

TI

2023-04-01



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R Markdown Cookbook, by Yihui Xie, Christophe Dervieux, Emily Riederer  
<https://bookdown.org/yihui/rmarkdown-cookbook/>

Happy Git and GitHub for the useR, by Jennifer Bryan <https://happygitwithr.com/index.html>

Qiita <https://qiita.com/kamorits/items/6f342da395ad57468ae3>  
[https://lbusett.github.io/insert\\_table/](https://lbusett.github.io/insert_table/)

This is a *sample* book written in **Markdown**. You can use anything that Pandoc’s Markdown supports; for example, a math equation  $a^2 + b^2 = c^2$ .

## 0.1 Usage

Each **bookdown** chapter is an .Rmd file, and each .Rmd file can contain one (and only one) chapter. A chapter *must* start with a first-level heading: **# A good chapter**, and can contain one (and only one) first-level heading.

Use second-level and higher headings within chapters like: **## A short section** or **### An even shorter section**.

The **index.Rmd** file is required, and is also your first book chapter. It will be the homepage when you render the book.

## 0.2 Render book

You can render the HTML version of this example book without changing anything:

1. Find the **Build** pane in the RStudio IDE, and
2. Click on **Build Book**, then select your output format, or select “All formats” if you’d like to use multiple formats from the same book source files.

Or build the book from the R console:

```
bookdown::render_book()
```

To render this example to PDF as a `bookdown::pdf_book`, you'll need to install XeLaTeX. You are recommended to install TinyTeX (which includes XeLaTeX): <https://yihui.org/tinytex/>.

### 0.3 Preview book

As you work, you may start a local server to live preview this HTML book. This preview will update as you edit the book when you save individual .Rmd files. You can start the server in a work session by using the RStudio add-in “Preview book”, or from the R console:

```
bookdown::serve_book()
```



# Chapter 1

## (PART\*)



# Chapter 2

1 ( )

$= -$   $= - \times 9$

•

•

( ) <https://www.datastadium.co.jp/news/information/2856>

WBC 2023 2 19 <https://www.nikkei.com/article/DGXZQODH1482H0U3A210C2000000/>

2 4 6

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• 4 —

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3

• “ ”

• “ ”

4

• — 2

- 2015/4/2 2 <https://toyokeizai.net/articles/-/67103>
- ... <https://www.tokyo-np.co.jp/article/234995>
- ... <https://www.sankei.com/article/20230209-IZROVT6MY5CGLE4KEOUDEYKQBE/>
- [https://cigs.canon/article/202121\\_6483.html](https://cigs.canon/article/202121_6483.html)
- <https://www.jwa.or.jp/service/weather-and-data/weather-and-data-02/>
- <https://www.konicaminolta.jp/business/solution/aisee/case/002.html>
- 23 <https://www.nikkei.com/article/DGXZQOUB1940O0Z11C22A0000000/>
- <https://business.nikkei.com/atcl/gen/19/00081/110200467/>
- 2021 8 <https://www.tdb.co.jp/report/watching/press/p210807.html>
- 
- 
- 5 ( )
- GDP
  - (2015)
  - 1% 1 GDP 0.24%
  - 1% 1 GDP 0.32%
  - (2015 ) %([http://www.esri.go.jp/jp/archive/e/\\_dis/e/\\_dis314/e/\\_dis314.pdf](http://www.esri.go.jp/jp/archive/e/_dis/e/_dis314/e/_dis314.pdf))
  - <https://www5.cao.go.jp/keizai1/mitoshi/mitoshi.html>
  - <https://www5.cao.go.jp/keizai1/mitoshi/2022/r050123mitoshi.pdf>
  - XX
  - <https://www.stat.go.jp/training/2kenkyu/pdf/rn/2-rn-002.pdf> <https://obamawhitehouse.archives.gov/blog/2013/06/11/what-great-gatsby-curve>
  - 6

## 2.1

### 2.1.1

SSDSE <https://www.nstac.go.jp/use/literacy/ssdse/>



Figure 2.1: image of histogram

e-Stat <https://www.nstac.go.jp/sys/files/static/SSDSE/data/2019/eStat-2019.pdf>

- SSDSE e-Stat SSDSE e-Stat  
Stat SSDSE  
<https://www.nstac.go.jp/statcompe/index.html>

2.1.2

Cracking The Mystery Of California’s High Egg Prices <https://www.hoover.org/research/cracking-mystery-californias-high-egg-prices>

2.2

- 
- 

1	( )
2	( )
3	
4	
5	



# Chapter 3

## 3.1

•

ID					...	GPA	( )
155001	3	S	A	...	3.67	45	
155002	3	C	B	...	1.73	90	
:	:	:	:		:	:	

{ }

## 3.2

## 3.3 (Stem-and-Leaf)

( ) 50 ( )

|—|—|—|—|—|—|—|—|—| 5 | 9 | 15 | 15 | 17 | 24 | 25 | 25 | 27 | 29 | 29 |  
29 | 32 | 32 | 34 | 34 | 35 | 36 | 36 | 38 | 38 | 39 | 39 | 39 | 39 | 43 | 44 | 44 | 44 |  
45 | 45 | 47 | 47 | 47 | 52 | 54 | 54 | 56 | 58 | 59 | 59 | 67 | 73 | 75 | 79 | 82 | 84 |  
84 | 89 | 99 |

( )  
• ( )  
•

29  
↑ ↑

10	1
0	59
1	557
2	4557999
3	2244566889999
4	344455777
5	2446899
6	7
7	359
8	2449
9	9

( ) 50  
• 25  
• 25  
•  
( , median) ,

3.4

( ) 50 ( )

0-9	2
10-19	3
20-29	7
30-39	13
40-49	9
50-59	7
60-69	1





1.

<hr/>	
<hr/>	
$n$	50
$x_{max}$	99
$x_{min}$	5
<hr/>	

2.  $m$ 

$$m \approx 1 + 3.32 \times \log_{10} \underset{\substack{\uparrow \\ n}}{50} \approx 1 + 3.32 \times 1.699 \approx 1 + 5.64 = 6.64$$

3.  $c$ 

$$c \approx \text{---} \approx \frac{99 - 5}{7} \approx 13$$

1.

---



---



---

2.

3.

1.

2.

**3.5.1**

( )

1. 30

2. 30

3. 50

4. 50

1. 13 2. 26 3. 34 4. 68

( ) 31 40

$$30 = \frac{30}{\text{---}} = \frac{13}{50} = 0.26$$

	( )	( )	
0-9	2	0.04	$\leftarrow 2/50$
10-19	3	0.06	$\leftarrow 3/50$
20-29	7	0.14	
30-39	13	0.26	$\leftarrow 13/50$
40-49	9	0.18	
50-59	7	0.14	
60-69	1	0.02	
70-79	3	0.06	
80-89	4	0.08	
90-99	1	0.02	
	50	1.00	



# Chapter 4

( )5 1 2 3 4 5 ~  
http://www.stat.go.jp/data/kakei/kaisetsu.htm  
1966 1966 5 (%)

	1	2	3	4	5
1966	5.6	12.4	17.7	23.8	40.5

US Department of Commerce, Statistical Abstract of the United States  
( ) 360 100

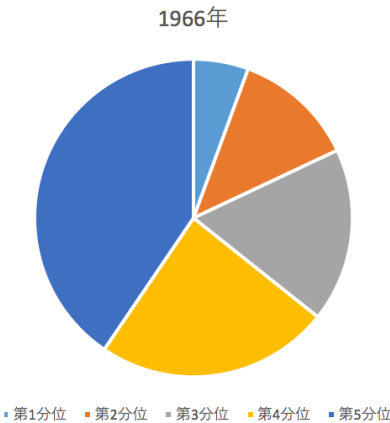


Figure 4.1: image of histogram

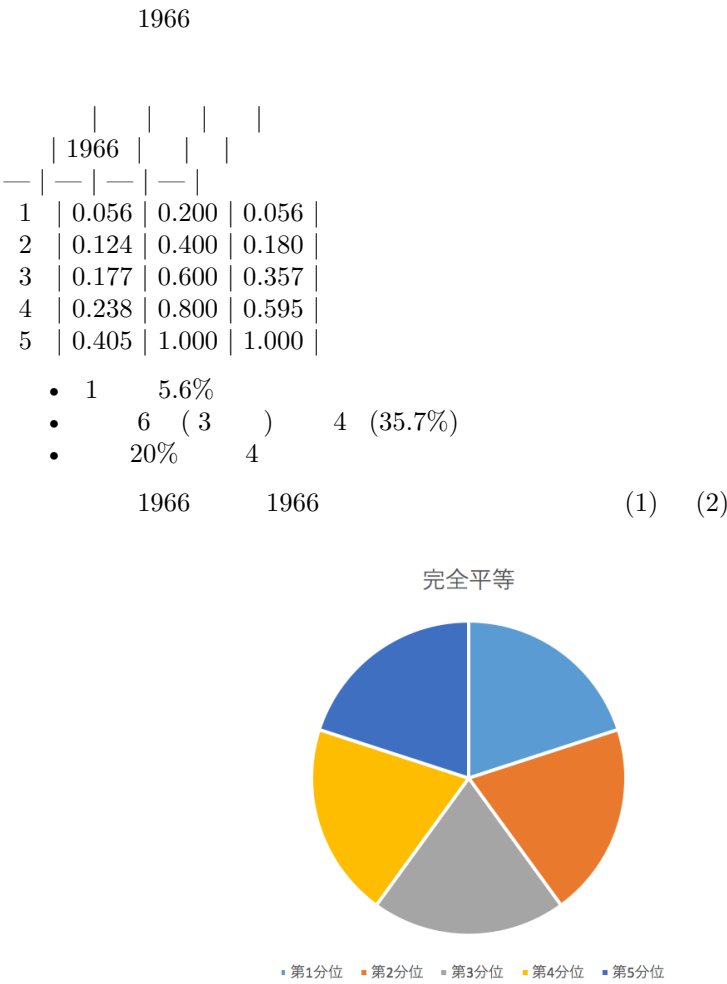


Figure 4.2: image of histogram

1966 (Lorenz curve) 1905 (M.O.Lorenz)

4.0.1

- 1. 1966
- 2.
- 3.

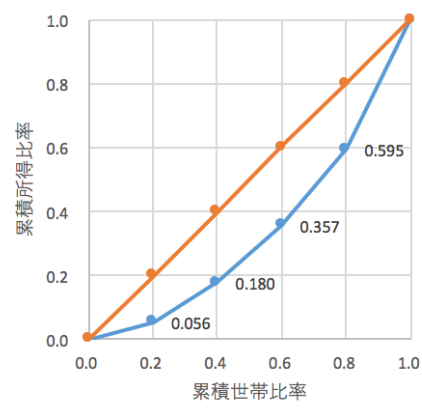


Figure 4.3: image of histogram

4.  
5. 2                    2  
2005                    2005

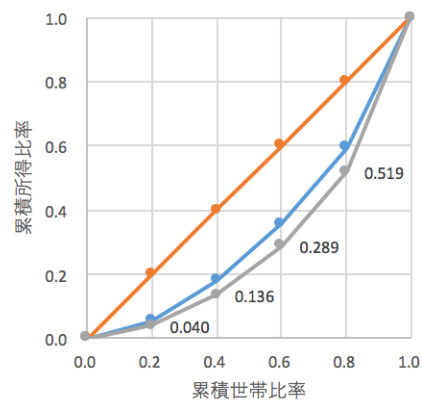


Figure 4.4: image of histogram

- 1969 2005
- 1966 2005

- 1. (Gini coefficient) ( )
- 2. 0 1 0 1

- 1. ( A ) 0.5
- 2. B

$$= ( A - B ) \times 2 = 1 - B \times 2$$

3.

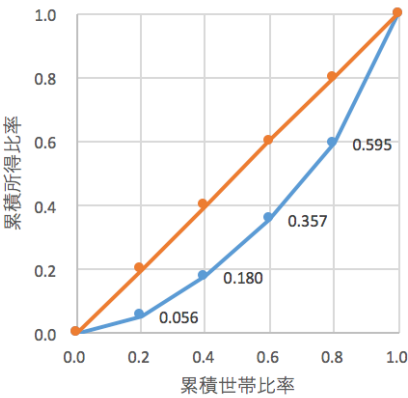


Figure 4.5: image of histogram

• 5

$$\begin{aligned} & \frac{1}{2} \times \underset{\uparrow}{0.056} \times \underset{\uparrow}{0.2} \\ & + \frac{1}{2} \times (0.056 + 0.180) \times 0.2 \\ & + \frac{1}{2} \times (0.180 + 0.357) \times 0.2 \\ & + \frac{1}{2} \times (0.357 + 0.595) \times 0.2 \\ & + \frac{1}{2} \times (\underset{\uparrow}{0.595} + \underset{\uparrow}{1.000}) \times \underset{\uparrow}{0.2} \\ & = 0.3376 \end{aligned}$$

4. 1969

$$= 1 - 0.3376 \times 2 = 0.3248$$

5. B



- 5 20% “ ” 0.2
- $\frac{1}{2}$
- 

$$\begin{aligned} \frac{1}{2} \times 0.2 \times \{ & \underset{\uparrow}{0.056} + (0.056 + 0.180) + (0.180 + 0.357) \\ & + (0.357 + 0.595) + (0.595 + 1.000) \} \\ = & 0.3376 \end{aligned}$$

2005 2005

1. B

$$\begin{aligned} B &= \frac{1}{2} \times 0.2 \times \{ 0.040 + \underset{\uparrow}{(0.040 + 0.136)} \\ & \quad + (0.136 + 0.289) + (0.289 + 0.519) \\ & \quad + (0.519 + 1.000) \} \\ &= 0.2968 \end{aligned}$$

2. 2005

$$= 1 - 2 \times 0.2968 = 0.4064$$

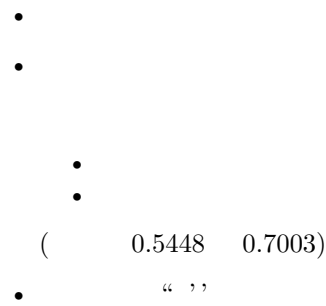
3. 0.3248(1969 ) 0.4064(2005 )



# Chapter 5

従業員の規模(人)	繊維工業		鉄鋼業	
	事業所	従業員	事業所	従業員
5~9	4073	26359	1566	10548
10~19	2039	27256	1388	18892
20~29	711	16928	650	15713
30~49	523	19660	511	19421
50~99	375	26008	448	30542
100~199	165	22756	189	26937
200~299	37	9163	59	14175
300~499	16	5450	42	16310
500~999	5	3643	24	15310
1000~	3	3188	25	59589
総数	7947	160411	4902	227437

Figure 5.1: image of histogram



従業員の規模(人)	繊維工業		鉄鋼業	
	事業所	従業員	事業所	従業員
	0.000	0.000	0.000	0.000
5~9	0.513	0.164	0.319	0.046
10~19	0.769	0.334	0.603	0.129
20~29	0.859	0.440	0.735	0.199
30~49	0.924	0.562	0.839	0.284
50~99	0.972	0.724	0.931	0.418
100~199	0.992	0.866	0.969	0.537
200~299	0.997	0.923	0.981	0.599
300~499	0.999	0.957	0.990	0.671
500~999	1.000	0.980	0.995	0.738
1000~	1.000	1.000	1.000	1.000

Figure 5.2: image of histogram

- ( )

5.1

3

- 1

$$\sum_{i=1}^n (X_i + c) = \sum_{i=1}^n X_i + nc$$

- 2

$$\sum_{i=1}^n cX_i = c \sum_{i=1}^n X_i$$

- 3

$$\sum_{i=1}^n (aX_i + b) = a \sum_{i=1}^n X_i + nb$$

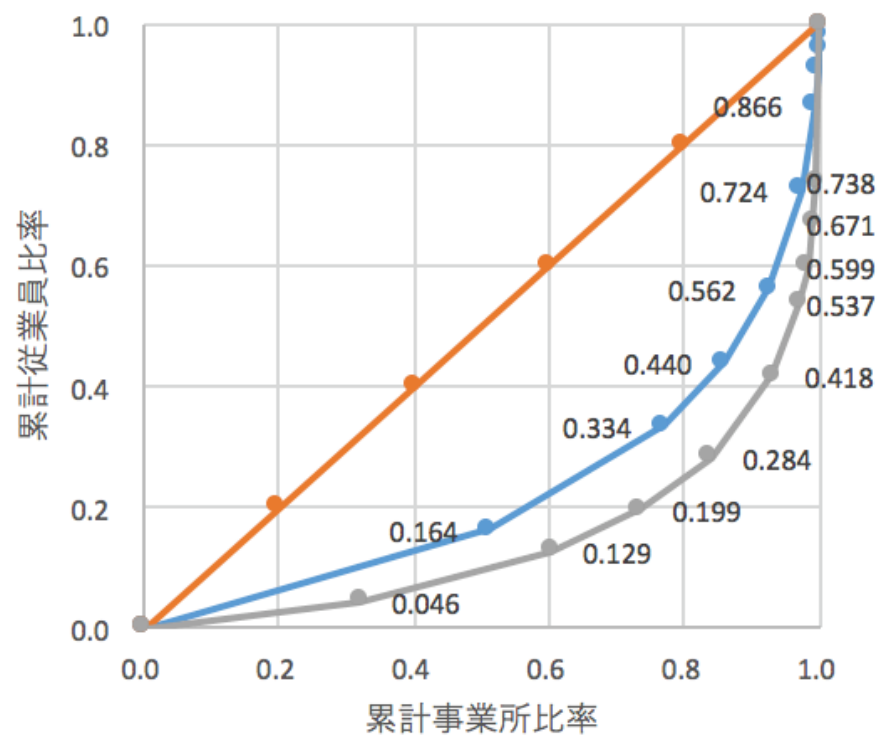


Figure 5.3: image of histogram

$$\begin{aligned} n \quad \{X_i\} &= \{X_1, X_2, \cdots, X_n\} & c & \quad \{X_i + c\} \\ \sum_{i=1}^n (X_i + c) &= (X_1 + c) + (X_2 + c) + \cdots + (X_n + c) \\ &= (X_1 + X_2 + \cdots + X_n) + \underbrace{(c + c + \cdots + c)}_{n \ c} \\ &= \sum_{i=1}^n X_i + nc \end{aligned} \tag{5.1}$$

$$\begin{aligned} n \quad \{X_i\} &= \{X_1, X_2, \cdots, X_n\} & c & \quad \{cX_i\} \\ \sum_{i=1}^n cX_i &= cX_1 + cX_2 + \cdots + cX_n \\ &= c(X_1 + X_2 + \cdots + X_n) \\ &= c \sum_{i=1}^n X_i \end{aligned} \tag{5.2}$$

(5.1) (5.2)

$$\begin{aligned} n \quad \{X_i\} & \quad a \quad b \quad \{aX_i + b\} \\ \sum_{i=1}^n (aX_i + b) &= (aX_1 + b) + (aX_2 + b) + \cdots + (aX_n + b) \\ &= \underbrace{(aX_1 + aX_2 + \cdots + aX_n)}_{a(X_1 + X_2 + \cdots + X_n)} + \underbrace{(b + b + \cdots + b)}_{n \ b} \\ &= a \sum_{i=1}^n X_i + nb \end{aligned} \tag{5.3}$$

(Gini\_Quintile2021.tex)

1.

I	II	III	IV	V
<hr/>				
I	$Q_1$	0.2	$y_1$	
II	$Q_2$	0.4	$y_2$	
III	$Q_3$	0.6	$y_3$	
IV	$Q_4$	0.8	$y_4$	
V	$Q_5$	1.0	$y_5$	

3.  $Q_i$   $i$   $y_i$   $i$

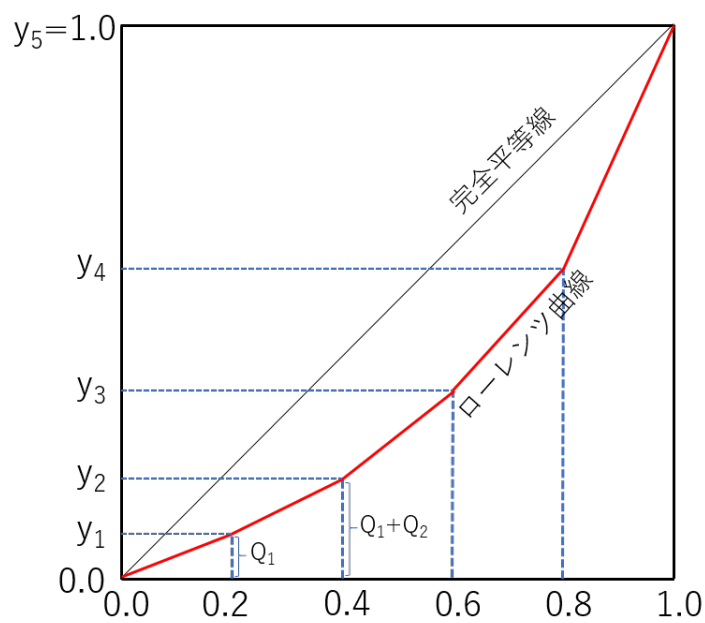


Figure 5.4: image of histogram

•

$$\begin{aligned}
 \text{I} &= \times \div 2 \\
 &= y_1 \times 0.2 \times \frac{1}{2} = 0.1 \times y_1
 \end{aligned}$$

$$\text{II} = (y_1 + y_2) \times \div 2 = (y_1 + y_2) \times 0.2 \times \frac{1}{2} = 0.1 \times (y_1 + y_2)$$

$$\text{III} = (y_2 + y_3) \times 0.2 \times \frac{1}{2} = 0.1 \times (y_2 + y_3)$$

$$\text{IV} = (y_3 + y_4) \times 0.2 \times \frac{1}{2} = 0.1 \times (y_3 + y_4)$$

$$\text{V} = (y_4 + y_5) \times 0.2 \times \frac{1}{2} = 0.1 \times (y_4 + 1)$$

$$\bullet \quad (B)$$

$$\begin{aligned} B &= 0.1 \times y_1 + 0.1 \times (y_1 + y_2) + 0.1 \times (y_2 + y_3) + 0.1 \times (y_3 + y_4) + 0.1 \times (y_4 + 1) \\ &= 0.1 \times \{y_1 + (y_1 + y_2) + (y_2 + y_3) + (y_3 + y_4) + (y_4 + 1)\} \\ &= 0.1 \times (2y_1 + 2y_2 + 2y_3 + 2y_4 + 1) \end{aligned}$$

$$\bullet \quad \frac{1}{2} \quad \quad \quad 2$$

$$\begin{aligned} \text{Gini} &= \underbrace{2 \times 0.5}_{A/2} - \underbrace{2 \times 0.1 \times (2y_1 + 2y_2 + 2y_3 + 2y_4 + 1)}_{B/2} \\ &= 1 - (0.4y_1 + 0.4y_2 + 0.4y_3 + 0.4y_4 + 0.2) \\ &= 0.8 - 0.4 \times (y_1 + y_2 + y_3 + y_4) \end{aligned} \tag{5.4}$$

$$\bullet \quad y \quad Q$$

$$\begin{aligned} y_1 &= Q_1 \\ y_2 &= Q_1 + Q_2 \\ y_3 &= Q_1 + Q_2 + Q_3 \\ y_4 &= Q_1 + Q_2 + Q_3 + Q_4 \end{aligned}$$

$$y_1 + y_2 + y_3 + y_4 = 4Q_1 + 3Q_2 + 2Q_3 + Q_4 \tag{5.5}$$

$$\bullet \quad (5.4) \quad (5.5)$$

$$\text{Gini} = 0.8 - 0.4 \times (4Q_1 + 3Q_2 + 2Q_3 + Q_4) \tag{5.6}$$

$$1966 \quad (5.6)$$

$$\begin{aligned} \text{Gini} &= 0.8 - 0.4 \times (4Q_1 + 3Q_2 + 2Q_3 + Q_4) \\ &= 0.8 - 0.4 \times (4 \times 0.056 + 3 \times 0.124 + 2 \times 0.177 + 0.238) \\ &= 0.8 - 0.4 \times (0.224 + 0.372 + 0.354 + 0.238) \\ &= 0.8 - 0.4 \times 1.188 = 0.8 - 0.4752 = 0.3248 \end{aligned}$$

Barro, R.J. (1999), Inequality, Growth and Investment, NBER Working Paper 7038.



$$\{X_i - \bar{X}\}$$

$n$

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$$

$$c = -\bar{X} \quad (5.1) \quad \{X_i - \bar{X}\}$$

$$\begin{aligned} \sum_{i=1}^n (X_i - \bar{X}) &= (X_1 - \bar{X}) + (X_2 - \bar{X}) + \cdots + (X_n - \bar{X}) \\ &= \underbrace{(X_1 + X_2 + \cdots + X_n)}_{\sum_{i=1}^n X_i} + \underbrace{\{(-\bar{X}) + (-\bar{X}) + \cdots + (-\bar{X})\}}_{n - \bar{X}} \end{aligned}$$

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i \quad \sum_{i=1}^n X_i = n\bar{X}$$

$$\begin{aligned} \sum_{i=1}^n (X_i - \bar{X}) &= \underbrace{(X_1 + X_2 + \cdots + X_n)}_{\sum_{i=1}^n X_i} + \underbrace{\{(-\bar{X}) + (-\bar{X}) + \cdots + (-\bar{X})\}}_{n - \bar{X}} \\ &= \sum_{i=1}^n X_i - n\bar{X} \\ &= 0 \end{aligned}$$



# Chapter 6

## 6.1

$$\begin{array}{ccccccccc} 1 & & 5 & & 100 & 300 & 600 & 900 & 1200 & & 5 \\ | & 1 & | & 2 & | & 3 & | & 4 & | & 5 & | \\ | & x_1 & | & x_2 & | & x_3 & | & x_4 & | & x_5 & | \\ | - | - | - | - | - | & ( \quad ) & | & 100 & | & 300 & | & 600 & | & 900 & | & 1200 & | \end{array}$$

$$= \frac{100 + 300 + 600 + 900 + 1200}{5} = 620( \quad )$$

$$\bullet \quad n \qquad x_1, x_2, \ldots, x_n$$

$$\bar{x} = \frac{x_1 + x_2 + \cdots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\bullet \qquad x \qquad \qquad \qquad ( \quad 1 \qquad \qquad x_1 \qquad \qquad )$$

$$\bar{x} = \frac{x_1 + x_2 + x_3 + x_4 + x_5}{5} = \frac{1}{5} \sum_{i=1}^5 x_i$$

1.
  - (a)
  - (b)

- (c)
- (d)
- (e) (=“ ”)

- 2.
  - (a) ( )
  - (b)

3.

- 
- 
- 

2                      10      10      30

24 12 80 16 28 16 32 16 52 24 ( )

\* 30

## 6.2

- median

- 

- 1.  $n$        $(n+1)/2$
- 2.  $n$        $n/2$      $n/2+1$

- 

- 1.
- 2.

1.

- Outlier

- 

- 

2.

- 

- 

3                      4      (A,B,C,D)

A: 3,4,5,6,7      B: 1,3,5,7,9  
C: 0,4,5,6,10    D: 0,1,5,9,10

$$\%(\bar{x}_A, \bar{x}_B, \bar{x}_C, \bar{x}_D) \quad \%(Me_A, Me_B, Me_C, Me_D)$$

4

•  
•

**6.3**

mode

1.

• Outlier  
•

2.

•  
•

5

•  
•

**6.4**

(2016) [ 3 ] ( )



# Chapter 7

1  
2 (X Y) 2 100  
• X A B 1m  
• Y C D 5mm

2  
X ( A B) 1000m Y ( C D) 1m  
2  
X ( A B) 1000m Y ( C D) 1m

• 1000m 1m 1m 5mm

$$\begin{aligned}
X &= \frac{1}{1000} = 0.001 \\
Y &= \frac{5}{1000} = 0.005
\end{aligned}$$

(coefficient of variation)

$$(CV) = \frac{sd(x)}{\bar{x}} = \frac{x}{x}$$

0 0

3

$$\frac{1991-1}{1996-1} = \frac{1990}{1995} = \frac{199}{199.5} \approx 99.75\%$$

•

•

$$6 \sim (1.5)$$

7

$$8.1 \sim (1.5)$$

9

•

$$\bar{x} = \frac{1}{6}(3+2+6+1+5+7) = \frac{24}{6} = 4$$

•

$$\begin{aligned} \text{MAD} &= \frac{1}{6}(|3-4| + |2-4| + |6-4| + |1-4| + |5-4| + |7-4|) \\ &= \frac{1}{6}(1+2+2+3+1+3) = \frac{12}{6} = 2 \end{aligned}$$

10

$$1. \quad (1.5)^2 = 2.25$$

$$\begin{aligned} &= \frac{1}{6}\{(3-4)^2 + (2-4)^2 + (6-4)^2 + (1-4)^2 \\ &\quad + (5-4)^2 + (7-4)^2\} \\ &= \frac{28}{6} = \frac{14}{3} = 4.66 \end{aligned}$$

2.

$$= \sqrt{4.66} = \sqrt{\frac{14}{3}} = 2.16$$



11

$$1. \quad \frac{55}{10} = \frac{11}{2}$$

2.

$$= 2 - 2$$

$$= \frac{77}{2} - \left(\frac{11}{2}\right)^2 = \frac{33}{4} = 8.25$$

3.

$$= \sqrt{\phantom{x}} = \sqrt{\frac{33}{4}} = \sqrt{8.25} = 2.872$$

12

$$4 \quad ( \quad ) \quad ( \quad )$$

1.

2.

3.

$$4 \quad \}$$

$$32 \quad 8 \quad 3$$

$$\text{A: } 56, \quad \text{B: } 28, \quad \text{C: } 32$$

$$\bar{x} \quad \text{sd}(x) \quad \text{“ ”}$$

$$= \frac{-}{\text{sd}(x)} = \frac{-\bar{x}}{\text{sd}(x)}$$

1. 3

$$z_A = \frac{56-32}{8} = 3, \quad z_A = \frac{28-32}{8} = -0.5 \quad z_A = \frac{32-32}{8} = 0$$

5

3

}

$$= 50 + 10 \times$$

$$\bullet \quad 3$$

$$50 + 10 \times 3 = 80, \quad 50 + 10 \times (-0.5) = 45, \quad 50 + 10 \times 0 = 50$$

6

80

50

1.

2. 80

16 ( )}

3

$$1 \quad 2 \quad 3 ( )$$

$$( ) : \text{sd}(x) = \sqrt{\text{Var}(x)} = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

1. 2( )

$$\text{Var}(x) = \frac{1}{3} \{(1-2)^2 + (2-2)^2 + (3-2)^2\} = \frac{2}{3}$$

2. 1

$$\text{sd}(x) = \sqrt{\frac{2}{3}} = 0.816( )$$

16 ( ( ) ) }

1

$$10,000 \quad 20,000 \quad 30,000 ( )$$

1.  $y = 10000 \times x$ 

2. 20000( )

$$\begin{aligned} \text{Var}(y) &= \frac{1}{3} \{(10000 - 20000)^2 + (20000 - 20000)^2 \\ &\quad + (30000 - 20000)^2\} = \frac{200000000}{3} \end{aligned}$$

3. 1

$$\begin{aligned} \text{sd}(y) &= \sqrt{\frac{200000000}{3}} = 8165( ) \\ &= 10000 \times \text{sd}(x) \end{aligned}$$

$$x_i \ a \ b \ y_i$$

$$s_y = |a|s_x\text{sd}(y) = |a| \times \text{sd}(x)$$

• 1 1



# Chapter 8

- $n \quad x_1, x_2, \dots, x_n$

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

- 
- 
- 
- 
- 
- (=“ ’ ’)
- 
- 
- 
- 
- $x \quad ( \quad 1 \quad x_1 \quad )$

$$\bar{x} = \frac{x_1 + x_2 + x_3 + x_4 + x_5}{5} = \frac{1}{5} \sum_{i=1}^5 x_i$$

}

-

●

•

•

•

- (=“ ”)

•

•

•

•

•

•

•

$$\}$$

•

median

•

- $n \quad (n+1)/2$

- $n \quad n/2 \quad n/2 + 1$

•

•

•

}

•

- Outlier

•

•

•

●

•

}

•

mode

$$\}$$

8.1.     }

- 
- Outlier
- 
- 
- 
- 
- }

8.1       }

- 
- 
- 
- 

8.2

(“     ”    ) }

- (range)

$$= x_{\max} - x_{\min}$$

  }   X   Y

“    ”    }       (   )       ”    (   )

%%%%%%%%%

(“     ”    ) }

- (interquartile range)

$$\text{IQR} = Q_3 - Q_1$$

- 
- $Q_1, Q_2, Q_3$    1   2   3       3
- }
- (range)           (outlier)

- 25% 50% (outlier) “ (range)”

$$1 \sim ( ) \} 15 \ 1$$

$$\begin{array}{ccccccccc} 24 & 12 & 14 & 24 & 11 & 18 & 19 & 14 & 18 & 32 \\ 24 & 22 & 24 & 18 & 36 & 18 & 12 & 24 & 20 & 34 \end{array}$$

•

- 25( ) (= 36 − 11)

- $Q_1 = \frac{1}{2}(14 + 18) = 16$   $Q_3 = \frac{1}{2}(24 + 24) = 24$

$$= 24 - 16 = 8( )$$

}

•

- $\Rightarrow$  “ ”,  $Q_2$

- 2  $\Rightarrow Q_1$

- 2  $\Rightarrow Q_3$

$$\} \ 7 \ 7 \quad Q_2$$

$$1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7( )$$

$$\} \ 10 \ 10 \quad Q_1, Q_2, Q_3$$

$$1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8 \ 9 \ 10( )$$

- $Q_2 \ 2$

- $Q_1 \ 2$

}

- $n$

$$x_{(1)} \leq x_{(2)} \leq \cdots x_{(n)}$$

•

- 25% 50% 75%

- $100\alpha\% \quad n\alpha \quad j \quad g$



$$\begin{cases} \frac{x_{(j)}+x_{(j+1)}}{2} & g=0 \\ x_{(j+1)} & g>0 \end{cases}$$

•

$n=7$

25%

$j=1$

2

50%

4

75%

6

}

7

7

2

$(Q_1)$

1

2

3

4

$\uparrow$

$Q_2$

5

6

7

$(\quad)$

}

5

42

•

•

ISIZE 2011/5/4

}

•

$n$

$$x_{(1)}\leq x_{(2)}\leq \cdots x_{(n)}$$

•

•

25%

50%

75%

•

100α%

$n\alpha$

$j$

$g$

$$\begin{cases} \frac{x_{(j)}+x_{(j+1)}}{2} & g=0 \\ x_{(j+1)} & g>0 \end{cases}$$

•

$n=42$

25%

$j=10$

11

50%

21

22

75%

32

}

%

42

$(\quad)$

$=11.4-4.9=6.5$

$\uparrow$

$\uparrow$

$(\quad)$

$=7.5-6.2=1.3$

$\uparrow$

$\uparrow$

$(\quad)$

$Q_3$

$Q_1$

(“ ’ ’ ” )}

- (mean absolute deviation)

$$\begin{aligned} \text{MAD} &= \frac{1}{n}(|\underbrace{x_1 - \bar{x}}_1| + |x_2 - \bar{x}| + \cdots + |x_n - \bar{x}|) \\ &= \frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}| = \end{aligned}$$

- 
- (= )

}

$$\begin{aligned} X &= 10 \quad ( ) \\ &= 0.8( ) \end{aligned}$$

( )

- 

### 8.2.1

- 
- 
- 
- 
- 
- 

$$K \quad \} \quad K \quad 5 \quad 42$$

$$= \underset{\uparrow}{11.4} - \underset{\uparrow}{4.9} = 6.5( )$$

$$= \underset{\uparrow}{7.5} - \underset{\uparrow}{6.2} = 1.3( )$$

$Q_3 \quad Q_1$

}

}

8.3.        }

51

- (    )
- (Box-whisker plot)
- $Q_1$      $Q_3$      $Q_2$      $\diamond$
- (1)        1.5        (2)
- 

8.3        }

(weighted arithmetic mean)}

$$\begin{aligned} x_w &= \frac{w_1x_1 + w_2x_2 + \cdots + w_nx_n}{\sum_{i=1}^n w_i} \\ &= \underbrace{\left(\frac{w_1}{\sum_{i=1}^n w_i}\right)}_1 x_1 + \cdots + \left(\frac{w_n}{\sum_{i=1}^n w_i}\right) x_n \end{aligned}$$

1        } C-3        }        2006 3

2

•

(    ) =  $\frac{47.1}{100} \times 145 + \frac{62.1}{100} \times 519 =$

•

$$= \frac{68.295 + 322.299}{145 + 519} = \frac{390.594}{664} = 0.588 = 58.8\%$$

$$\begin{aligned} &= \underbrace{\hspace{1cm}} \times \hspace{1cm} + \underbrace{\hspace{1cm}} \times \hspace{1cm} \\ &= \frac{\boxed{\hspace{1cm}}}{664} \times 47.1 + \frac{\boxed{\hspace{1cm}}}{664} \times 62.1 \\ &= 0.2183 \times 47.1 + 0.7816 \times 62.1 \\ &= 10.28 + 48.54 \\ &= 58.82\% \end{aligned}$$

$$\begin{aligned} & 2.1 \quad \} \\ & \quad , \quad 4.1 \quad 1.8 \\ & 8.1 \quad \quad \% \quad . \end{aligned}$$

$$\begin{aligned} G &= \sqrt[8]{1.07 \times 1.28 \times 1.32 \times 1.21 \times 1.11 \times 1.09 \times 1.05 \times 1.01} \\ &= \sqrt[8]{2.8068} \quad \leftarrow \\ &= 1.137 \quad \leftarrow \end{aligned}$$

$$\begin{aligned} & 1.14 \quad 14\% \setminus ( : \sim ) \\ & \text{(geometric mean)} \} \end{aligned}$$

$$\begin{aligned} & \bullet \quad n \quad ( \quad 5\% \quad 1.05 ) \\ & \bullet \end{aligned}$$

$$X_1 \times X_2 \times \cdots \times X_n$$

$$\bullet \quad n$$

$$G = \sqrt[n]{X_1 \times X_2 \times \cdots X_n}$$

$$\begin{aligned} & 2.1 \quad \} \text{ C-4 } 1 \quad \} \quad , \quad 4.1 \quad 1 \quad 2 \\ & 2.1 \quad \quad \% \quad . \end{aligned}$$

$$\begin{aligned} & (1) 1.0\% \sim (2) 5.9\% \sim (3) 6.0\% \sim (4) 11.0\% \sim \\ & (1) \end{aligned}$$

$$\begin{aligned} G &= \sqrt{1.01} \times 1.11 \\ &= \sqrt{1.1211} \\ &= 1.0588 ( \quad 5 \quad ) \end{aligned}$$

$$1.059 \quad 5.9\%$$

$$( \quad ) \quad g(\%) \quad 2$$

$$\begin{aligned} \left(1 + \frac{g}{100}\right)^2 &= \frac{1.1211}{1.01 \times 1.11} \\ \left(1 + \frac{g}{100}\right) &= \sqrt{1.1211} = 1.0588. \\ \frac{g}{100} &= 0.0588 \end{aligned}$$

3 } C-5 } 1 (%)

•

(1)  $\frac{1}{5}(4.2 + 12.5 + 6.3 + 7.3 + 13.4)$   
(2)  $\sqrt[5]{1.042 \times 1.125 \times 1.063 \times 1.073 \times 1.134}$   
(3)  $\sqrt[5]{0.042 \times 0.125 \times 0.063 \times 0.073 \times 0.134}$

•  $\sqrt[5]{1.042 \times 1.125 \times 1.063 \times 1.073 \times 1.134}$   
•  $\sqrt[5]{0.042 \times 0.125 \times 0.063 \times 0.073 \times 0.134}$   
•  $\sqrt[5]{4.2 \times 12.5 \times 6.3 \times 7.3 \times 13.4}$

(2)

( 3 ) } C-6 }

•

• ( )

(1) ~ (2) ~ (3)

•  $G = \sqrt[5]{1.5162} = 1.087 \quad 8.7\%$   
•  $G = \sqrt[5]{\boxed{\phantom{000}}} = \boxed{\phantom{000}} \quad 7.7\%$   
•  $G = \sqrt[5]{\boxed{\phantom{000}}} = \boxed{\phantom{000}} \quad 9.7\%$

4 } C-7 } 2 (X Y) 2 100

• X A B 1m  
• Y C D 5mm

(1)X ~ (2)Y ~

( 4 ) } C-8 } X ( A B) 1000m Y ( C D) 1m

(1)X  $\sim$  (2)Y  $\sim$

- 1000m 1m 1m 5mm

$$X = \frac{1}{1000} = 0.001$$

$$Y = \frac{5}{1000} = 0.005$$

(coefficient of variation)}

$$(\text{CV}) = \frac{\text{sd}(x)}{\bar{x}} = \frac{x}{x}$$

0 0

5 } C-9 } 1991 1 1996 1 ( ) ( )

%

(1)  $\sim$  (2)  $\sim$  (3)

- 
- 
- 

6  $\sim$ ( )} 15

- 

$$\bar{x} = \frac{870}{15} = 58( )$$

- 61( )

7 } 3 ( ) ( )



$$\bullet \quad \frac{55}{10} = \frac{11}{2}$$

•

$$= 2 - 2$$

$$= \frac{77}{2} - \left(\frac{11}{2}\right)^2 = \frac{33}{4} = 8.25$$

•

$$= \sqrt{\quad} = \sqrt{\frac{33}{4}} = \sqrt{8.25} = 2.872$$

$$12 \quad \} \quad 4 \quad ( \quad ) \quad ( \quad )$$

•

•

•

$$\begin{array}{l} 13 \quad \} \quad 32 \quad 8 \quad 3 \\ \quad \quad \quad \quad \bar{x} \quad \text{sd}(x) \quad \text{“ ”} \end{array}$$

$$= \frac{\quad}{\quad} = \frac{\quad - \bar{x}}{\text{sd}(x)}$$

$$\bullet \quad 3$$

$$z_A = \frac{56 - 32}{8} = 3, \quad z_A = \frac{28 - 32}{8} = -0.5 \quad z_A = \frac{32 - 32}{8} = 0$$

$$14 \quad \} \quad 3$$

}

$$= 50 + 10 \times$$

$$\bullet \quad 3$$

$$50 + 10 \times 3 = 80, \quad 50 + 10 \times (-0.5) = 45, \quad 50 + 10 \times 0 = 50$$

$$15 \quad \} \quad 80 \quad 50$$

•



- 80  
16      (      )}
- 3

1   2   3 (   )

(   )    :    $\text{sd}(x) = \sqrt{\text{Var}(x)} = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$

- 2(   )

$\text{Var}(x) = \frac{1}{3}\{(1 - 2)^2 + (2 - 2)^2 + (3 - 2)^2\} = \frac{2}{3}$

- 1

$\text{sd}(x) = \sqrt{\frac{2}{3}} = 0.816(   )$

16 (      (      ) )    }

10,000   20,000   30,000 (   )

- $y = 10000 \times x$
- 20000(   )

$\text{Var}(y) = \frac{1}{3}\{(10000 - 20000)^2 + (20000 - 20000)^2$   
 $+ (30000 - 20000)^2\} = \frac{200000000}{3}$

- 1

$\text{sd}(y) = \sqrt{\frac{200000000}{3}} = 8165(   )$   
 $= 10000 \times \text{sd}(x)$

    }    $x_i$     $a$     $b$        $y_i$

$\text{sd}(y) = |a| \times \text{sd}(x)$

- 1                      1



## Chapter 9

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 9.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.



# Chapter 10

$$\begin{array}{ccccccc} & & ( & ) & & & \\ \bullet & & Q_1 & & Q_3 & & Q_2 & & \diamond \\ \bullet & & (1) & & & & 1.5 & & (2) \\ \bullet & & & & & & & & \end{array}$$



# Chapter 11

## 11.1 2

K  
“ ”  $m^2$

## 11.2 2

(Scatter Plot)}

- $n$

$$\{(x_1, y_1), (x_2, y_2), \cdots, (x_n, y_n)\}$$

$(y) \ (x) \ \ xy$

- 2
- $x \text{ space}( ) \ y \text{ rent}( ) \ 42 \ 42$

## 11.3 2

(covariance)}

- $x \ y$

$$\text{Cov}(x, y) = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

•

- 1  $x$

$$\text{Var}(x) = s_x^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(x_i - \bar{x})$$

- 2  $x, y$        $x_i - \bar{x}$        $y_i - \bar{y}$   
 $\text{K} \quad \quad \quad \}$
- $y$      $x$       5.0203

$$\begin{aligned} \text{Cov}(x, y) \\ = s_{xy} &= \frac{1}{42} \sum_{i=1}^{42} (x_i - \bar{x})(y_i - \bar{y}) \\ &= 5.0203 \end{aligned}$$

•

(correlation coefficient)}

•

$$\begin{aligned} \text{Corr}(x, y) &= \frac{\text{Cov}(x, y)}{\text{sd}(x) \times \text{sd}(y)} \\ &= \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2}} \\ &= \frac{s_{xy}}{s_x s_y} \end{aligned}$$

•

1.  $-1 \leq \text{Corr}(x, y) \leq 1$
  2. 2
  - 3.
- }



Chapter 12

# (1)

12.1

$$\begin{matrix} \bullet \\ \bullet \end{matrix} \rightarrow$$

$x \quad y$   
(a)

$$y = \beta_0 + \beta_1x$$

(b)2

$$y = \beta_0 + \beta_1x + \beta_2x^2$$

(b)3

$$\begin{aligned} y &= \beta_0 + \beta_1x \\ &\quad + \beta_2x^2 + \beta_3x^3 \end{aligned}$$

## 12.2

( ,simple regression)

$$2 \quad x \quad y \quad 1$$

$$y_i = \beta_0 + \beta_1 x_i + u_i, \quad i = 1, 2, \dots, n$$

(= )

• ( )

•

## 12.3 2 ( )

2

- ( )  $\beta_0, \beta_1$  ( )
- 2 (Ordinary Least Square method: OLS)

$$\min_{\{\beta_0, \beta_1\}} S(\beta_0, \beta_1) = \sum_{i=1}^n \underbrace{\{ \overset{\uparrow}{y_i} - (\overset{\uparrow}{\beta_0} + \overset{\uparrow}{\beta_1} \overset{\uparrow}{x_i}) \}^2}_{\substack{y \\ x \\ i}}$$

- 2  $y_i$  2 ( 2 )

Excel

1. B C
2. C11 C12
3. D
4. E
5. F 2 F9

## 12.4 2 ( )

$$2 \quad \beta_0 \quad \beta_1$$

- 2

$$\min_{\{\beta_0, \beta_1\}} S(\beta_0, \beta_1) = \sum_{i=1}^n \underbrace{\{ \overset{\substack{\uparrow \\ S \\ \beta_0, \beta_1}}{y_i} - (\beta_0 + \overset{\substack{\uparrow \\ x}}{\beta_1 x_i}) \}}_i^2$$

$$\bullet \quad S(\beta_0, \beta_1) \quad \beta_0, \beta_1 \quad ( \quad 1 \quad ) \quad \Rightarrow \quad 2 \quad 2$$

$$\frac{\partial S(\beta_0, \beta_1)}{\partial \beta_0} = -2 \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i) = 0 \quad \Rightarrow \quad \sum_{i=1}^n u_i = 0$$

$$\frac{\partial S(\beta_0, \beta_1)}{\partial \beta_1} = -2 \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i) x_i = 0 \quad \Rightarrow \quad \sum_{i=1}^n u_i x_i = 0$$

$\beta_0, \beta_1$

OLS

$$1. \quad i \quad \{y_i - \beta_0 - \beta_1 x_i\}^2 \beta_0$$

$$2\{y_i - \beta_0 - \beta_1 x_i\} \times (-1)$$

$$2. \quad 1 \quad n \quad = 0$$

$$\frac{\partial S}{\partial \beta_0} = -2 \sum_{i=1}^n \underbrace{\{y_i - \beta_0 - \beta_1 x_i\}}_{u_i} = 0 \Rightarrow \sum_{i=1}^n u_i = 0$$

$$3. \quad i \quad \{y_i - \beta_0 - \beta_1 x_i\}^2 \beta_1$$

$$2\{y_i - \beta_0 - \beta_1 x_i\} \times (-x_i)$$

$$4. \quad 1 \quad n \quad = 0$$

$$\frac{\partial S}{\partial \beta_1} = -2 \sum_{i=1}^n x_i \underbrace{\{y_i - \beta_0 - \beta_1 x_i\}}_{u_i} = 0 \Rightarrow \sum_{i=1}^n x_i u_i = 0$$

$$5. \quad 1 \quad (\sum u_i = 0)$$

$$\begin{aligned} \sum (y_i - \beta_0 - \beta_1 x_i) &= 0 \\ \sum y_i - \sum \beta_0 - \sum \beta_1 x_i &= 0 \\ n\bar{y} - n\beta_0 - \beta_1 n\bar{x} &= 0 \\ \bar{y} - \beta_0 - \beta_1 \bar{x} &= 0 \end{aligned}$$

$$\beta_0 = \bar{y} - \beta_1 \bar{x}$$

$$6. \quad 2 \quad (\sum x_i u_i = 0)$$

$$\begin{aligned} \sum (x_i + \quad) u_i &= 0 \\ \sum (x_i - \bar{x}) u_i &= 0 \\ \sum (x_i - \bar{x}) \underbrace{(y_i - \beta_0 - \beta_1 x_i)}_{u_i} &= 0 \\ \sum (x_i - \bar{x}) \{y_i - (\bar{y} - \beta_1 \bar{x}) - \beta_1 x_i\} &= 0 \\ \sum (x_i - \bar{x}) \{(y_i - \bar{y}) - \beta_1 (x_i - \bar{x})\} &= 0 \end{aligned}$$

$$\beta_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}$$

## 12.5 2

2

$$2 \quad \beta_0, \beta_1 \quad (\text{2}, \text{OLS estimator})$$

$$\hat{\beta}_0 = \bar{y} - \beta_1 \bar{x} \quad \hat{\beta}_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{\text{Cov}(x, y)}{\text{Var}(x)}$$

- $\hat{\beta}_0, \hat{\beta}_1$  (= )  $\beta_0, \beta_1$  “ ”
- (OLS estimate)

Excel

- $= \bar{x}$
- $= \bar{y}$
- $= \sum_i^4 (x_i - \bar{x})(y_i - \bar{y})$
- $= \sum_i^4 (x_i - \bar{x})^2$

## 12.6

$$1. \quad (\hat{\beta}_0) \quad (\hat{\beta}_1)$$

$$\hat{\beta}_0 = 17.0 \quad \hat{\beta}_1 = 30.0$$

$$x_i \quad (\text{fitted value})'' \quad y \quad ''$$

$$\underset{y \uparrow}{\hat{y}_i} = \hat{\beta}_0 + \hat{\beta}_1 x_i$$

2.  $x_i$

$$\underset{\uparrow}{\hat{y}_i} = \hat{\beta}_0 + \hat{\beta}_1 x_i = 17.0 + 30.0 x_i$$

(12.1)

3. (12.1)      1.0(m)

$$17.0 + 30.0 \times 1.0 = 47.0(\text{kg})$$

4. (12.1)      1.1(m)

$$17.0 + 30.0 \times 1.1 = 50.0(\text{kg})$$

5.    0.1(m)          3.0(kg)

$$\frac{1.1(\text{m}) - 1.0(\text{m})}{1.1(\text{m}) - 1.0(\text{m})}$$
$$= \frac{50.0 - 47.0}{1.1 - 1.0}$$
$$= 30.0 \qquad \leftarrow \qquad (\hat{\beta}_1)$$

42    (m<sup>2</sup>)   ( )

$$\widehat{\text{rent}}_i = 3.172 + 0.209 \text{ area}_i, \qquad i = 1, \dots, 42$$

1.    20m<sup>2</sup>          XXX

2.    1m<sup>2</sup>          XXX

1994   2005    12          (income)          (cons)

$$\widehat{\text{cons}}_t = 13.44 + 0.5406 \text{ income}_t, \qquad t = 1994, \dots, 2005$$

1.          0.5406          “       ”

2.          1          XXX

(vegetable compound) 1907 1960 (54 ) 1000

$$\widehat{\text{sales}}_t = 488.8 + 1.434 \text{ advertisement}_t, \qquad t = 1907, \dots, 1960$$

Palda, Kristian S. (1964). *The Measurement of Cumulative Advertising Effects*. Englewood Cliffs, N.J.: Prentice-Hall.

- 1000 XXX XXX

12.7 ( 2 )

1.

$$\sum y_i = \sum \hat{y}_i$$

2. ( ) 0

$$\sum \hat{u}_i = \frac{1}{n} \sum \hat{u}_i = 0$$

3.  $x_i \hat{u}_i$

$$\sum x_i \hat{u}_i = 0$$

## Chapter 13

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 13.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a `{.unnumbered}` or the shorter `{-}` at the end of the heading, like in this section.





## Chapter 14

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 14.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.



## Chapter 15

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 15.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.



## Chapter 16

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 16.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.



## Chapter 17

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 17.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.





## Chapter 18

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 18.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a {.unnumbered} or the shorter {-} at the end of the heading, like in this section.



## Chapter 19

# Hello bookdown

All chapters start with a first-level heading followed by your chapter title, like the line above. There should be only one first-level heading (#) per .Rmd file.

### 19.1 A section

All chapter sections start with a second-level (##) or higher heading followed by your section title, like the sections above and below here. You can have as many as you want within a chapter.

#### An unnumbered section

Chapters and sections are numbered by default. To un-number a heading, add a `{.unnumbered}` or the shorter `{-}` at the end of the heading, like in this section.



# Chapter 20

## Cross-references

Cross-references make it easier for your readers to find and link to elements in your book.

### 20.1 Chapters and sub-chapters

There are two steps to cross-reference any heading:

1. Label the heading: `# Hello world {#nice-label}`.
  - Leave the label off if you like the automated heading generated based on your heading title: for example, `# Hello world = # Hello world {#hello-world}`.
  - To label an un-numbered heading, use: `# Hello world {-#nice-label}` or `{# Hello world .unnumbered}`.
2. Next, reference the labeled heading anywhere in the text using `\@ref(nice-label)`; for example, please see Chapter 20.
  - If you prefer text as the link instead of a numbered reference use: any text you want can go here.

### 20.2 Captioned figures and tables

Figures and tables *with captions* can also be cross-referenced from elsewhere in your book using `\@ref(fig:chunk-label)` and `\@ref(tab:chunk-label)`, respectively.

See Figure 20.1.

```
par(mar = c(4, 4, .1, .1))
plot(pressure, type = 'b', pch = 19)
```

Don't miss Table 20.1.

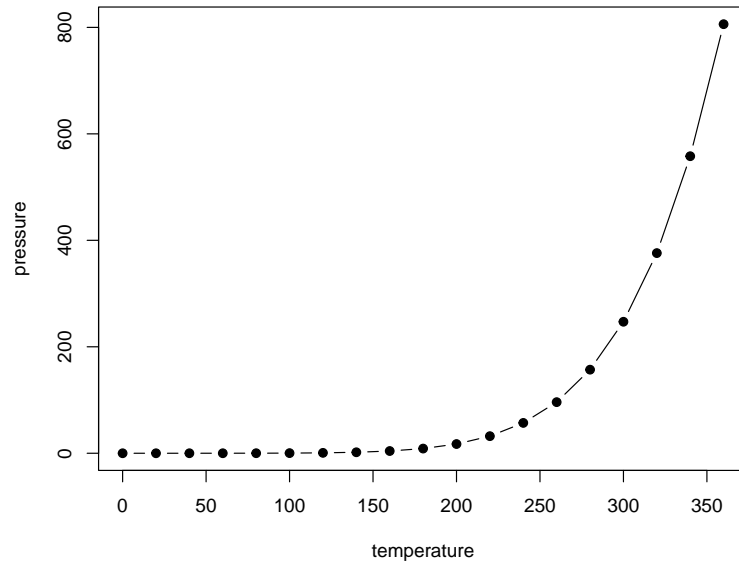


Figure 20.1: Here is a nice figure!

```
knitr::kable(  
  head(pressure, 10), caption = 'Here is a nice table!',  
  booktabs = TRUE  
)
```

Table 20.1: Here is a nice table!

temperature	pressure
0	0.0002
20	0.0012
40	0.0060
60	0.0300
80	0.0900
100	0.2700
120	0.7500
140	1.8500
160	4.2000
180	8.8000





# Chapter 21

## Parts

You can add parts to organize one or more book chapters together. Parts can be inserted at the top of an .Rmd file, before the first-level chapter heading in that same file.

Add a numbered part: `# (PART) Act one {-}` (followed by `# A chapter`)

Add an unnumbered part: `# (PART\*) Act one {-}` (followed by `# A chapter`)

Add an appendix as a special kind of un-numbered part: `# (APPENDIX) Other stuff {-}` (followed by `# A chapter`). Chapters in an appendix are prepended with letters instead of numbers.



## Chapter 22

# Footnotes and citations

### 22.1 Footnotes

Footnotes are put inside the square brackets after a caret `^[]`. Like this one <sup>1</sup>.

### 22.2 Citations

Reference items in your bibliography file(s) using `@key`.

For example, we are using the **bookdown** package (Xie, 2023) (check out the last code chunk in `index.Rmd` to see how this citation key was added) in this sample book, which was built on top of R Markdown and **knitr** (Xie, 2015) (this citation was added manually in an external file `book.bib`). Note that the `.bib` files need to be listed in the `index.Rmd` with the YAML `bibliography` key.

The `bs4_book` theme makes footnotes appear inline when you click on them. In this example book, we added `cs1: chicago-fullnote-bibliography.cs1` to the `index.Rmd` YAML, and include the `.cs1` file. To download a new style, we recommend: <https://www.zotero.org/styles/>

The RStudio Visual Markdown Editor can also make it easier to insert citations: <https://rstudio.github.io/visual-markdown-editing/#/citations>

---

<sup>1</sup>This is a footnote.



# Chapter 23

## Blocks

### 23.1 Equations

Here is an equation.

$$f(k) = \binom{n}{k} p^k (1-p)^{n-k} \quad (23.1)$$

You may refer to using `\@ref{eq:binom}`, like see Equation (23.1).

### 23.2 Theorems and proofs

Labeled theorems can be referenced in text using `\@ref{thm:tri}`, for example, check out this smart theorem 23.1.

**Theorem 23.1.** *For a right triangle, if  $c$  denotes the length of the hypotenuse and  $a$  and  $b$  denote the lengths of the **other** two sides, we have*

$$a^2 + b^2 = c^2$$

Read more here <https://bookdown.org/yihui/bookdown/markdown-extensions-by-bookdown.html>.

### 23.3 Callout blocks

The `bs4_book` theme also includes special callout blocks, like this `.rmdnote`.

You can use **markdown** inside a block.

```
head(beaver1, n = 5)
#>   day time  temp activ
#> 1 346  840 36.33     0
#> 2 346  850 36.34     0
#> 3 346  900 36.35     0
#> 4 346  910 36.42     0
#> 5 346  920 36.55     0
```

It is up to the user to define the appearance of these blocks for LaTeX output.

You may also use: `.rmdcaution`, `.rmdimportant`, `.rmdtip`, or `.rmdwarning` as the block name.

The R Markdown Cookbook provides more help on how to use custom blocks to design your own callouts: <https://bookdown.org/yihui/rmarkdown-cookbook/custom-blocks.html>

## Chapter 24

# Sharing your book

### 24.1 Publishing

HTML books can be published online, see: <https://bookdown.org/yihui/bookdown/publishing.html>

### 24.2 404 pages

By default, users will be directed to a 404 page if they try to access a webpage that cannot be found. If you'd like to customize your 404 page instead of using the default, you may add either a `_404.Rmd` or `_404.md` file to your project root and use code and/or Markdown syntax.

### 24.3 Metadata for sharing

Bookdown HTML books will provide HTML metadata for social sharing on platforms like Twitter, Facebook, and LinkedIn, using information you provide in the `index.Rmd` YAML. To setup, set the `url` for your book and the path to your `cover-image` file. Your book's `title` and `description` are also used.

This `bs4_book` provides enhanced metadata for social sharing, so that each chapter shared will have a unique description, auto-generated based on the content.

Specify your book's source repository on GitHub as the `repo` in the `_output.yml` file, which allows users to view each chapter's source file or suggest an edit. Read more about the features of this output format here:

[https://pkgs.rstudio.com/bookdown/reference/bs4\\_book.html](https://pkgs.rstudio.com/bookdown/reference/bs4_book.html)

Or use:

```
?bookdown::bs4_book
```



# Bibliography

Xie, Y. (2015). *Dynamic Documents with R and knitr*. Chapman and Hall/CRC, Boca Raton, Florida, 2nd edition. ISBN 978-1498716963.

Xie, Y. (2023). *bookdown: Authoring Books and Technical Documents with R Markdown*. R package version 0.32.