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BOOTH'S ALGORITHM

(SIGNED & UNSIGNED)

Content

- Introduction.
- History.
- Flow chart.
- Example for unsigned multiplication.
- Example for signed multiplication.

Objectives:-

- To provide knowledge on signed and unsigned multiplications
- To solve problems on booth's algorithm.
- To teach procedure for binary multiplication using booth's algorithm.

What is booth’s algorithm?

- Booth's multiplication algorithm is an algorithm which multiplies 2 signed or unsigned integers in 2's complement.
- This approach uses fewer additions and subtractions than more straightforward algorithms.

History

The algorithm was invented by **Andrew Donald Booth** in 1950 while doing research on crystallography at Birkbeck College in Bloomsbury, London.

Booth at work in about 1948

Points to remember(for unsigned)

- Firstly take two registers Q and M
- Load multiplicand and multiplier in this registers
- For eg., In 4 * 5 , 4 is multiplicand and 5 is multiplier.

Points to remember(for unsigned)

- We also need third register A, which is initialize to 0(zero).
- We also need a register to store carry bit resulting from addtion . Hence, we take one bit register Q-1

Points to remember(for unsigned)

- Multiplicand(M) is added to register Q and the result is stored in register A
- Then all bits of the A,Q,Q-1 are shifted to the right one bit.
- Depending upon last bit of Q and single bit of Q-1 following arithmetic operations are performed.

Points to remember(for unsigned)

- Possible arithmetic actions:
  - 00 → no arithmetic operation
  - 01 → add multiplicand to left half of product
  - 10 → subtract multiplicand from left half of product
  - 11 → no arithmetic operation

Points t0 remember(signed)

- Firstly signed integers is converted into unsigned using 2's complement
- Then its is loaded in registers.
- Example
- 2's compliment of (-5)
- Binary :- 0111
- 1's compliment:- 1000

  \+ 1

- 2's compliment:- 1001

Binary addition.

- Following are the possibilities in binary addition
- 1+0--> 1
- 1+1--> 0 with carry 1
- 0+1-->1
- 0+0-->0
- Example

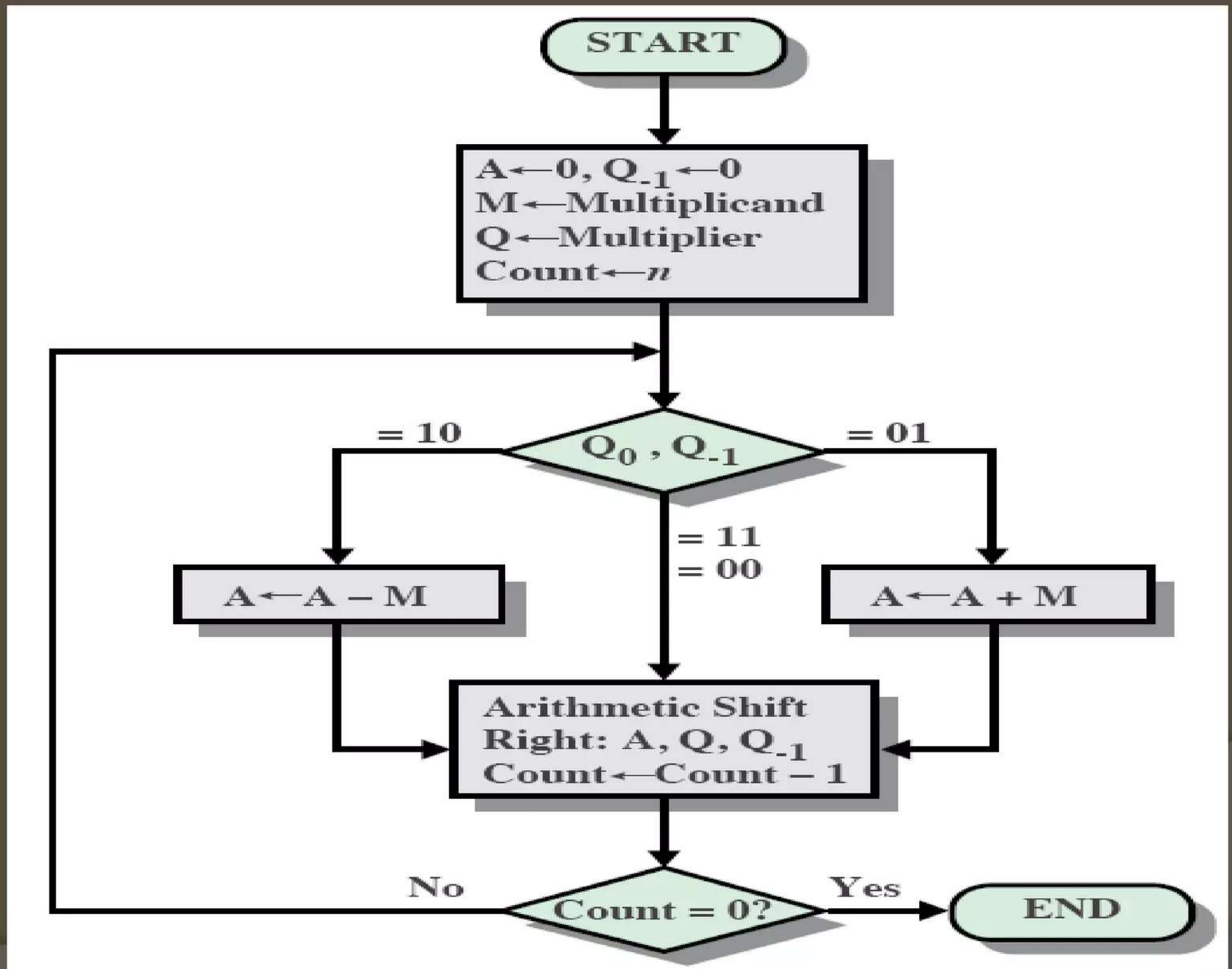
```
 (1)  11111    (left half of product)
     +00010    (multiplicand)
      00001    (drop the leftmost carry)
```

Binary subtraction

- Following are the possibilities in binary subtraction.
- 1-0--> 1
- 1-1--> 0
- 0-1--> 1 with carry 1
- 0-0--> 0
- Example

```
   (1)  00000  (left half of product)
       -00010          (mulitplicand)
        11110   (uses a phantom borrow)
```

Flow chart


START
A←0, Q-1←0
M←Multiplicand
Q←Multiplier
Count←n
Q0 , Q-1
= 10
= 01
= 11
= 00
A←A – M
A←A + M
Arithmetic Shift
Right: A, Q, Q-1
Count←Count – 1
No
Count = 0?
Yes
END

Booth : (7) x (3)

A	Q	Q-1	M	
		3	7	
0000	0011	0	0111	
1001	0011	0	0111	A <-(A - M) 1st cycle
1100	1001	1	0111	Shift
1110	0100	1	0111	Shift
0101	0100	1	0111	A <-(A + M) 2nd cycle
0010	1010	0	0111	Shift
0001	0101	0	0111	Shift

Booth : (7) x (-3)

A	Q	Q-1 (-3)	M 7	
0000	1101	0	0111	
1001	1101	0	0111	A <- (A - M) 1st cycle
1100	1110	1	0111	Shift
0011	1110	1	0111	A <- (A + M) 2nd cycle
0001	1111	0	0111	Shift
1010	1111	0	0111	A <- (A - M) 3rd cycle
1101	0111	1	0111	Shift
1110	1011	1	0111	Shift

References

- www.slideshare.net
- http://www.csci.csusb.edu
- Computer organization and architecture -Williamstallings.

☺THANK YOU ☺

Any questions?