

# Homework Assignment 1

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1. Write R code to do the following:

- (a) Simulate a random number representing the number of shots that a basketball player makes in 10 tries, if the results of the shots are independent and she has a 40% chance of making each shot.

```
set.seed(23)
shots_made = rbinom(10, 1, 0.4)
sum(shots_made)

## [1] 6

# alternative
rbinom(n = 1, size = 10, prob = 0.4)

## [1] 6
```

- (b) Simulate a random number representing the number of shots that a basketball player makes in 10 tries, if the results of the shots are independent and her chance of making a shot is 10% for the first shot, 20% for the second shot, 30% for the third, etc.

```
set.seed(18)
tries = 10
shots_made = rep(NA, tries)
for (i in 1:tries) {
  shots_made[i] = rbinom(1, 1, 0.1*i)
}
sum(shots_made)

## [1] 6

# alternative
probs = seq(0.1, 1, by = 0.1)
shots_made_1 = rbinom(10, 1, probs)
sum(shots_made_1)

## [1] 5
```

2. (a) Write R code to simulate 100 data points from a linear model with intercept 1, slope 2, and residual standard deviation 3, where the predictors are sampled at random uniformly from the range (0,4). Fit a linear regression to these data using lm, print the fitted model using the display function from the arm package, and report whether the estimates of the intercept and slope fall within 1 standard error of the true parameter values.

```
#install.packages("arm")
library(arm)

## Loading required package: MASS
## Loading required package: Matrix
```

```

## Loading required package: lme4
##
## arm (Version 1.14-4, built: 2024-4-1)
## Working directory is /Users/tiow/Downloads/1 STAT5293G004 Gelman/STAT_5293/Homeworks
set.seed(21)
n = 100
beta_0 = 1 # true intercept
beta_1 = 2 # true slope

predictor = runif(n, 0, 4)
residuals = rnorm(n, 0, 3) #residual standard deviation 3
y = beta_0 + predictor * beta_1 + residuals

fitted_linear_model = lm(y ~ predictor)
display(fitted_linear_model)

```

```

## lm(formula = y ~ predictor)
##             coef.est  coef.se
## (Intercept) 0.74      0.62
## predictor   2.03      0.25
## ---
## n = 100, k = 2
## residual sd = 2.95, R-Squared = 0.41
if (abs(coef(fitted_linear_model)[1] - beta_0) <= se.coef(fitted_linear_model)[1]) {
  print("Intercept estimate falls within 1 standard error of the true intercept value.")
}

```

```

## [1] "Intercept estimate falls within 1 standard error of the true intercept value."
if (abs(coef(fitted_linear_model)[2] - beta_1) <= se.coef(fitted_linear_model)[2]) {
  print("Slope estimate falls within 1 standard error of the true slope value.")
}

```

```

## [1] "Slope estimate falls within 1 standard error of the true slope value."

```

(b) Fit the regression model using *stan\_glm* and print the results.

```
#install.packages("rstanarm")
library(rstanarm)
```

```

## Loading required package: Rcpp
## This is rstanarm version 2.32.1
## - See https://mc-stan.org/rstanarm/articles/priors for changes to default priors!
## - Default priors may change, so it's safest to specify priors, even if equivalent to the defaults.
## - For execution on a local, multicore CPU with excess RAM we recommend calling
##   options(mc.cores = parallel::detectCores())
##
## Attaching package: 'rstanarm'
## The following objects are masked from 'package:arm':
##   invlogit, logit

```

```
stan_linear_model = stan_glm(y ~ predictor, data = data.frame(y, predictor), refresh = 0) # add refresh
```

```
print(stan_linear_model)
```

```
## stan_glm
##   family:      gaussian [identity]
##   formula:     y ~ predictor
##   observations: 100
##   predictors:   2
##   -----
##           Median MAD_SD
## (Intercept) 0.7    0.6
## predictor   2.0    0.2
##
## Auxiliary parameter(s):
##           Median MAD_SD
## sigma 3.0    0.2
##
##   -----
## * For help interpreting the printed output see ?print.stanreg
## * For info on the priors used see ?prior_summary.stanreg
```

(c) Write a Stan program, fit the model using the *cmdstanr* package, and print the results.

```
#cmdstanr::install_cmdstan(cores = 4) #install the C++ toolchain and the CmdStan engine
```

```
#install.packages("cmdstanr", repos = c("https://mc-stan.org/r-packages/",getOption("repos")))
library(cmdstanr)
```

```
## This is cmdstanr version 0.8.0
```

```
## - CmdStanR documentation and vignettes: mc-stan.org/cmdstanr
```

```
## - CmdStan path: /Users/tiow/.cmdstan/cmdstan-2.38.0
```

```
## - CmdStan version: 2.38.0
```

```
#example(stan_model, package = "rstan", run.dontrun = TRUE)
```

```
stan_data = list(n = 100, x = predictor, y = y) #prepare the data
```

```
mod = cmdstan_model("linear_model.stan")          #compile the model
```

```
fit_cmdstan = mod$sample()                         #fit model using MCMC
```

```
  data = stan_data,
```

```
  seed = 21,
```

```
  chains = 4,
```

```
  parallel_chains = 4,
```

```
  refresh = 0
```

```
)
```

```
## Running MCMC with 4 parallel chains...
```

```
## Chain 4 Informational Message: The current Metropolis proposal is about to be rejected because of the
```

```
## Chain 4 Exception: normal_lpdf: Scale parameter is 0, but must be positive! (in '/var/folders/7h/m_g')
```

```
## Chain 4 If this warning occurs sporadically, such as for highly constrained variable types like covar
```

```
## Chain 4 but if this warning occurs often then your model may be either severely ill-conditioned or m
```

```
## Chain 4
```

```
## Chain 1 finished in 0.1 seconds.  
## Chain 2 finished in 0.0 seconds.  
## Chain 3 finished in 0.0 seconds.  
## Chain 4 finished in 0.1 seconds.  
##  
## All 4 chains finished successfully.  
## Mean chain execution time: 0.1 seconds.  
## Total execution time: 0.2 seconds.  
fit_cmdstan$print()  
  
##   variable     mean    median     sd     mad      q5      q95 rhat ess_bulk ess_tail  
##   lp__    -157.81 -157.48 1.25 1.06 -160.31 -156.42 1.00    1430    2411  
## intercept    0.74    0.74 0.65 0.64   -0.33    1.81 1.00    1730    1611  
## slope       2.03    2.03 0.26 0.25    1.60    2.46 1.00    1704    1616  
## sigma        3.00    2.99 0.22 0.21    2.65    3.39 1.00    1796    1804
```