


"Life is not a problem to be solved"

→ Skill Evaluation Contest

→ Mock interview

Q1) Given an integer array $arr[N]$, find the max subarray sum out of all subarrays.

eg:- $arr \rightarrow \{-2, \begin{matrix} 3 & 4 & -1 & 5 \\ 1 & 2 & 3 & 4 \end{matrix}, -10, 7\}$
 $\rightarrow \text{sum} = 11.$

$arr \rightarrow \{-3, \begin{matrix} 4 & 6 & 8 \end{matrix}, -10, 2, 7\}$
 $\rightarrow \text{sum} = 18$

$arr \rightarrow \{4, 5, 2, 1, 6\}$
 $\text{sum} = 18$

$arr \rightarrow \{-4, -3, -6, -9, -2\}$
 $\text{sum} = -2.$

Brute Force:-

\rightarrow Look at all subarrays $\rightarrow O(n^2)$
 \rightarrow Find sum of each $\rightarrow O(n)$ (independently)
 $\left. \begin{matrix} \rightarrow O(n^2) \\ \rightarrow O(n) \end{matrix} \right\} n^2 * n$
 \downarrow
 $O(n^3)$ T.C.

$(i, j) \rightarrow + arr[j+1]$
 $(i, j+1)$

```

fn maxSum ( ar [], n ) {
    max = -∞
    for ( i → 0 to n-1 ) {
        sum = 0
        for ( j → i to n-1 ) {
            sum += ar[j]
            if ( sum > max ) {
                max = sum
            }
        }
    }
    return max
}

```

$O(n^2)$ T.C.
 $O(1)$ S.C.

Cases :-

1) All Positive $\{3, 4, 7, 1, 2\}$

sum(arr)

2) All Negative $\{-3, -4, -7, -1, -2\}$

max(arr)

3) If +ve are placed in betw. $\{-----\textcircled{++++}-----\}$

take all +ves

4) $\{+++----\}$ or $\{-----+++++\}$

take all +ves

5) $\{\textcircled{++++}----\textcircled{++++}\}$

$\{4 \quad 5 \quad -3 \quad -9 \quad 1 \quad 1\}$

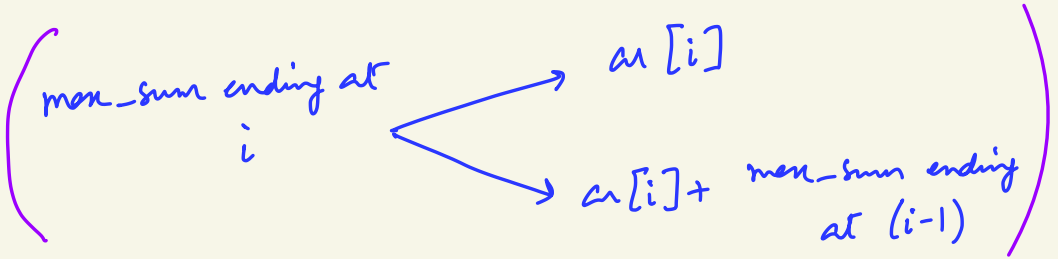
$\{4 \quad 5 \quad -9 \quad -80 \quad \underline{12} \quad 11\}$

$\{4 \quad 15 \quad -8 \quad -10 \quad 12 \quad 8\}$

$\{-2, 3, 4, -1, 5, -10, 7\}$

max
sum
ending
here

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $-2 \quad 3 \quad 7 \quad 6 \quad 11 \quad 1 \quad 8$



$\{-3, -4, 5, -1, 2, -4, 6, -1\}$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$
 $-3 \quad -4 \quad 5 \quad 4 \quad 6 \quad 2 \quad 8 \quad 7$
 $0 \quad 0$
 \downarrow
 $\underline{\underline{8.}}$

[Kadane's Algorithm]

$\text{max_sum}[i] = \text{max sum of subarray ending at } i$

$$= \max \left(\begin{array}{l} \text{ar}[i], \\ \text{ar}[i] + \text{ar}[i-1], \\ \text{ar}[i] + \text{ar}[i-1] + \text{ar}[i-2], \\ \vdots \\ \text{ar}[i] + \text{ar}[i-1] + \dots + \text{ar}[0] \end{array} \right)$$

$$= \text{ar}[i] + \max \left(\begin{array}{l} 0, \\ \text{ar}[i-1], \\ \text{ar}[i-1] + \text{ar}[i-2], \\ \vdots \\ \text{ar}[i-1] + \text{ar}[i-2] + \dots + \text{ar}[0] \end{array} \right)$$

$$\text{max_sum}[i] = \text{ar}[i] + \max(0, \text{max_sum}[i-1])$$

$$[\text{ans} = \max_i (\text{max_sum}[i])]$$


```

fn max_sum(arr[], n) {
    max = -10, curr = 0
    for (i → 0 to n-1) {
        curr += arr[i]
        if (curr > max)
            max = curr

        if (curr < 0)
            curr = 0
    }
    return max
}

```

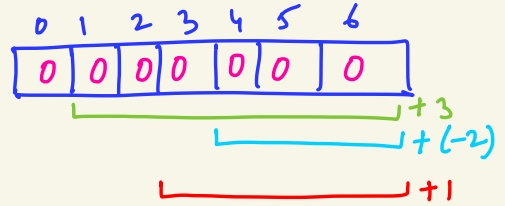
$O(n)$ T.C.
 $O(1)$ S.C.

Q2) Given $arr[n]$, where each element is 0, return final array after performing multiple queries.

query(i, x) \rightarrow Add x to all nos. from i to $n-1$.

eg:- $n=7$

queries:-
(1, 3)
(4, -2)
(3, 1)

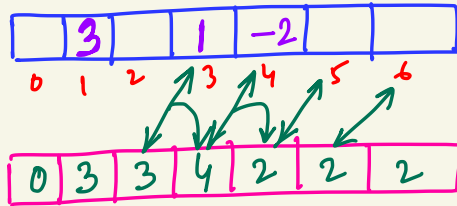


0 3 3 3 3 3 3

0 3 3 3 1 1 1

0 3 3 4 2 2 2

$O(n * q)$ T.C.
 $O(1)$ S.C



```

fn(i → 0 to q-1) {
    ar[Q[i][0]] += Q[i][1]
}

```

$\underbrace{\text{index}}$
 \underbrace{x}

$O(n+q)$ T.C.

```

fn(i → 1 to n-1) {
    ar[i] += ar[i-1]
}
return ar

```

$O(1)$ S.C

Q3) ar[n], queries

Query: $(i, j, x) \rightarrow$ Add x to all the elements from i to j .
 $i \leq j$.

$n=7$

$(1, 3, 2)$

$(2, 5, 3)$

$(5, 6, -1)$

0	1	2	3	4	5	6
0	0	0	0	0	0	0

2 2 2

5 5 3 3 2 -1

$n=7$

$(1, 3, 2) \rightarrow (1, 6, 2)$
 $(2, 5, 3) \rightarrow (4, 6, -2)$

$(2, 5, 3)$

$(5, 6, -1)$

0	2	5	5	3	2	-1
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0	1	2	3	4	5	6
0	0	0	0	0	0	0

+2

+2

+3

-2

-1

-3

0	2	5	5	3	2	-1
---	---	---	---	---	---	----

for combineQueries (arr[], Q[][[]], n, q) {

for (i → 0 to q-1) {

l = Q[i][0]

r = Q[i][1]

x = Q[i][2]

arr[l] += x

if (r < n-1) {

arr[r+1] -= x

}

}

for (i → 1 to n-1) {

arr[i] += arr[i-1]

}

return arr

}

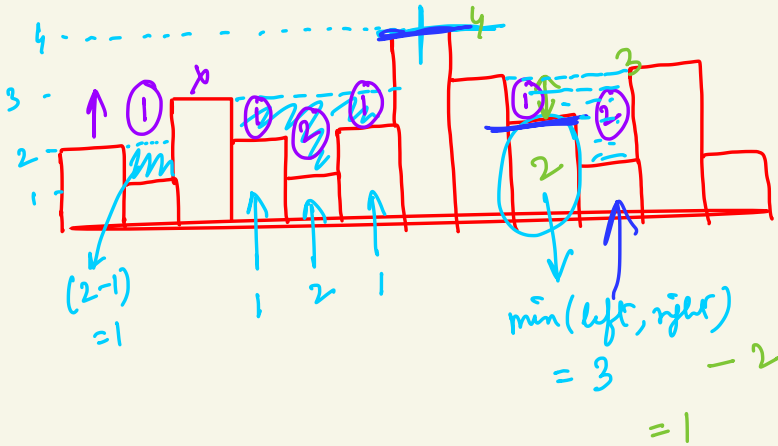
$O(n+q)$ T.C

$O(1)$ S.C.

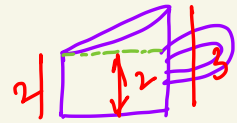
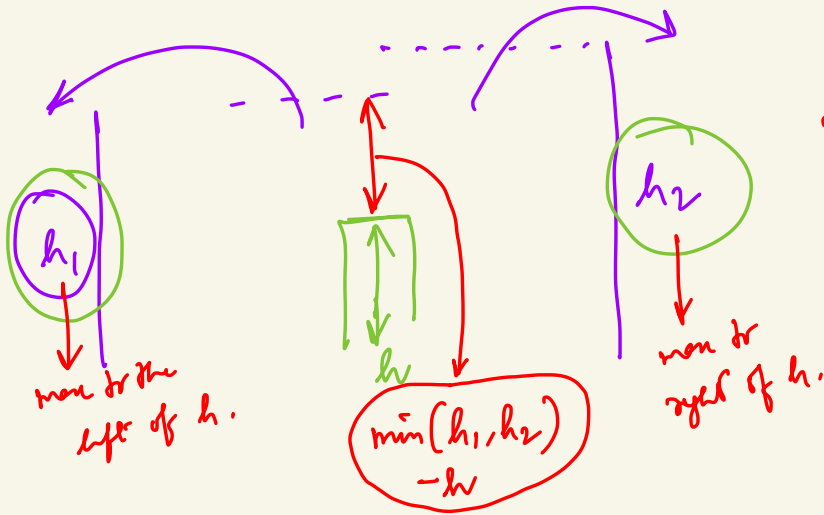
Q4) Trapping Rainwater Problem

Given n buildings with their heights, find the rainwater trapped between the buildings.

arr $\rightarrow \{ 2, 1, 3, 2, 1, 2, 4, 3, 2, 1, 3, 1 \}$



ans $\rightarrow 8$.



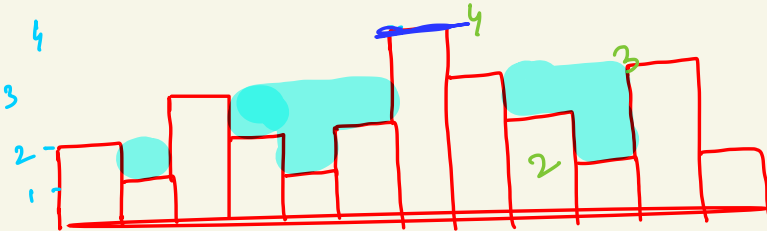
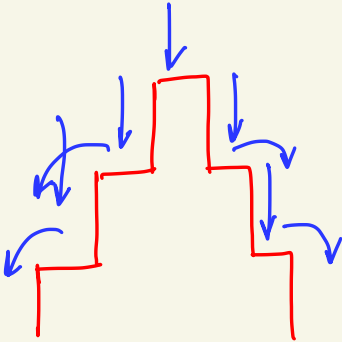
$$ans = \sum_i ans[i]$$

ht. of water above building i

$$= \sum \left[\min(\text{max-left}[i], \text{max-right}[i]) - ar[i] \right]$$

$\max(ar[j])$
 $j \in [0, i]$

$\max(ar[j])$
 $j \in [i, n-1]$



Brute force :-

for every i :-

calculate max-left, max-right

$$(\min(\text{max-left}, \text{max-right}) - \text{ar}[i])$$

$O(n^2)$ T.C.

$O(1)$ S.C.

Optimisation :-

precalculate all left-max and right-max

ans = 0

left-max = [0]*n

left-max[0] = ar[0]

for ($i \rightarrow 1$ to $n-1$) {

left-max[i] = max(ar[i], left-max[i-1])

}

right-max = [0]*n

right-max[n-1] = ar[n-1]

for ($i \rightarrow n-2$ to 0) {

right-max[i] = max(ar[i], right-max[i+1])

}

ans = 0

for ($i \rightarrow 0$ to $n-1$) {

ans += min(left-max[i], right-max[i]) - ar[i]

}

return ans

	4	2	5	7	4	2	3	6	8	2	3
lm →	4	4	5	7	7	7	7	7	8	8	8
rm →	8	8	8	8	8	8	8	8	8	3	3
ans →	0	2	0	0	3	5	4	1	0	1	0

↓
16.

$O(n)$ T.C.

$O(n)$ S.C.