

1 Give Float (32-bit) rep of the following:  
Put final answers in hex form

a)  $14.125 = \underline{1110} . \underline{001}$  } Fixed point notation  
not floating point yet

INT:

14

$$14/2 = 7.0 \text{ r } 0$$

$$7/2 = 3.5 \text{ r } 1$$

$$3/2 = 1.5 \text{ r } 1$$

$$1/2 = 0.5 \text{ r } 1$$

DEC:

0.125

$$0.125 \times 2 = 0.25 \text{ w } 0$$

$$0.25 \times 2 = 0.5 \text{ w } 0$$

$$0.5 \times 2 = 1.0 \text{ w } 1$$

$$1.110.001$$

3

$$= 1.110001 \times 2^3$$

$$\text{Exp} = 127 + 3 = 130 = 10000010$$

$$\text{Man} = 110001$$

$$\text{Sign} = 0$$

(positive #)

Sign

Exp

23 bits



Man

$$14.125 = 01000001011000100000000000000000$$

4    1    6    2    0    0    0    0

$$= \boxed{0x41620000}$$

②  $-7.53125 = 111.10001_2$

INT: 7

$$7/2 = 3.5 \quad r1 \uparrow$$

$$3/2 = 1.5 \quad r1$$

$$1/2 = 0.5 \quad r1$$

DEC: 0.53125

$$0.53125 \times 2 = \underbrace{1.0625}_{\text{w1}}$$

$$0.0625 \times 2 = \underbrace{0.125}_{\text{w0}}$$

$$0.125 \times 2 = \underbrace{0.25}_{\text{w0}}$$

$$0.25 \times 2 = \underbrace{0.5}_{\text{w0}}$$

$$0.5 \times 2 = \underbrace{1.0}_{\text{w1}}$$

111, 10001

$$1.1110001 \times 10^2$$

$$\text{Exp} = 2 + 127 = 129 = 10000001$$

$$\text{Man} = 1110001$$

$$\text{Sign} = 1$$

Sign

1

Exp

10000001

Man

111000100000000000000000

$$-7.53125 = \underline{1100000011110001} \underline{0000000000000000}$$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 12 0 15 1 0 0 0 0  
 $\downarrow \quad \downarrow$   
 C F

$$= \boxed{0x\text{C0F10000}}$$

①

$$\underline{8675} . \underline{309} =$$

$$10000111100011.010011110001101$$

INT

8675



$$8675 / 2 = 4337.5 \quad r1$$

$$4337 / 2 = 2168.5 \quad r1$$

$$2168 / 2 = 1084.0 \quad r0$$

$$1084 / 2 = 542.0 \quad r0$$

$$542 / 2 = 271.0 \quad r0$$

$$271 / 2 = 135.5 \quad r1$$

$$135 / 2 = 67.5 \quad r1$$

$$67 / 2 = 33.5 \quad r1$$

$$33 / 2 = 16.5 \quad r1$$

$$16 / 2 = 8.0 \quad r0$$

$$8.0 / 2 = 4.0 \quad r0$$

$$4.0 / 2 = 2.0 \quad r0$$

$$2.0 / 2 = 1.0 \quad r0$$



1/2

0.5

r1

DEC

.309

.309 x 2

0.618

$\omega_0$

0.618 x 2

1.236

$\omega_1$

.236 x 2

0.472

$\omega_0$

.472 x 2

0.944

$\omega_0$

0.944 x 2

1.888

$\omega_1$

0.888 x 2

1.776

$\omega_1$

0.776 x 2

1.552

$\omega_1$

0.552 x 2

1.104

$\omega_1$

0.104 x 2

0.208

$\omega_0$

0.208 x 2

0.416

$\omega_0$

0.416 x 2	0.832	W0
0.832 x 2	1.664	W1
0.664 x 2	1.328	W1
0.328 x 2	0.656	W0
0.656 x 2	1.312	W1
0.312 x 2	0.624	W0

10000111100011.01001110001101

13

1.0000111100011010011110001101  $\times 10^{13}$

$$\text{Exp} = 127 + 13 = 140 = 10001100$$

$$\text{MAN} = 0000111100011010011100$$

$$\text{SIGN} = 0$$

Sign

exp

man

0

10001100

00001111000110100111100

01000110000001111000110100111100  
 ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
 4 6 0 7 8 13 3 12

= 0x46078D3C

2

Q 001111100000100000000000000000000000

Sign = 0

Exp = 0111110 = 126 - 127 = -1

Man = 00001

$$(-1)^0 \times (1.00001) \times 2^{-1}$$



$$= (-1)^0 \times (1.03125) \times 2^{-1}$$

$$= \boxed{0.515625}$$

② 01000010110111100000000000000000

$$\text{Sign} = 0$$

$$\text{Exp} = 10000101 - 127 = 133 - 127 = 6$$

$$\text{Man} = 101111$$

$$(1)^0 \times (1.101111) \times 2^{+6}$$

$$= (1)^0 \times (1.7343) \times 2^{+6}$$

$$= \boxed{110.99}$$

③ 110000101111010010000000000000

$$\text{Sign} = 1$$

$$\text{Exp} = 10000101 - 127 = 6$$

$$\text{Mn} = 111101001$$

$$= (-1)^1 \times (1.953125) \times 2^6$$

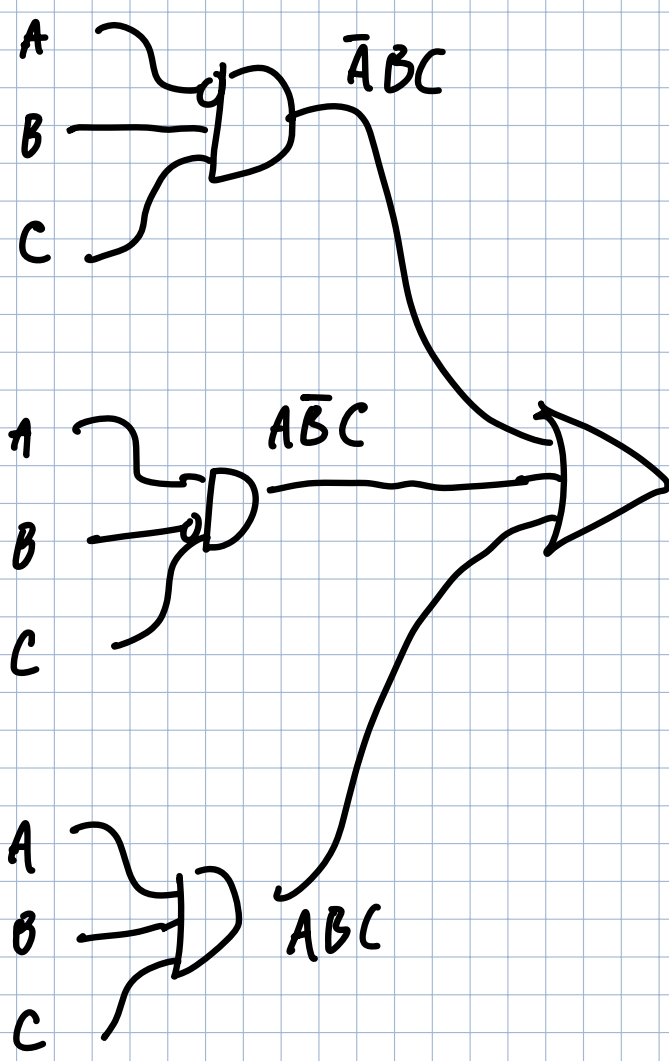
$$= -125$$

3

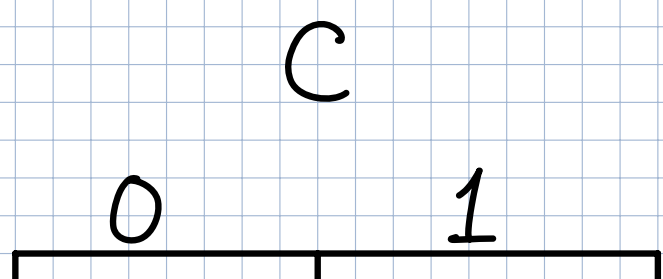
Ex: Sum of products Form

<u>input</u>			<u>output</u>
A	B	C	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1

0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1



$$f(A,B,C) = \bar{A}BC + \bar{A}\bar{B}C + ABC$$



AB	00	0	0
	01	0	1
	11	0	1
	10	0	1
		BC	
		AC	

$$f(A, B, C) = BC + AC$$

4

A	B	C	D	X	
0	0	0	0	0	
0	0	0	1	1	$\bar{A}\bar{B}\bar{C}D$

$$\begin{array}{cccc|c}
 0 & 0 & 1 & 0 & 0 \\
 0 & 0 & 1 & 1 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 + \\
 \bar{A}\bar{B}CD
 \end{array}$$

$$\begin{array}{cccc|c}
 0 & 1 & 0 & 0 & 0 \\
 0 & 1 & 0 & 1 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 + \\
 \bar{A}B\bar{C}D
 \end{array}$$

$$\begin{array}{cccc|c}
 0 & 1 & 1 & 0 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 + \\
 \bar{A}BC\bar{D}
 \end{array}$$

$$\begin{array}{cccc|c}
 0 & 1 & 1 & 1 & 0 \\
 \hline
 \end{array}
 \quad +$$

$$\begin{array}{cccc|c}
 1 & 0 & 0 & 0 & 0 \\
 \hline
 \end{array}$$

$$\begin{array}{cccc|c}
 1 & 0 & 0 & 1 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 A\bar{B}\bar{C}D \\
 +
 \end{array}$$

$$\begin{array}{cccc|c}
 1 & 0 & 1 & 0 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 A\bar{B}C\bar{D}
 \end{array}$$

$$\begin{array}{cccc|c}
 1 & 0 & 1 & 1 & 0 \\
 \hline
 \end{array}
 \quad +$$

$$\begin{array}{cccc|c}
 1 & 1 & 0 & 0 & 0 \\
 \hline
 \end{array}$$

$$\begin{array}{cccc|c}
 1 & 1 & 0 & 1 & 1 \\
 \hline
 \end{array}
 \quad \begin{array}{l}
 AB\bar{C}D \\
 +
 \end{array}$$

$$\begin{array}{cccc|c}
 1 & 1 & 1 & 0 & 1 \\
 \hline
 \end{array}
 \quad ABC\bar{D}$$

1 1 1 1 0

$$f(A, B, C, D) = \bar{A}\bar{B}\bar{C}D + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}BC\bar{D} + \\ A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + AB\bar{C}D + ABC\bar{D}$$

$\bar{C}D$        $CD$        $\bar{A}\bar{B}D$

00      01      11      10

AB	00	0	1	1	0
	01	0	1	0	1
	11	0	1	0	1
	10	0	1	0	1

$BC\bar{D}$

$AC\bar{D}$

The Karnaugh map shows the function f(A, B, C, D) with the following groupings and prime implicants:

- $\bar{C}D$ : A group of four cells (01, 11) in the first two rows.
- $\bar{A}\bar{B}D$ : A group of two cells (01, 11) in the first row.
- $BC\bar{D}$ : A group of two cells (01, 11) in the third row.
- $AC\bar{D}$ : A group of two cells (01, 11) in the fourth row.

$$\bar{C}D$$

$$f(A, B, C, D) = \bar{C}D + \bar{A}\bar{B}D + BC\bar{D} + AC\bar{D}$$