Final Test Applied Algorithms, 23/12/2016

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Bài A. kseq

 $\begin{array}{lll} \text{Input:} & \text{stdin} \\ \text{Output:} & \text{stdout} \\ \text{Time limit:} & 2 \text{ giây} \\ \text{Memory:} & 512 \text{ MB} \end{array}$

Given a sequence of positive integers $a = \langle a_1, \ldots, a_n \rangle$. A k-sequence of a is defined to be a sub-sequence of a containing k consecutive elements: $a_i, a_{i+1}, \ldots, a_{i+k-1}$. The weight of a k-sequence is defined to be the sum of its elements. Given a positive integer k, you are required to write a program that finds a k-sequence having maximal weight.

Input

The input consists following lines:

- line 1: contains n and k ($5 \le n \le 1000000, 1 \le k \le 50000$)
- line 2: contains n positive integers $a_1, \ldots, a_n \ (a_i \le 1000)$

Result

Write the weight of the k-sequence found.

Example

stdin	stdout
6 3	30
2 3 20 4 6 5	

Explanation

The 3-sequence of maximal weight is 20, 4, 6 and its weight is 20 + 4 + 6 = 30.

Bài B. netalz

Input: stdin
Output: stdout
Time limit: 2 giây
Memory: 512 MB

Given a communication network which is modelled as an undirected connected graph G = (V, E) in which $V = \{1, ..., N\}$ is the set of nodes. The distance between two nodes u and v of G is denoted by d(u, v) and is defined to be the length (i.e., the number of edges) of the shortest path between u and v on G. The eccentricity e(u) of a node u is defined to be the maximum distance between u and other nodes of G:

$$e(u) = \max_{v \in V} d(u, v)$$

The radius r(G) of the graph G is define to be the minimum eccentricity:

$$r(G) = \min_{u \in V} e(u)$$

You are required to write a program that computes the radius of a G.

Input

The input consists following lines:

- line 1: contains N and M ($5 \le N \le 5000, 5 \le M \le 500000$) in which N is the number of nodes and M is the number of edges of the graph G
- line i+1 ($\forall i = 1, ..., M$): contains u and v in which (u, v) is an edges of G.

Result

Write out the radius of G.

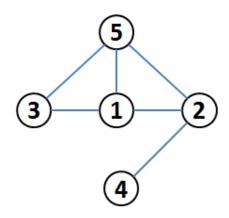
Example

	stdin	stdout
5 6		2
1 2		
1 3		
1 5		
2 4		
2 5		
3 5		

Explanation

The graph is described in Figure 1. The distance between nodes are:

- d(1,2)=1
- d(1,3) = 1
- d(1,4)=2
- d(1,5) = 1
- d(2,3) = 2
- d(2,4)=1



Hình 1: Illustration of the communication network G

- d(2,5) = 1
- d(3,4) = 3
- d(3,5) = 1
- d(4,5) = 2

The eccentricity of nodes are:

- e(1) = 2
- e(2) = 2
- e(3) = 3
- e(4) = 3
- e(5) = 2

Finally, the radius of the given graph is 2.

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Bài C. primes

 $\begin{array}{lll} \text{Input:} & \text{stdin} \\ \text{Output:} & \text{stdout} \\ \text{Time limit:} & 1 \text{ giây} \\ \text{Memory:} & 512 \text{ MB} \end{array}$

Given a positive integer n. Your task is to calculate how many ways to represent n as sum of at most k different prime numbers.

Input

The input contains two integers $n, k \ (1 \le n \le 4000, 1 \le k \le 10)$.

Result

Write the number of ways to represent n as sum of at most k different prime numbers.

Example

stdin	stdout
28 4	5

Explanation

28 can be represented as sum of at most 4 different prime numbers by one of the following ways:

- 28=2+3+23
- 28=2+7+19
- 28=3+5+7+13
- 28=5+23
- 28=11+17

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Bài D. machine3

Input: stdin
Output: stdout
Time limit: 1 s
Memory: 128 MB

An engineer needs to schedule a machine to run on some given periods $1, \ldots, n$ to produce a chemical product \mathcal{C} . Each period i is represented by a starting time point s_i and terminating time point t_i ($s_i < t_i$). You can assume that there is no two periods with the same terminate point. Due to a technical constraint, the machine must run on exactly two periods that are not overlap (two periods i and j are not overlap if $t_i < s_j$ or $t_j < s_i$). If the machine is runned on the period i, then the amount of \mathcal{C} it will produce is equal to the duration of the period i (which is equal to $t_i - s_i$). Help the engineer to select k ($k \le 3$) not-overlap periods to run the machine such that the amount of \mathcal{C} produced is maximal.

Input

The input consists the following lines:

- Line 1: contains two positive integers n and k $(2 \le n \le 10^6, k \le 3)$;
- Line i + 1: contains two positive integers s_i and t_i $(1 \le s_i < t_i \le 3 \times 10^6)$.

Result

The output consists of only one single integer which is the amount of product \mathcal{C} the machine will produce in the k selected periods. In case there is no solution (there does not exist two periods that are not overlap), the output contains the value -1.

Example

	stdin	stdout
5 2		8
8 12		
6 11		
3 9		
2 5		
1 4		

Explanation

The machine will be runned on two periods [2, 5] and [6, 11] and produce 8 unit of product C.