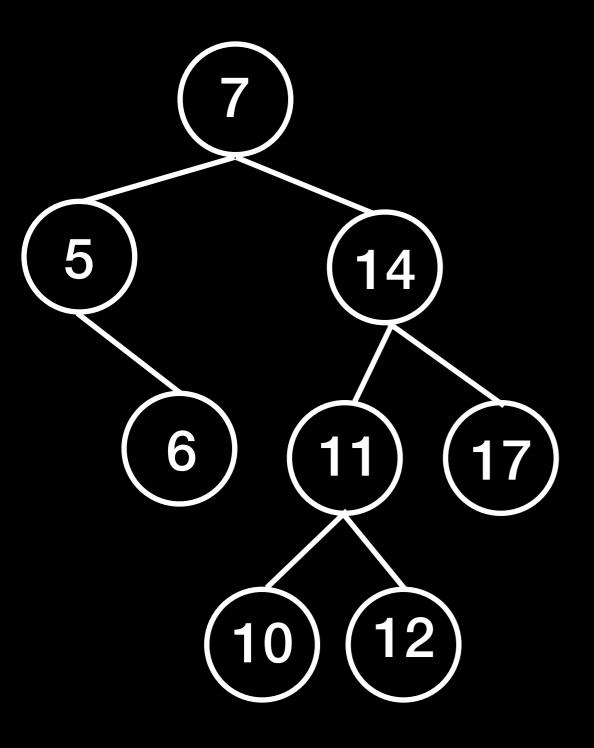


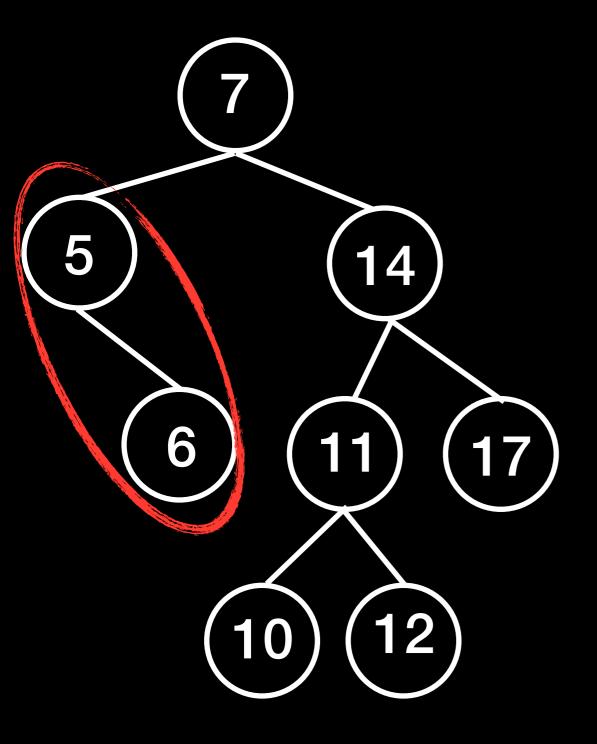


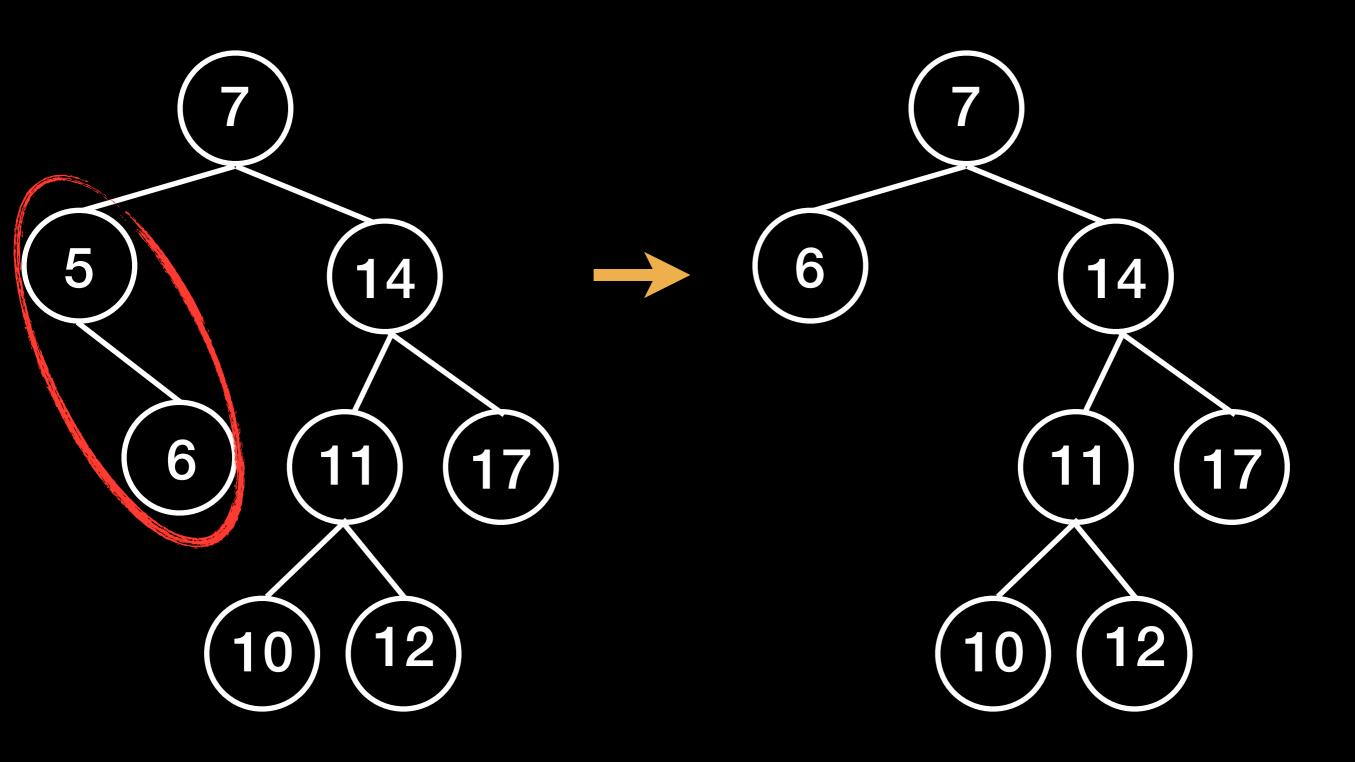
Still balanced, no rotations needed

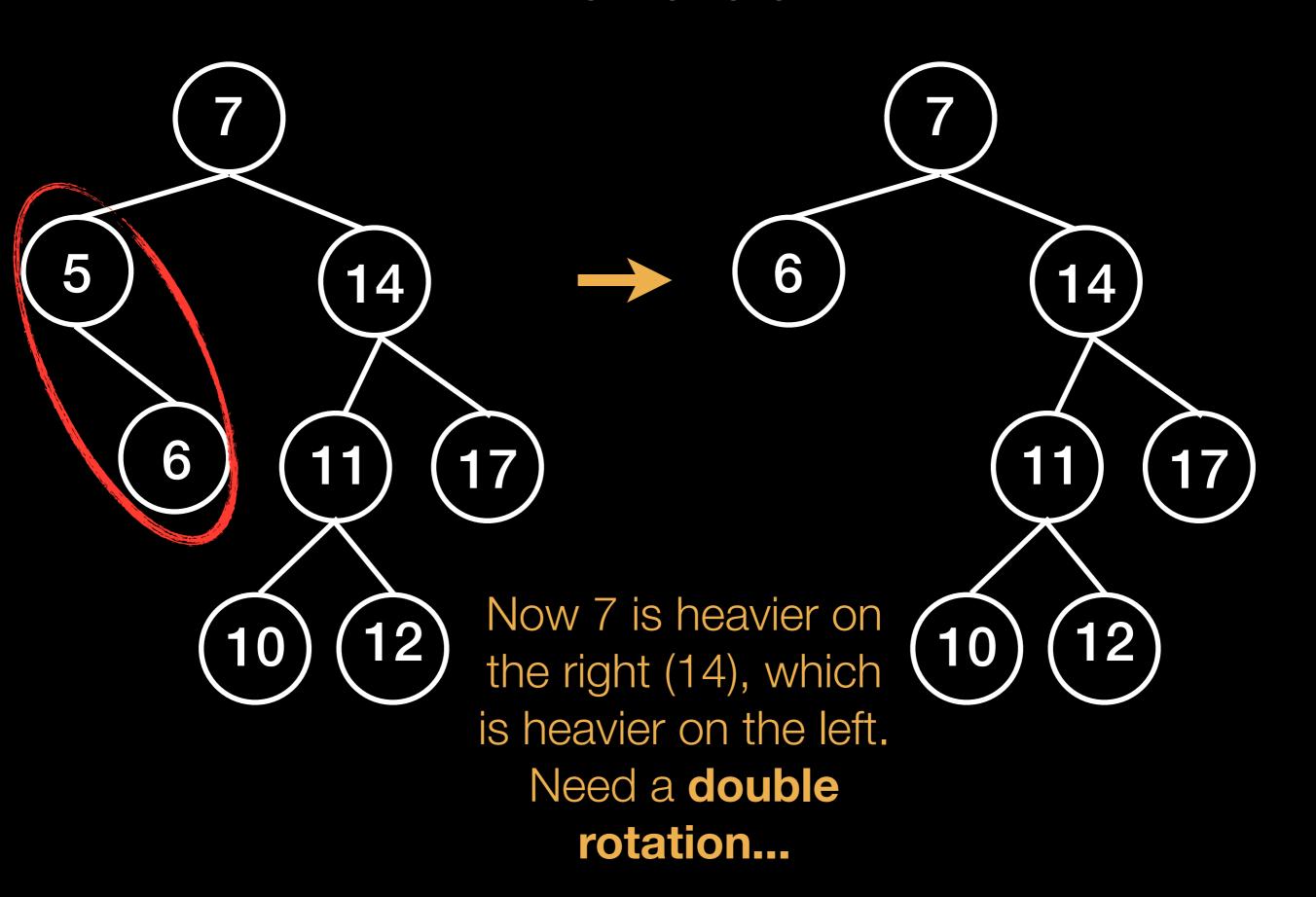


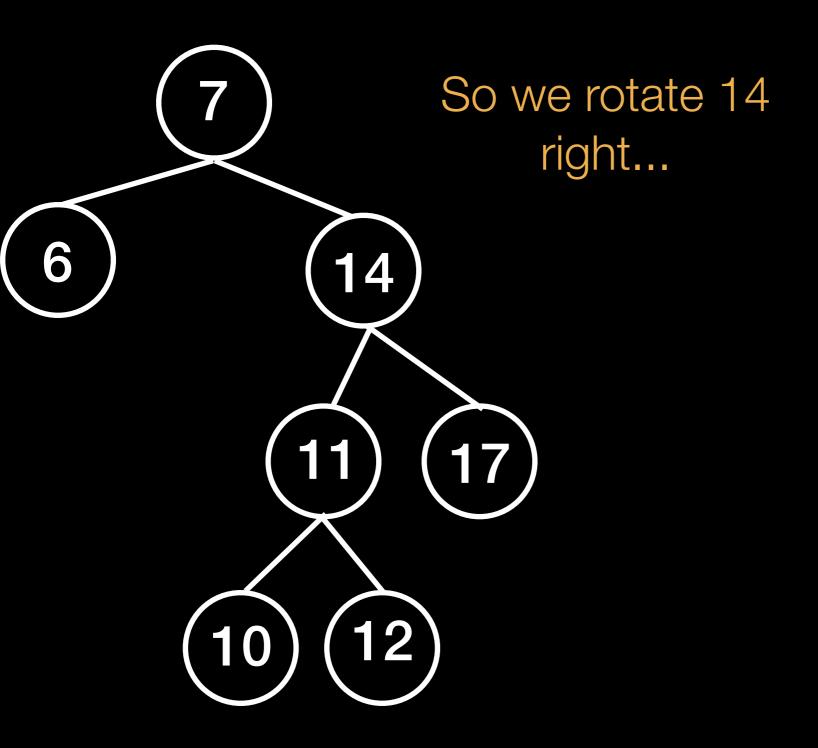
Still balanced, no rotations needed

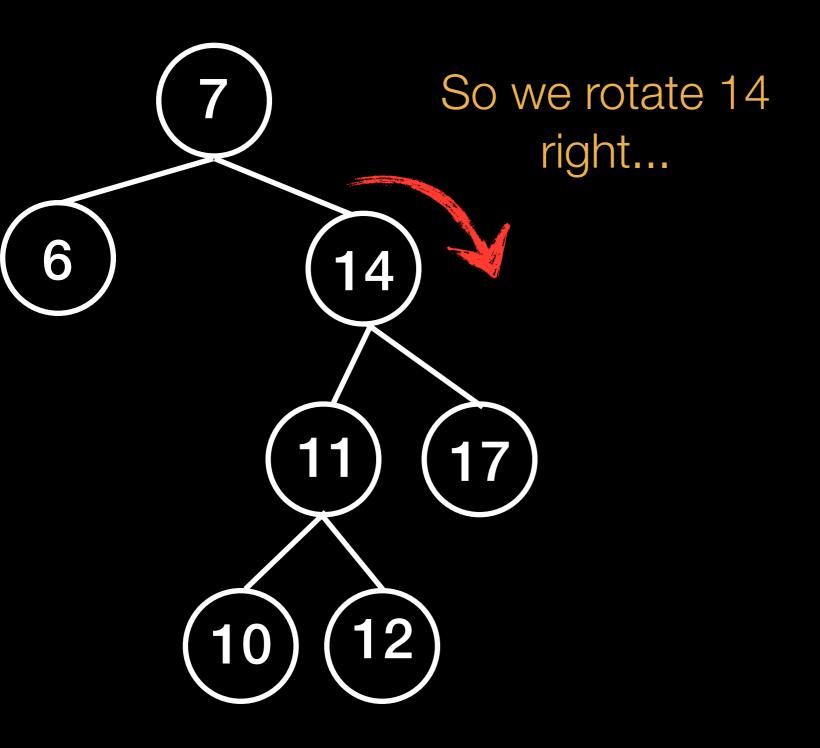


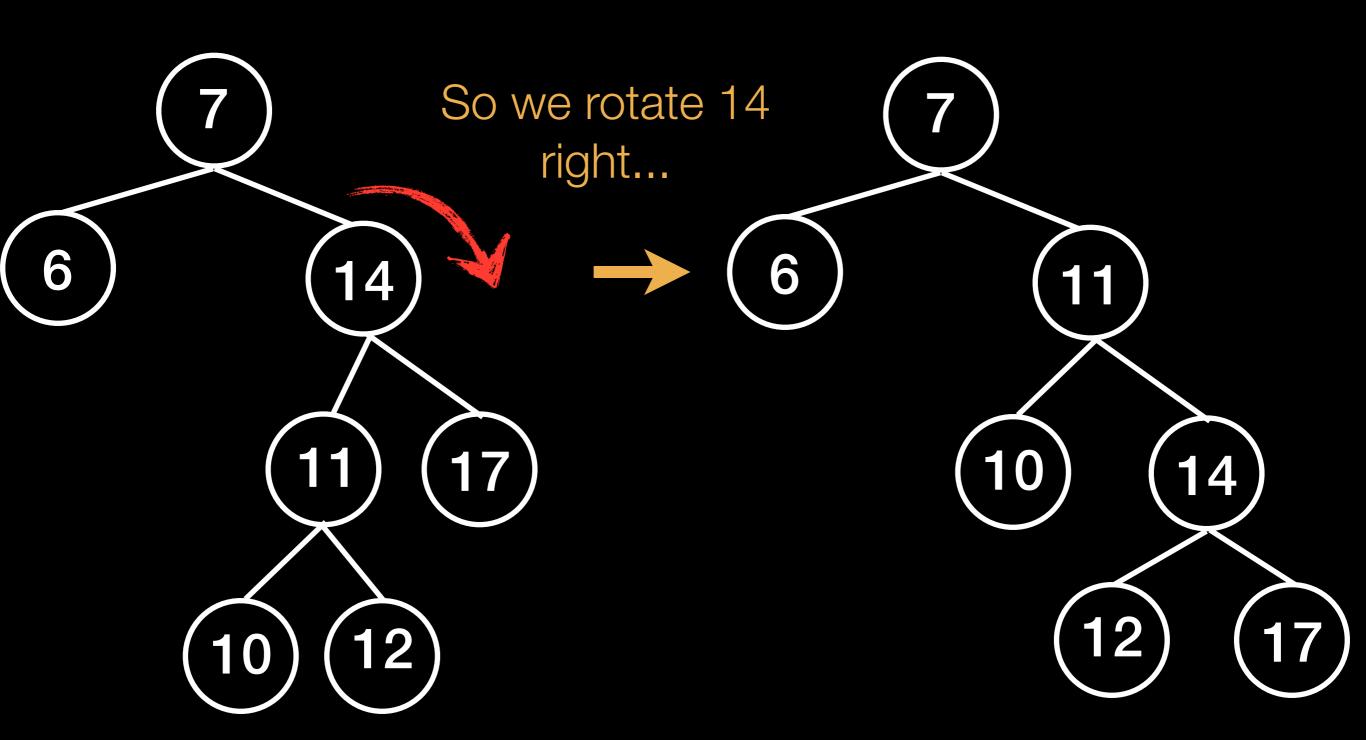


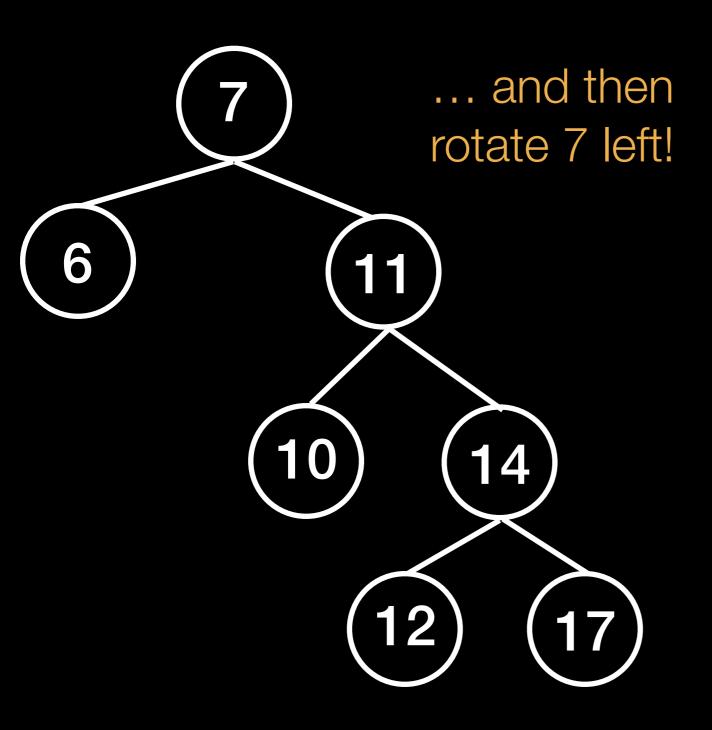


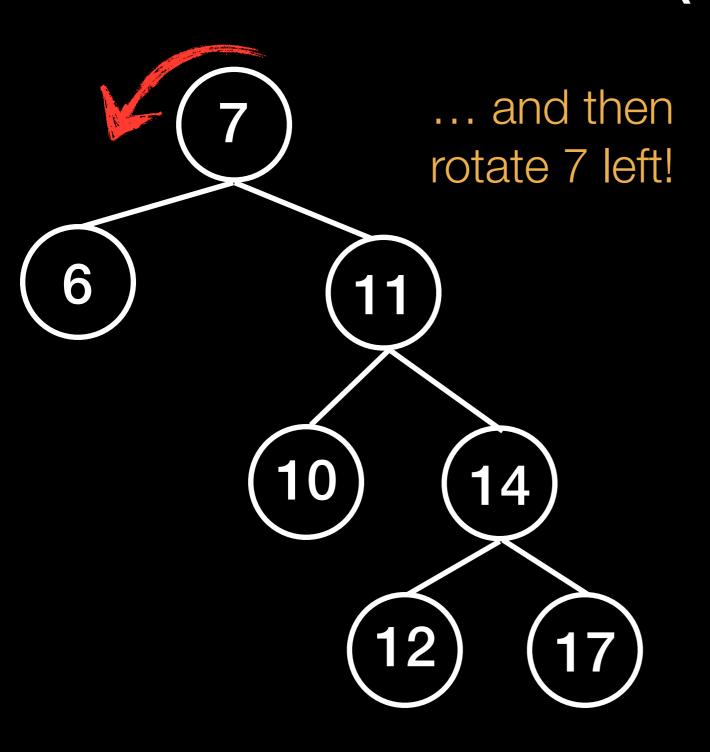


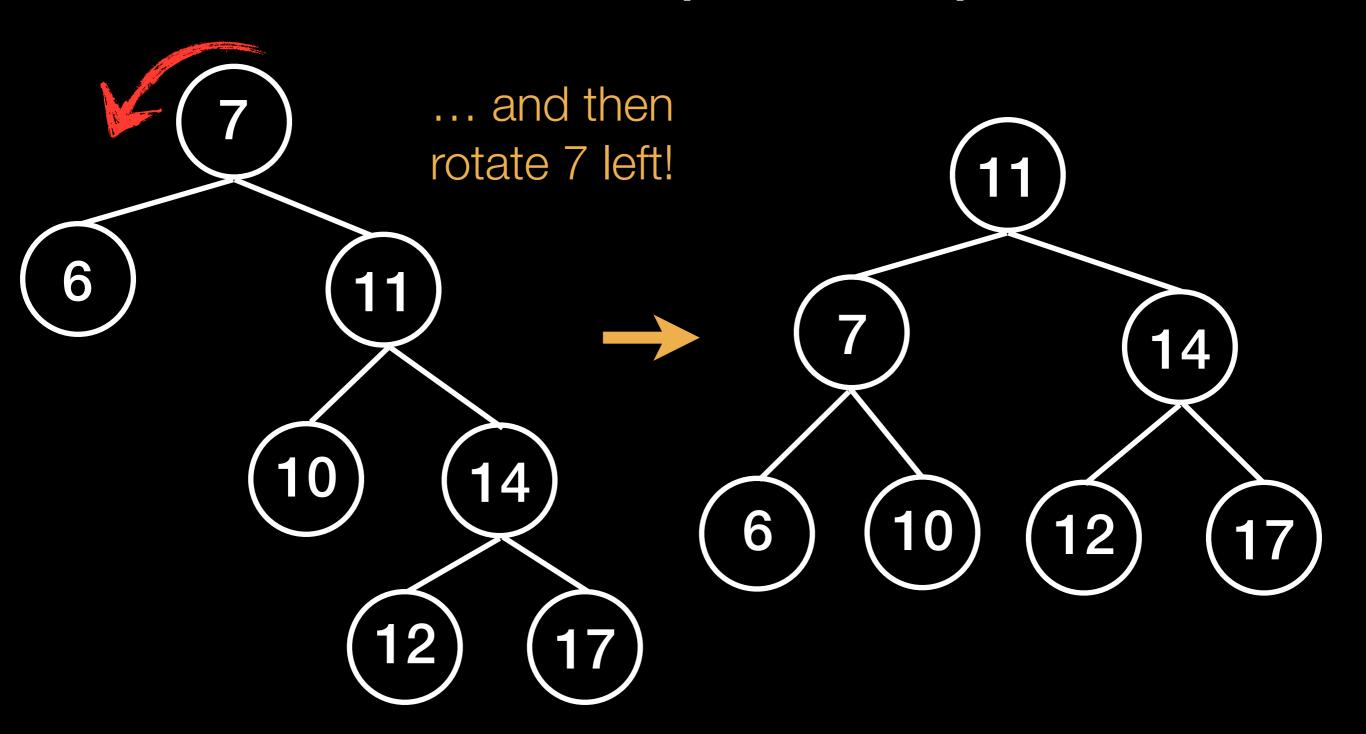












1) The node is unbalanced and

1) The node is unbalanced and

2) The node's balance factor is positive, but its right subtree's balance factor is negative,

or

The node's balance factor is negative, but its left subtree's balance factor is positive

1) The node is unbalanced and

2) The node's balance factor is positive, but its right subtree's balance factor is negative,

or

The node's balance factor is negative, but its left subtree's balance factor is positive

Balance factor = height(right subtree) - height(left subtree)

How do we represent a binary heap?

What are the indices for the children of node *i*?

What are the indices for the children of node *i*?

$$2*i+1$$
 and $2*i+2$

What are the indices for the children of node *i*?

$$2*i+1$$
 and $2*i+2$

What is the index of the parent of node *i*?

What are the indices for the children of node *i*?

$$2*i+1$$
 and $2*i+2$

What is the index of the parent of node *i*?

$$(i - 1) / 2$$

What are the indices for the children of node *i*?

$$2*i+1$$
 and $2*i+2$

What is the index of the parent of node *i*?

$$(i - 1) / 2$$

How do we add a node to a heap?

How do we represent a binary heap? An array

What are the indices for the children of node *i*?

$$2*i+1$$
 and $2*i+2$

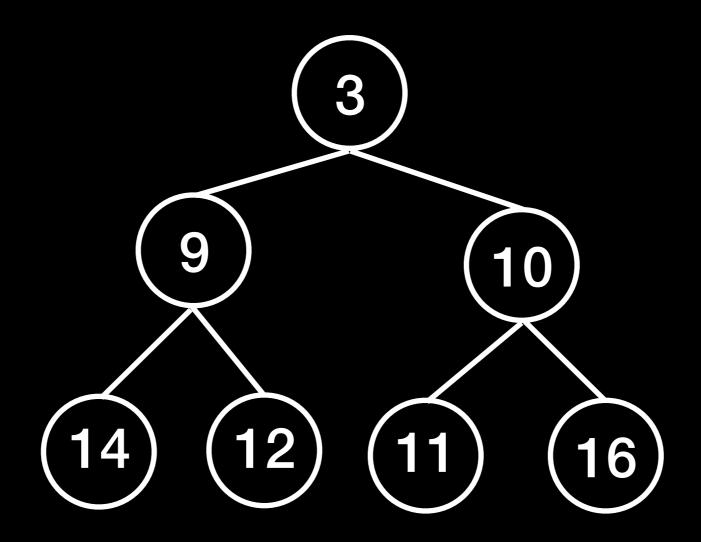
What is the index of the parent of node i?

$$(i-1)/2$$

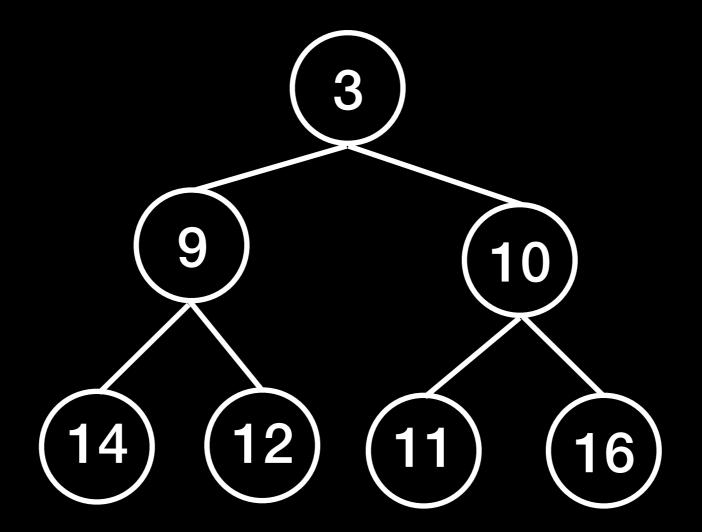
How do we add a node to a heap?

Insert it after the last item, then percolate it up

Simulate heap sort on this heap



Simulate heap sort on this heap



We'll work this out on the chalk board

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

bucket = hash(x) % 11

	0	
	1	
bucket = hash(x) % 11	2	
	3	
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	
	9	
	10	

	O	
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	
	9	
	10	

	0	
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	
	9	
	10	43

	0	
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	8
	9	
	10	43

	0	11
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	8
	9	
	10	43

	0	11
	1	
bucket = hash(x) % 11	2	
	3	3 14
If 'bucket' is in use, try	4	
the next one	5	
	6	
	7	
	8	8
	9	
	10	43

	O	
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	14
the next one	5	
	6	
	7	
	8	8
	9	
	10	43

11
3
14
8
43

	0	11
	1	
bucket = hash(x) % 11	2	
	3	3 25
If 'bucket' is in use, try	4	14
the next one	5	
	6	
	7	
	8	8
	9	
	10	43

	0	11
	1	
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	14
the next one	5	25
	6	
	7	
	8	8
	9	
	10	43

	O	11
	1	23
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	14
the next one	5	25
	6	
	7	
	8	8
	9	
	10	43

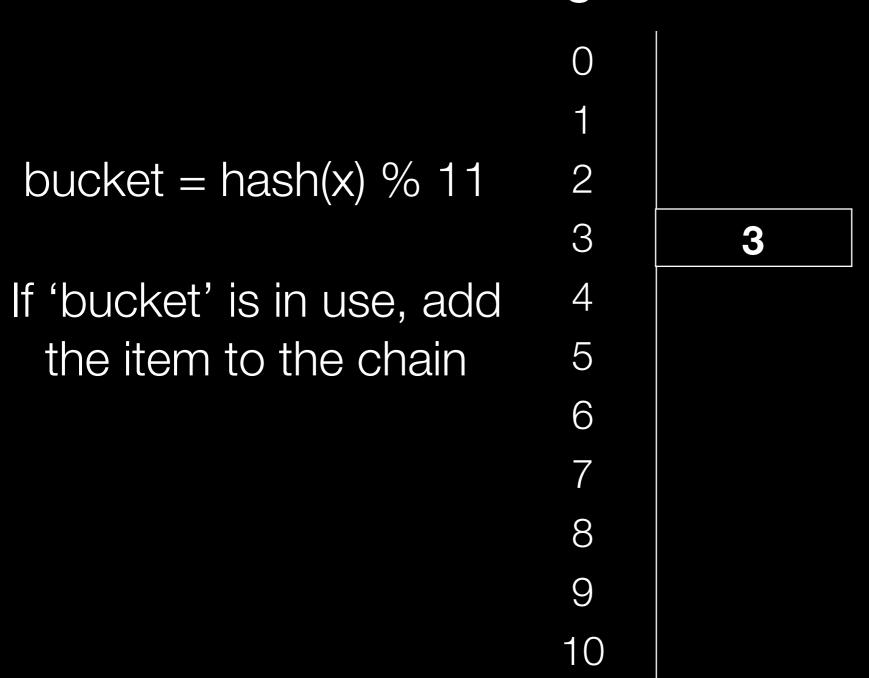
	0	11 44
	1	23
bucket = hash(x) % 11	2	
	3	3
If 'bucket' is in use, try	4	14
the next one	5	25
	6	
	7	
	8	8
	9	
	10	43

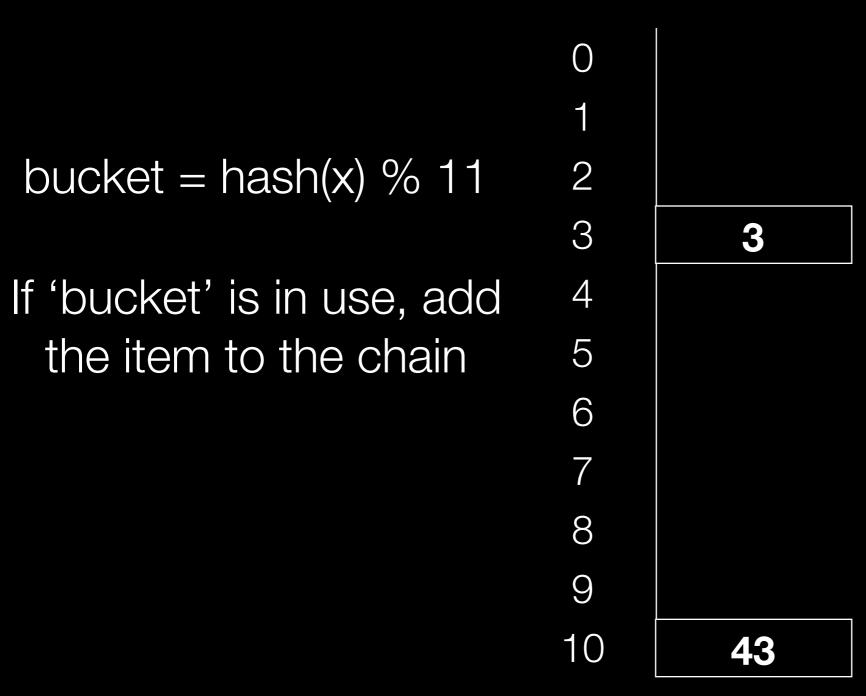
	0	11
	1	23
bucket = hash(x) % 11	2	44
	3	3
If 'bucket' is in use, try	4	14
the next one	5	25
	6	
	7	
	8	8
	9	
	10	43

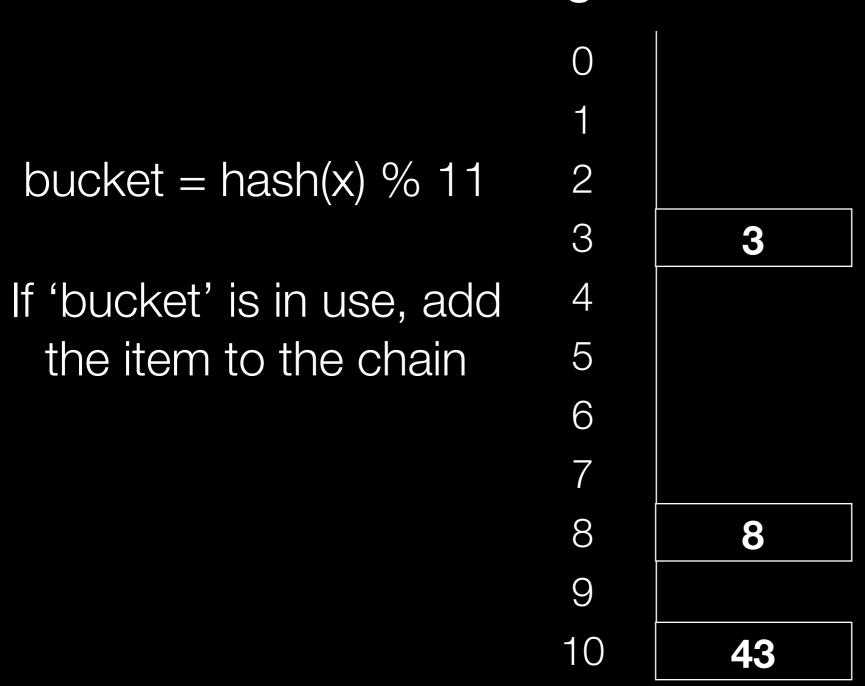
```
3
10
```

```
bucket = hash(x) \% 11
                            3
                           10
```

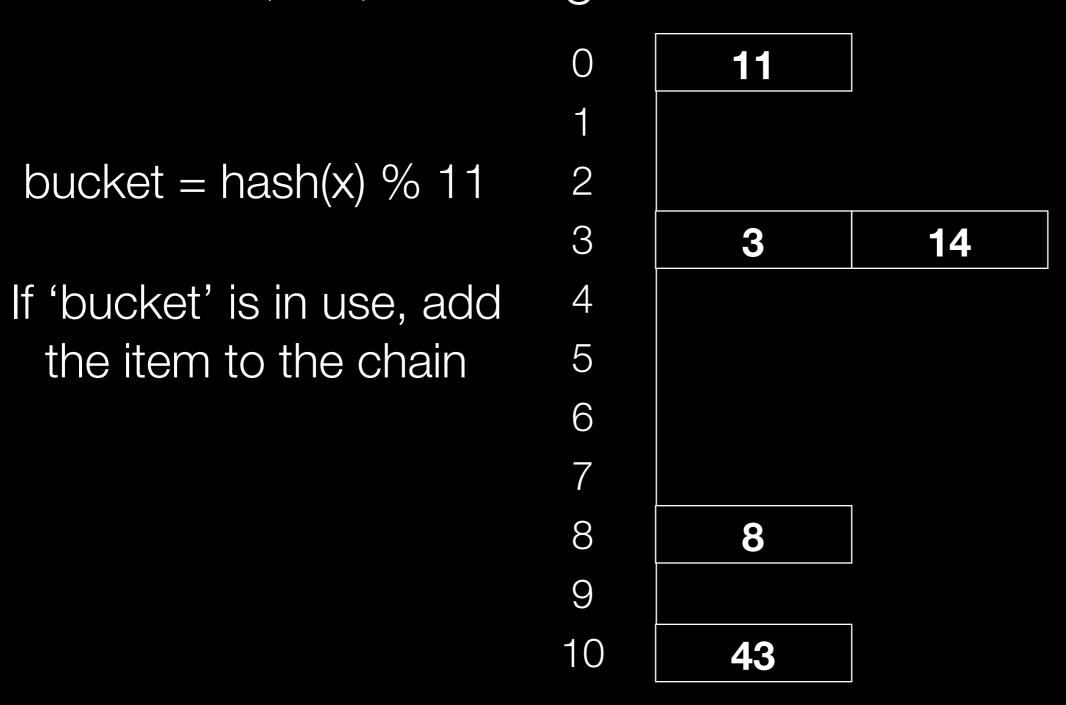
```
bucket = hash(x) \% 11
                             2
                             3
If 'bucket' is in use, add
 the item to the chain
                             5
                             6
                             10
```

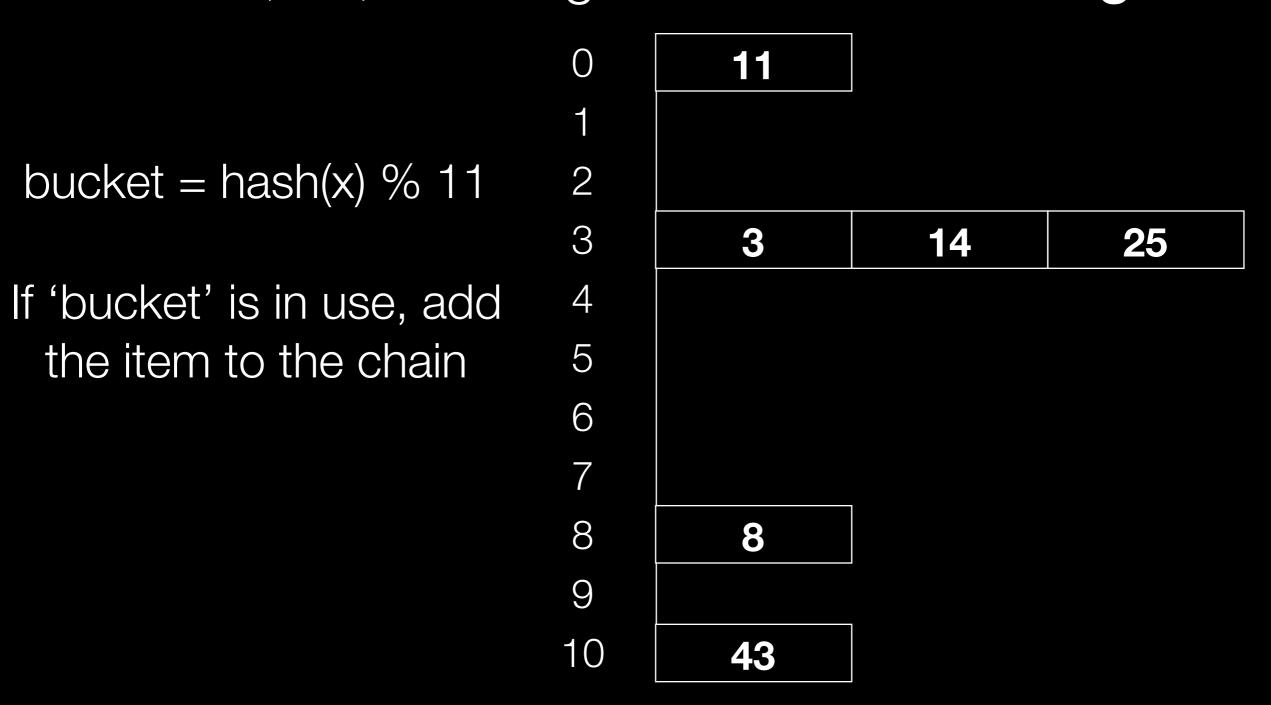


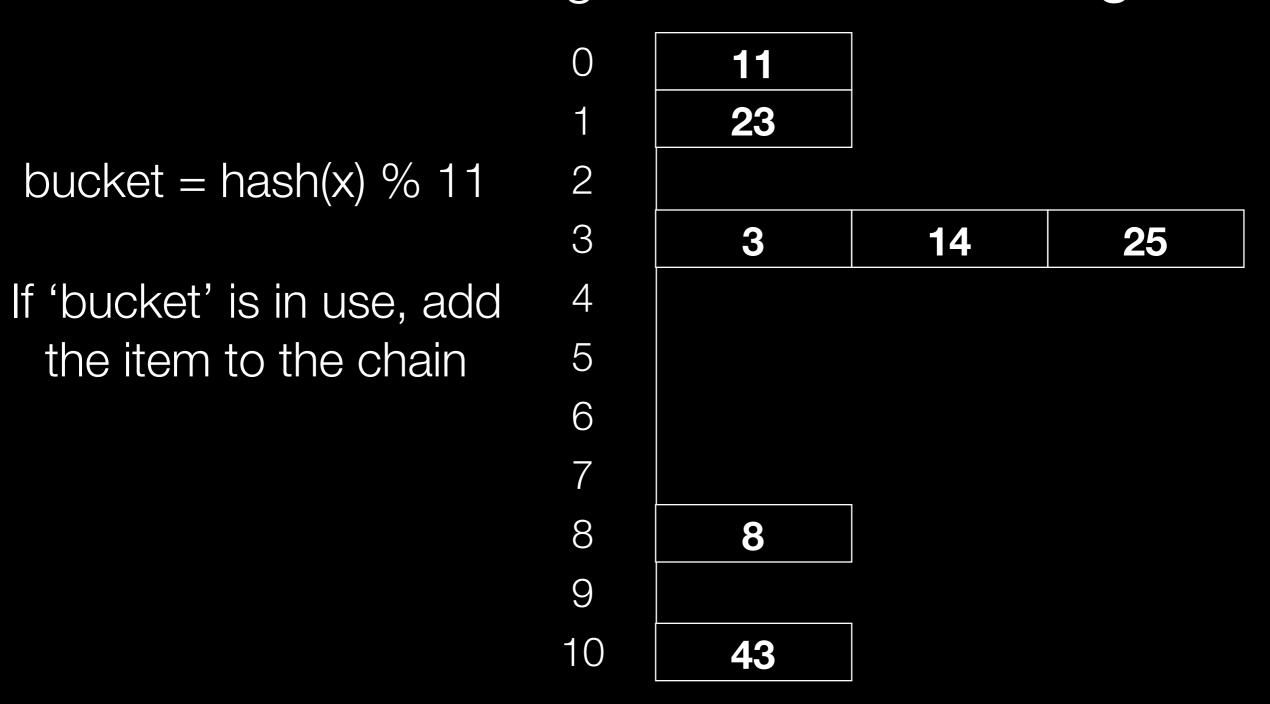


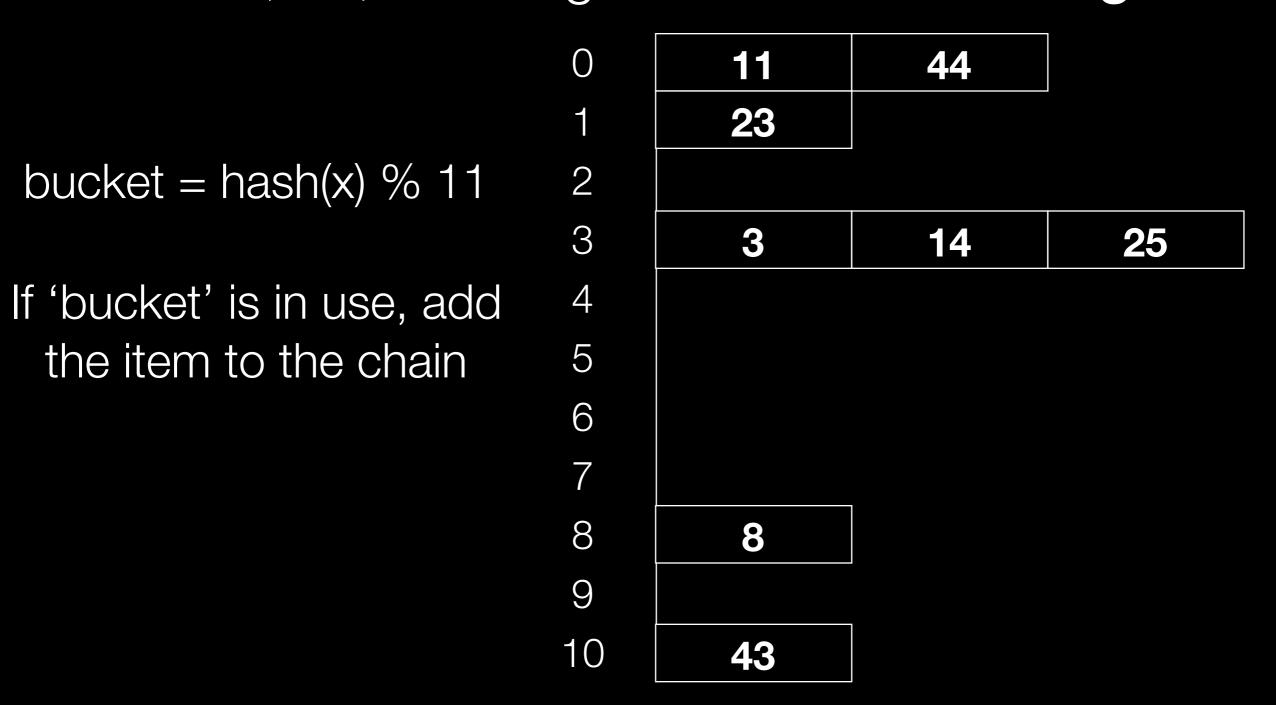


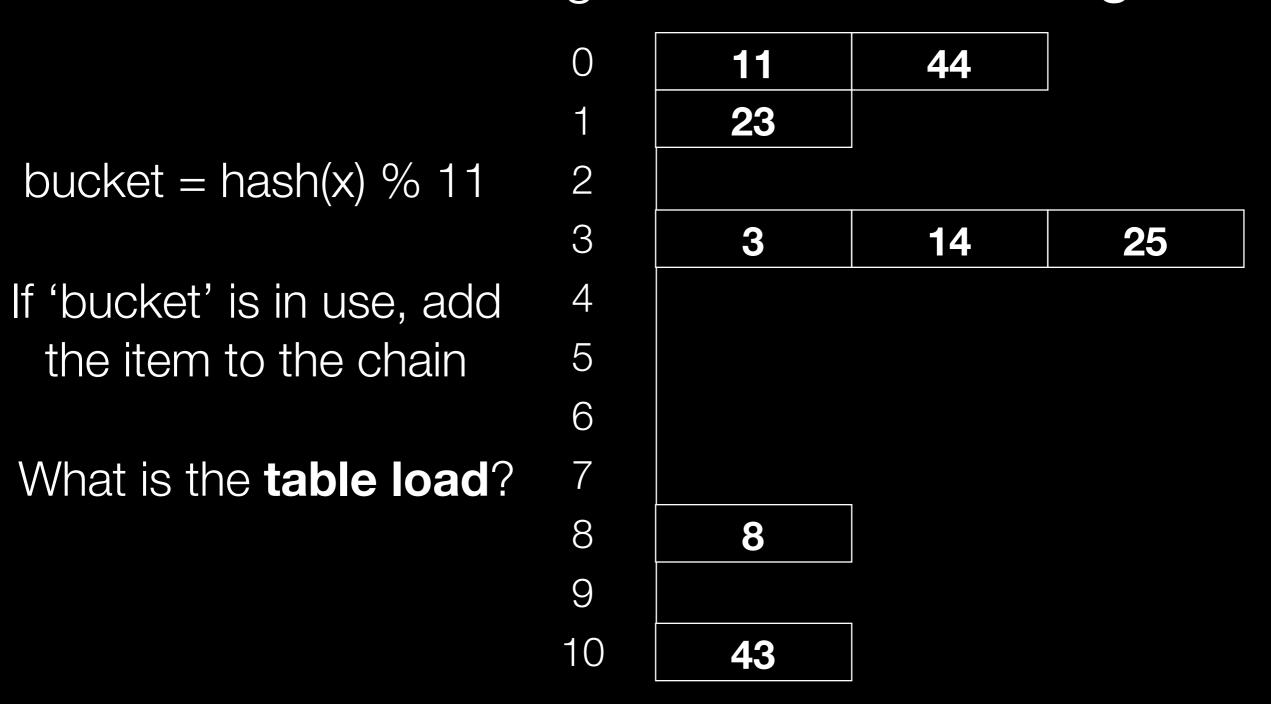
bucket = hash(x) % 11If 'bucket' is in use, add the item to the chain

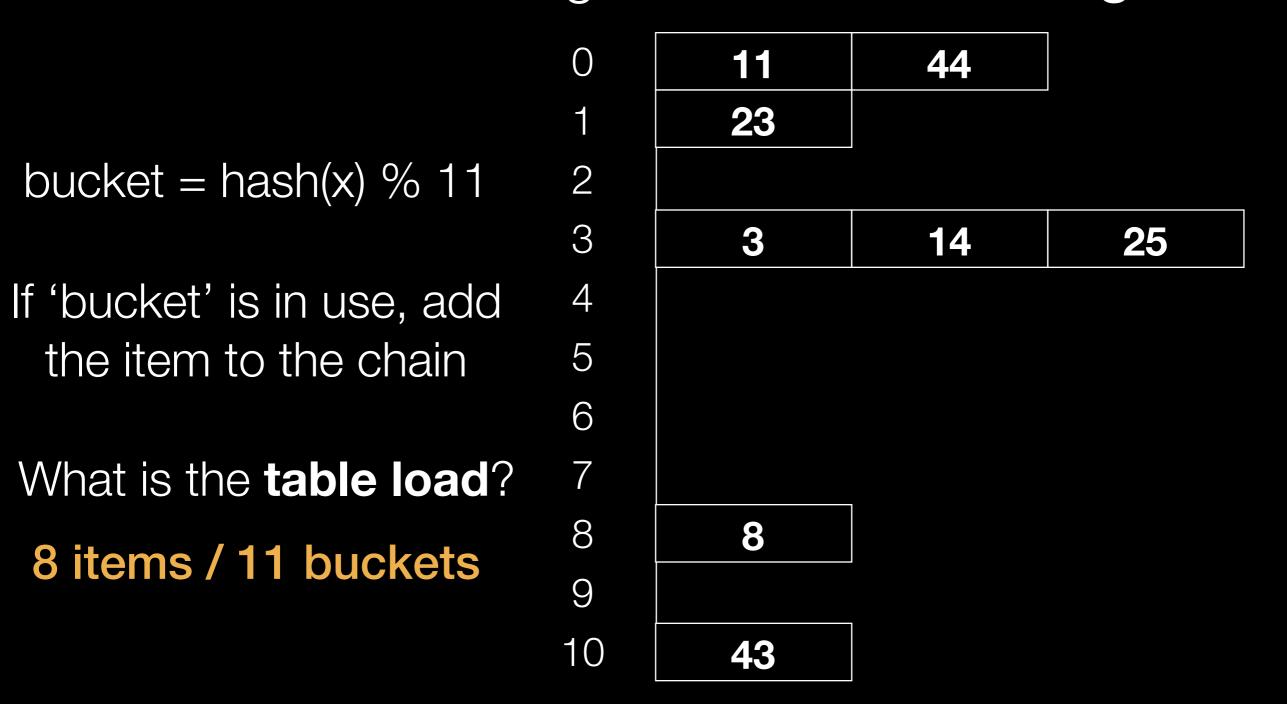












Does every key in a hash table need to be unique?

Does every key in a hash table need to be unique? Yes, that's the point of storing key/value pairs

Does every key in a hash table need to be unique? Yes, that's the point of storing key/value pairs

Does each key in a hash table need to hash to a unique value?

Does every key in a hash table need to be unique? Yes, that's the point of storing key/value pairs

Does each key in a hash table need to hash to a unique value?

No, but we should use a hash function with as few collisions as possible

Does every key in a hash table need to be unique? Yes, that's the point of storing key/value pairs

Does each key in a hash table need to hash to a unique value?

No, but we should use a hash function with as few collisions as possible

Does hash table performance increase or decrease as the number of buckets increases?

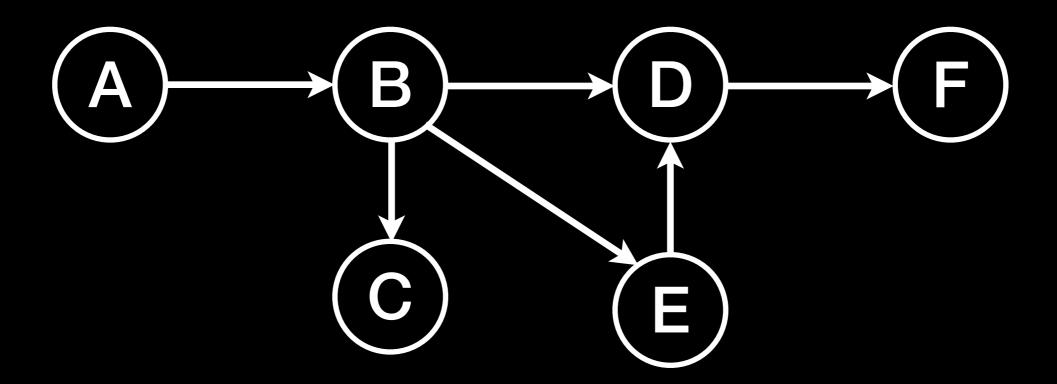
Does every key in a hash table need to be unique? Yes, that's the point of storing key/value pairs

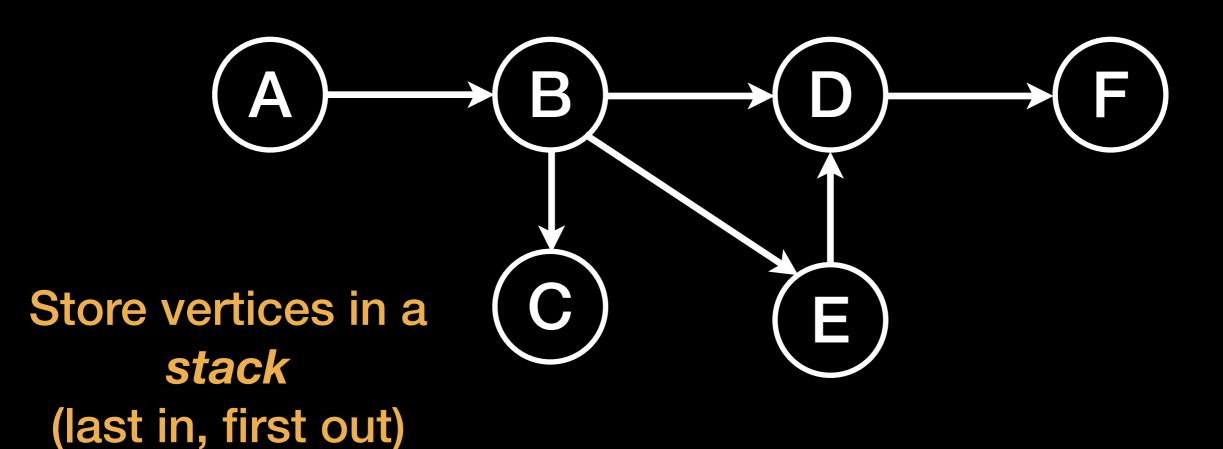
Does each key in a hash table need to hash to a unique value?

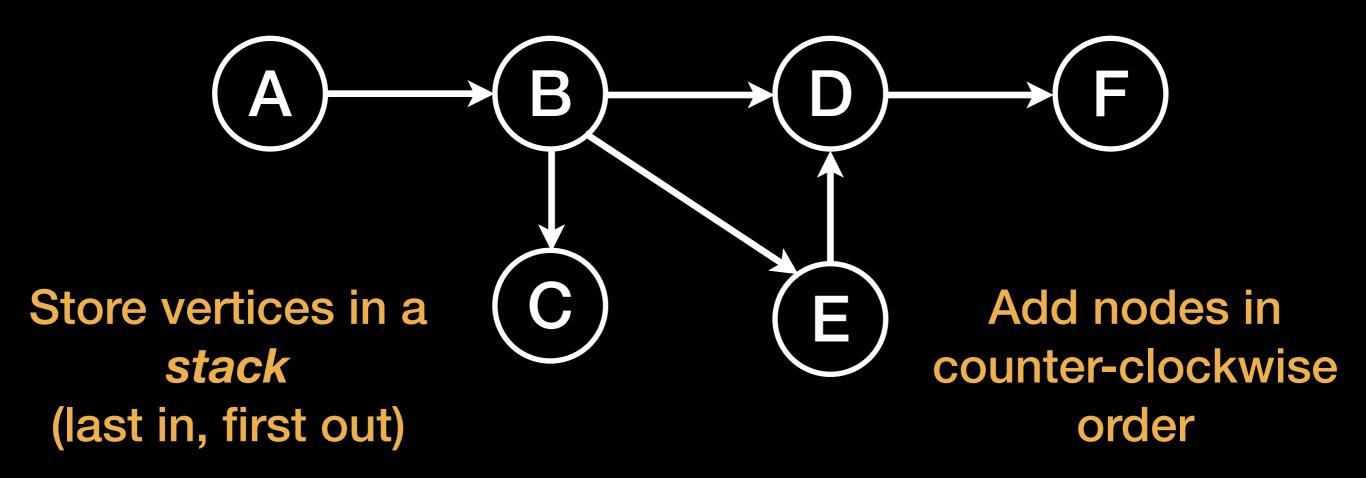
No, but we should use a hash function with as few collisions as possible

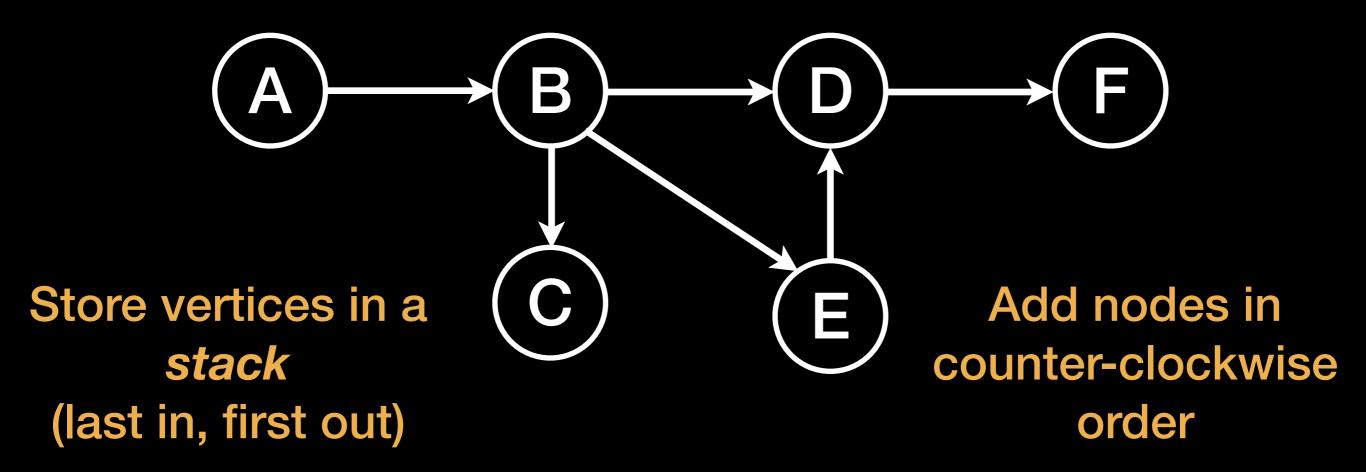
Does hash table performance increase or decrease as the number of buckets increases?

It should increase

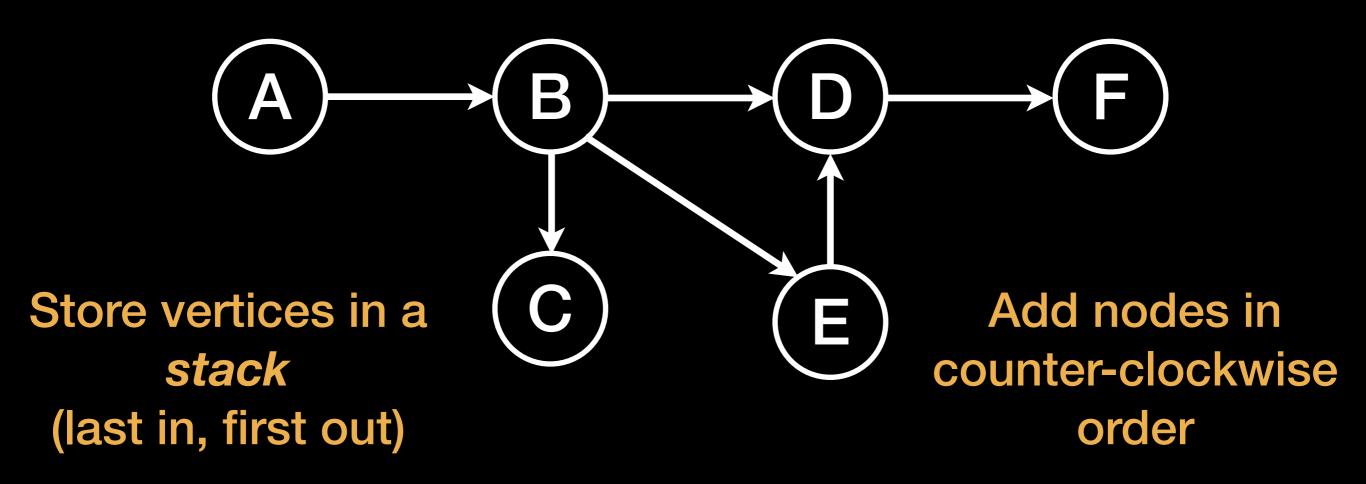






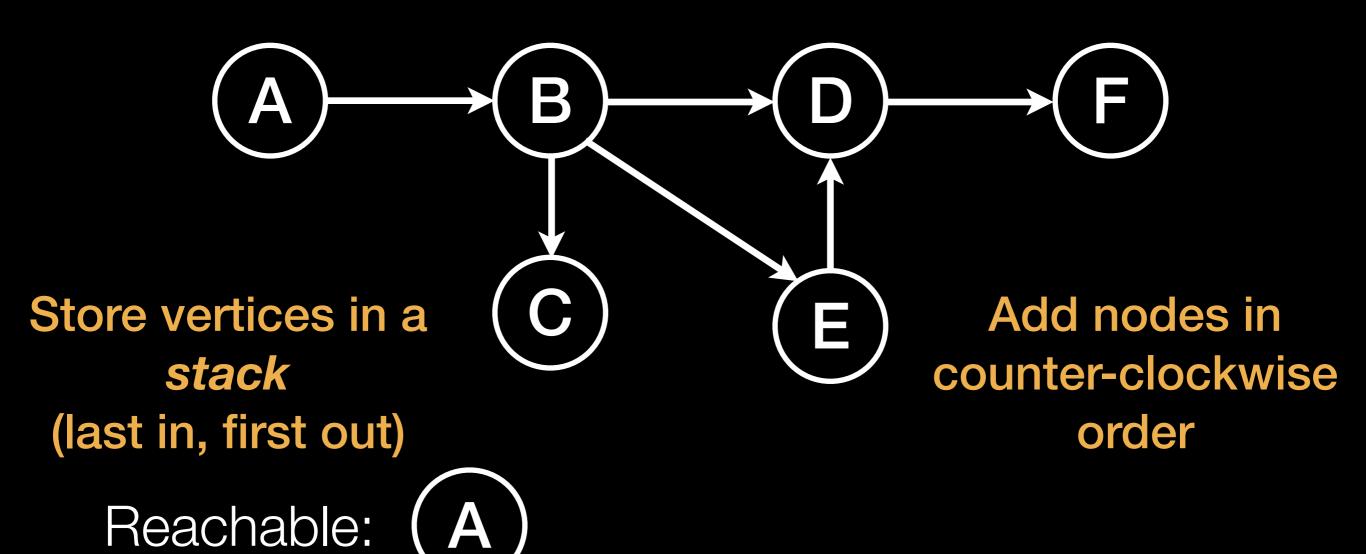


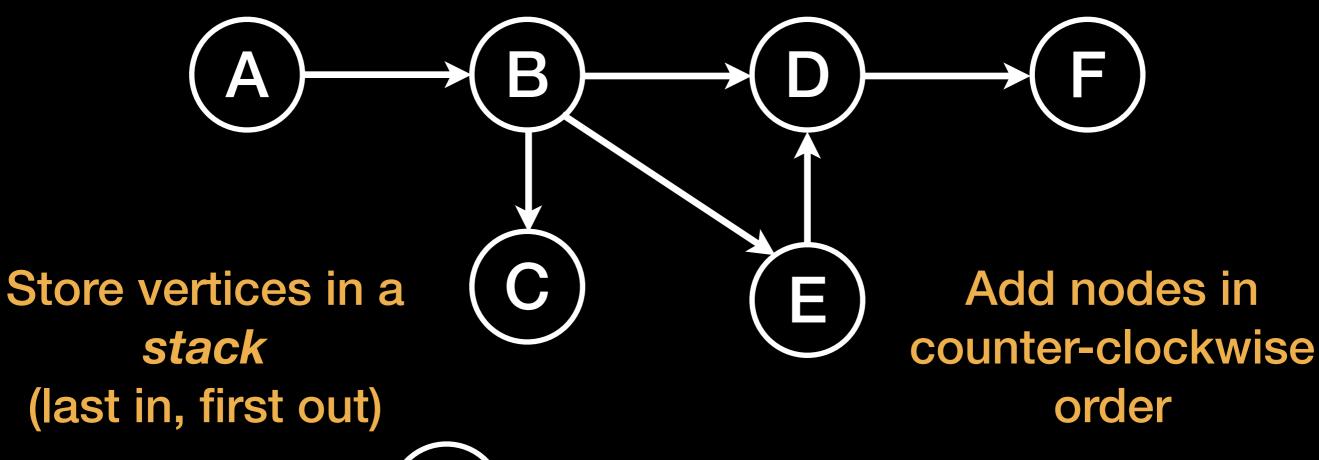
Reachable:



Reachable:

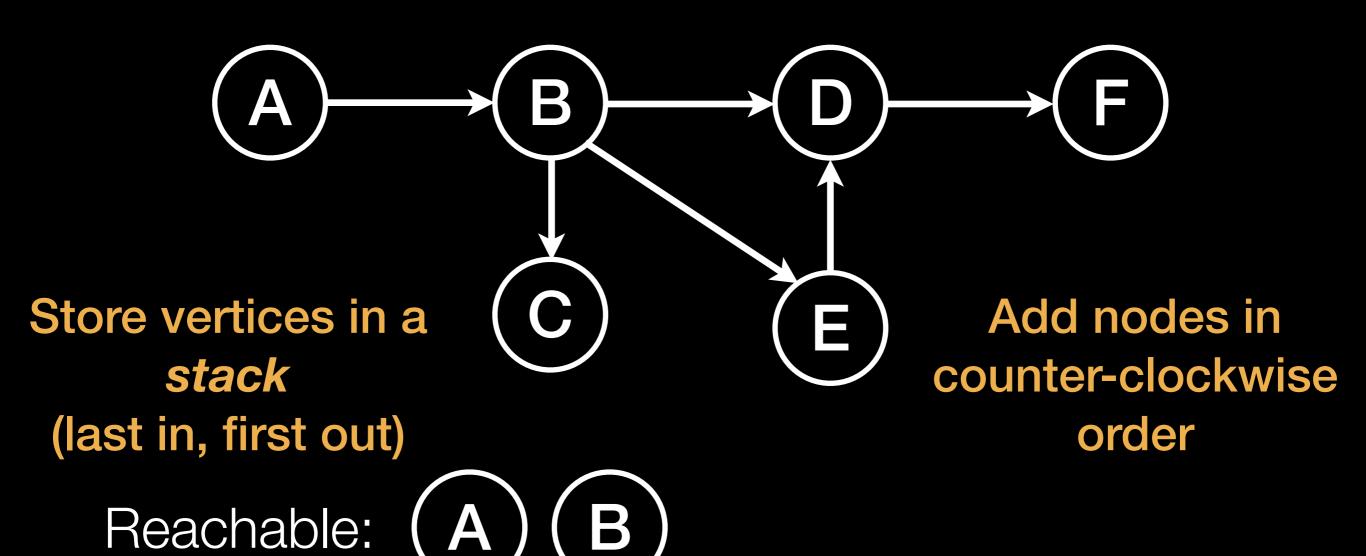
Known: (A)

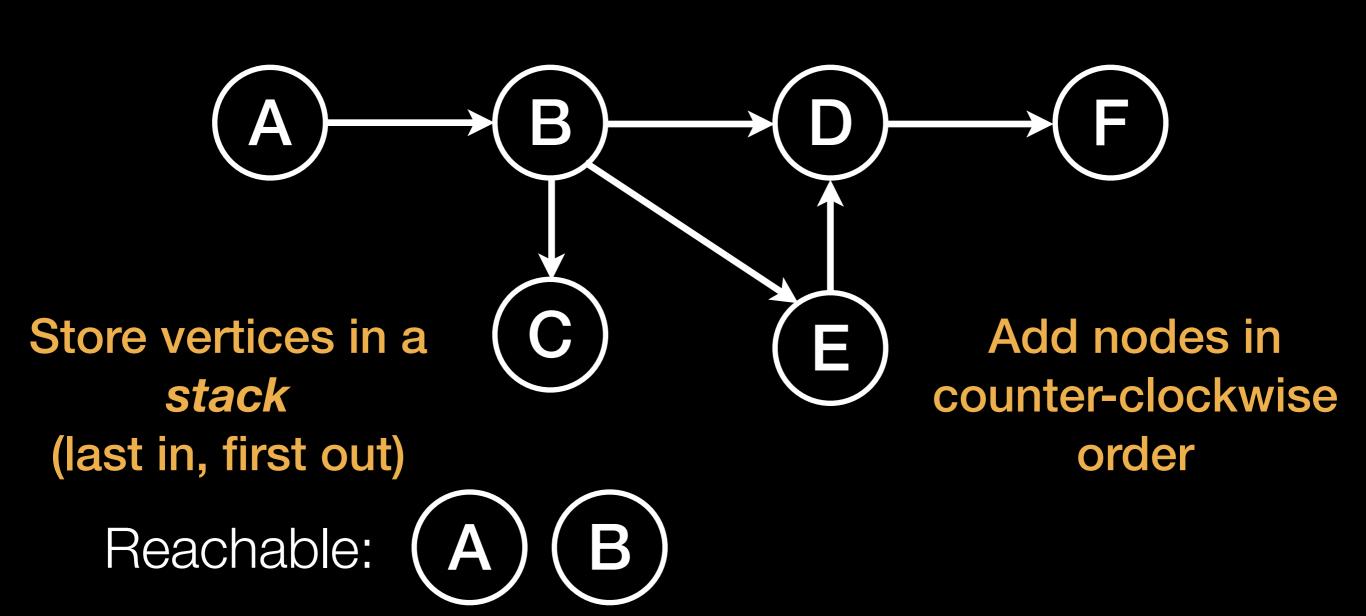




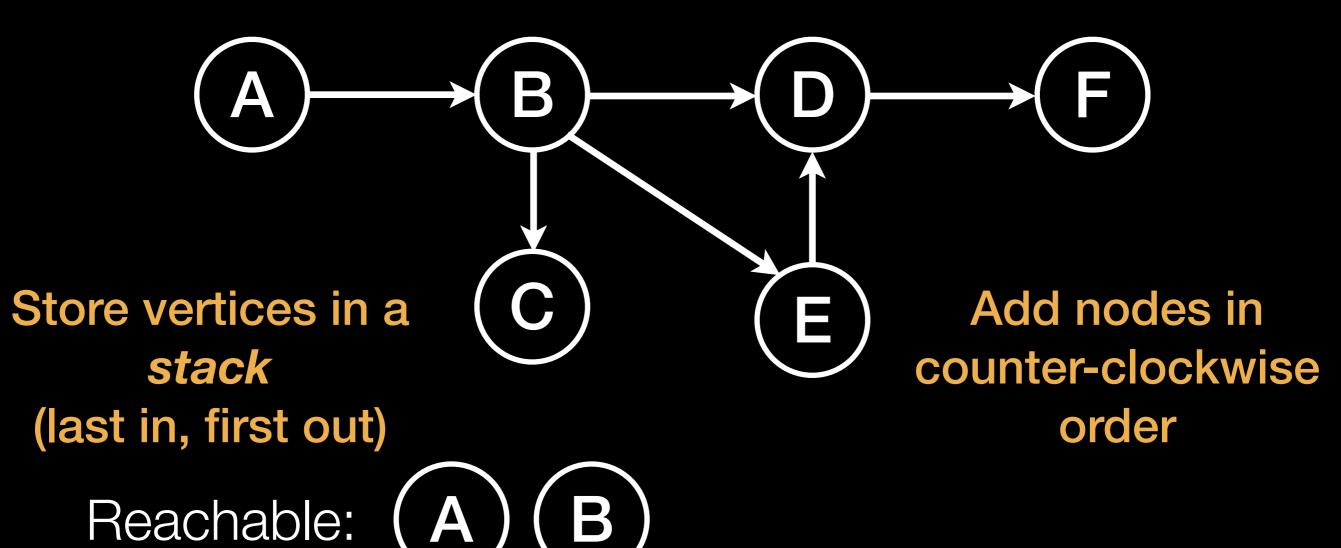
Reachable: (A)

Known: (B)

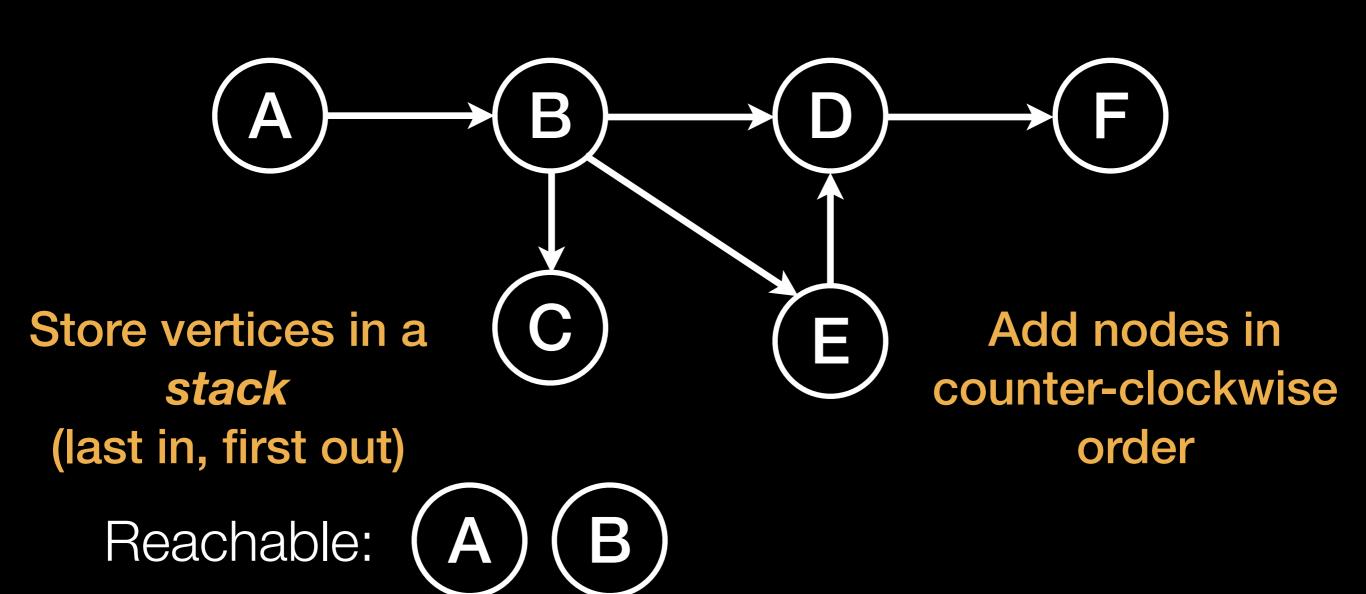


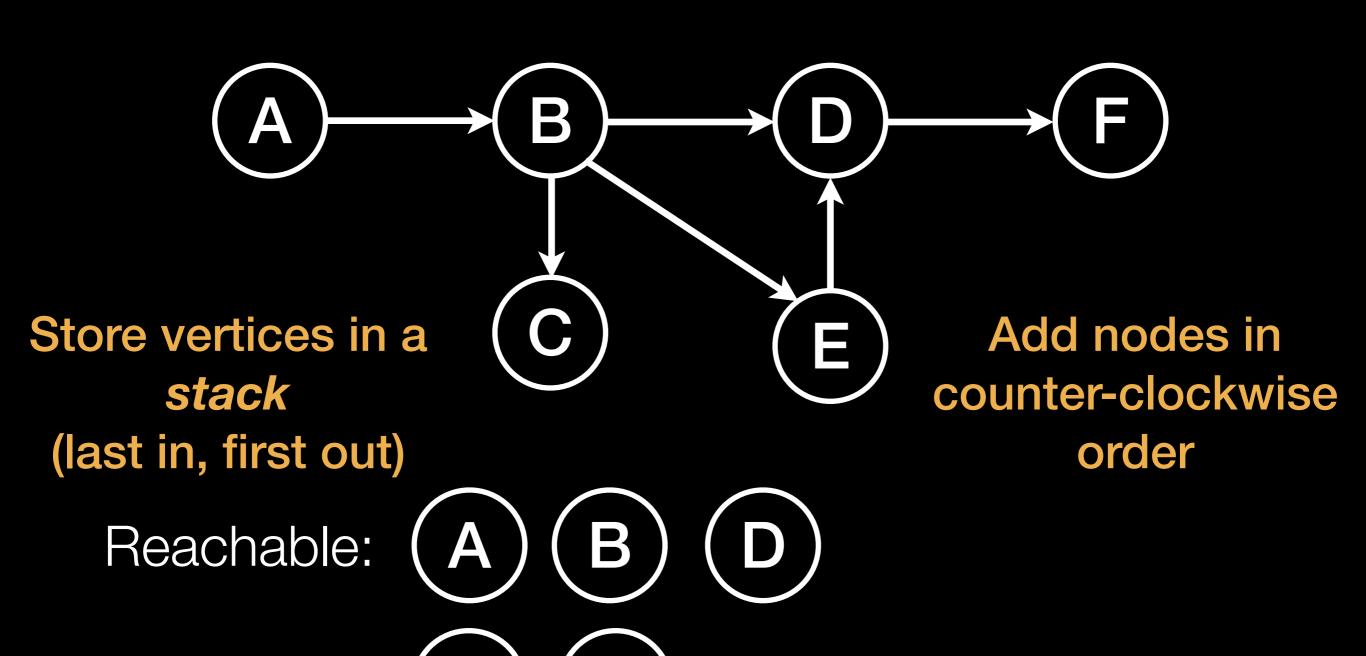


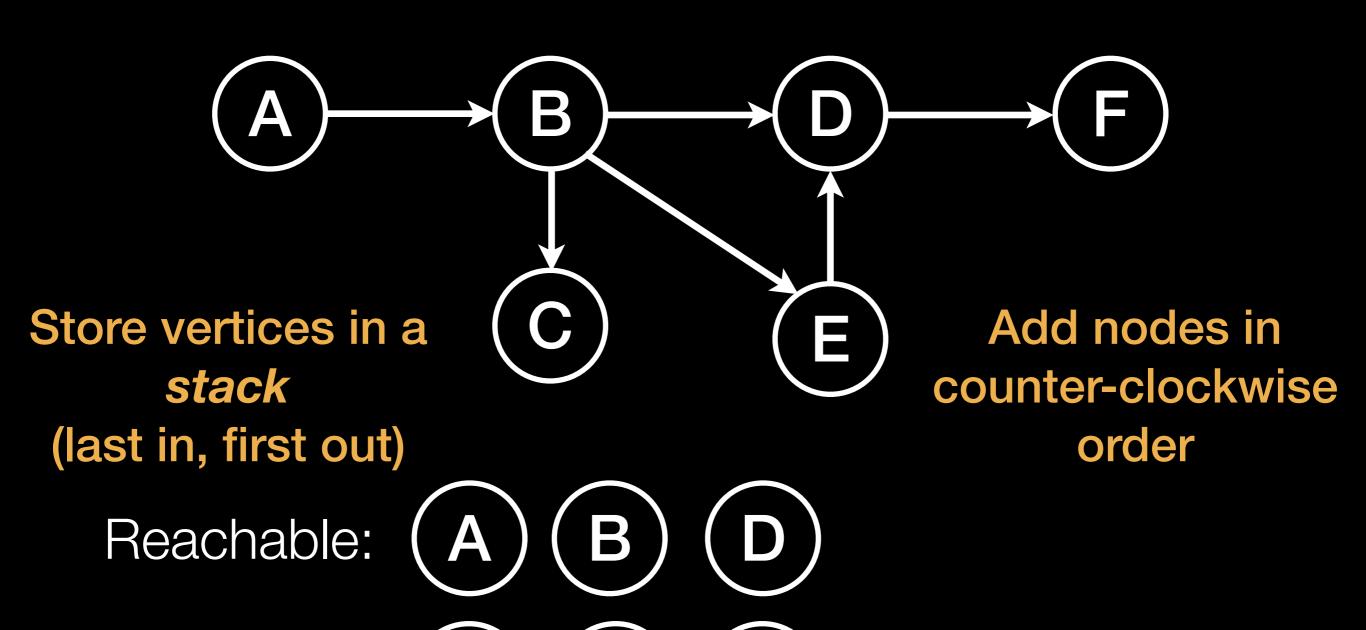
Known: (C)

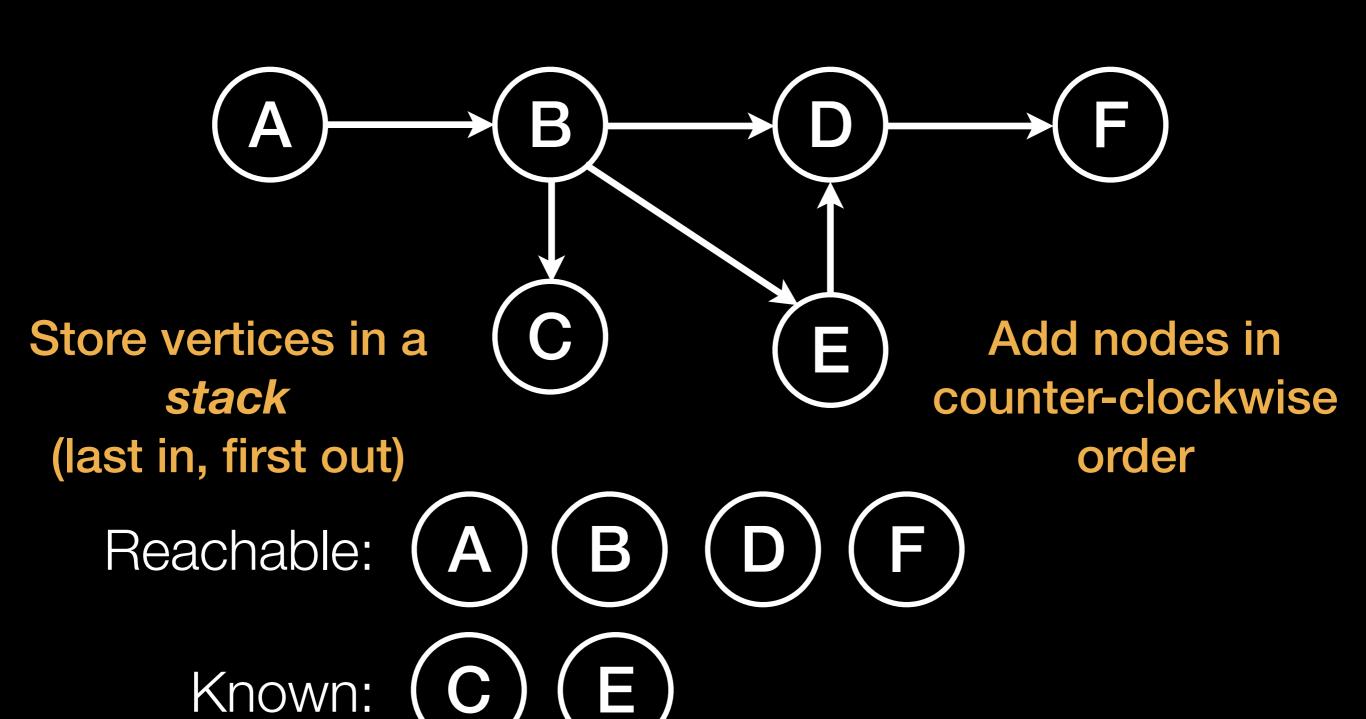


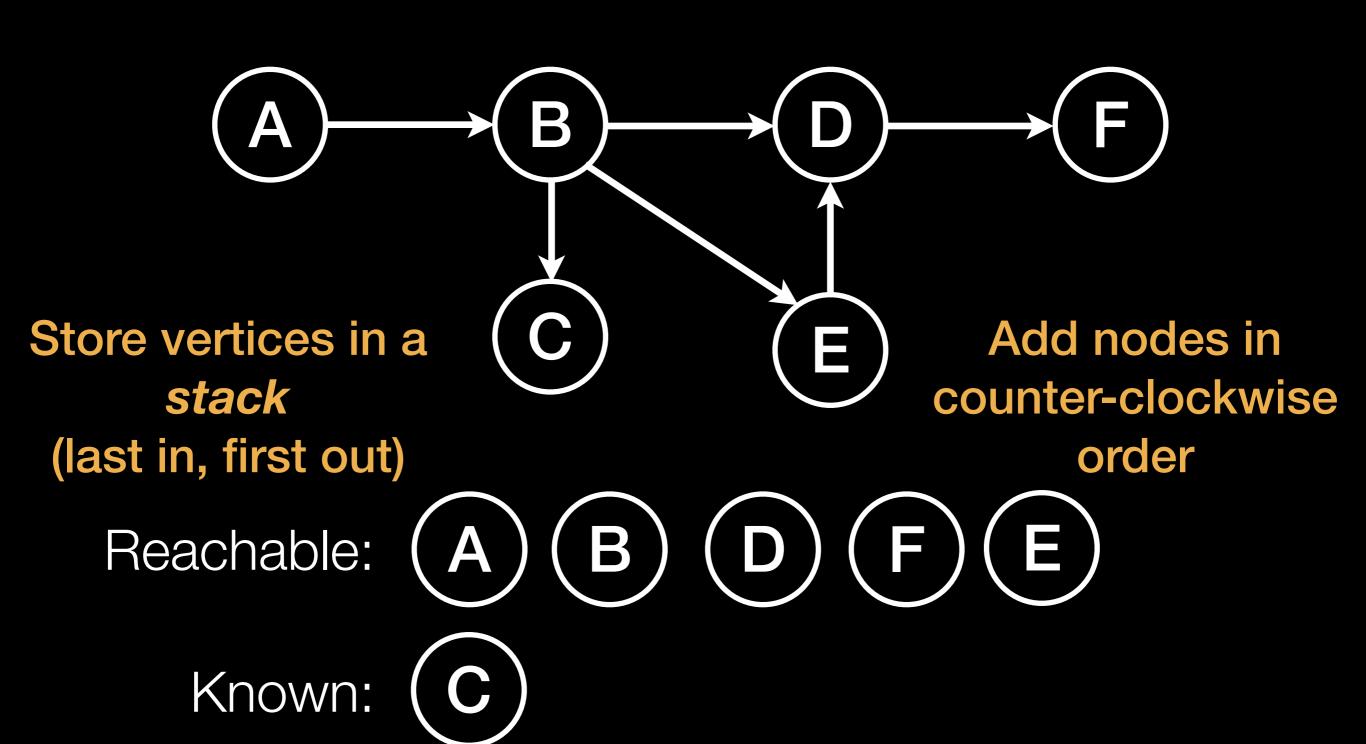
Known: (C) (E

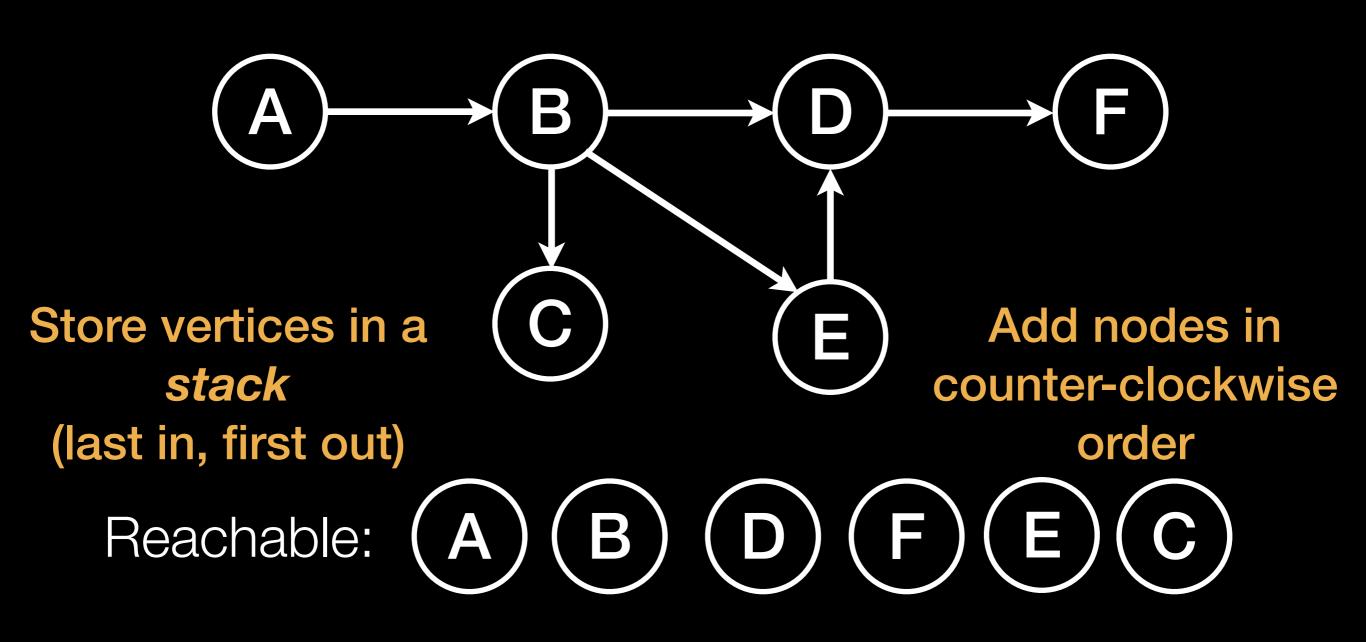


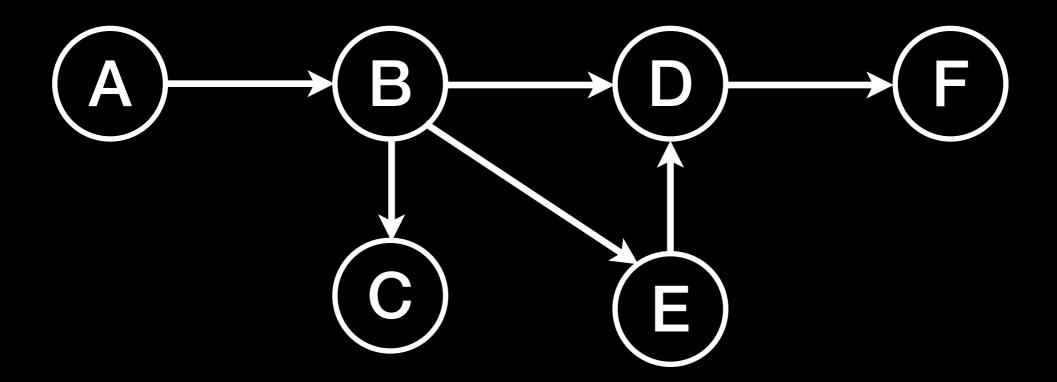


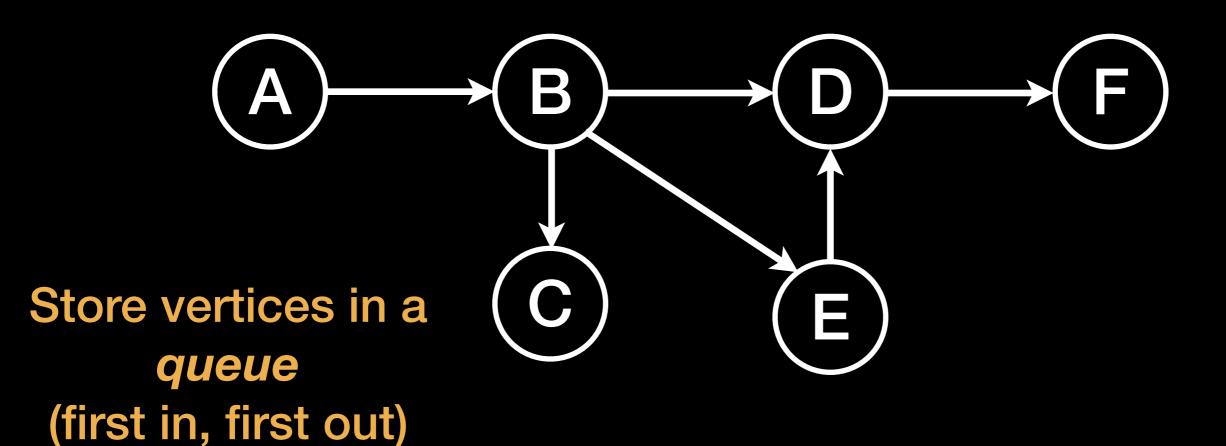


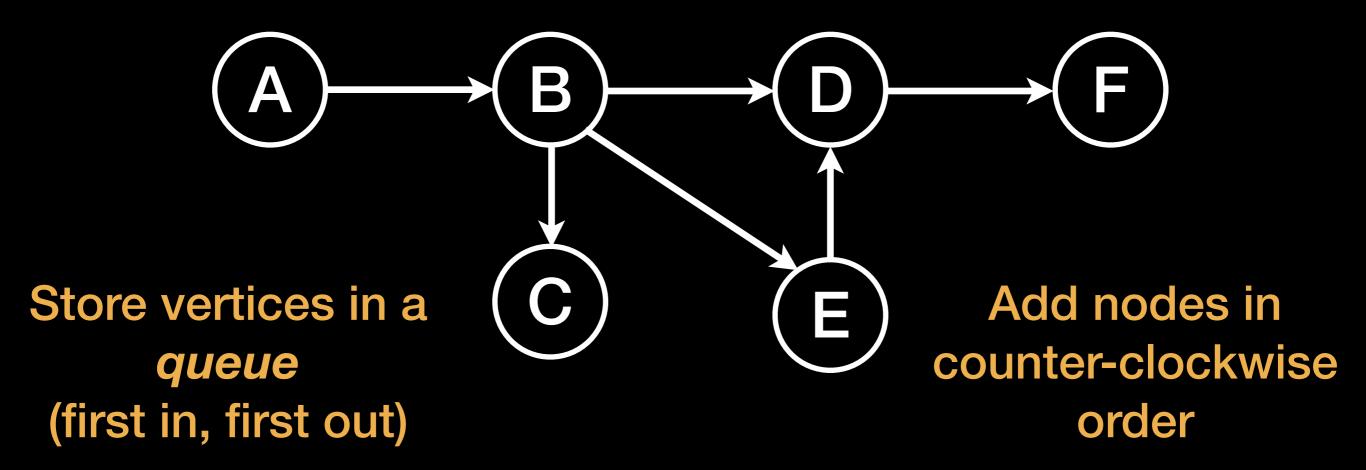


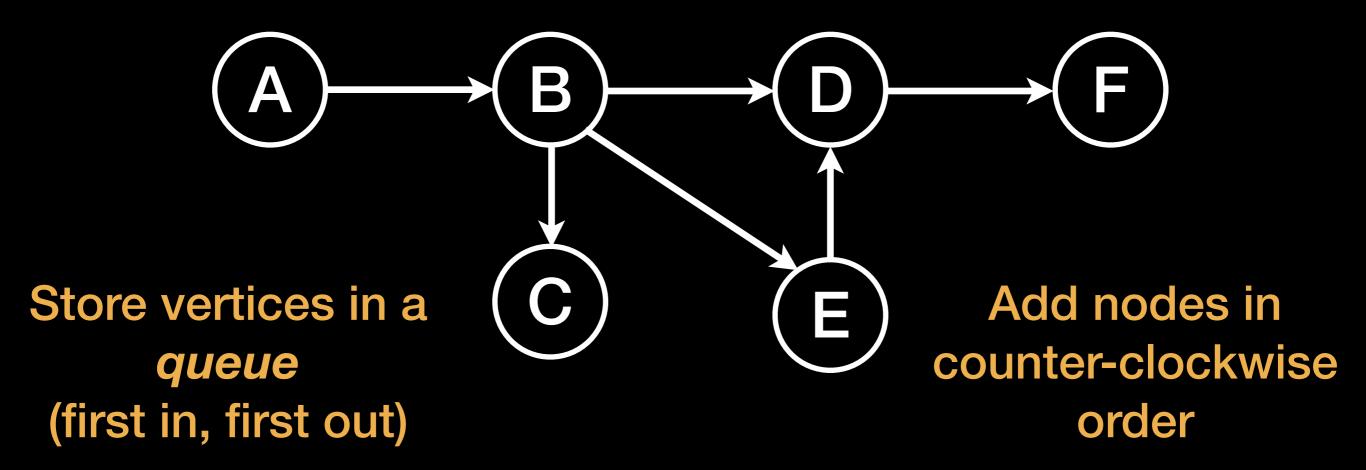




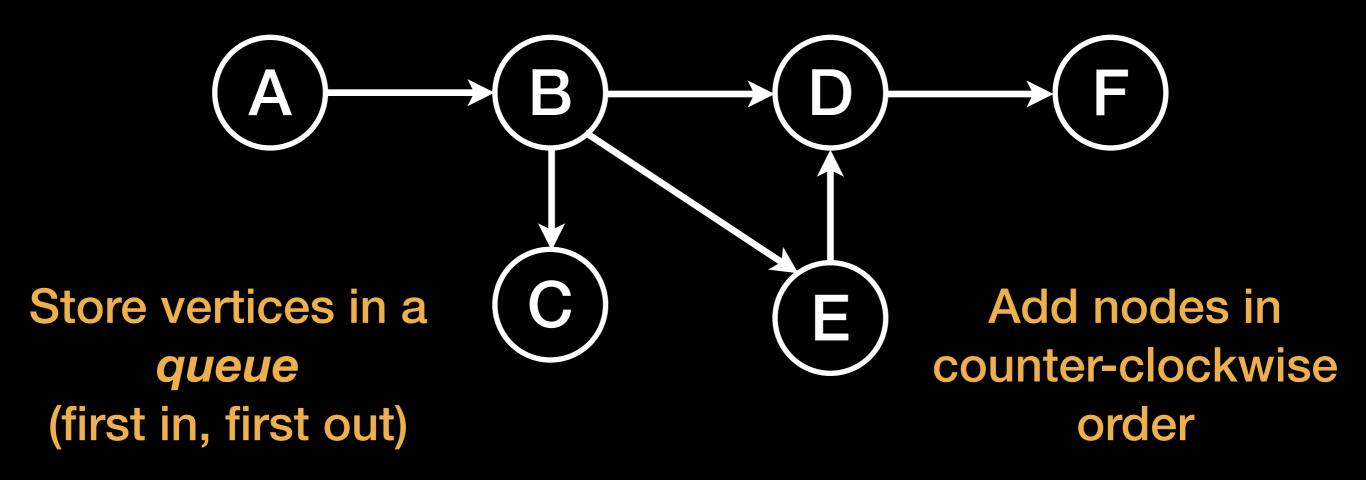






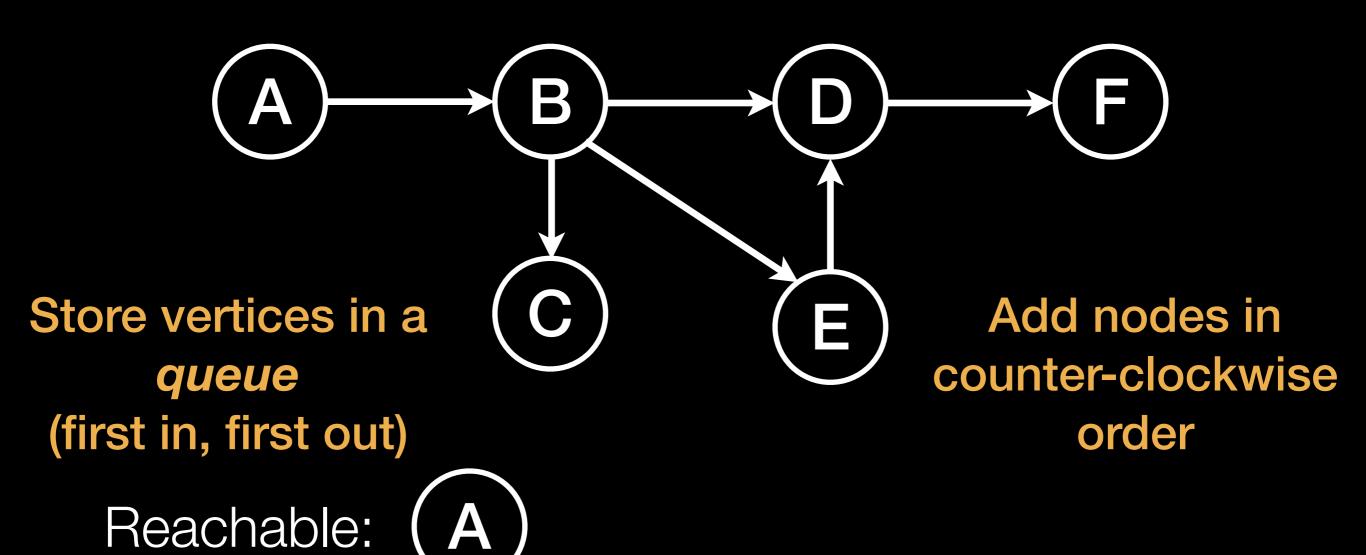


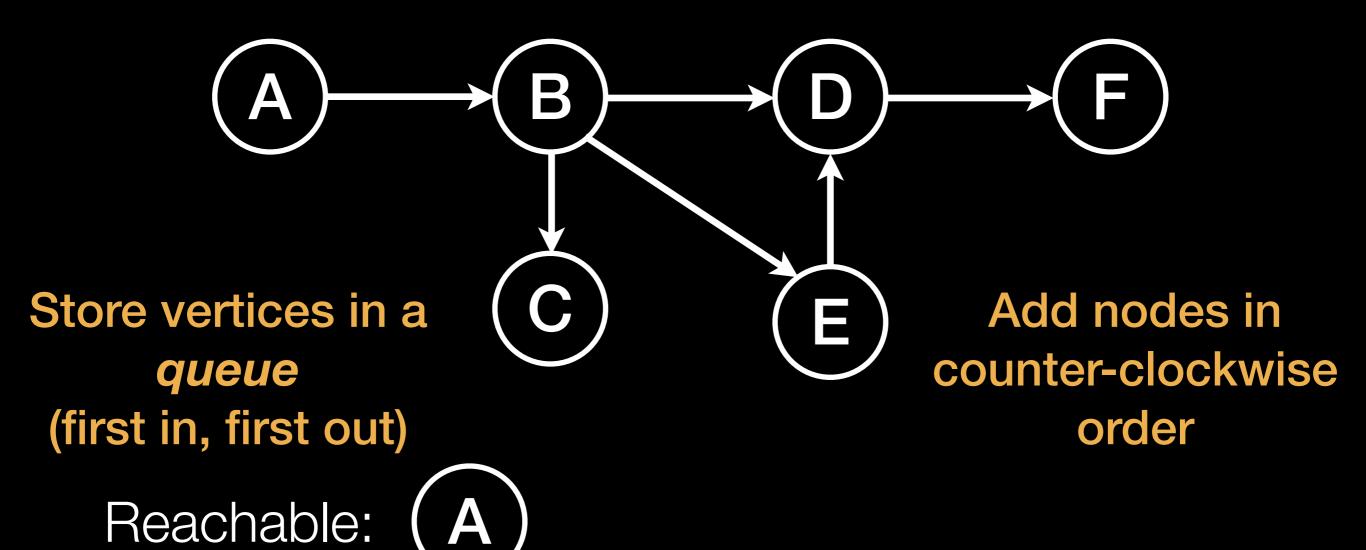
Reachable:



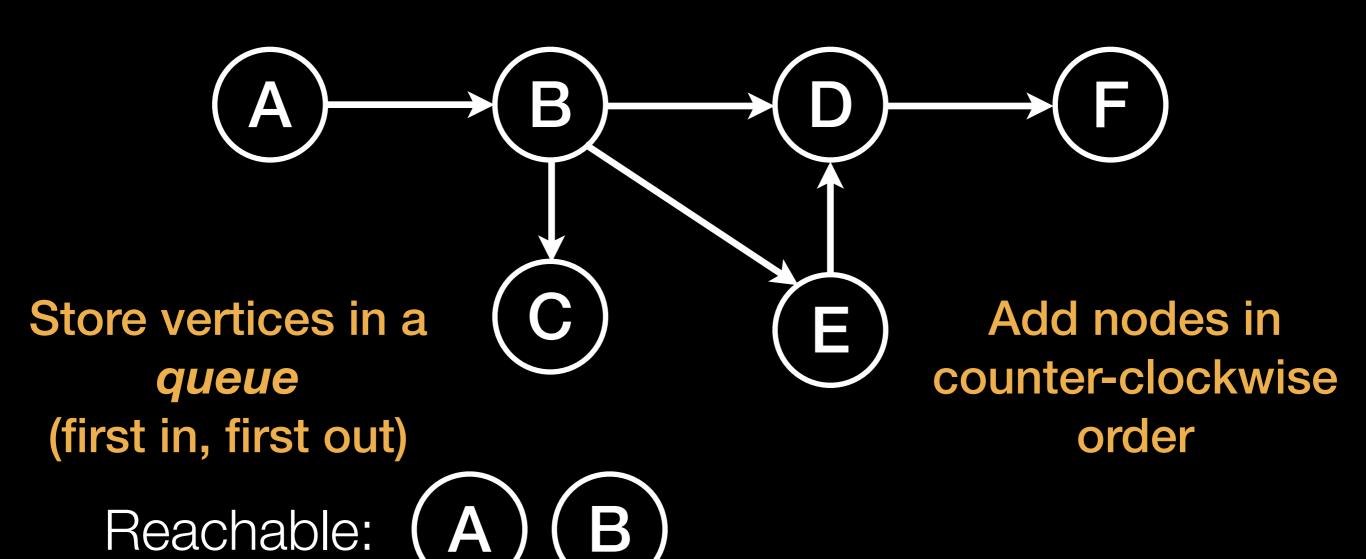
Reachable:

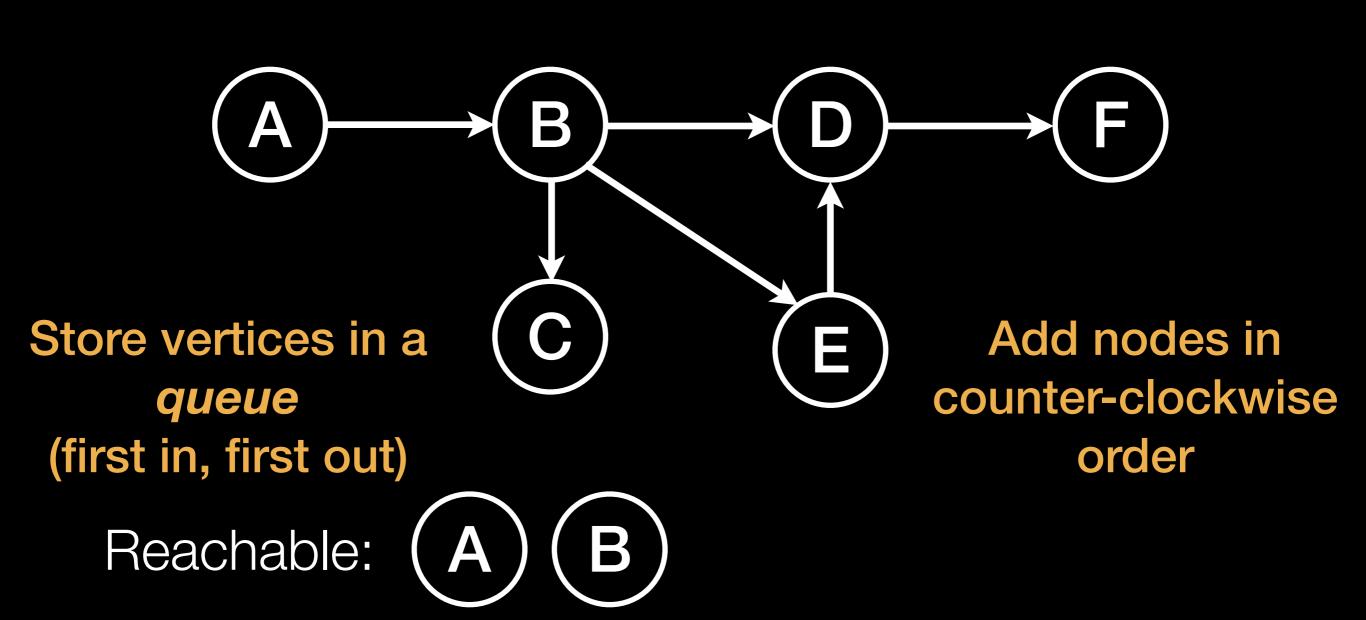
Known: (A)



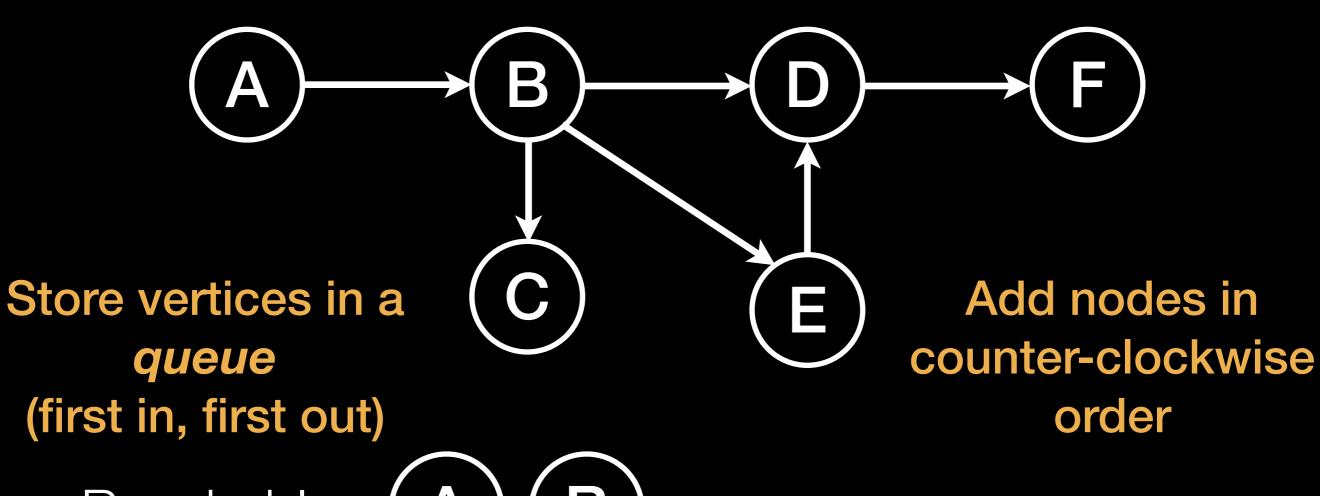


Known: (B)



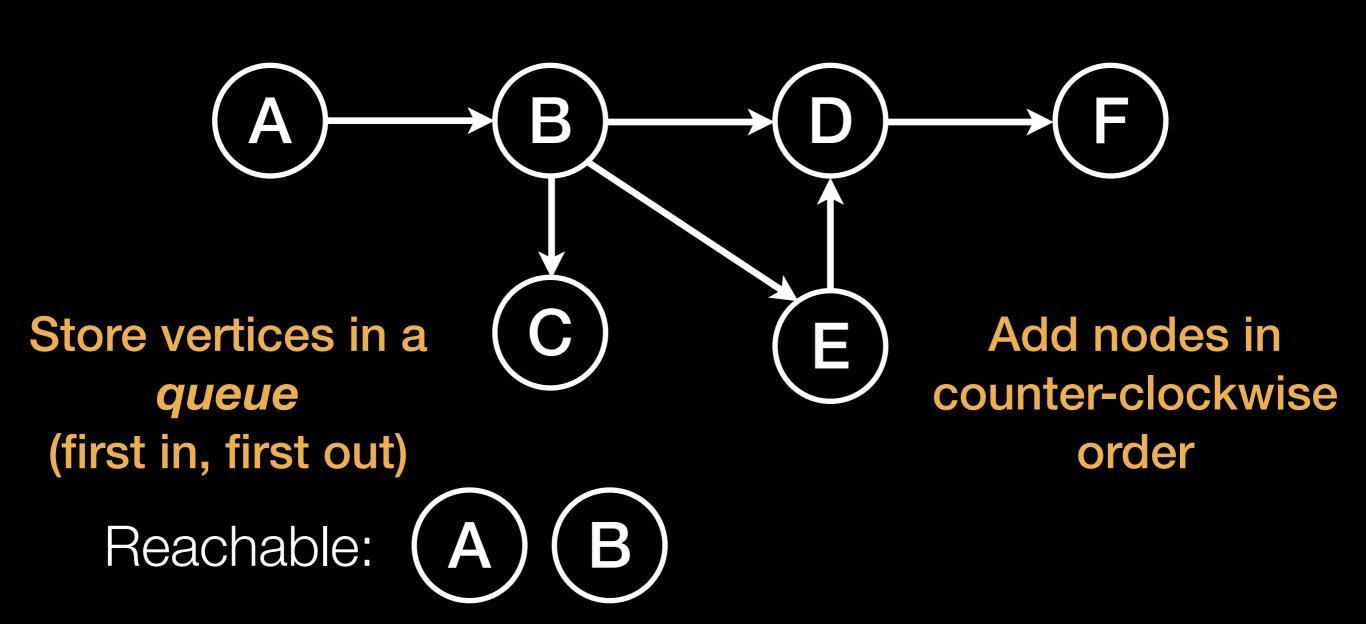


Known: (C)



Reachable: (A) (B)

Known: (C) (E)



Known: C E D

