## Algumas Séries de Maclaurin (Taylor).

**4.** 
$$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots + \frac{x^n}{n!} + \dots = \sum_{k=0}^{\infty} \frac{x^k}{k!}$$
, sendo  $x \in R$ 

**P.** 
$$\ln(1+x)=x-\frac{x^2}{2}+\frac{x^3}{3}-\frac{x^4}{4}+\dots+(-1)^n\frac{x^{n+1}}{n+1}+\dots=\sum_{k=0}^{\infty}(-1)^k\frac{x^{k+1}}{k+1}$$
, sendo  $x \in R$ 

$$\text{ arctan} = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots + \left(-1\right)^n \frac{x^{2n+1}}{2n+1} + \dots = \sum_{k=0}^{\infty} \left(-1\right)^k \frac{x^{2k+1}}{2k+1}, \text{ sendo } x \in \mathbb{R}$$

$$sinx = x - \frac{x^3}{3!} + \frac{x^5}{5!} + \dots + (-1)^{n+1} \frac{x^{2n+1}}{(2n+1)!} + \dots = \sum_{k=0}^{\infty} (-1)^{k+1} \frac{x^{2k+1}}{(2k+1)!}, \text{ sendo } x \in \mathbb{R}$$

$$\text{ $c$ osx} = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} \dots + \left(-1\right)^{n+1} \frac{x^{2n}}{(2n)!} + \dots = \sum_{k=0}^{\infty} \left(-1\right)^{k+1} \frac{x^{2k}}{(2k)!} \text{ , sendo } x \in \mathbb{R}$$

F. 
$$\sinh x = x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots + \frac{x^{2n+1}}{(2n+1)!} + \dots = \sum_{k=0}^{\infty} \frac{x^{2k+1}}{(2k+1)!}$$
, sendo  $x \in R$ 

**e** cos **k**=1+
$$\frac{x^2}{2!}$$
+ $\frac{x^4}{4!}$ + $\frac{x^6}{6!}$ ....+ $\frac{x^{2n}}{(2n)!}$ +....= $\sum_{k=0}^{\infty} \frac{x^{2k}}{(2k)!}$ , sendo  $x \in R$ 

$$I = \frac{1}{1-x} = 1 + x + x^2 + x^3 + x^4 + \dots + x^n + \dots = \sum_{k=0}^{\infty} x^k \text{, sendo } |x| < 1$$

$$1 - \frac{1}{1+x} = 1 - x + x^2 - x^3 + x^4 - \dots + (-1)^n x^n + \dots = \sum_{k=0}^{\infty} (-1)^k x^k, \text{ sendo } |x| < 1$$

$$1 \over (1+x)^2 = -1 + 2x - 3x^2 + 4x^3 - 5x^4 + \dots + (-1)^{n+1}(n+1)x^n + \dots = \sum_{k=0}^{\infty} (-1)^{k+1}(k+1)x^k \text{ , sendo } |x| < 1$$

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