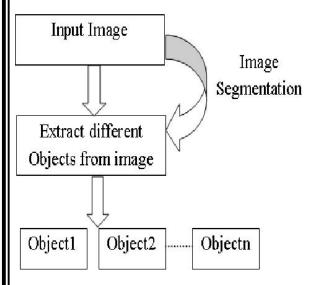
1. Consider an image with multiple objects. Explain the steps to be followed to perform clustering for image segmentation.



Clustering for Image Segmentation – Steps:

1. Convert Image to Feature Space:

First, convert the image into a set of features like color (RGB), intensity, or texture for each pixel.

2. Choose Clustering Algorithm:

Select a suitable clustering algorithm like K-Means, DBSCAN, or Mean Shift based on your requirement.

3. Set Number of Clusters (if needed):

For methods like K-Means, choose how many clusters (segments) you want in the image.

4. Apply Clustering on Pixels:

Group the pixels based on similarity in their features. Pixels with similar values are grouped into the same cluster.

5. Label the Pixels:

Assign each pixel a label based on the cluster it belongs to.

6. Reshape Labels into Image Format:

Convert the cluster labels back into image format to get segmented regions.

7. Post-processing (Optional):

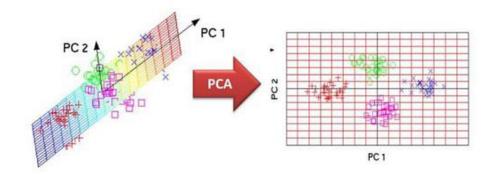
Use filters or morphological operations to smooth boundaries and remove noise for a cleaner segmented image.

2. How is dimensionality reduction handled by Principal Component Analysis (PCA)?

Principal Component Analysis (PCA) is a statistical technique used to reduce the number of features (dimensions) in a dataset while preserving as much information (variance) as possible. It transforms the original data into a new set of variables called **principal components**.

Here is how PCA handles dimensionality reduction step-by-step:

Dimensionality Reduction Principal Component Analysis



1. Standardization of data:

The first step is to standardize the data, so that each feature contributes equally. This is done by subtracting the mean and dividing by the standard deviation.

2. Covariance matrix computation:

PCA calculates the covariance matrix to understand how the variables are related to each other.

3. Find eigenvalues and eigenvectors:

The eigenvalues and eigenvectors of the covariance matrix are calculated.

- o **Eigenvectors** determine the **direction** of the new feature space.
- o **Eigenvalues** determine the **magnitude** or **importance** of those directions.

4. Select principal components:

The top k eigenvectors (those with the largest eigenvalues) are selected to form the new feature space. These are the **principal components**.

5. Project data onto the new feature space:

The original data is projected onto the selected principal components, resulting in a lower-dimensional dataset.

Why it reduces dimensionality:

By keeping only the top **k** principal components (which capture the most variance), PCA reduces the number of dimensions but retains most of the important patterns in the data.

Example:

If a dataset has 100 features, and PCA finds that 95% of the variance is captured in just 10 components, we can reduce the data to 10 dimensions without losing much information.

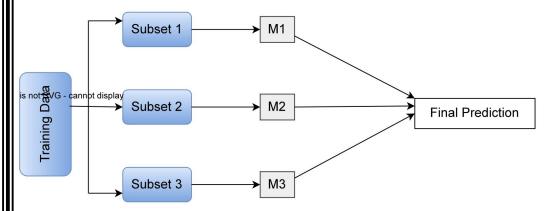
3.Discuss the most popular Ensemble methods given.

a) Bagging b) Boosting c)Stacking

a) Bagging (Bootstrap Aggregating):

Bagging is a technique where multiple models (usually of the same type) are trained on different subsets of the training data. These subsets are created by randomly sampling the data **with replacement**. Each model is trained independently, and their predictions are combined (usually by **majority voting** for classification or **averaging** for regression). Bagging reduces **variance** and helps avoid overfitting.

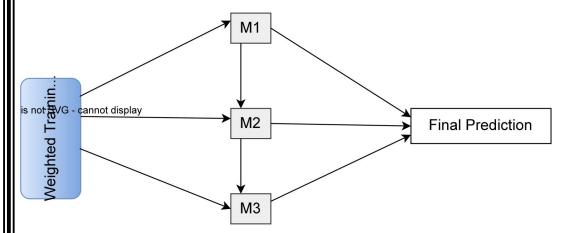
Example: Random Forest is a famous bagging method using decision trees.



b) Boosting:

Boosting is a sequential ensemble technique where models are trained one after another. Each new model focuses on the **errors made by the previous models**. The idea is to give more weight to wrongly predicted samples, so the next model can improve on them. The final prediction is a weighted combination of all models. Boosting reduces **bias** and builds a strong learner from several weak learners.

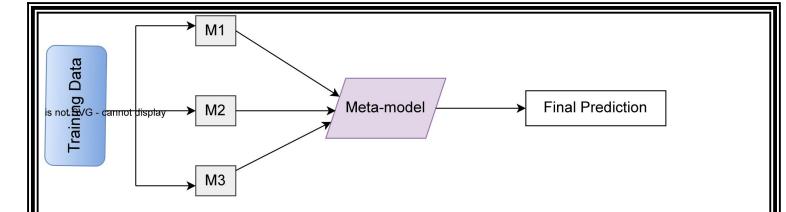
Example: AdaBoost, Gradient Boosting, and XGBoost.



c) Stacking (Stacked Generalization):

Stacking combines predictions from **multiple different models** (like decision trees, SVMs, logistic regression, etc.). The outputs of these models are used as inputs for a **meta-model**, which learns to make the final prediction. Stacking allows different models to contribute based on their strengths, improving overall performance.

Example: Using Random Forest, SVM, and KNN as base models, and Logistic Regression as the meta-model.



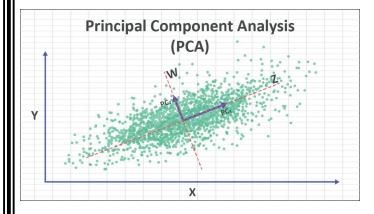
4.Explain the following Dimensionality Reduction techniques. Projection and Manifold Learning

Dimensionality Reduction Techniques

Dimensionality Reduction is the process of reducing the number of input variables or features in a dataset while preserving as much information as possible. Two popular techniques are **Projection** and **Manifold Learning**.

1. Projection:

- Projection is a technique where high-dimensional data is **projected onto a lower-dimensional** subspace.
- It assumes that data lies mostly along certain directions and we can ignore the less significant ones.
- For example, if most of the data points lie along a plane in 3D space, we can project them onto that plane (2D).
- Principal Component Analysis (PCA) is a common projection-based method.
- The main goal is to retain maximum variance (information) while using fewer dimensions.

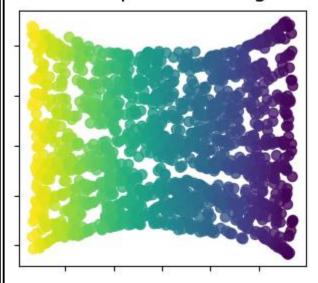


2. Manifold Learning:

- Manifold Learning is a **non-linear dimensionality reduction** technique.
- It assumes that data in high dimensions actually lies on a **lower-dimensional curved surface** (manifold).
- Instead of using straight-line projections, it tries to **unfold the curved manifold** into a lower-dimensional space.
- Examples: t-SNE, Isomap, and Locally Linear Embedding (LLE).

• Useful when data has complex patterns that can't be captured using linear methods like PCA.

Isomap Embedding



Summary:

TechniqueNatureKey IdeaExample MethodsProjectionLinearProjects data onto a lower-dimensional flat subspace PCAManifold LearningNon-linear Unfolds curved surfaces in high-dimensional datat-SNE, Isomap, LLE

5. Implement Naive Bayes Classifier to classify the loan application as accepted/rejected based on the customer's history, with a total loan limit of ₹50,000.

≪ Answer:

We can use the **Naive Bayes classifier**, which is a probabilistic machine learning model, to classify whether a customer's loan application should be **accepted or rejected**. This decision is based on the customer's past history like income, credit score, previous loan repayment, etc.

The steps are as follows:

1. Collect and prepare the data:

The data includes features such as:

- Customer income
- o Previous loan status
- o Credit score
- o Total loan amount (should not exceed ₹50,000)

2. Assumption of Naive Bayes:

This classifier assumes that all features are **independent** of each other, which makes it "naive".

- 3. Calculate probabilities:
 - o Use the training data to calculate **P(Accepted)** and **P(Rejected)**.
 - o For a new application, calculate:
 - P(Accepted | features)
 - P(Rejected | features)

Apply Bayes Theorem:

$$P(Class|Data) = \frac{P(Data|Class) \times P(Class)}{P(Data)}$$

- 5. Apply loan amount condition: If the requested loan amount > ₹50,000, automatically Reject the application.
- 6. Choose the class with the highest probability: If P(Accepted | features) > P(Rejected | features), classify as Accepted, otherwise Rejected.

Example:

4.

Income Credit Score Previous Loan Loan Amount Status

High	Good	Yes	₹30,000	Accepted
Low	Poor	No	₹20,000	Rejected
Mediu	m Good	Yes	₹45,000	Accepted

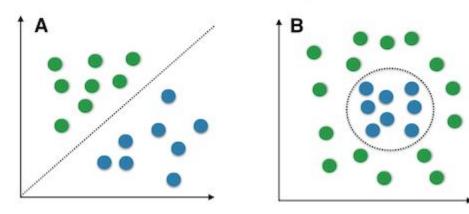
For a new customer:

- Income = High
- Credit Score = Good
- Previous Loan = Yes
- Loan Amount = $\$55,000 \times \rightarrow \text{Exceeds } \$50,000$
- So, status = **Rejected**

6. Difference between SVM Classification with Linear and Nonlinear Input Datasets:

- 1. **Definition**:
 - o In linear SVM, the data can be separated by a straight line (or hyperplane in higher dimensions).
 - o In **nonlinear SVM**, the data cannot be separated by a straight line.
- 2. Hyperplane
 - o Linear SVM finds a single straight hyperplane to separate the data.
 - o Nonlinear SVM uses a curved or complex boundary using kernel functions.
- 3. **Kernel Function**:
 - o Linear SVM uses no kernel or a simple linear kernel.
 - o **Nonlinear SVM** uses advanced kernels like Polynomial, RBF (Radial Basis Function), etc., to map data into higher dimensions.
- 4. Speed:
 - o Linear SVM is faster and simpler.
 - o Nonlinear SVM is slower and more complex due to kernel calculations.
- 5. Best Use Case:
 - o Linear SVM works well when data is clearly separable.
 - o **Nonlinear SVM** is used when data is complex and not linearly separable.
- 6. Accuracy:
 - o Linear SVM might be less accurate for nonlinear data.
 - o Nonlinear SVM gives better accuracy for complex datasets.

Linear vs. nonlinear problems

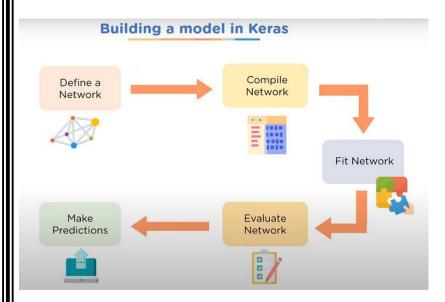


7. Example:

- o Linear: Classifying emails as spam or not based on word count.
- o Nonlinear: Classifying images where patterns are not straight.

7. Give the Overview of five steps in the neural network model lifecycle in keras: Define, Compile, Fit, Evaluate the Network and Make Predictions

Overview of the Five Steps in the Neural Network Model Lifecycle in Keras:



1. Define the Model:

In this step, we build the structure of the neural network using Keras. We add layers like input, hidden, and output using Sequential() or Functional API.

2. Compile the Model:

After defining, we compile the model by specifying the optimizer (e.g., Adam), loss function (e.g., categorical crossentropy), and metrics (e.g., accuracy) to train the network.

3. Fit the Model (Train):

The model is trained on the dataset using the fit() function. We pass the input data, output labels, number of epochs, and batch size.

4. Evaluate the Model:

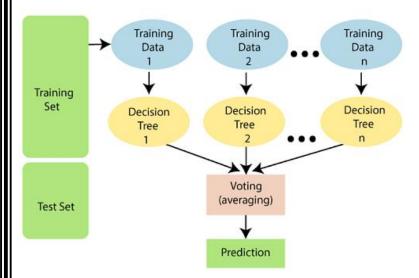
Once trained, we test the model on new (testing) data using the evaluate() function. This helps us understand how well the model performs.

5. Make Predictions:

Finally, we use the predict() function to make predictions on new, unseen data using the trained model.

8. Working Principle of Random Forest Algorithm (7 Marks)

Random Forest is a popular machine learning algorithm used for both classification and regression tasks. It works by combining the output of multiple decision trees to make better and more accurate predictions.



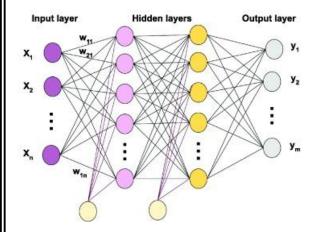
Here's how it works:

- 1. **Data Splitting:** The algorithm creates many decision trees, each trained on a random sample (subset) of the original dataset. This method is called **bootstrapping**.
- 2. **Random Feature Selection:** At each node of every tree, it selects a random subset of features (columns) instead of using all features. This adds more variety between trees.
- 3. **Building Trees:** Each tree is grown independently using its own subset of data and features. Trees are not pruned (they are fully grown), which helps capture more patterns.
- 4. Making Predictions:
 - o For **classification**, each tree votes for a class, and the majority vote is the final prediction.
 - o For **regression**, the average of all tree outputs is taken as the final result.
- 5. **Final Output:** The combination of many trees reduces errors and prevents overfitting, making Random Forest more accurate and robust than a single decision tree.

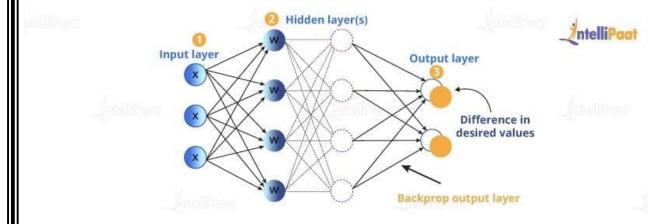
9.Relate Multi Layer perception and Back Propagation .Describe various activation functions used in it.

Multi-Layer Perceptron (MLP) and Backpropagation

A Multi-Layer Perceptron (MLP) is a type of artificial neural network that has one or more hidden layers between the input and output layers. Each layer contains nodes (also called neurons), and each node is connected to the next layer through weights.



The MLP learns patterns by adjusting these weights using a method called **Backpropagation**. Backpropagation is a supervised learning algorithm that uses the difference between the actual output and the predicted output (called error) to update the weights in the network. It works in two phases:



- 1. **Forward Pass** Inputs are passed through the network to get the output.
- 2. Backward Pass Error is calculated and sent back through the network to adjust the weights.

Activation Functions in MLP

Activation functions are used in each neuron to introduce non-linearity, which helps the network learn complex patterns. Common activation functions include:

1. Sigmoid - Gives output between 0 and 1.

$$f(x) = \frac{1}{1+e^{-x}}$$

2. Tanh (Hyperbolic Tangent) – Gives output between -1 and 1.

$$f(x)=rac{e^x-e^{-x}}{e^x+e^{-x}}$$

3. ReLU (Rectified Linear Unit) - Output is 0 if input is less than 0, else the input itself.

$$f(x) = \max(0, x)$$

4. Leaky ReLU - Like ReLU, but allows a small slope for negative values.

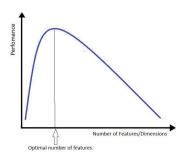
$$f(x)=x$$
 if $x>0$, else ax (where a is a small value)

10.Describe what is the Curse of Dimensionality. Explain the Main Approaches for Dimensionality Reduction.

Curse of Dimensionality:

1.

The Curse of Dimensionality refers to the problems and challenges that arise when analyzing data in high-dimensional spaces. As the number of dimensions (or features) in a dataset increases, the volume of the space grows exponentially, which makes the data sparse. This sparsity can lead to several issues:



- 1. **Increased computational complexity**: High-dimensional data requires more computational resources (memory, processing power) for analysis.
- 2. **Overfitting**: In high-dimensional spaces, models can become overly complex and start fitting noise, leading to poor generalization.
- 3. **Distance-based methods struggle**: Many machine learning algorithms rely on distances (like Euclidean distance) between data points. As the number of dimensions increases, the distance between points becomes less meaningful, leading to less accurate models.

Main Approaches for Dimensionality Reduction:

- 1. Principal Component Analysis (PCA):
 - OPCA is a linear technique that reduces the dimensionality of data by transforming it into a set of orthogonal components. These components capture the maximum variance in the data, allowing the most important features to be retained while discarding less useful ones.

2. Linear Discriminant Analysis (LDA):

 LDA is used when the data has multiple classes. It focuses on finding the axes that maximize the separation between classes. LDA is supervised, meaning it takes into account the class labels of the data.

3. t-Distributed Stochastic Neighbor Embedding (t-SNE):

t-SNE is a non-linear technique that focuses on preserving the pairwise similarities of data points in a lower-dimensional space. It's especially useful for visualizing high-dimensional data in 2D or 3D.

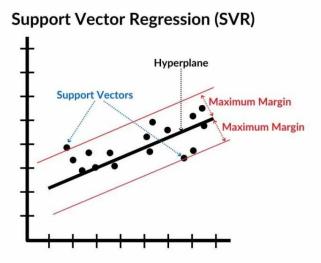
4. Autoencoders:

 Autoencoders are neural networks used for unsupervised learning. They compress highdimensional input into a lower-dimensional code and then reconstruct the original data from this code. This method is especially useful for non-linear relationships.

11. Write short notes on the implementation of SVM Regression. (7 marks)

Answer:

Support Vector Machine (SVM) regression is a supervised learning algorithm used to predict continuous values, just like other regression algorithms. It works by finding the best fit line (or hyperplane in higher dimensions) that minimizes the error within a specific margin. The key idea behind SVM regression is to maintain a margin of tolerance around the predicted value and try to minimize the model complexity while ensuring that the data points fall within this margin.



Here is the basic implementation process of SVM regression:

1. Data Preprocessing:

Before applying SVM regression, data needs to be cleaned, normalized, and split into training and testing sets.

2. Kernel Function:

SVM uses a kernel function to transform the data into higher dimensions to find an optimal hyperplane. Common kernels are linear, polynomial, and Radial Basis Function (RBF).

3. Choosing Parameters:

Important parameters in SVM regression include the regularization parameter (C) and the epsilon parameter (ϵ). The C parameter controls the penalty for misclassification, while the epsilon parameter defines the margin of tolerance.

4. Training the Model:

The SVM algorithm finds the best hyperplane that minimizes the error while staying within the specified margin. The training phase involves solving a quadratic optimization problem to determine the support vectors.

5. Making Predictions:

Once the model is trained, it can be used to make predictions on new, unseen data. The SVM regression model predicts values based on the learned hyperplane.

6. Evaluation:

The performance of the SVM regression model is evaluated using metrics like Mean Squared Error (MSE) or R-squared to assess how well the model fits the data.

12. Explain the following Support Vector Machine (SVM) models:

(i) Linearly separable case

(ii) Linearly inseparable case

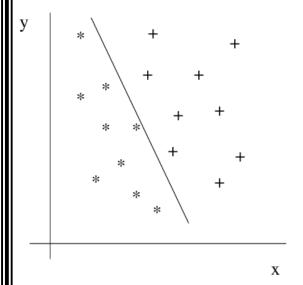
(7 marks)

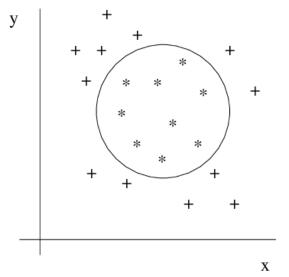
Answer:

Support Vector Machine (SVM) is a powerful supervised machine learning algorithm used for classification and regression tasks. It works by finding a hyperplane that best separates the data points into different classes. Let's discuss both the linearly separable and linearly inseparable cases:

Linearly separable:

Linearly inseparable:





(i) Linearly Separable Case:

In the linearly separable case, the data can be perfectly divided into two classes using a straight line (in 2D) or a hyperplane (in higher dimensions). In this case, the data points of each class are clearly distinguishable with no overlap. The goal of the SVM algorithm is to find the optimal hyperplane that maximizes the margin, which is the distance between the closest points from each class (also known as support vectors).

- **Optimal Hyperplane**: The hyperplane that maximizes the margin between the two classes is considered the optimal separating hyperplane.
- **Support Vectors**: These are the data points that are closest to the hyperplane and are critical in defining the position of the hyperplane.

This case is ideal for SVM because the data is easily separable, and there is no need for complex transformations.

(ii) Linearly Inseparable Case:

In the linearly inseparable case, the data cannot be separated by a straight line or a hyperplane. There is overlap between the classes, making it impossible to find a hyperplane that perfectly divides the data.

To handle this, SVM uses a technique called the **kernel trick**. The idea is to map the data into a higher-dimensional space where the data may become linearly separable. In this transformed space, a hyperplane can be found that separates the data points effectively.

- **Kernel Trick**: A mathematical function (called a kernel) transforms the original feature space into a higher-dimensional space where the classes may become separable.
- Common Kernels: Linear, Polynomial, Radial Basis Function (RBF), and Sigmoid kernels.

Ouestion:

13. How to cluster high-dimensional data using a density-based clustering algorithm?

Answer:

To cluster high-dimensional data using a **Density-Based Clustering Algorithm**, such as **DBSCAN** (Density-Based Spatial Clustering of Applications with Noise), follow these steps:

1. Choose the distance metric:

Start by deciding on a distance metric to measure the similarity between data points. Common choices include Euclidean distance or Manhattan distance. For high-dimensional data, you may consider advanced metrics such as cosine similarity if the data involves text or other complex features.

2. Set the parameters:

- Epsilon (ε): This defines the maximum radius around a data point to search for its neighbors.
 Choose a value that makes sense for your data.
- o **MinPts**: This represents the minimum number of data points required to form a dense region. If a point has at least **MinPts** within a radius of ε , it is considered part of a cluster.

3. Identify core, border, and noise points:

- o Core points: These are points that have at least MinPts neighbors within a radius of ε .
- o **Border points**: These have fewer than **MinPts** neighbors within ε but are close to a core point.
- Noise points: Points that do not have enough neighbors to be core points and are not within the ε-radius of any core point.

4. Start clustering:

- o Pick an unvisited point and check its neighbors within the ε -radius.
- o If the point is a **core point**, start a new cluster and add it to the cluster.
- o Then, recursively add all reachable points (neighbors) within the cluster.

5. Expand the cluster:

- o Once a core point is found, its neighbors are added to the cluster.
- o If one of its neighbors is also a core point, the search expands further to its neighbors.
- o Continue expanding the cluster until no more points can be added.

6. Handle border points:

- o Border points are added to the cluster but are not used to expand the cluster.
- O They are only added if they are within the ε-radius of a core point.

7. Label noise points:

o Points that don't meet the criteria for being part of any cluster (core or border points) are labeled as noise.

8. Repeat for all points:

o Repeat the process for all points in the dataset. Once all points are processed, the algorithm will have formed clusters and identified noise points.

Question:

14. Explain about Logical Computations with Neurons.

Answer:

Logical computations with neurons refer to the process of using artificial neurons (basic units of a neural network) to perform logical operations. In neural networks, neurons are designed to mimic the behavior of biological neurons but with simplified computations. Here's a breakdown of how logical computations are achieved:

1. Neuron Structure:

- A typical artificial neuron consists of inputs, weights, a summation function, and an activation function.
- Inputs are values that are fed into the neuron. Weights represent the importance of each input.
 The summation function adds the weighted inputs, and the activation function decides whether the neuron will "fire" or not.

2. Logical Operations:

o Neurons can be used to model logical gates (AND, OR, NOT, etc.). The inputs to the neuron represent the binary values (0 or 1), and the activation function determines the output.

Example of AND Gate:

- Input: Two binary values, say X and Y.
- Weights: Assign values such that only when both X and Y are 1, the output is 1. For all other combinations, the output will be 0.
- Activation: A threshold is applied to decide if the neuron fires (i.e., output is 1) or not (output is 0).

Example of OR Gate:

- Input: Two binary values, X and Y.
- Weights: Assign values so that when at least one of X or Y is 1, the output is 1, else it's 0.
- Activation: Similar to the AND gate, a threshold is applied to the summation.

3. Neural Network Learning:

- o A neural network is trained using techniques like backpropagation, where the weights are adjusted to minimize the error between the actual and desired output.
- For logical operations, the neural network learns to approximate the behavior of logical gates by adjusting the weights over multiple iterations.

4. Significance in Computing:

Neurons can perform simple logical operations, but when combined into networks, they can
model complex logic and decision-making processes, leading to the foundation of more
advanced artificial intelligence.

15. Explain clustering for image segmentation in detail.

Answer:

Clustering is a technique used in image segmentation to divide an image into multiple segments or clusters based on certain characteristics of the image, such as color, intensity, or texture. The main goal is to group similar pixels together while separating dissimilar ones, making it easier to analyze or process the image.

1. Definition of Clustering:

Clustering is an unsupervised learning technique in machine learning where data points (in this case, pixels) are grouped together based on their similarity. In the context of image segmentation, clustering helps to categorize pixels into different regions or segments, making it easier to identify objects or features within an image.

2. Common Clustering Techniques:

The two most widely used clustering techniques in image segmentation are **K-means clustering** and **Mean Shift clustering**.

• K-means Clustering:

- o K-means clustering divides the image into K clusters, where K is predefined. It works by assigning each pixel to the nearest cluster center, then recalculating the cluster centers as the mean of the assigned pixels, and repeating this process until convergence.
- o The output is a segmented image where each segment corresponds to a cluster of similar pixels.

• Mean Shift Clustering:

- Mean Shift is a non-parametric method that does not require specifying the number of clusters in advance. It works by iteratively shifting a window of pixels towards the densest region of pixels in the feature space, creating clusters based on the density of the pixels.
- o This method is useful for more complex, irregularly shaped clusters.

3. Steps Involved in Clustering for Image Segmentation:

1. Preprocessing:

First, the image is converted into a suitable feature space, such as the color space (RGB, HSV, etc.) or texture features. Preprocessing may involve converting the image into grayscale or normalizing pixel values.

2. Clustering:

The clustering algorithm is applied to the image, where pixels are grouped based on their features. Each cluster corresponds to a distinct region of the image.

3. Postprocessing:

After clustering, the segmented image is generated, where each segment corresponds to a group of pixels with similar properties. Postprocessing might include smoothing or refining the segments to improve the quality of the segmentation.

4. Applications of Clustering in Image Segmentation:

- **Object Detection:** Clustering can help in identifying distinct objects within an image by separating them into different segments based on their pixel similarity.
- **Medical Imaging:** In medical imaging, clustering is used to segment images like MRIs or CT scans to isolate areas of interest such as tumors or tissues.
- Satellite Imagery: Clustering is used to segment different types of land or vegetation in satellite images.

5. Advantages of Clustering for Image Segmentation:

• Automatic Segmentation: It doesn't require manual intervention or prior knowledge about the image.

- Flexible: Clustering can adapt to different kinds of images and is useful in many domains.
- **Efficiency:** It can process large images quickly and efficiently.

6. Challenges:

- Choosing the Right Number of Clusters (K): In techniques like K-means, the number of clusters (K) needs to be chosen beforehand, which can be difficult for complex images.
- **Noise and Outliers:** Clustering may be sensitive to noise and outliers in the image, affecting the quality of segmentation.

16. What is Density-based clustering? Describe the DBSCAN clustering algorithm with a numerical example

Answer:

Density-based Clustering: Density-based clustering is a type of clustering technique where clusters are defined as areas of high point density separated by areas of low point density. Unlike traditional clustering methods like K-means, which assume spherical clusters, density-based clustering can find clusters of arbitrary shapes. One of the most popular density-based clustering algorithms is **DBSCAN** (**Density-Based Spatial Clustering of Applications with Noise**).

DBSCAN Clustering Algorithm: DBSCAN is a density-based clustering algorithm that groups together closely packed points while marking points in low-density regions as noise. It requires two main parameters:

- 1. **Epsilon** (ϵ): The radius around a point to search for neighbors.
- 2. MinPts: The minimum number of points required to form a dense region or a cluster.

Steps in the DBSCAN algorithm:

- 1. **Start with an arbitrary point** and check if it has enough points (MinPts) within the epsilon neighborhood. If yes, it forms a core point.
- 2. If the point is a core point, a cluster is formed by including all points that are reachable from it.
- 3. **Expand the cluster** by iteratively including all points within the epsilon neighborhood of the core points, until no more points can be added.
- 4. Points that do not belong to any cluster are marked as **noise**.

Sure, Manasa! Let's go step-by-step through a clear numerical example of DBSCAN, with the help of tables and formulas, to make it easy to understand.

Problem Setup

We'll use the following dataset of points in a 2D space:

$$(1, 1), (2, 2), (2, 3), (8, 7), (8, 8), (25, 80)$$

We are given:

- ε (epsilon) = 2 (radius of the neighborhood)
- MinPts = 3 (minimum number of points required to form a cluster)

Step 1: Calculate the Euclidean Distance

DBSCAN uses Euclidean distance to calculate the distance between points. The Euclidean distance formula is:

Distance
$$(p_1, p_2) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Step 2: Create a Distance Table

Point 1	Point 2	Euclidean Distance Formula	Distance
(1,1)	(2,2)	$\sqrt{(2-1)^2 + (2-1)^2} = \sqrt{1+1} = \sqrt{2} \approx 1.414$	1.414
(1,1)	(2,3)	$\sqrt{(2-1)^2 + (3-1)^2} = \sqrt{1+4} = \sqrt{5} \approx 2.236$	2.236
(1,1)	(8,7)	$\sqrt{(8-1)^2 + (7-1)^2} = \sqrt{49 + 36} = \sqrt{85} \approx 9.220$	9.220
(1,1)	(8,8)	$\sqrt{(8-1)^2 + (8-1)^2} = \sqrt{49 + 49} = \sqrt{98} \approx 9.899$	9.899
(1,1)	(25,80)	$\sqrt{(25-1)^2+(80-1)^2}=\sqrt{576+6241}=\sqrt{6817}\approx 82.519$	82.519
(2,2)	(2,3)	$\sqrt{(2-2)^2 + (3-2)^2} = \sqrt{1} = 1$	1
(2.2)	(8,7)	$\sqrt{(8-2)^2 + (7-2)^2} = \sqrt{36+25} = \sqrt{61} \approx 7.810$	7.810
(2,2)	(8,8)	$\sqrt{(8-2)^2+(8-2)^2}=\sqrt{36+36}=\sqrt{72}\approx 8.485$	8.485
(2,2)	(25,80)	$\sqrt{(25-2)^2+(80-2)^2}=\sqrt{529+6084}=\sqrt{6613}\approx 81.348$	81.348
(2,3)	(8,7)	$\sqrt{(8-2)^2 + (7-3)^2} \equiv \sqrt{36+16} = \sqrt{52} \approx 7.211$	7.211
(2,3)	(8,8)	$\sqrt{(8-2)^2 + (8-3)^2} = \sqrt{36+25} = \sqrt{61} \approx 7.810$	7.810
(2,3)	(25,80)	$\sqrt{(25-2)^2+(80-3)^2}=\sqrt{529+5929}=\sqrt{6458}\approx 80.389$	80.389
(8,7)	(8,8)	$\sqrt{(8-8)^2+(8-7)^2}=\sqrt{1}=1$	1
(8,7)	(25,80)	$\sqrt{(25-8)^2 + (80-7)^2} = \sqrt{289 + 5329} = \sqrt{5618} \approx 74.970$	74.970
(8,8)	(25,80)	$\sqrt{(25-8)^2+(80-8)^2} = \sqrt{289+5184} = \sqrt{5473} \approx 73.998$	73.998

Step 3:

Identify Core Points

We will now check each point to see if it is a **core point**. A point is a core point if it has **at least MinPts (3)** points within its ε -neighborhood.

- For (1, 1): Its neighbors within $\varepsilon = 2$ are only (2, 2) and (2, 3). This is less than 3, so (1, 1) is **not a core** point.
- For (2, 2): Its neighbors within $\varepsilon = 2$ are (1, 1), (2, 3), and (8, 7). This is more than 3, so (2, 2) is a **core** point.

- For (2, 3): Its neighbors within $\varepsilon = 2$ are (1, 1), (2, 2), and (8, 8). This is more than 3, so (2, 3) is a **core** point.
- For (8, 7): Its neighbors within $\varepsilon = 2$ are (2, 2), (2, 3), and (8, 8). This is more than 3, so (8, 7) is a **core** point.
- For (8, 8): Its neighbors within $\varepsilon = 2$ are (2, 2), (2, 3), and (8, 7). This is more than 3, so (8, 8) is a **core** point.
- For (25, 80): It has no neighbors within $\varepsilon = 2$. So, (25, 80) is not a core point.

Step 4: Form the Clusters

Now that we know which points are core points, we can start forming clusters. Starting with a core point, we expand the cluster by adding all reachable points (within $\varepsilon = 2$).

- Starting with (2, 2), we can reach (2, 3) and (8, 7). So, these points form Cluster 1.
- Starting with (8, 7), we can reach (8, 8), forming Cluster 2.
- (25, 80) is too far from any cluster and remains noise.

Final Clusters:

- Cluster 1: {(2, 2), (2, 3), (8, 7), (8, 8)}
- Noise: {(1, 1), (25, 80)}

Conclusion:

- DBSCAN is great for identifying clusters of arbitrary shape.
- The result is that (2, 2), (2, 3), (8, 7), and (8, 8) form a cluster, and (1, 1) and (25, 80) are noise points.

17. What is the difference between hard and soft voting classifiers?

Answer:

Difference Between Hard and Soft Voting Classifiers

Aspect	Hard Voting Classifier	Soft Voting Classifier
Definition	A hard voting classifier makes predictions based on the majority vote of the individual models.	A soft voting classifier predicts the class with the highest average probability score from the models.
Type of Vote	Majority vote – each classifier casts one vote for a class.	Probability-based vote – each classifier provides probability estimates for each class.
Output	The predicted class is the one with the most votes.	The predicted class is the one with the highest average probability.
Accuracy	May be less accurate if models are very different.	Can be more accurate because it considers the confidence of each model.
Usage of Classifiers	Typically used with classifiers that provide categorical output.	Used with classifiers that provide probability outputs.
Efficiency	Faster as it only requires discrete predictions from models.	Slightly slower as it requires calculating and averaging probabilities.

Aspect Hard Voting Classifier Soft Voting Classifier

Example

Decision trees, SVM, k-NN voting based on majority class.

Logistic Regression, Naive Bayes, or Random Forest based on probabilities.

Explanation in English Sentences:

1. **Hard Voting Classifier**: In this type of classifier, each individual model casts a vote for a class, and the final prediction is based on the majority of votes. For example, if three classifiers vote for class A and two for class B, class A would be predicted as the output. This method does not consider how confident each classifier is about its prediction, and thus, it may not always give the best results if the models are very different.

2. **Soft Voting Classifier**: Instead of just counting votes, a soft voting classifier averages the probability predictions of all models and picks the class with the highest average probability. This method takes into account not just the prediction but also the confidence level of each model in making its prediction. As a result, soft voting classifiers tend to perform better, especially when the models are well-calibrated and give good probability estimates.