

91

National Institute of Technology, Hamirpur  
Department of Computer Science and Engineering  
Third Year-Fifth Semester (End Semester Examination)  
CSD312-Design and Analysis of Algorithms

Time: 3hrs

Max. Marks 60

Give algorithm whenever possible.

For all problems, if you include any new algorithm in your solution, please also include a brief English description of what the algorithm does.

1. (5 Marks) An element in an array  $X$  is called a leader if it is greater than all elements to the right of it in  $X$ . Device a linear time algorithm to find all the leaders in an array. Show that  $X[9] = \{14, 20, 13, 15, 7, 8, 9, 4, 3\}$  has three leaders as 20, 15 and 9.
2. (5 Marks) We want to merge nine given sorted files where the number of records in each file is given as  $\{12, 34, 56, 73, 24, 11, 34, 56, 78\}$ . Suppose you want to pairwise merge these files, then find a single merged file such that minimum number of record moves are performed. Mention number of moves required by your procedure.
3. (5 Marks) A vertex  $v$  is called sink of graph  $G$  if there is a path from every vertex in  $G$  to  $v$ . Write an efficient algorithm to check if a Directed Acyclic Graph (DAG) has a sink. (also give an example) (Hint: A DAG may have at most one sink).
4. (2+2+1 Marks) Create a complete undirected graph with vertex set  $\{0, 1, 2, 3, 4\}$ . Entry  $W_{ij}$  in the matrix  $W$  below is the weight of the edge  $\{i, j\}$ .

$$W = \begin{pmatrix} 0 & 1 & 8 & 1 & 4 \\ 1 & 0 & 12 & 4 & 9 \\ 8 & 12 & 0 & 7 & 3 \\ 1 & 4 & 7 & 0 & 2 \\ 4 & 9 & 3 & 2 & 0 \end{pmatrix}$$

- a) Find out that what is the minimum possible weight of a spanning tree  $T$  in this graph such that vertex 0 is a leaf node in the tree  $T$ ? Explain the procedure in one or two lines.
- b) What is the minimum possible weight of a path  $P$  from vertex 1 to vertex 2 in this graph such that  $P$  contains at most 3 edges?
5. (7 marks) Can we have a graph in which a negative weighted cycle is not reachable from source  $S$ ? If no, then why it is not possible and is that mean, Bellman – Ford algorithm will always detect negative weight cycle, if one exists. If yes, then can Bellman-Ford algorithm detect that cycle and what final value will be returned by the algorithm? Elaborate by considering an example.
6. (4+3 Marks) Depth-First Search can be used to do *in-order traversal* of a binary search tree. That is, given a binary search tree  $T$  containing  $n$  distinct elements  $a_1 < a_2 < \dots < a_n$ , DFS can be used to return an array  $[a_1, a_2, \dots, a_n]$  containing these elements in sorted order. Give algorithm and an example for inOrderTraversal using DFS.

7. (8 Marks) Give a dynamic programming solution for the SUBSET-SUM problem. Explain why this solution does not put the subset sum problem in NP-hard?
8. (3+3+2 Marks) Write algorithm to insert element into a min-heap and draw the min-heap that results from insertion of following elements in order into an initially empty min-heap: 7, 6, 5, 4, 3, 2, 1. Show the result after the deletion of root of this heap.
9. (3+5+2 Marks) Give algorithm of quick sort and apply to sort the list E, X, A, M, P, L, E in alphabetic order. What value of  $q$  does PARTITION return when all elements in the array  $A[p \dots r]$  have the same value?