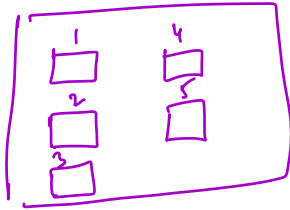


Hotel



Room nr. Occupied

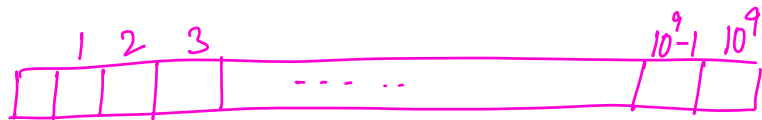
- 1 → ✓
- 2 → ✗
- 3 → ✗
- 4 → ✓
- 5 → ✓



covid → drop in business

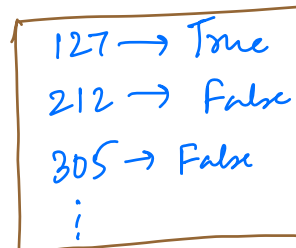
1000 room nr.

- 127
- 212
- 305
- ⋮
- 10321
- ⋮



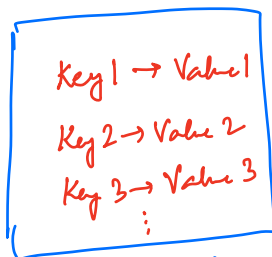
Problem → We're overflying space for  $10^9$  elements, while we're using only 1000 of them.

Solution → Hash Map.



< Integer, Boolean >  
< int, bool >

< key, value >



Hash Map

→ for one key, the HM stores only 1 value. (almost)

HashMap  $\rightarrow$  T.C. of search is  $O(1)$  on average, S.C. is  $O(n)$ .  
Key must be unique  
Value can be anything

1) Population of each country.

HashMap  $\langle$  String, Integer/Long  $\rangle$  pop. Country

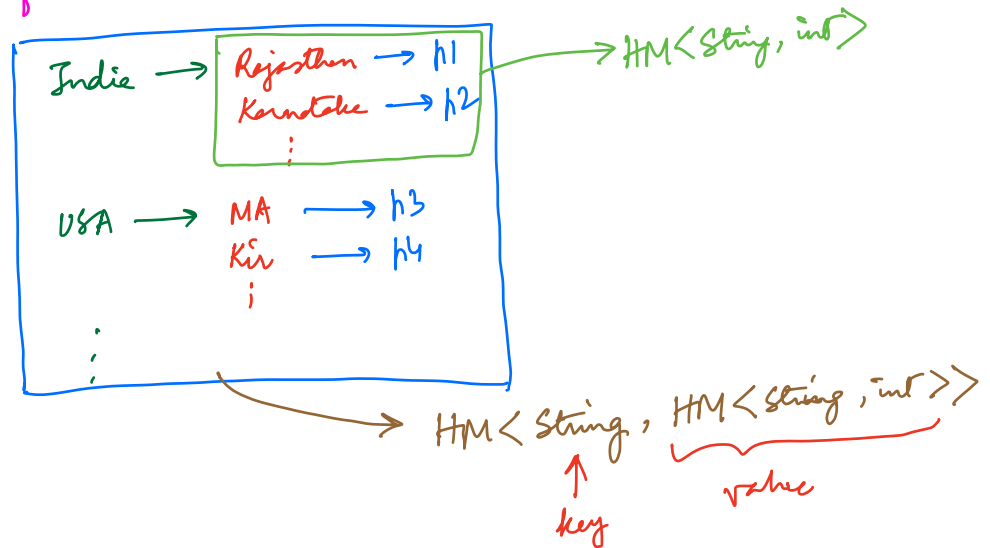
2) No. of states of every country

HashMap  $\langle$  String, Integer  $\rangle$  no. of States Per Country

3) Names of states of every country

HashMap  $\langle$  String, List  $\langle$  String  $\rangle$   $\rangle$  states Per Country

4) Population of each state in each country.

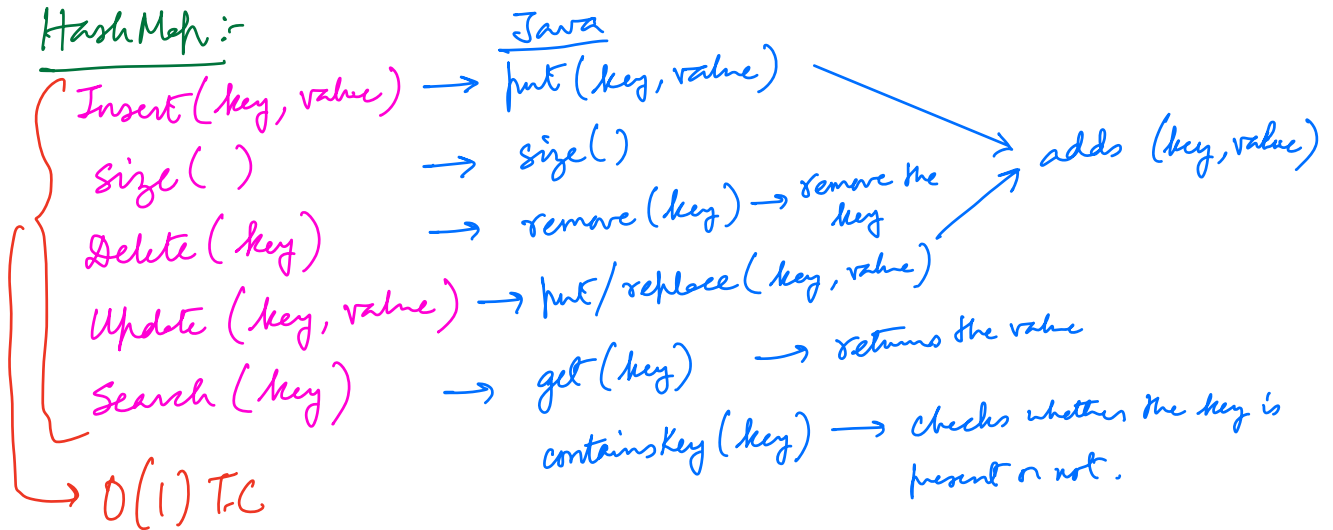


HashMap  $\langle$  String, HashMap  $\langle$  String, Integer  $\rangle$   $\rangle$  pop. of States Per Country;

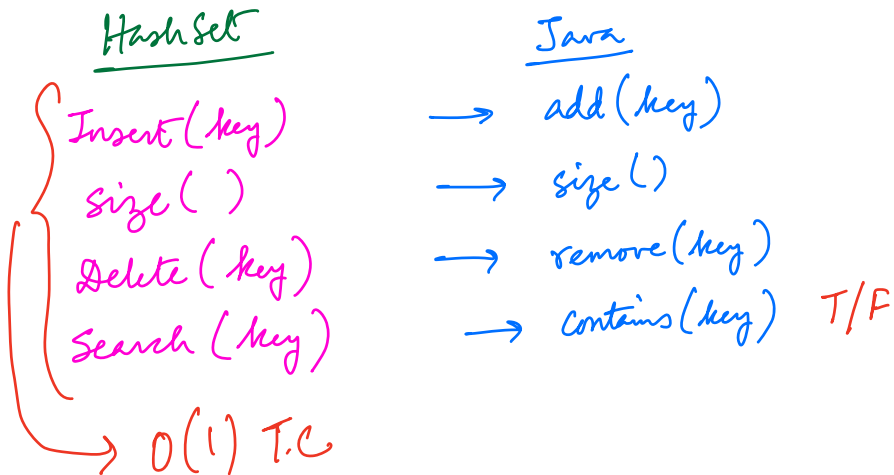
HashSet  $\rightarrow$  Helps in storing keys.

- $\rightarrow$  Key must be unique
- $\rightarrow$  Like HashMap, we can search a key in  $O(1)$  time in HashSet.

## HashMap :-



## HashSet



Adding  $n$  (key, value) pairs in a HashMap takes  $O(n)$  T.C,  $O(n)$  S.C

	Java	C++	Python	JS	C#
Hash Map	HashMap	unordered-map	dict	map	dict
Hash Set	HashSet	unordered-set	set	set	HashSet

Q1) Given  $n$  elements and  $q$  queries, find the frequency of each element in the queries.

$n=10$

2 6 3 8 2 8 2 3 8 10

$q=4$

2 8 3 5  
↓ ↓ ↓ ↓  
3 3 2 0

Brute force → For each query, iterate the array and count.

$O(q*n)$  T.C

$O(1)$  S.C.

Optimal approach → Store  $\langle \text{Element, Frequency} \rangle$  in HM.

2 6 3 8 2 8 2 3 8 10

2 8 3 5  
↓ ↓ ↓ ↓  
3 3 2 0

2 → ~~1~~ ~~2~~ 3  
6 → 1  
3 → ~~1~~ 2  
8 → ~~1~~ ~~2~~ 3  
10 → 1

```
fn frequency(A[], Q[]) {
```

```
    HashMap<int, int> hm;
```

```
    q = len(Q)
```

```
    n = len(A)
```

```
    for (i → 0 to n-1) {
```

```
        if (hm.containsKey(A[i])) {
```

```
            r = hm.get(A[i])
```

```
            hm.put(A[i], r+1)
```

```
        }
```

```
        else {
```

```
            hm.put(A[i], 1)
```

```
        }
```

```
    }
```

```
    for (i → 0 to q-1) {
```

```
        if (hm.containsKey(Q[i])) {
```

```
            print(hm.get(Q[i]))
```

```
        }
```

```
        else {
```

```
            print(0)
```

```
        }
```

```
    }
```

```
}
```

$O(n)$  TC

$O(q)$  TC

$O(n+q)$  TC

$O(n)$  S.C

Q2) Given  $n$  elements, find the first non-repeating element.

$n=6$   
1 2 (3) 1 2 5

2	→	2
1	→	2
5	→	1
3	→	1

HM.

```
fn firstNonRepeating(A[]) {  
    HashMap<int, int> hm;  
    n = len(A)  
    for (i → 0 to n-1) {  
        if (hm.containsKey(A[i])) {  
            r = hm.get(A[i])  
            hm.put(A[i], r+1)  
        }  
        else {  
            hm.put(A[i], 1)  
        }  
    }  
    for (i → 0 to n-1) {  
        if (hm.get(A[i]) == 1)  
            return A[i]  
    }  
    return -1  
}
```

$O(n)$  T.C

$O(n)$  S.C

[Break till 10:41 PM]

Q3) Given  $n$  elements, find the count of distinct elements.

$n = 5$

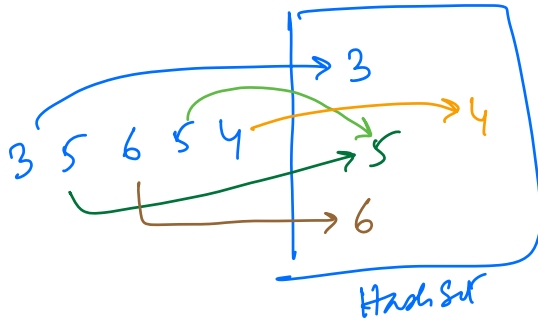
3 5 6 5 4

ans = 4

$n = 3$

4 4 4

ans = 1

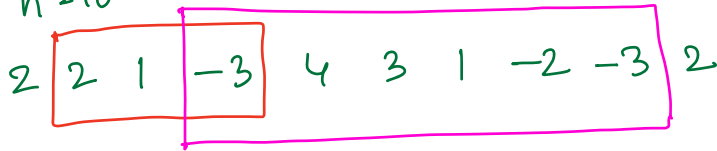


```
fn countDistinct(A[]) {  
    HashSet<int> set  
    n = len(A)  
    for (i → 0 to n-1) {  
        set.add(A[i])  
    }  
    return set.size()  
}
```

$O(n)$  TC  
 $O(n)$  SC

Q4) Given  $n$  elements, check if there exists a subarray with sum equal to 0.

$n = 10$



Ans  $\rightarrow$  True.

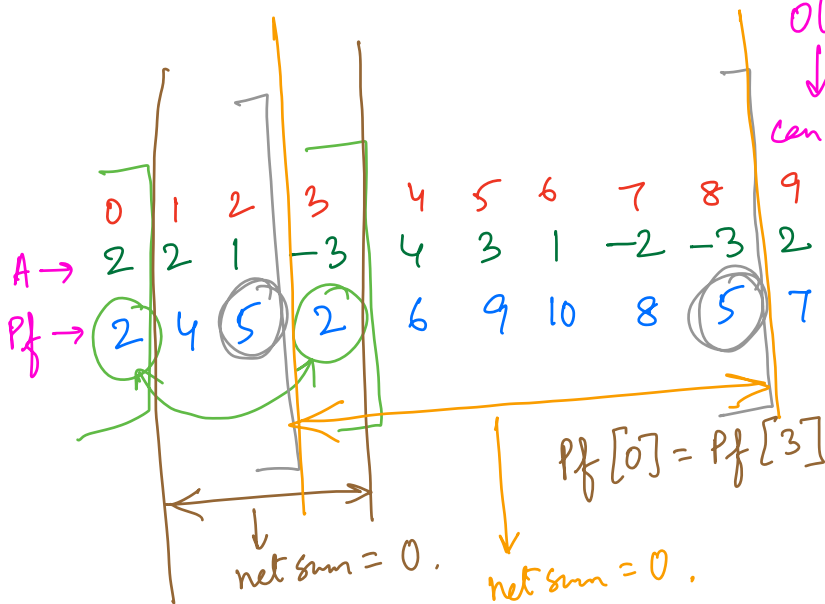
Brute Force  $\rightarrow$  Find the sum of each of  $O(n^2)$  subarrays

$O(n^3)$  TC

$\downarrow$  Prefix Sum / Carry Forward Technique.

$O(n^2)$

$\downarrow$  Can we optimise further?



$$Pf[2] = Pf[8]$$

$$\Rightarrow Pf[2] = Pf[2] + \text{sum}(A[3] \dots A[8])$$

$$\Rightarrow \text{sum}(A[3] \dots A[8]) = 0.$$

$$Pf[0] = Pf[3]$$

$$Pf[0] = [Pf[0] + \text{sum}(A[1] \dots A[3])]$$

$$\Rightarrow \text{sum}(A[1] \dots A[3]) = 0$$

$$Pf[l] = Pf[r] \Rightarrow \text{sum}(A[l+1] \dots A[r]) = 0$$

$$Pf[l] = 0 \Rightarrow \text{sum}(A[0] \dots A[l]) = 0.$$

$$A \rightarrow \left\{ \begin{array}{c|c} \text{sum} = 0 & \\ \hline -2, -1, 3, & 4 \end{array} \right\}$$

$$Pf \rightarrow 0 \left| \begin{array}{c|c} -2 & -3 \\ -2 & -3 \end{array} \right| 0 \quad 4$$



```
fn findZeroSubarraySum(A[]) {
```

```
    HashSet<int> set
```

```
    n = len(A)
```

```
    sum = 0
```

```
    for (i → 0 to n-1) {
```

```
        sum += A[i]
```

```
        if (sum == 0 || set.contains(sum))
```

```
            return true
```

```
        set.add(sum)
```

```
    }
```

```
    return false
```

```
}
```

$O(n)$  T.C

$O(n)$  S.C

Q5) You have the list of IDs where each ID (integer) represents a learner who tried a contest. A learner's ID shows up  $x$  times if they try  $x$  contests. Write a program that looks at this list and finds out how many students have tried the least nr. of contests.

$l\_ids = \{101, 102, 103, 101, 102, 101, 104, 105, 106, 105, 105\}$

101	→	3
102	→	2
103	→	1
104	→	1
105	→	3
106	→	1

min = 1

↓

3 keys whose value is 1.  
(learners)

- store all elems with freq. in HM (IDs)
  - iterate the HM/array and find min value
  - iterate the HM and find how many keys have the min value.
- } together

```

for findLeast(A[]) {
    HashMap<int, int> hm;
    n = len(A)
    for (i → 0 to n-1) {
        if (hm.containsKey(A[i])) {
            v = hm.get(A[i])
            hm.put(A[i], v+1)
        }
        else {
            hm.put(A[i], 1)
        }
    }
    int min = Integer.MAX_VALUE;
    int cnt = 0
    for (int x : hm.keySet()) {
        if (hm.get(x) == min)
            cnt++
        else if (hm.get(x) < min) {
            min = hm.get(x)
            cnt = 1
        }
    }
    return cnt
}

```

101	→	3
102	→	2
103	→	1 ✓
104	→	1
<hr/>		
105	→	3
106	→	1

$\min = 2 \times 10^9 \leftarrow 3 < \min$   
 $\text{cnt} = 0$

~~$\min = 3$~~      $\min = 2$   
 ~~$\text{cnt} = 1$~~      $\text{cnt} = 1$

$1 < 2$      $\min = 1$   
 $\text{cnt} = 1$

$1 == 1$      $\min = 1, \text{cnt} = 2$

$1 == 1$     " ,  $\text{cnt} = 3$  . ✓