

# Recap

- Description of defects in crystalline materials
  - Higher dimensional defects - Various Interfaces
  - One-dimensional defects - Dislocations
  - Point defects
- Vacancies in a metallic crystal
  - Entropy of configuration leads to eqm. conc.
  - Temperature dependence of this conc.

# Defects in Ionic/Covalent Materials

Additional Reading:  
Section 5.5 and 5.6

## Physical Chemistry of Ionic Materials

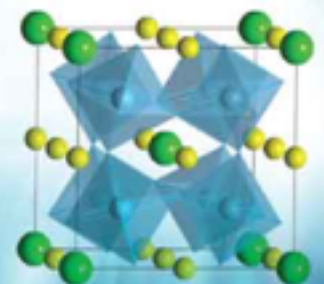
Ions and Electrons in Solids

JOACHIM MAIER

WILEY

## SOLID STATE CHEMISTRY AND ITS APPLICATIONS

SECOND EDITION STUDENT EDITION

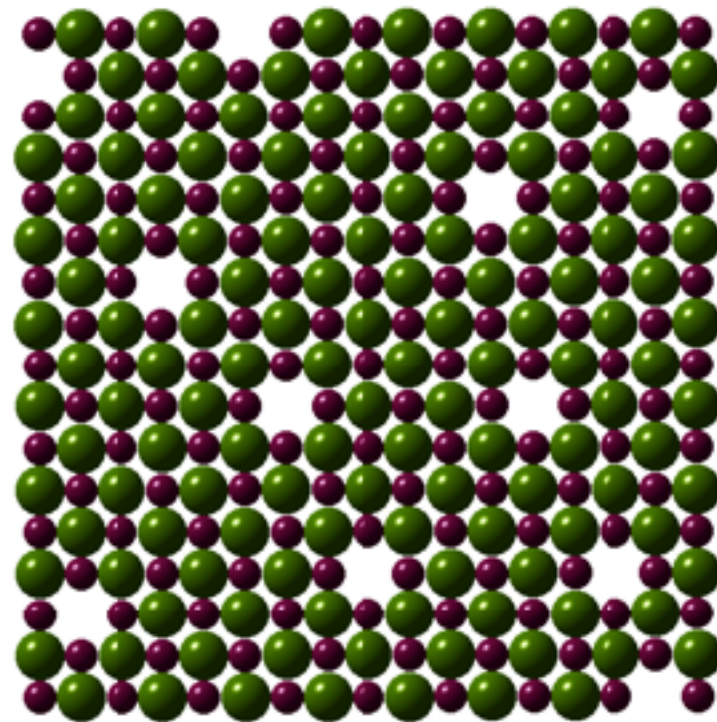
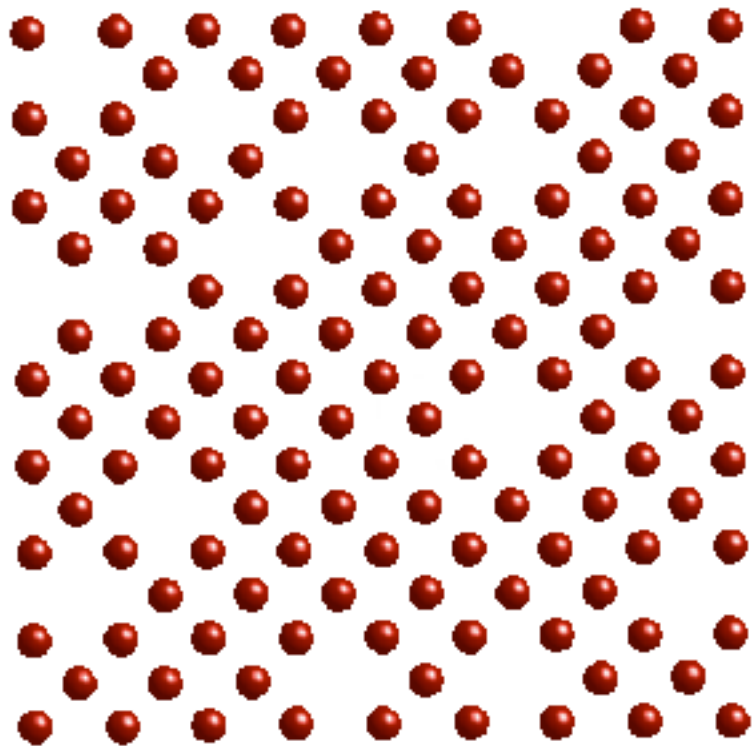


ANTHONY R. WEST

Section 2.2 and 2.3

WILEY

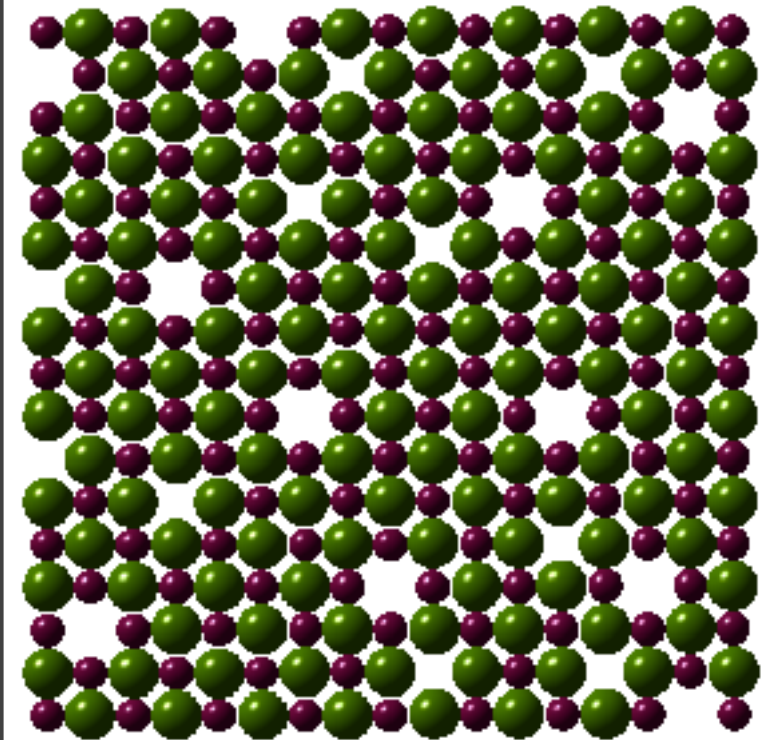
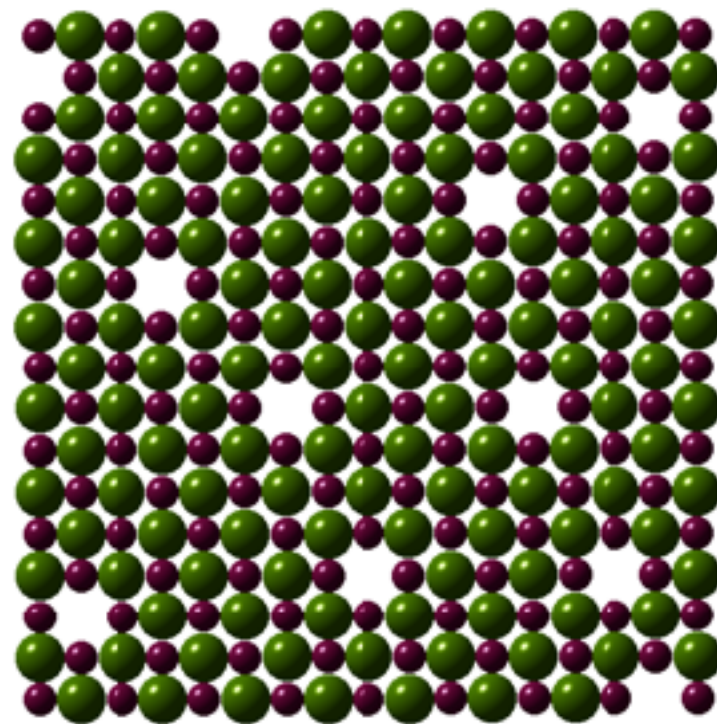
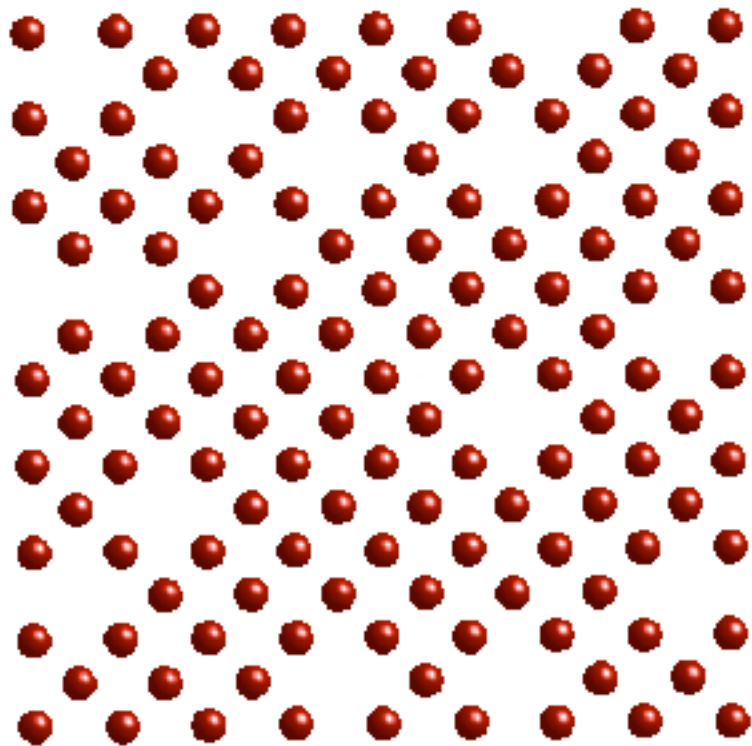




# Metallic vs Ionic crystals

---





# Metallic vs Ionic crystals

---

# Defects in Ionic Crystals

Local Electroneutrality demands that:

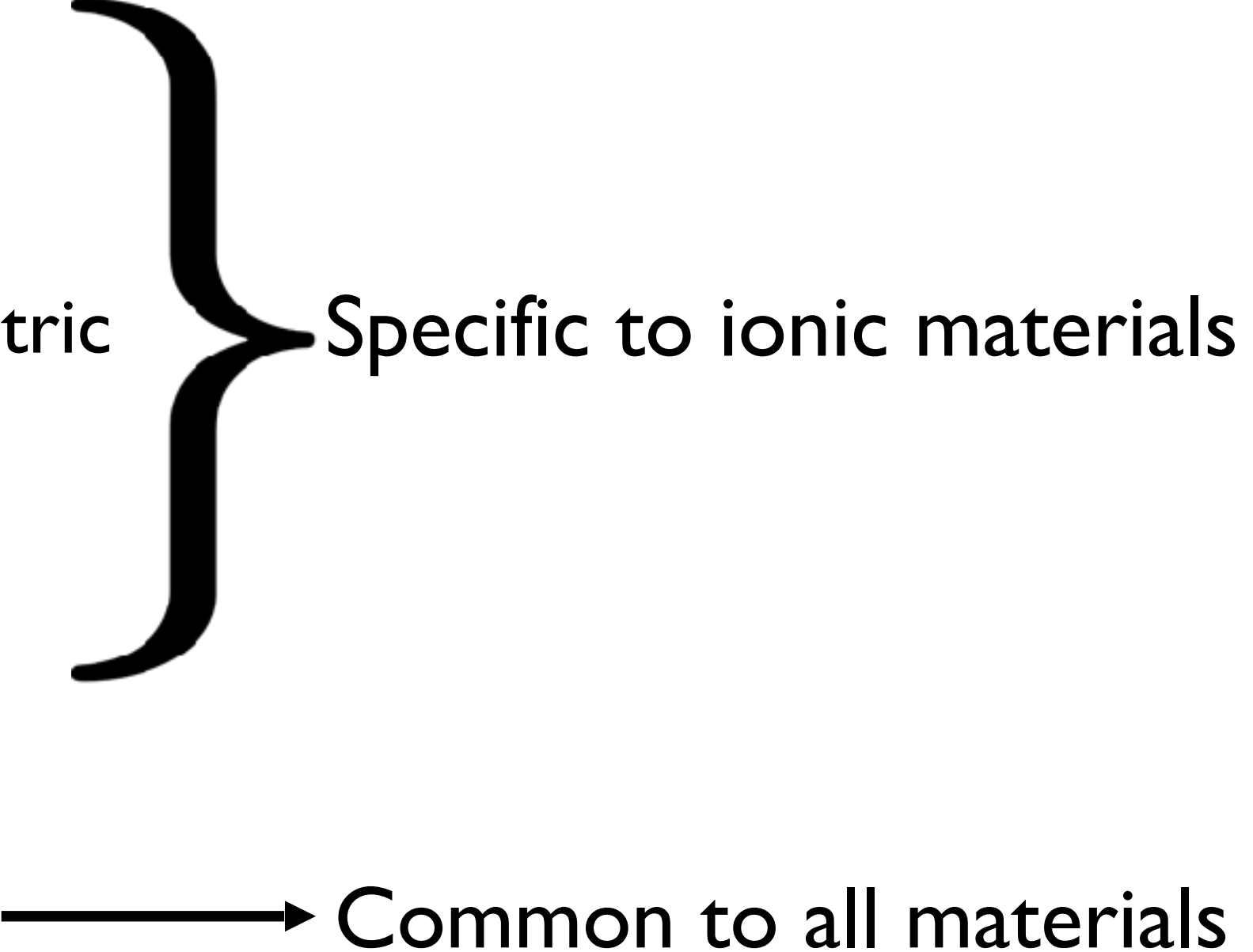
$\text{Nil} \Rightarrow \text{Positive Defect} + \text{Negative Defect}$

$$\left( \frac{n_{d+}}{n_+} \right) \times \left( \frac{n_{d-}}{n_-} \right) = \exp - \frac{\Delta G_m^*}{RT}$$

Composed of bonding and vibrational properties of the defect pair

Many other possibilities for defects exist

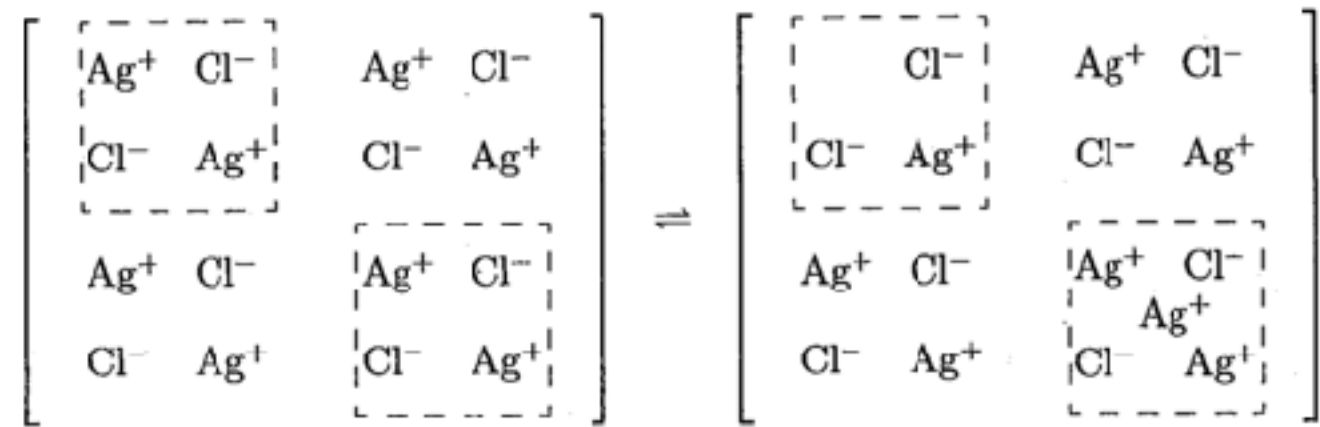
# Types of Defects in Ionic Crystals

- Stoichiometric
  - Non-stoichiometric
  - Electronic
  - Extrinsic doping
- 
- Specific to ionic materials
- Common to all materials

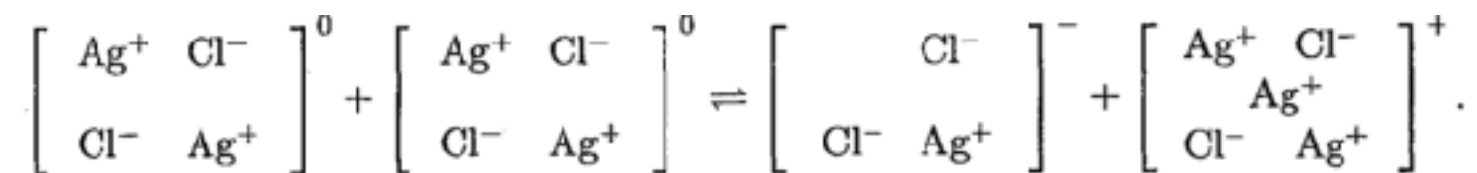
# Stoichiometric defects

- Internal defect reactions
- Cation to anion ratio maintained in the crystal
  - Remove an ion from its' site and place it at a different site, but within the crystal lattice
    - Frenkel
    - Anion Frenkel
  - Remove/add cations and anions in pairs from their sites/ surfaces and place them in surface/interstitial positions
    - Schottky
    - Anti-Schottky

# Frenkel Defect Pair Formation



Considering only the sections that have changed





# Notation for defects - Kröger-Vink

General Format :  $M_s^c$

- $M$  corresponds to the structural element
  - Atoms
  - Vacancies
  - electrons/holes
- $S$  - Lattice site that the structural element occupies
  - Regular site
  - Interstice
- $C$  - Charge of the defect relative to site that it occupies

# Kröger-Vink notation - $\text{AgCl}$

$V'_{\text{Ag}} \Rightarrow$  Vacancy on a silver site

$V_{\text{Cl}}^{\bullet} \Rightarrow$  Vacancy on a chlorine site

$\text{Ag}_i^{\bullet} \Rightarrow$  Silver Interstitial

$\text{Cl}'_i \Rightarrow$  Chlorine interstitial

The Frenkel defect reaction becomes:  $\text{Ag}_{\text{Ag}}^{\text{x}} + V_i^{\text{x}} \rightleftharpoons \text{Ag}_i^{\bullet} + V'_{\text{Ag}}$

# Mass Action Law - Frenkel defect

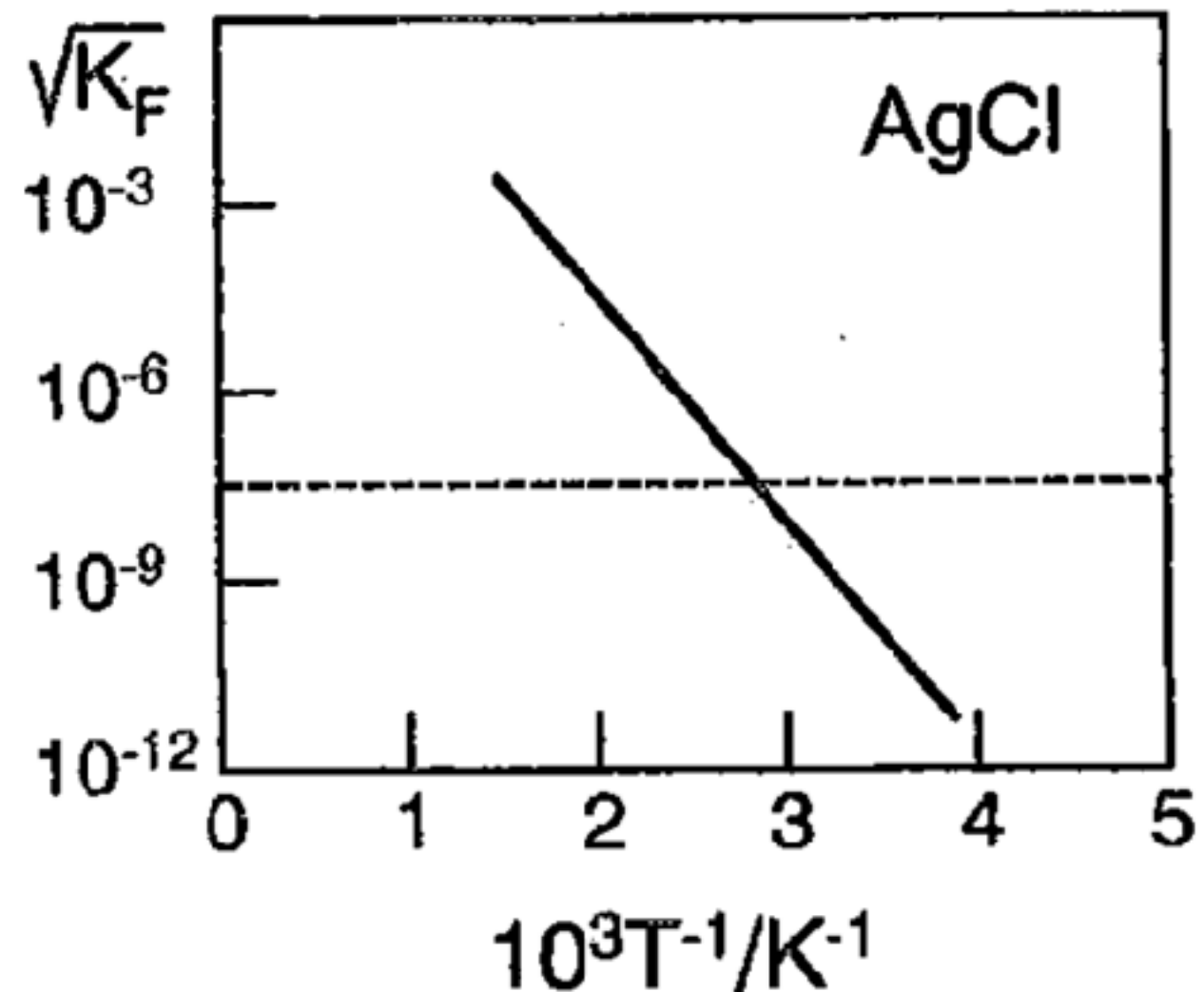
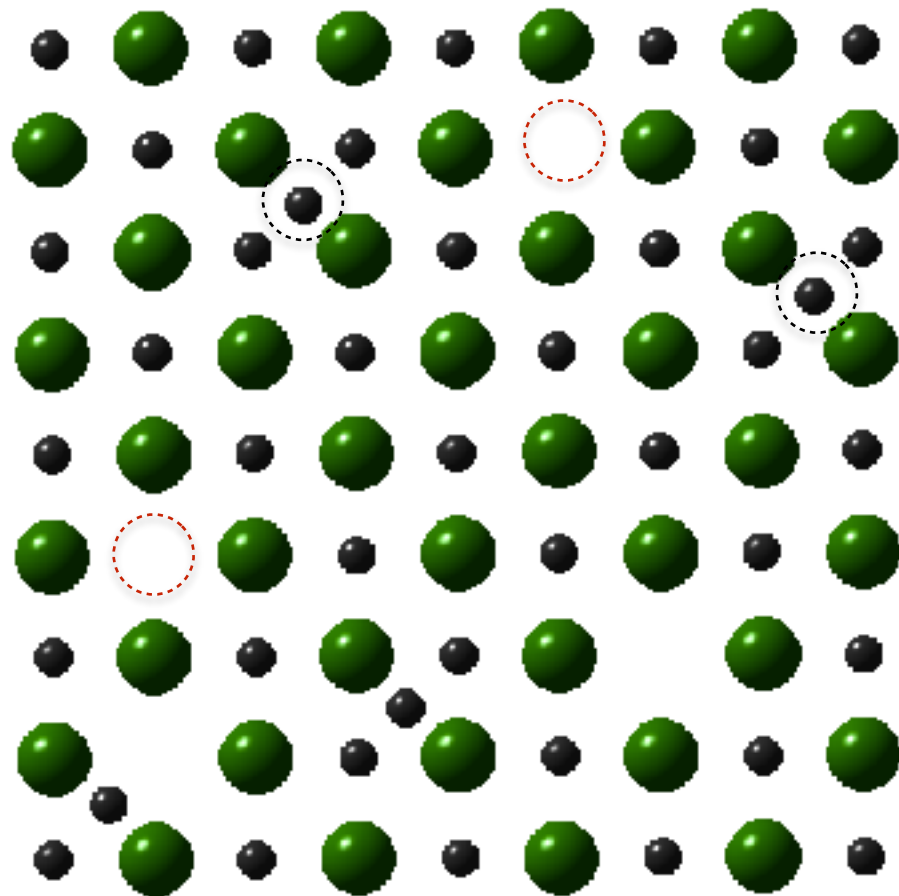
where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

$$[Ag_i^\bullet] [V'_{Ag}] = \alpha N^2 \times K_F$$

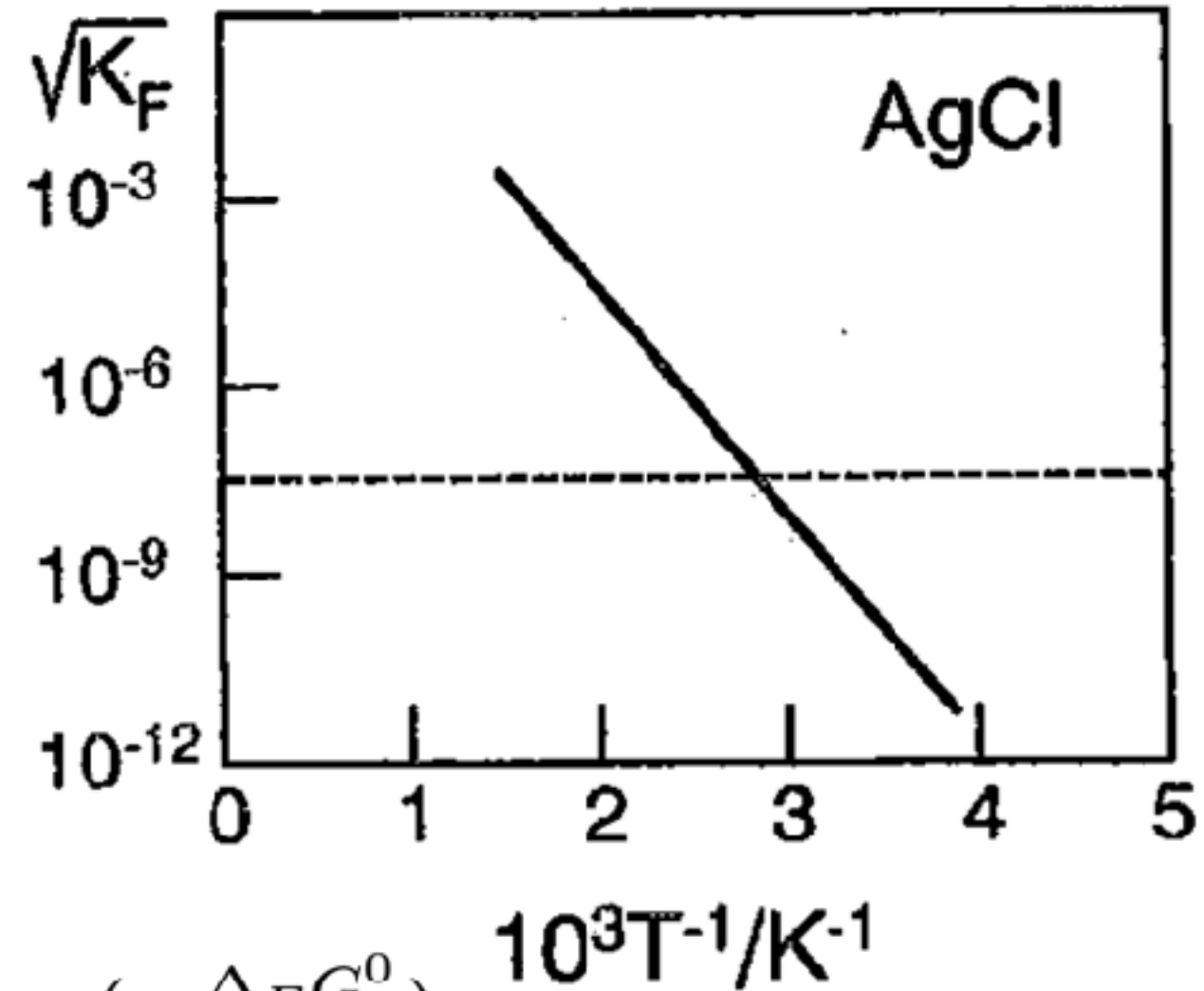
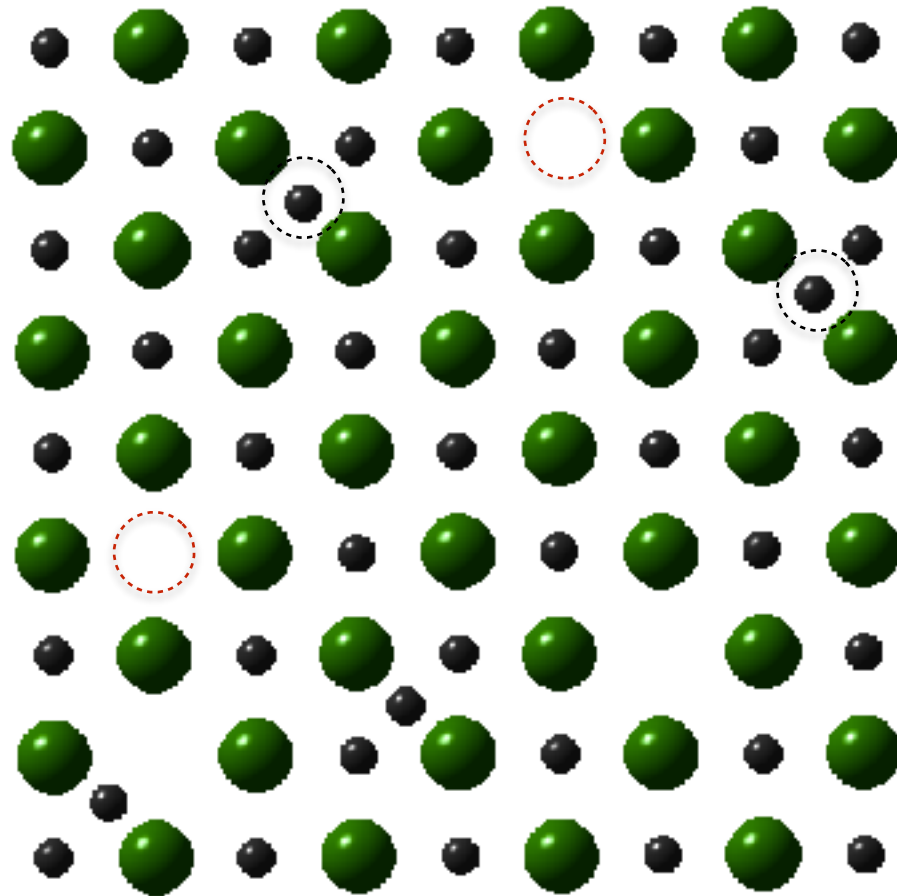
$N \rightarrow$  No. of atomic sites/cc

$\alpha \rightarrow$  Interstitial/atomic

electroneutrality:  $[Ag_i^\bullet] = [V'_{Ag}] = \sqrt{K_F(T)} \times N\sqrt{\alpha}$

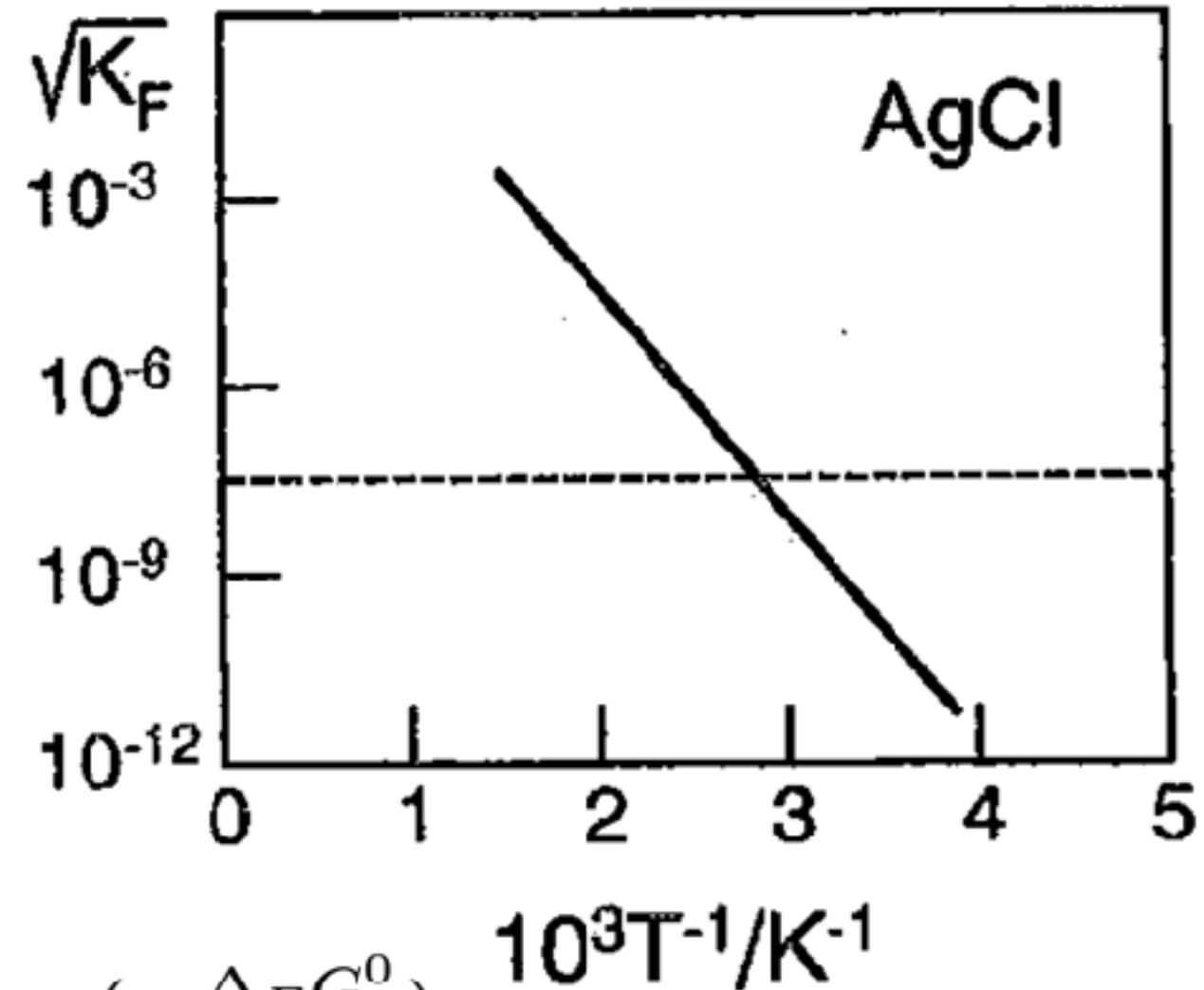
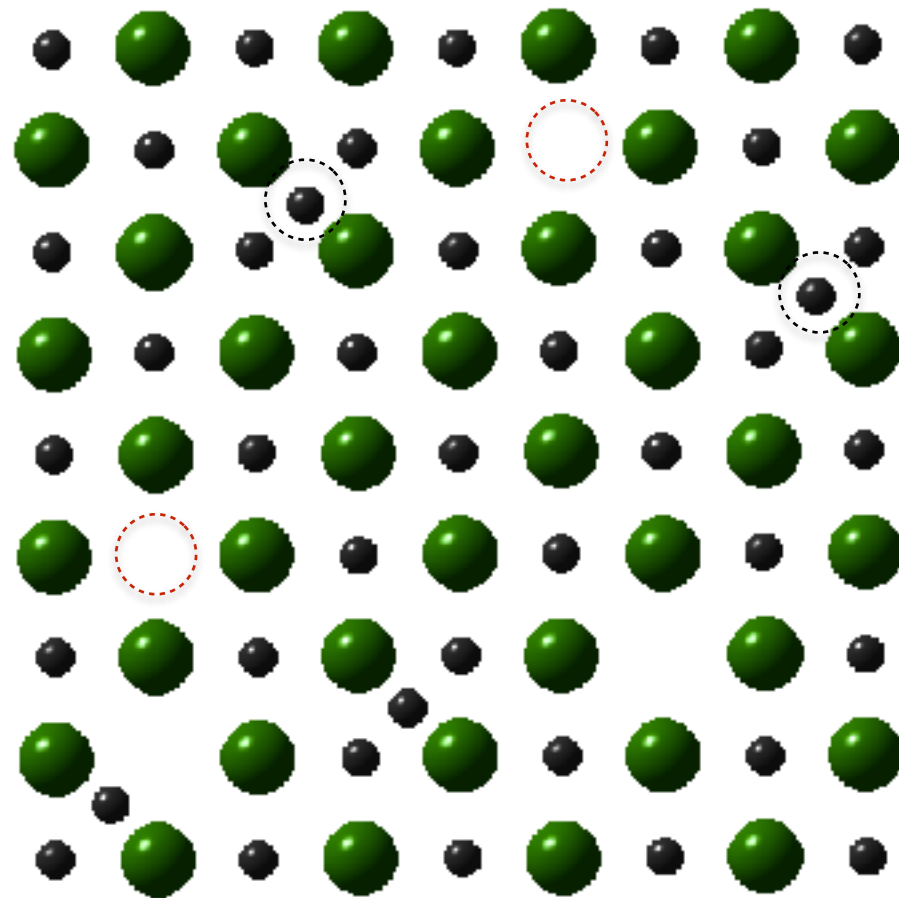


# Energetics - Frenkel defect



where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

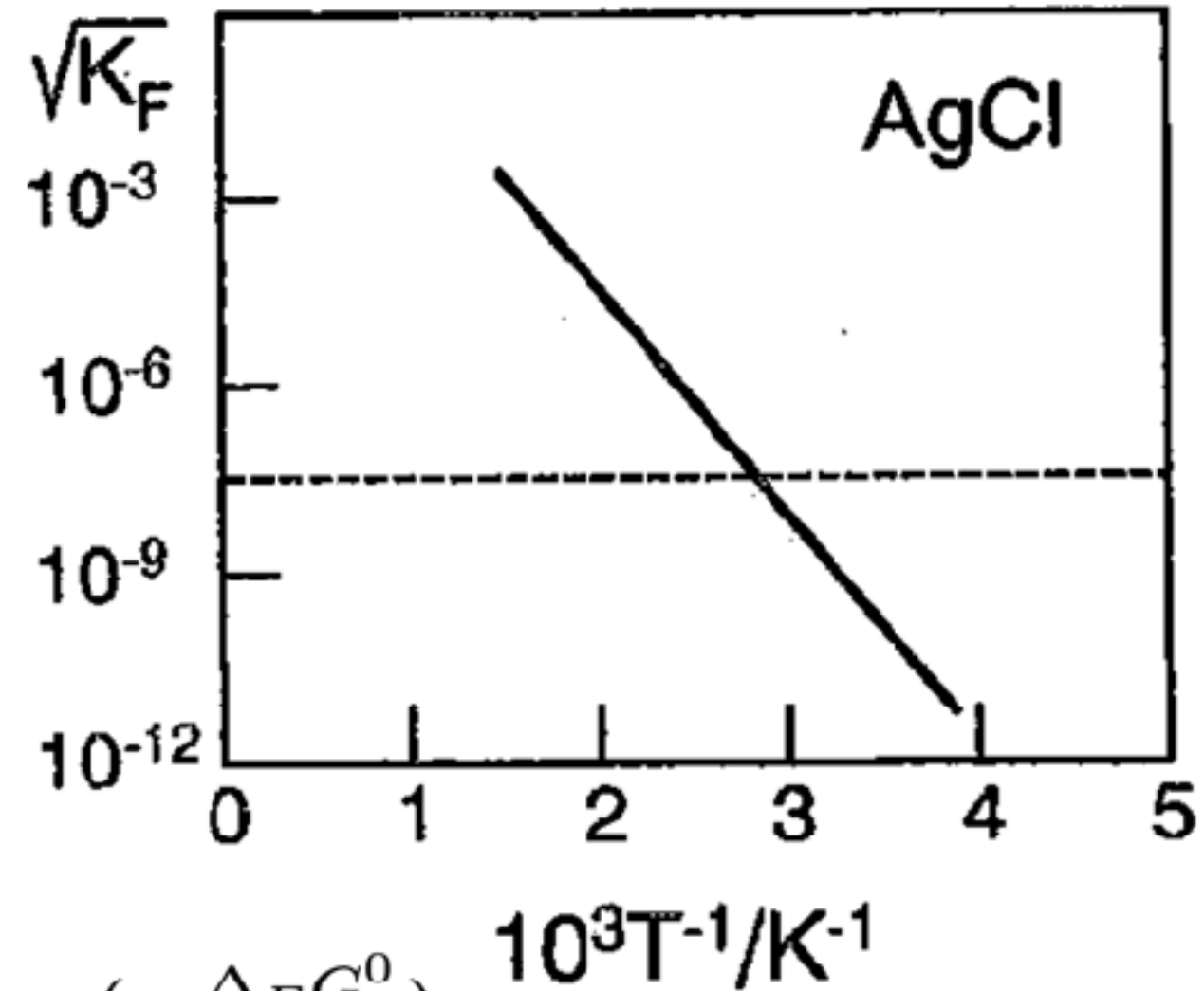
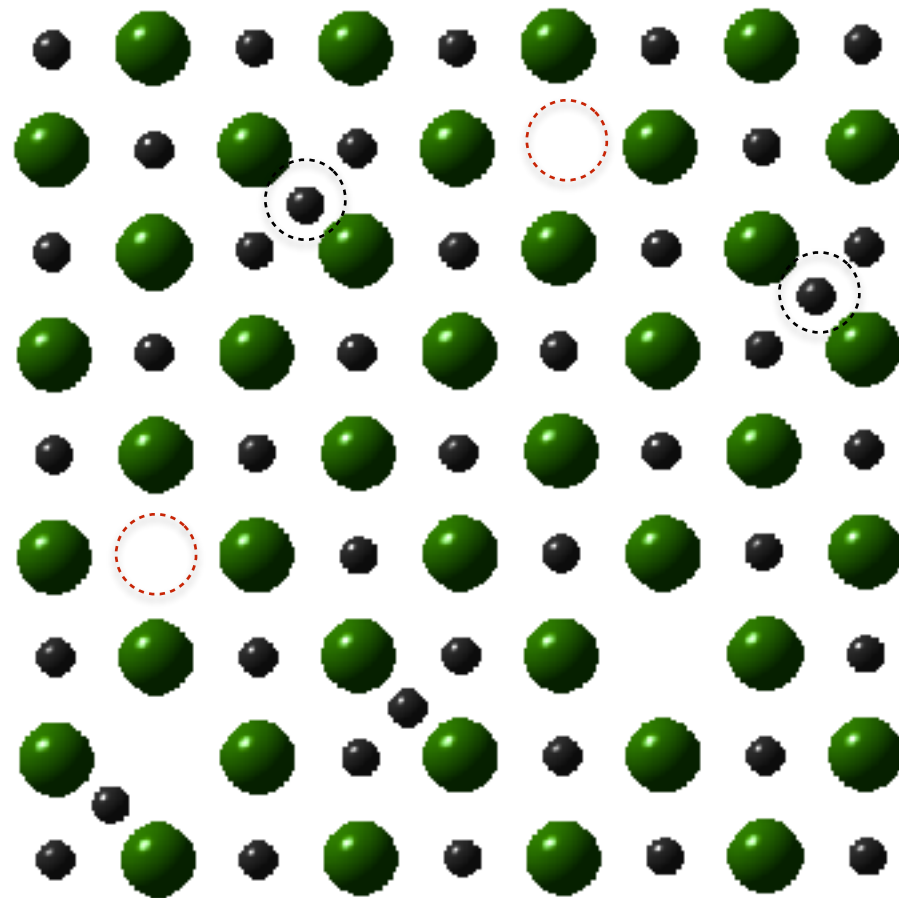
# Energetics - Frenkel defect



where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

$$\Rightarrow [Ag_i^\bullet] = [V'_{Ag}] = N\sqrt{\alpha \times K_F} = \exp\left(\frac{\Delta S_F^0}{2R}\right) \exp\left(-\frac{\Delta H_F^0}{2RT}\right)$$

# Energetics - Frenkel defect



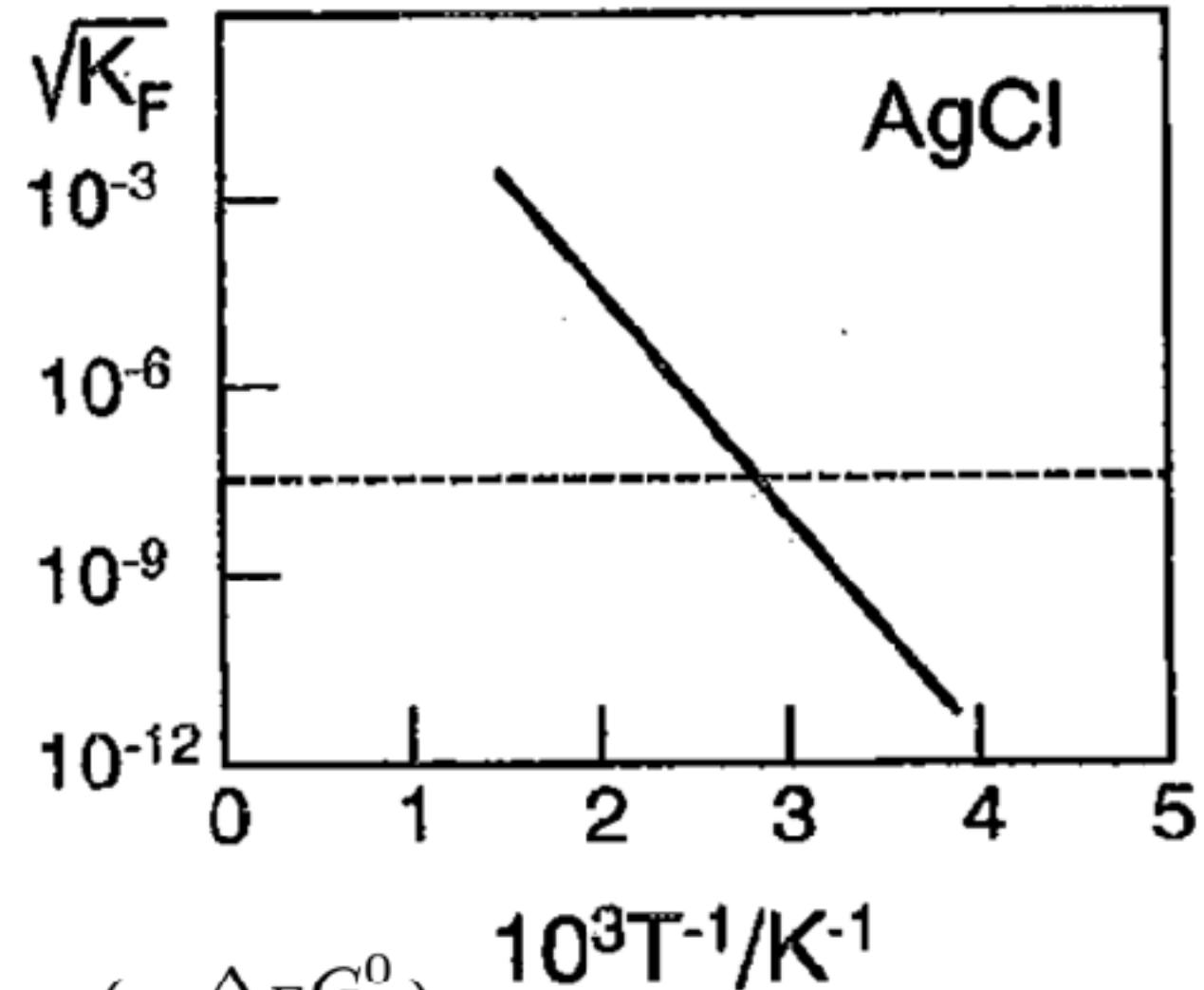
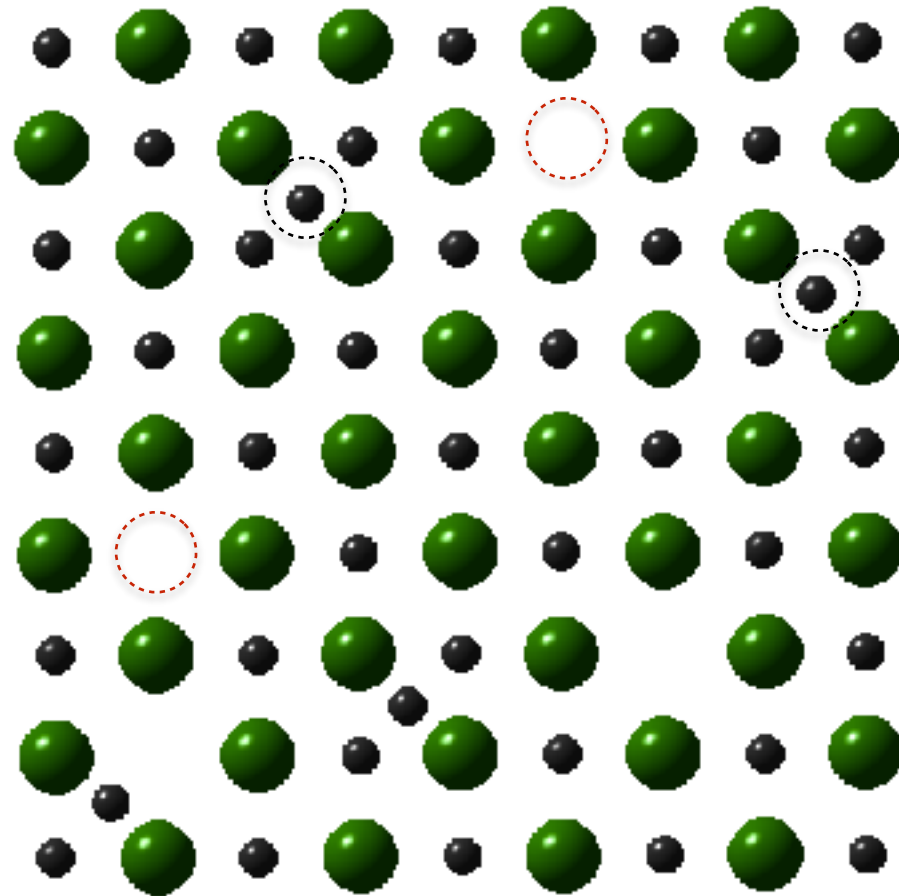
where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

$$\Rightarrow [Ag_i^\bullet] = [V'_{Ag}] = N\sqrt{\alpha \times K_F} = \exp\left(\frac{\Delta S_F^0}{2R}\right) \exp\left(-\frac{\Delta H_F^0}{2RT}\right)$$

$$\Delta S_F^0 \approx 9.4R$$



# Energetics - Frenkel defect



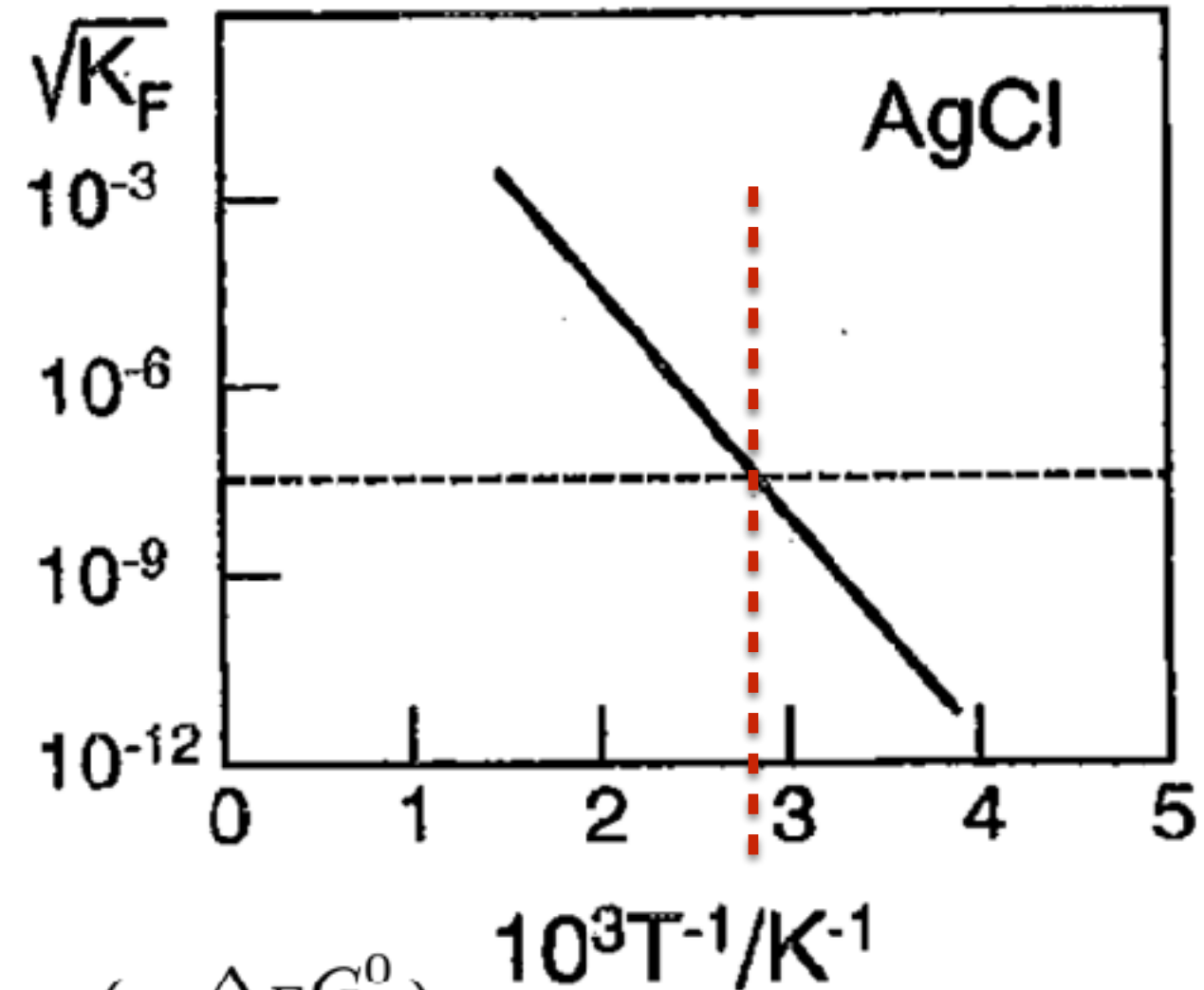
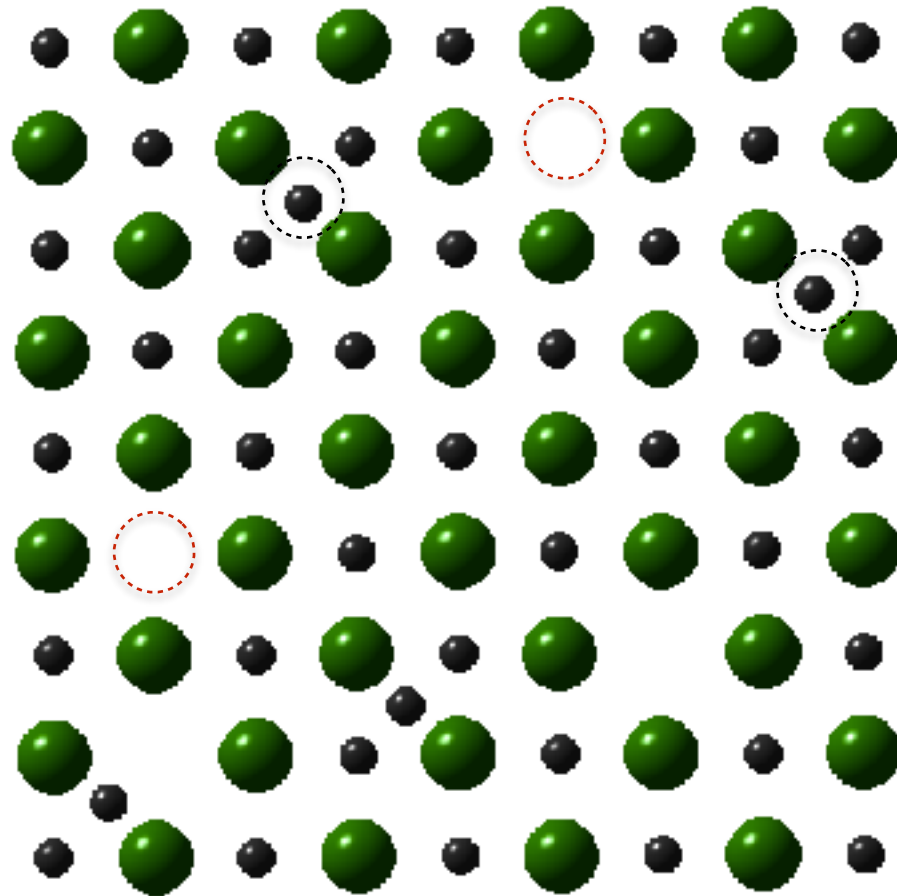
where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

$$\Rightarrow [Ag_i^\bullet] = [V'_{Ag}] = N\sqrt{\alpha \times K_F} = \exp\left(\frac{\Delta S_F^0}{2R}\right) \exp\left(-\frac{\Delta H_F^0}{2RT}\right)$$

$$\Delta S_F^0 \approx 9.4R$$

$$\Delta H_F^0 \approx 140 \text{ kJ.mol}^{-1}$$

# Energetics - Frenkel defect



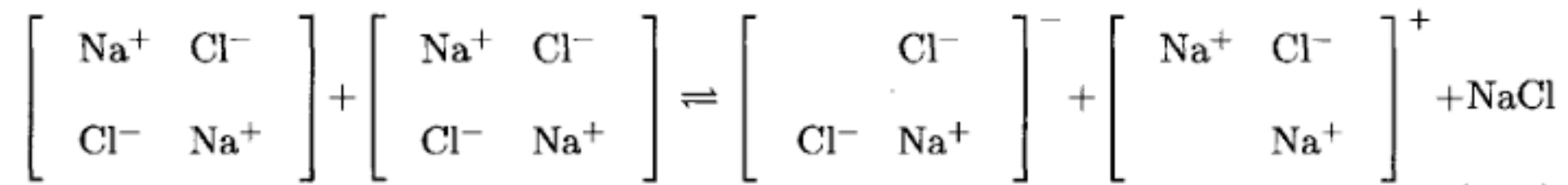
where  $K_F = \exp\left(-\frac{\Delta_F G^0}{RT}\right)$

$$\Rightarrow [Ag_i^\bullet] = [V'_{Ag}] = N\sqrt{\alpha \times K_F} = \exp\left(\frac{\Delta S_F^0}{2R}\right) \exp\left(-\frac{\Delta H_F^0}{2RT}\right)$$

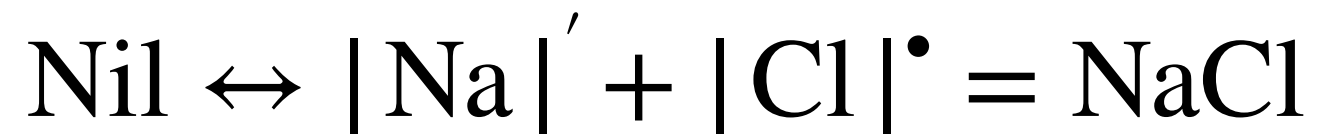
$$\Delta S_F^0 \approx 9.4R$$

$$\Delta H_F^0 \approx 140 \text{ kJ.mol}^{-1}$$

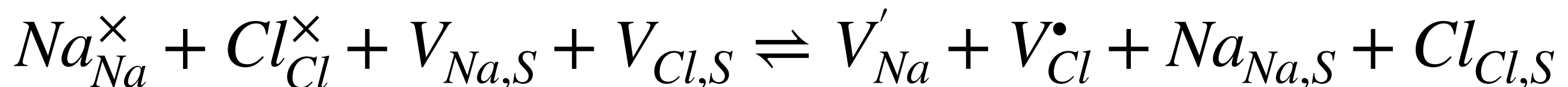
# Schottky defect - NaCl



Building Element Notation :



Kroger-Vink Notation :

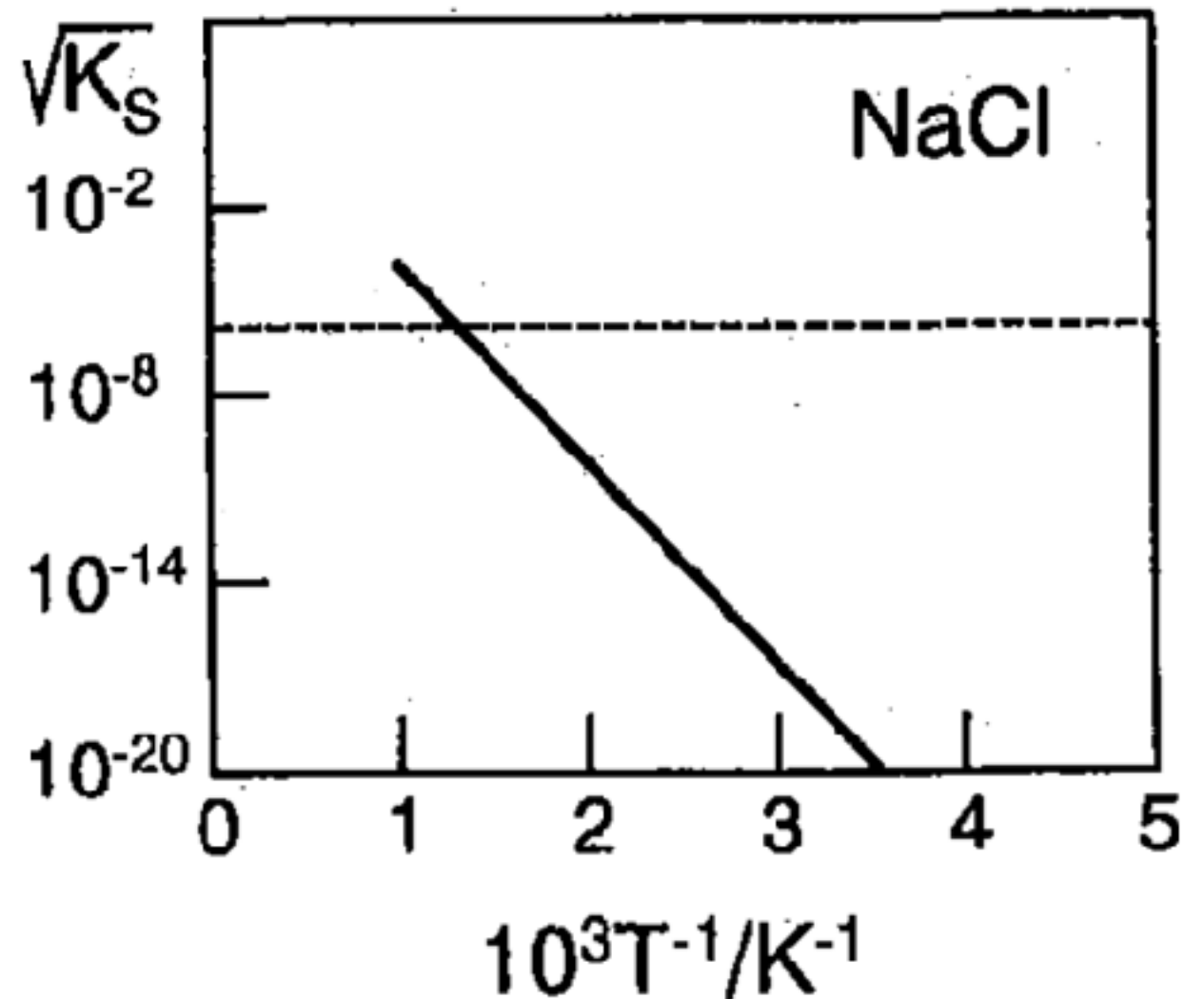
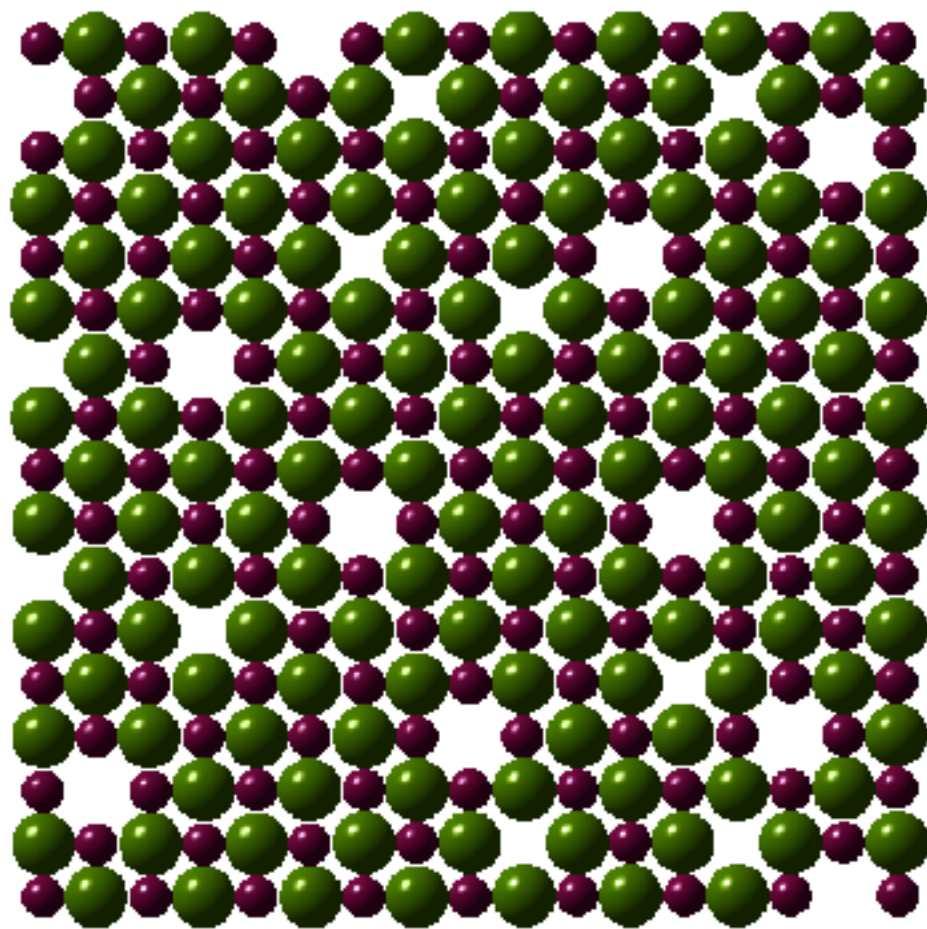


# Mass Action Law - Schottky defect

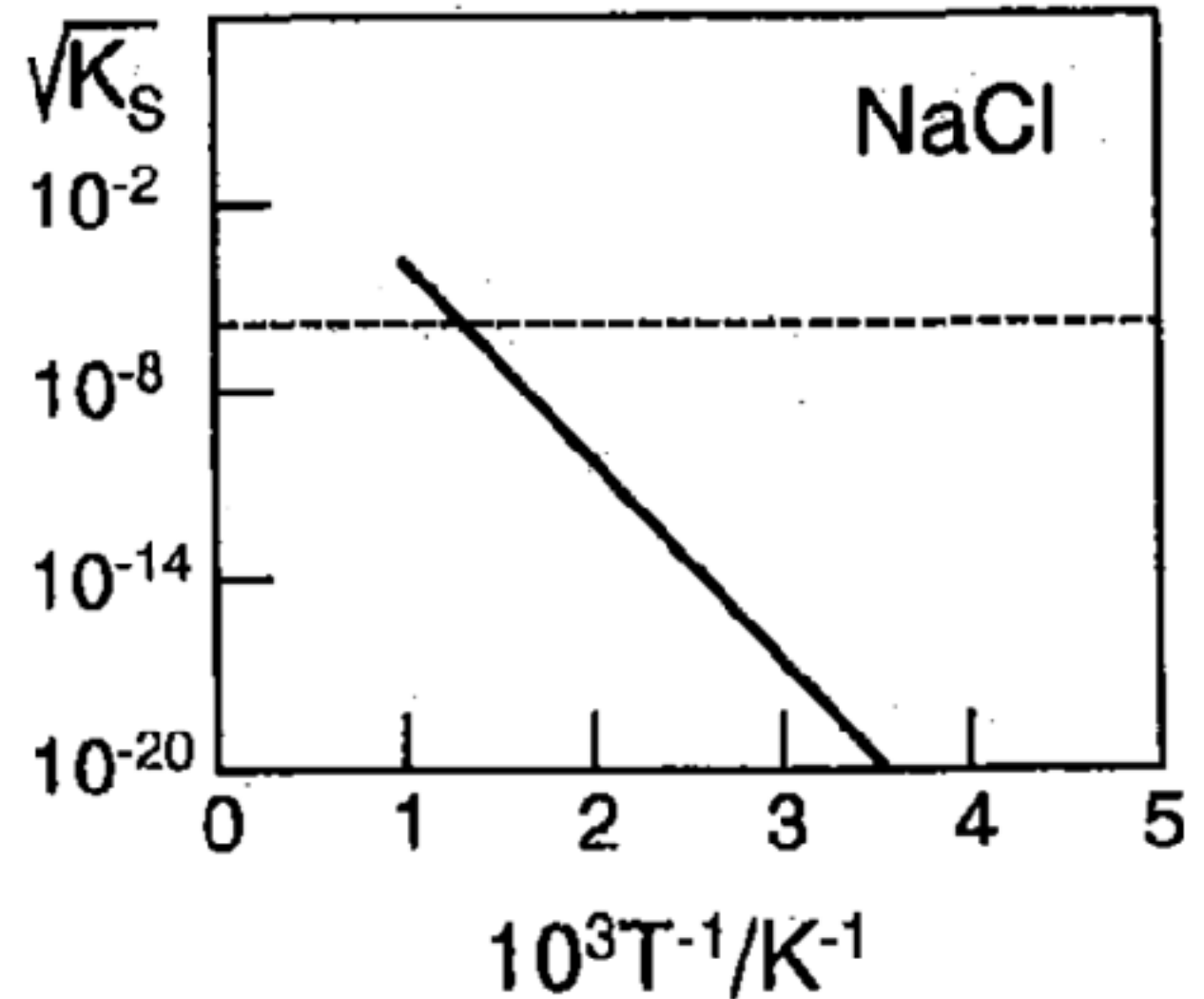
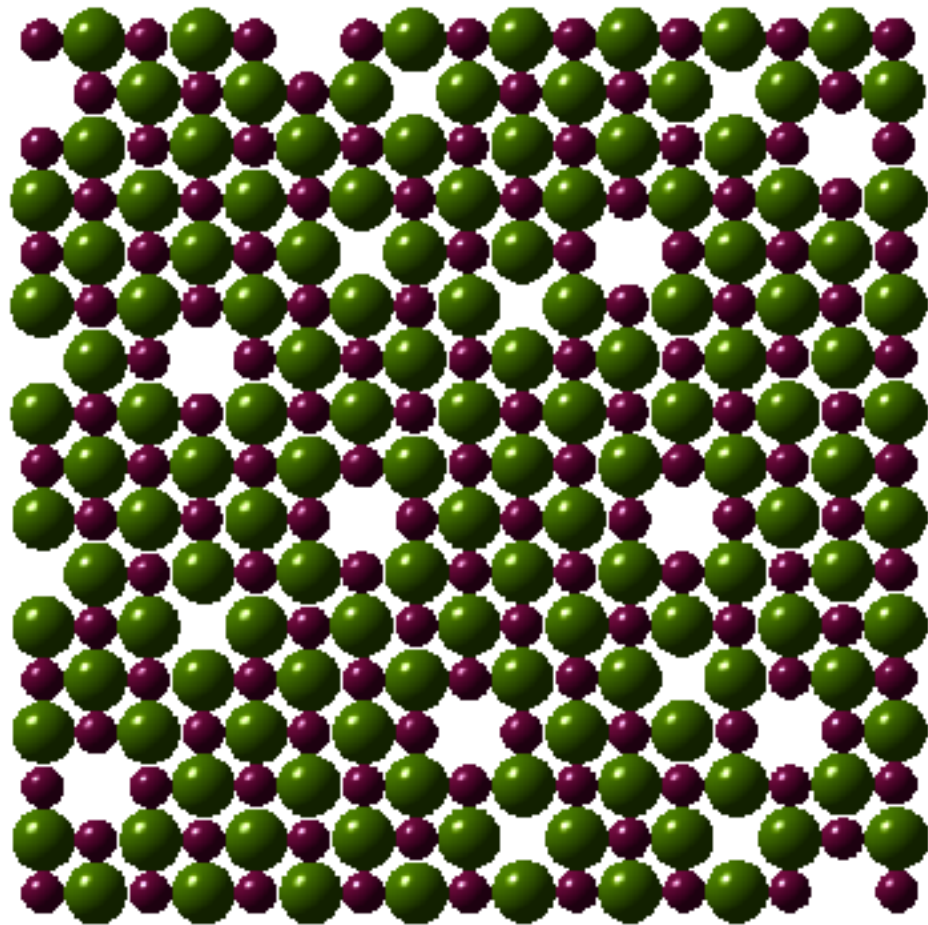
Schottky reaction:



electroneutrality:  $[V^{\bullet}_{Cl}] = [V'_{Na}] = \sqrt{K_s(T)} \times N$

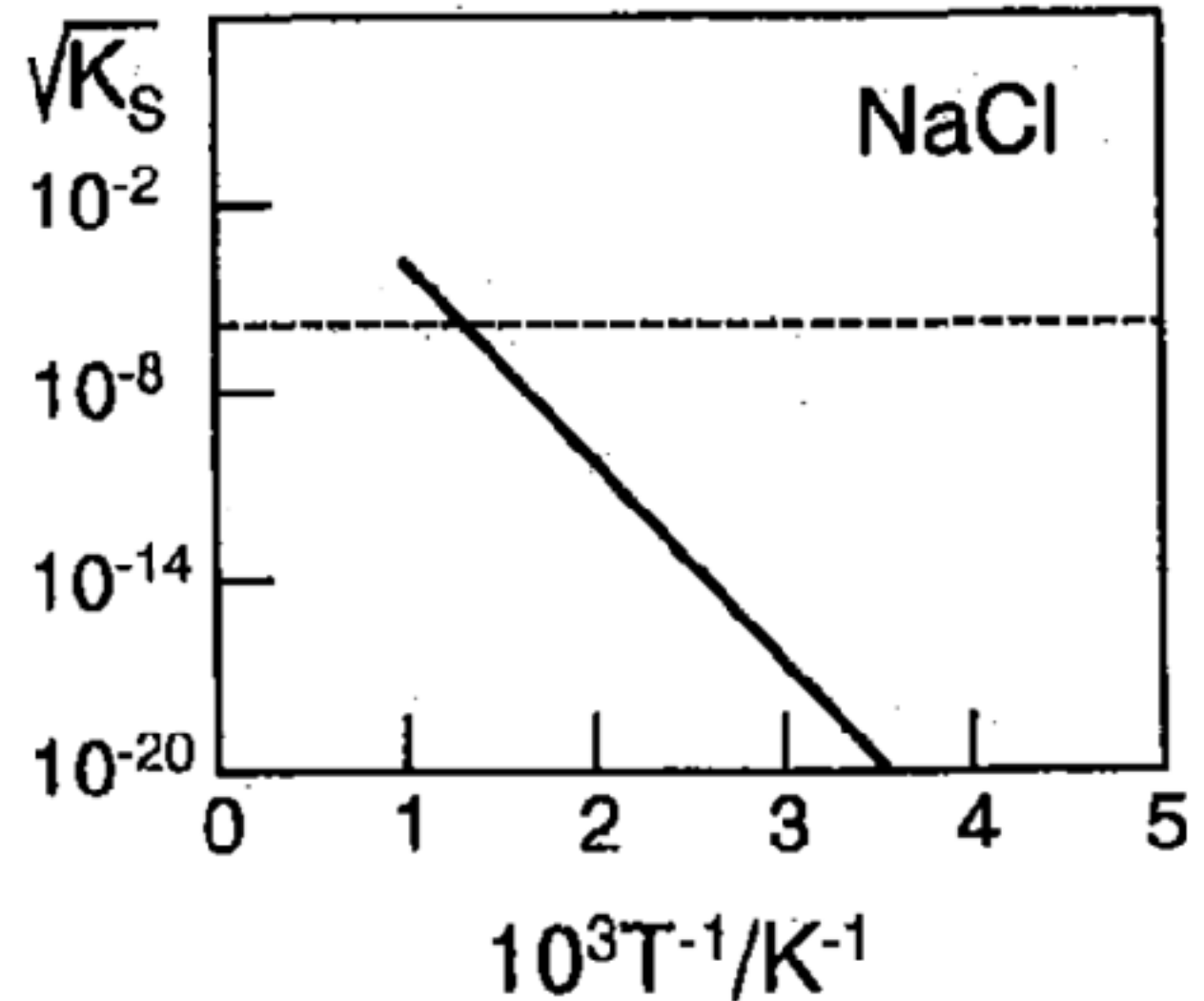
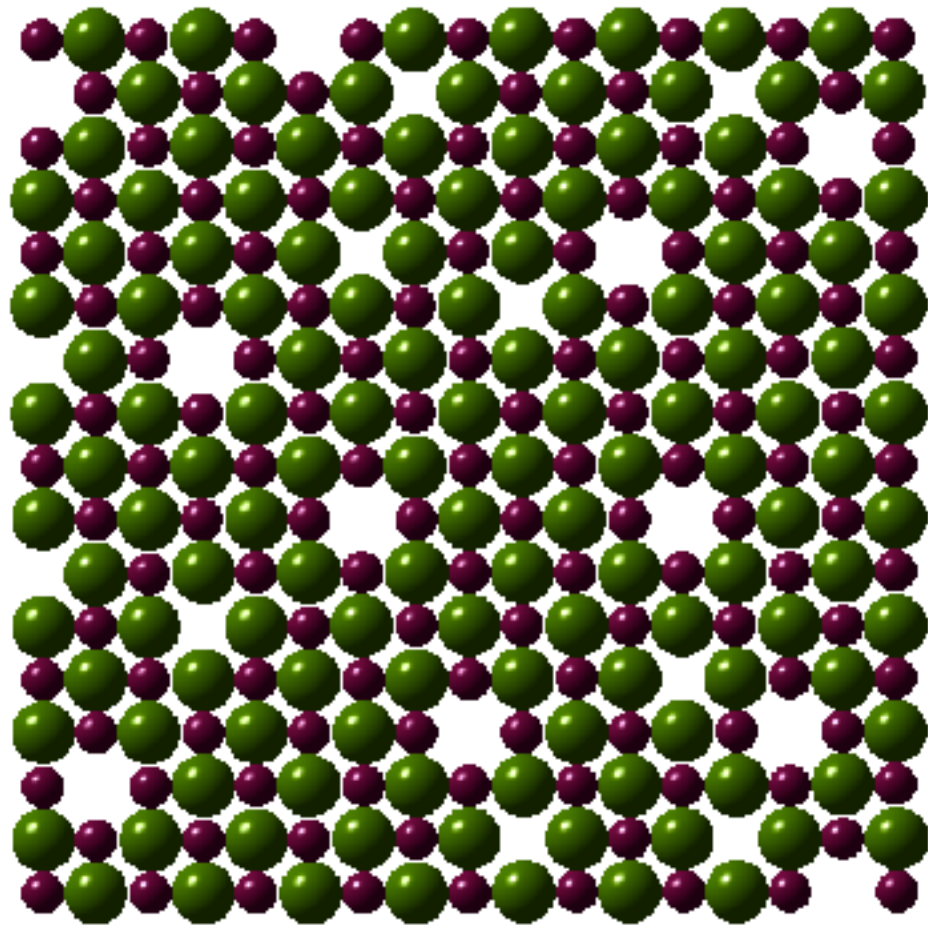


# Energetics - Schottky defect





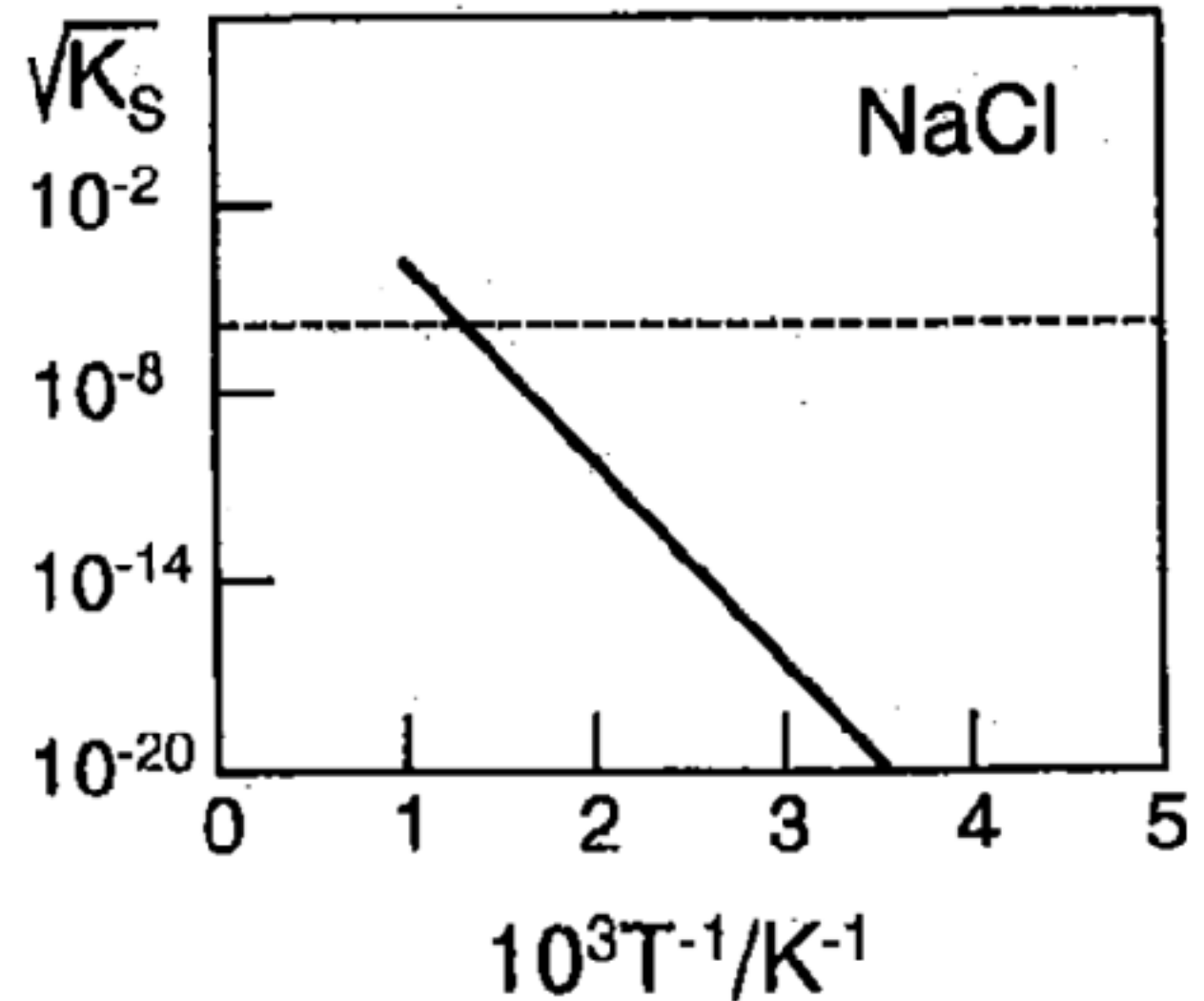
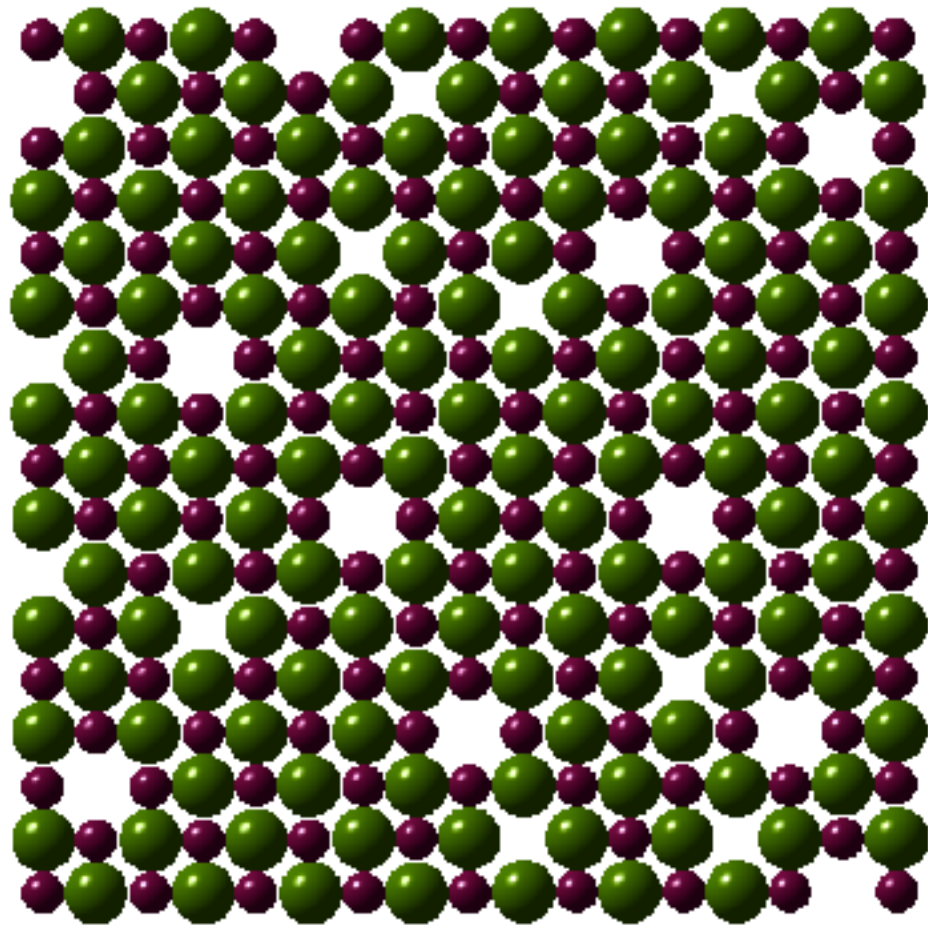
# Energetics - Schottky defect



$$\Rightarrow [V_{Cl}^{\bullet}] = [V'_{Na}] = N\sqrt{K_S} = \exp\left(\frac{\Delta S_S^0}{2R}\right) \exp\left(-\frac{\Delta H_S^0}{2RT}\right)$$



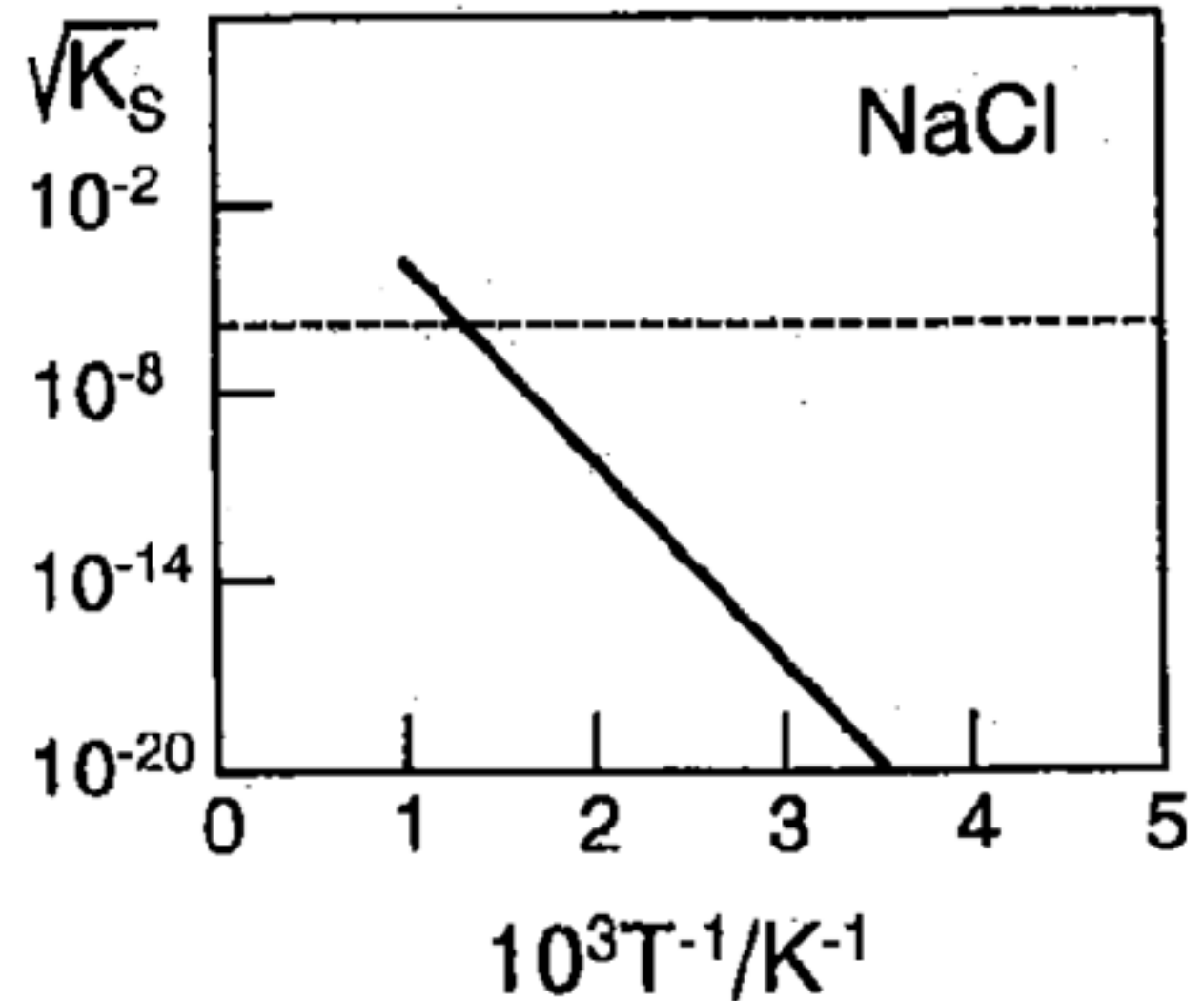
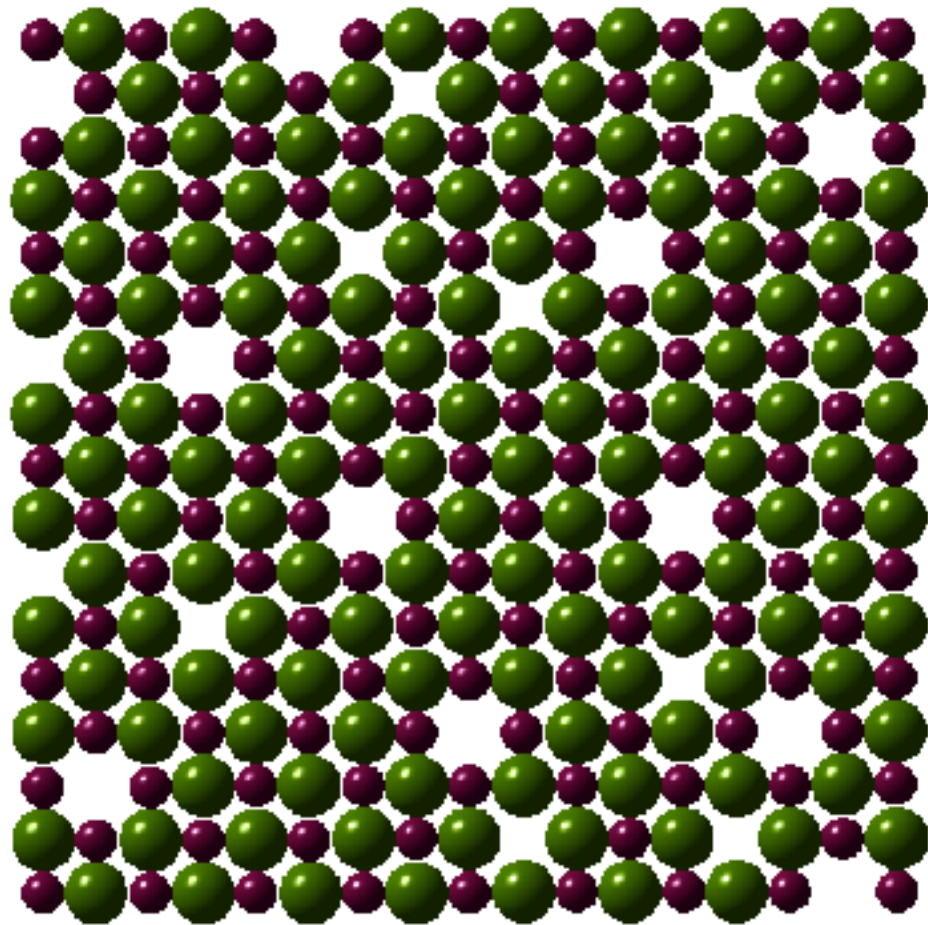
# Energetics - Schottky defect



$$\Rightarrow [V_{Cl}^{\bullet}] = [V'_{Na}] = N\sqrt{K_S} = \exp\left(\frac{\Delta S_S^0}{2R}\right) \exp\left(-\frac{\Delta H_S^0}{2RT}\right)$$

$$\Delta S_S^0 \approx 9.8R$$

# Energetics - Schottky defect

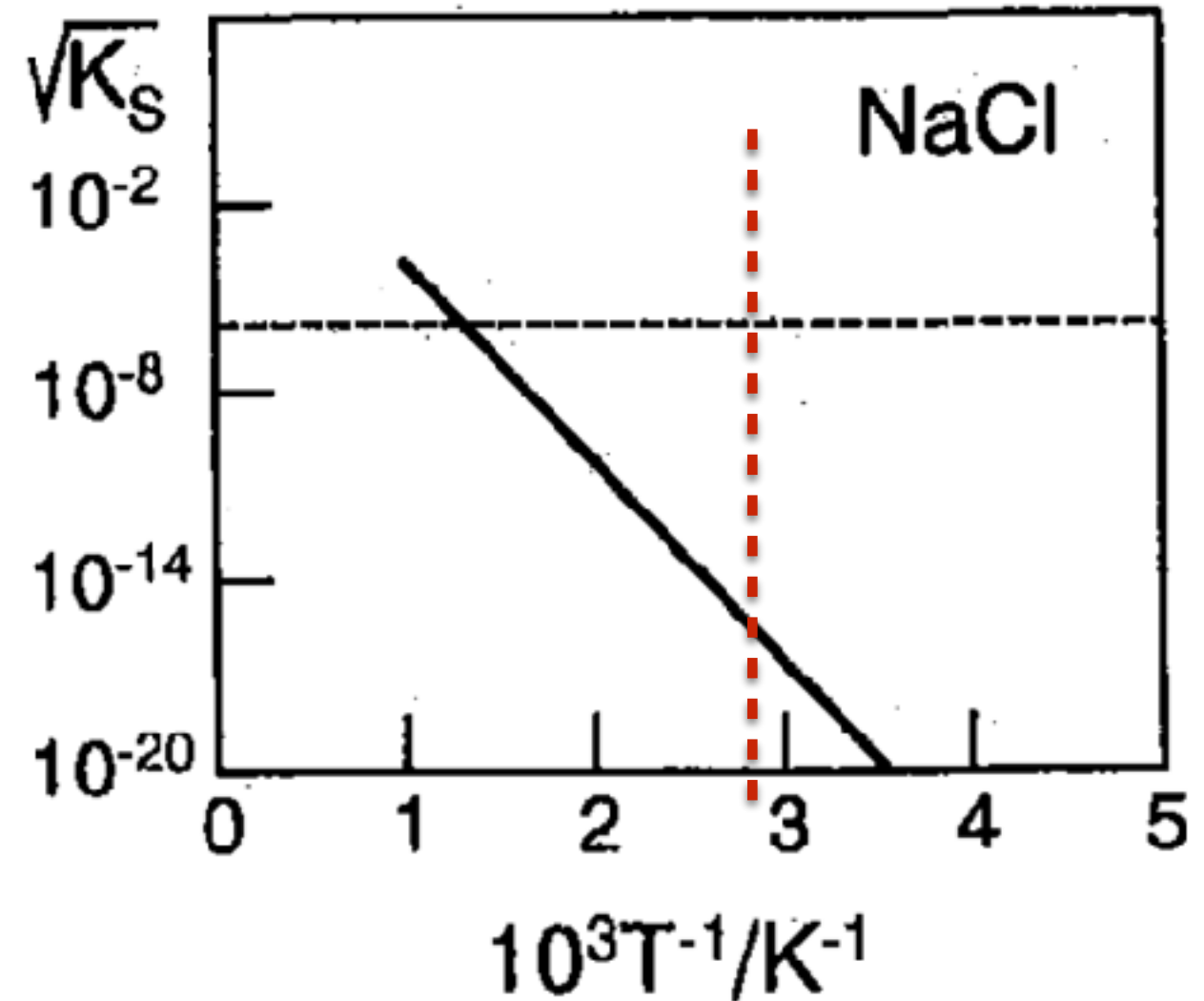
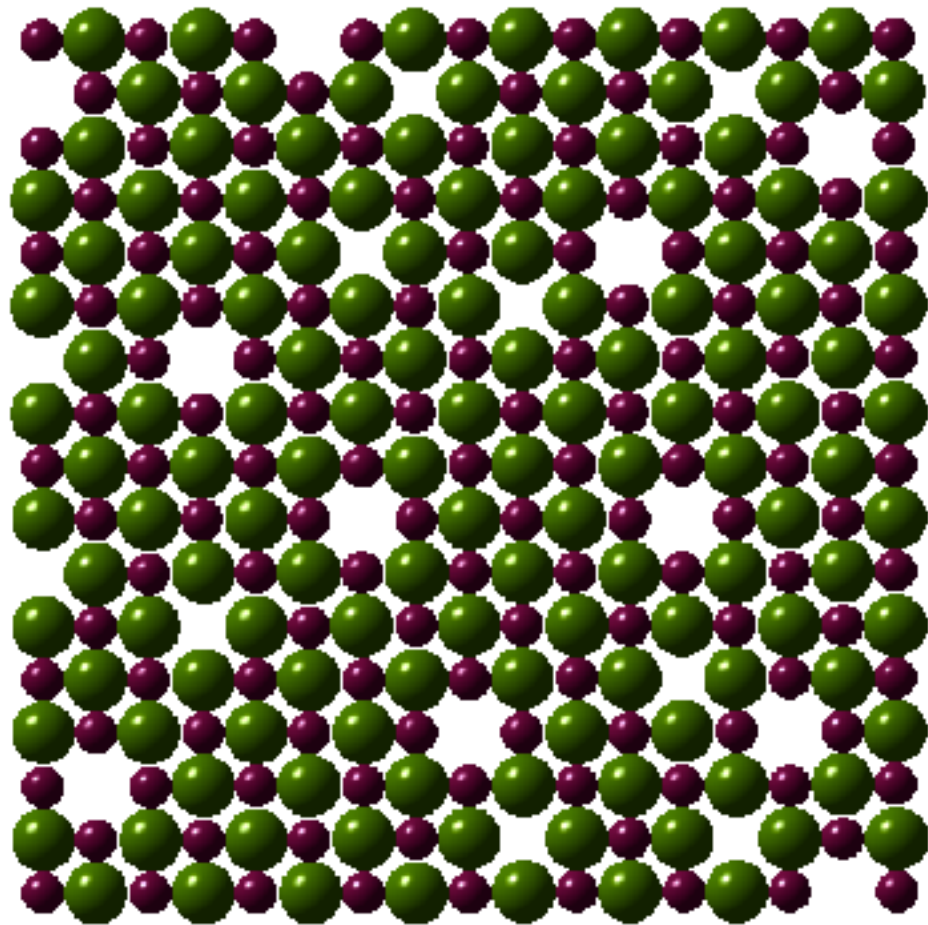


$$\Rightarrow [V_{Cl}^{\bullet}] = [V'_{Na}] = N\sqrt{K_S} = \exp\left(\frac{\Delta S_S^0}{2R}\right) \exp\left(-\frac{\Delta H_S^0}{2RT}\right)$$

$$\Delta S_S^0 \approx 9.8R$$

$$\Delta H_S^0 \approx 240 \text{ kJ.mol}^{-1}$$

# Energetics - Schottky defect

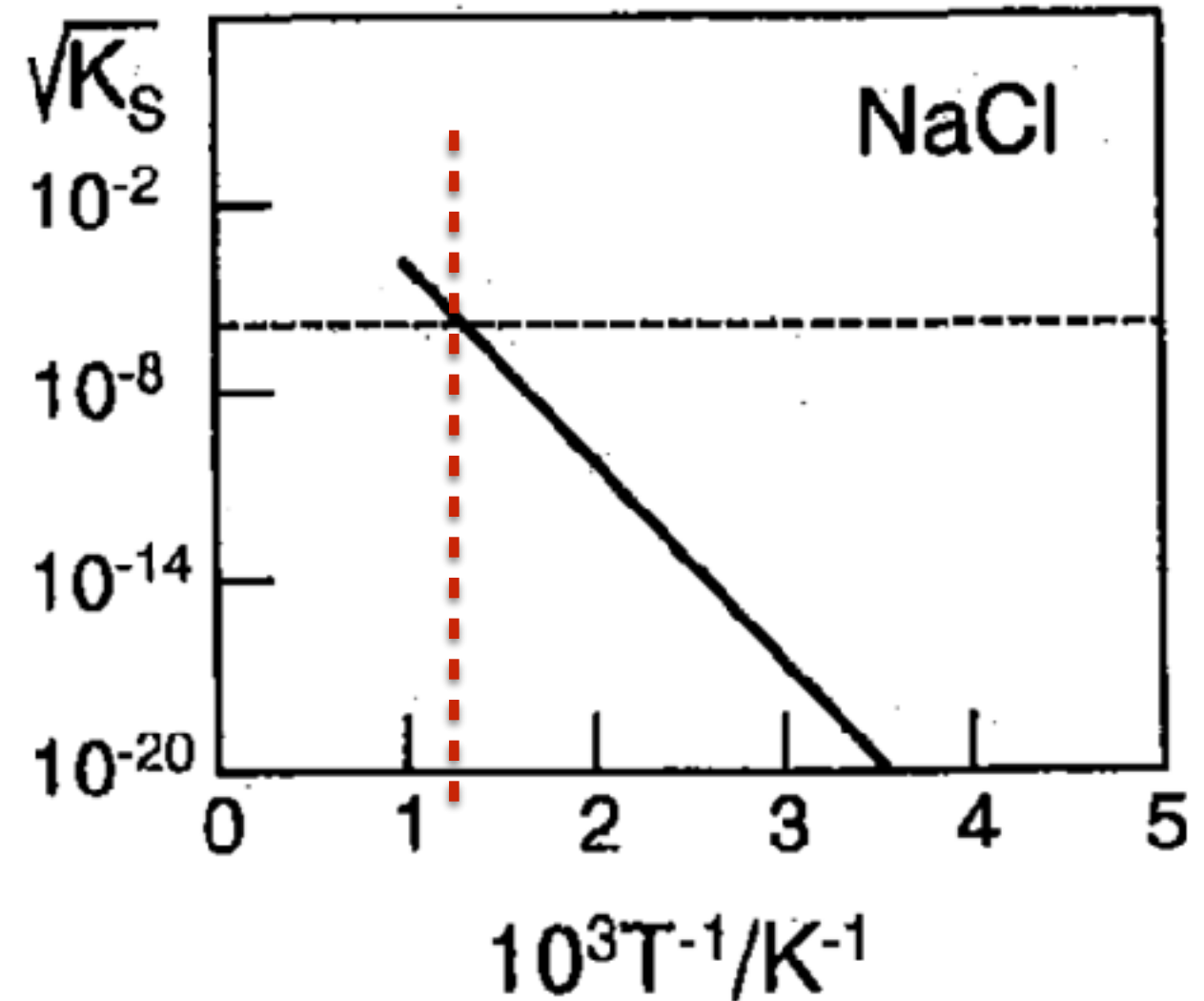
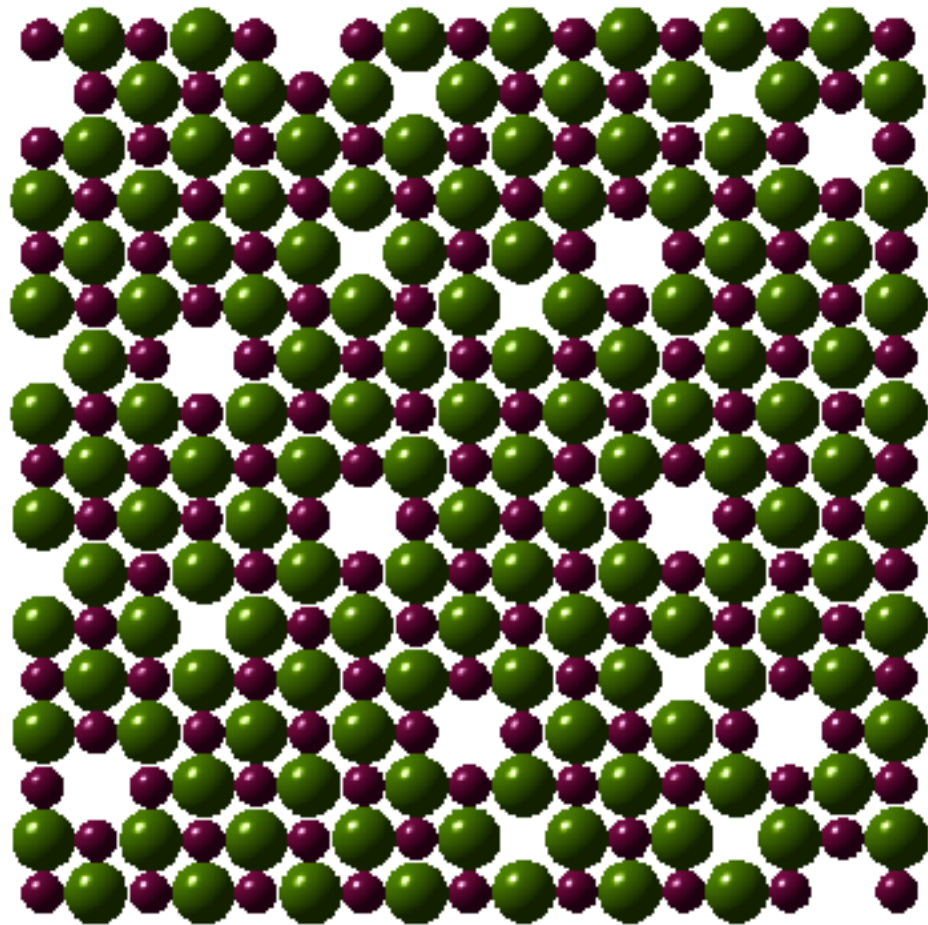


$$\Rightarrow [V_{Cl}^{\bullet}] = [V'_{Na}] = N\sqrt{K_S} = \exp\left(\frac{\Delta S_S^0}{2R}\right) \exp\left(-\frac{\Delta H_S^0}{2RT}\right)$$

$$\Delta S_S^0 \approx 9.8R$$

$$\Delta H_S^0 \approx 240 \text{ kJ.mol}^{-1}$$

# Energetics - Schottky defect



$$\Rightarrow [V_{Cl}^{\bullet}] = [V'_{Na}] = N\sqrt{K_S} = \exp\left(\frac{\Delta S_S^0}{2R}\right) \exp\left(-\frac{\Delta H_S^0}{2RT}\right)$$

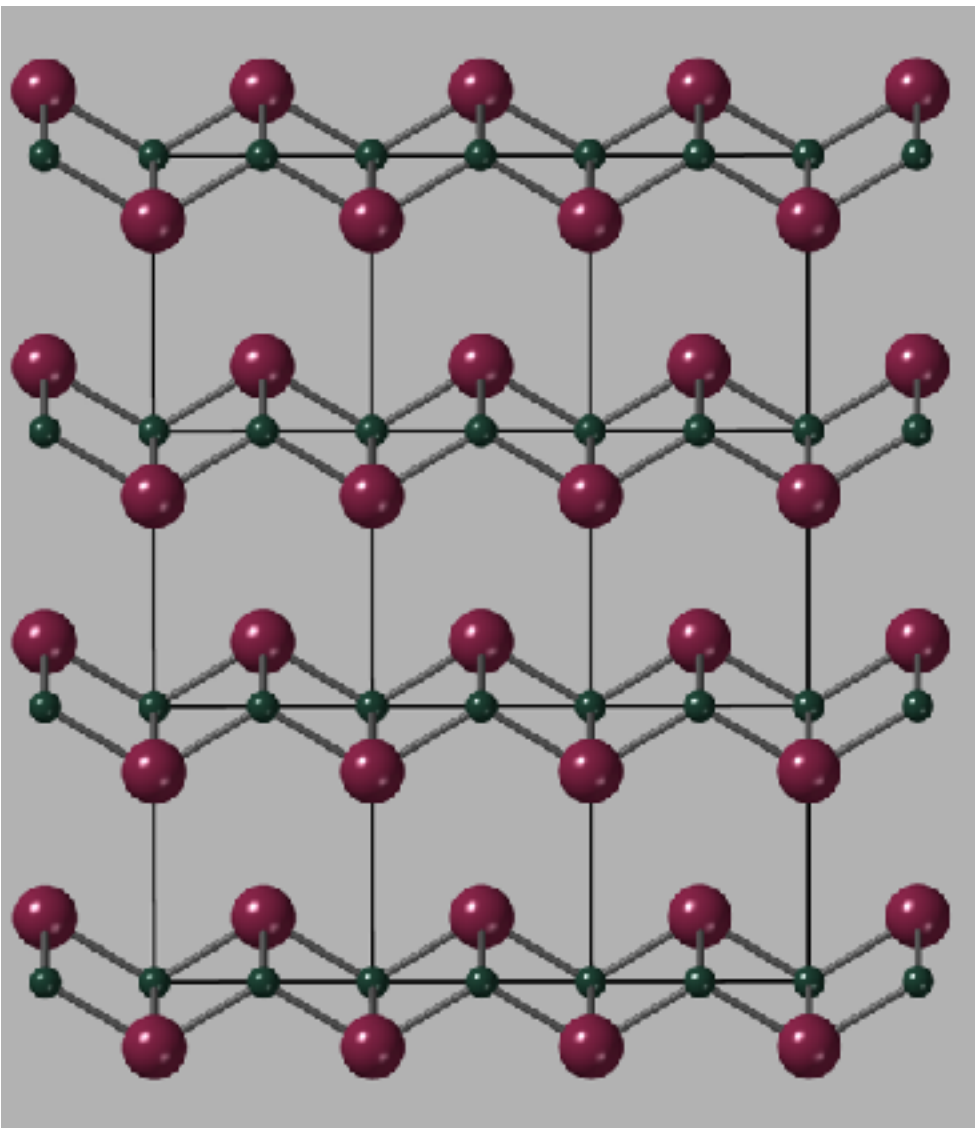
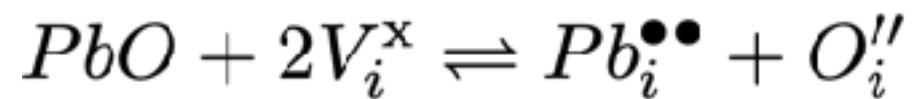
$$\Delta S_S^0 \approx 9.8R$$

$$\Delta H_S^0 \approx 240 \text{ kJ.mol}^{-1}$$

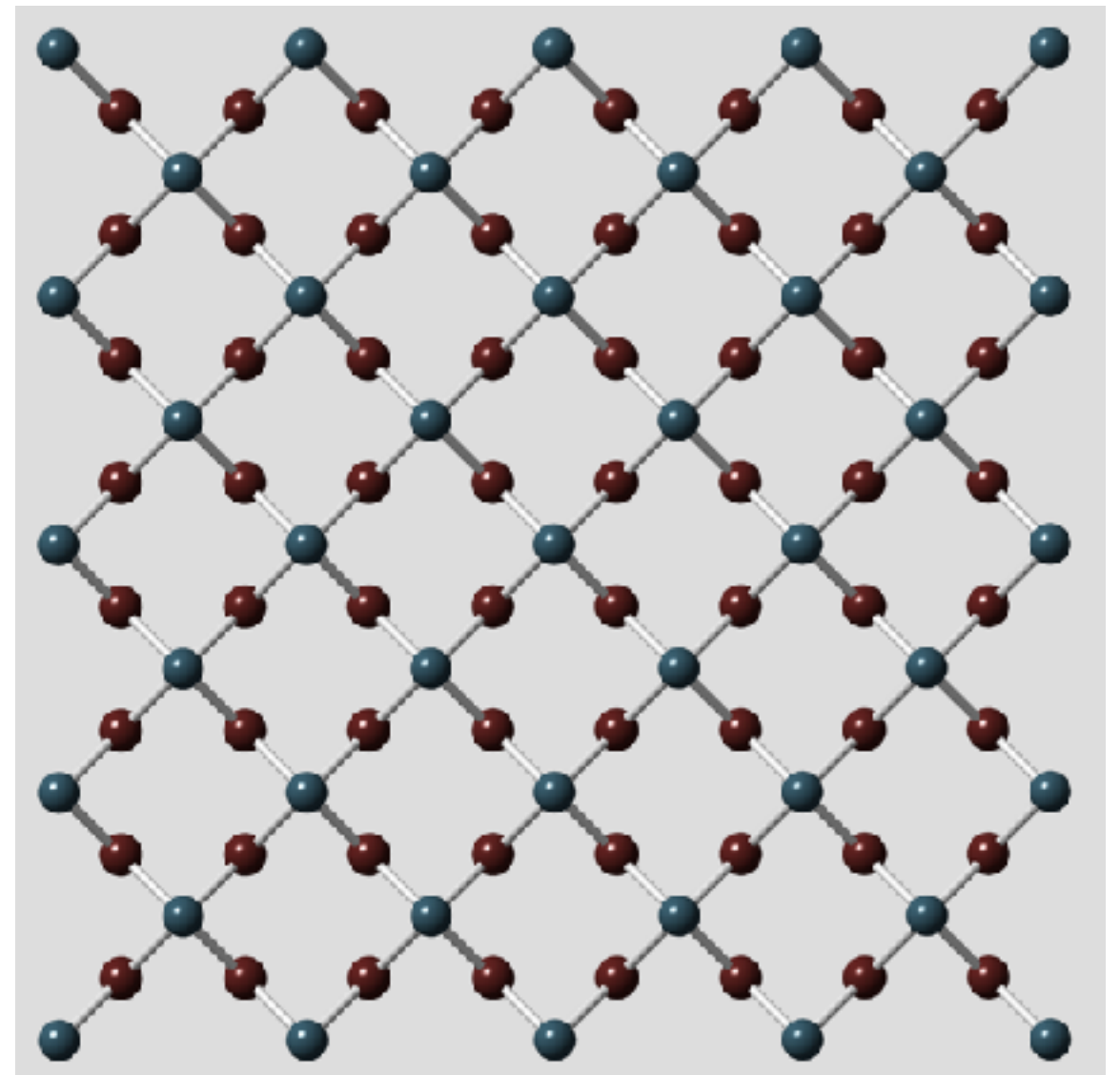
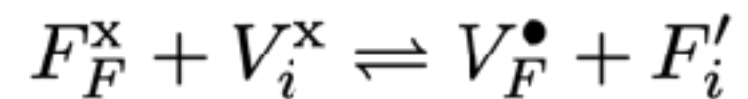


# Other stoichiometric internal reactions

## Anti-Schottky



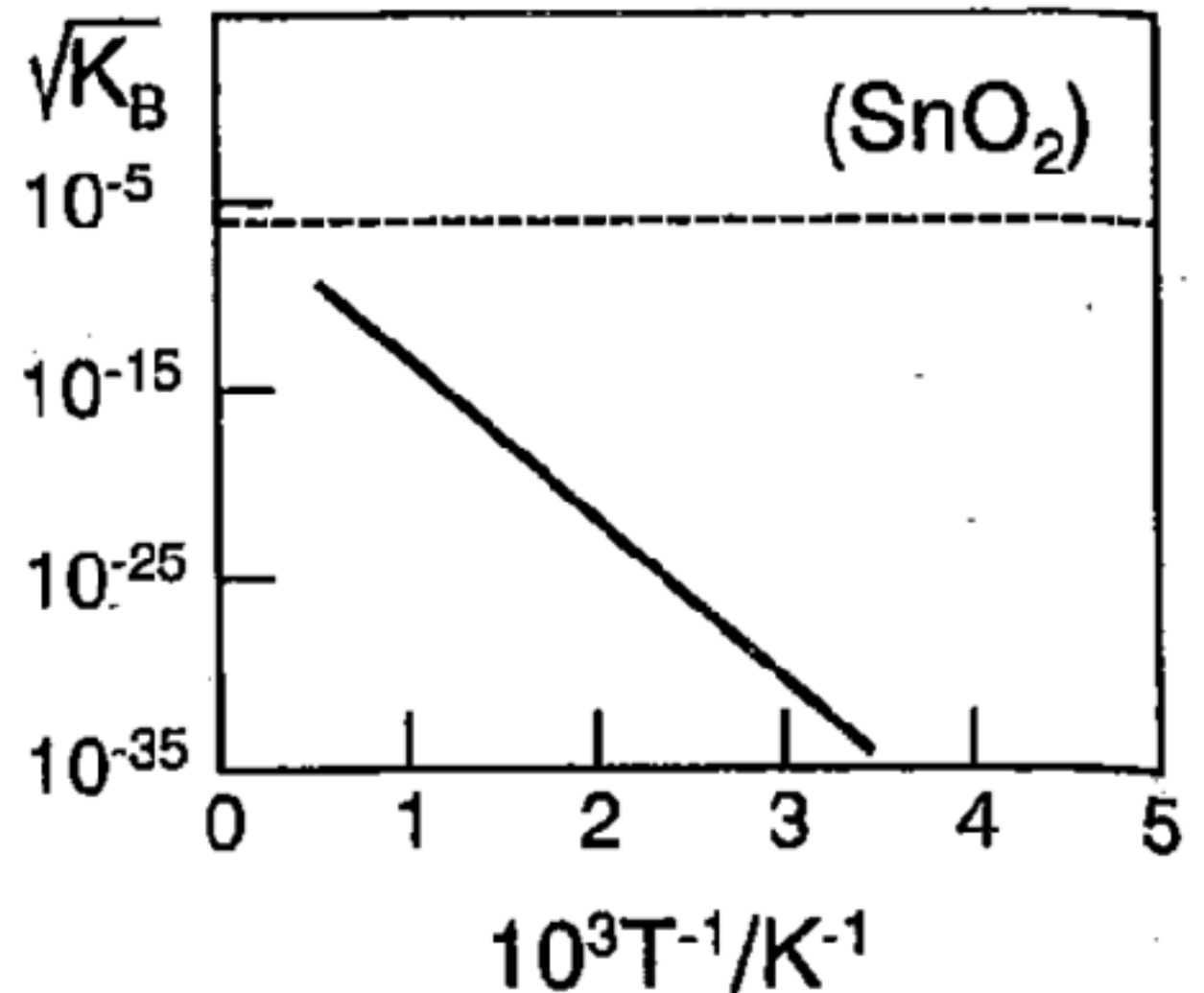
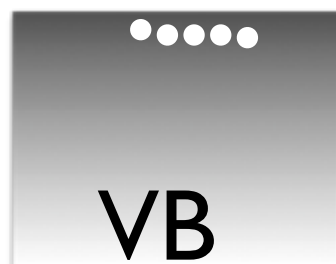
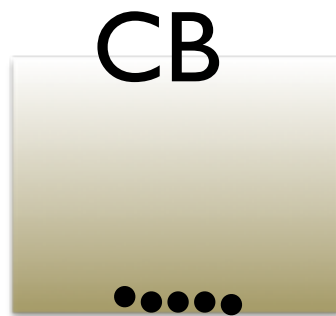
## Anion Frenkel



# Electronic defects

Band-to-band:  $e_{\text{VB}}^{\times} + h_{\text{CB}}^{\times} \rightleftharpoons h_{\text{VB}}^{\bullet} + e_{\text{CB}}'$

electroneutrality:  $[e'] = [h^{\bullet}] = \sqrt{K_B(T)} \times N_c N_v$





# Internal Defect Reactions - MX

**Defect creation processes occurring due to non-zero T without involvement of neighboring phases**

Example Materials	Defect Rxn	Kroger-Vink Notation
AgCl	Frenkel (F)	$Ag_{Ag}^x + V_i^x \rightleftharpoons Ag_i^\bullet + V'_{Ag}$
NaCl	Schottky (S)	$Na_{Na}^x + Cl_{Cl}^x \rightleftharpoons V_{Cl}^\bullet + V'_{Na} + NaCl$
CsF	Anion-Frenkel ( $\bar{F}$ )	$F_F^x + V_i^x \rightleftharpoons V_F^\bullet + F'_i$
PbO	Anti-Schottky ( $\bar{S}$ )	$PbO + 2V_i^x \rightleftharpoons Pb_i^{\bullet\bullet} + O_i^{''}$
All	Band-Band (B)	$Nil \rightleftharpoons h^\bullet + e'$

# Internal Defect Reactions - MX

**Defect creation processes occurring due to non-zero T without involvement of neighboring phases**

Example Materials	Defect Rxn	Kroger-Vink Notation
AgCl	Frenkel (F)	$Ag_{Ag}^x + V_i^x \rightleftharpoons Ag_i^\bullet + V'_{Ag}$
NaCl	Schottky (S)	$Na_{Na}^x + Cl_{Cl}^x \rightleftharpoons V_{Cl}^\bullet + V'_{Na} + NaCl$
CsF	Anion-Frenkel ( $\bar{F}$ )	$F_F^x + V_i^x \rightleftharpoons V_F^\bullet + F'_i$
PbO	Anti-Schottky ( $\bar{S}$ )	$PbO + 2V_i^x \rightleftharpoons Pb_i^{\bullet\bullet} + O_i^{''}$
All	Band-Band (B)	$Nil \rightleftharpoons h^\bullet + e'$

Acid-base

Redox

# Extrinsic defect incorporation

# Extrinsic defect incorporation

Doping

Alloying

# Extrinsic defect incorporation

```
graph TD; A[Extrinsic defect incorporation] --> B[Doping]; A --> C[Alloying]; A --> D[Interstitial]; B --> D; C --> D;
```

Doping

Alloying

Interstitial

C in Fe  
O<sub>2</sub> in UO<sub>2</sub>

# Extrinsic defect incorporation

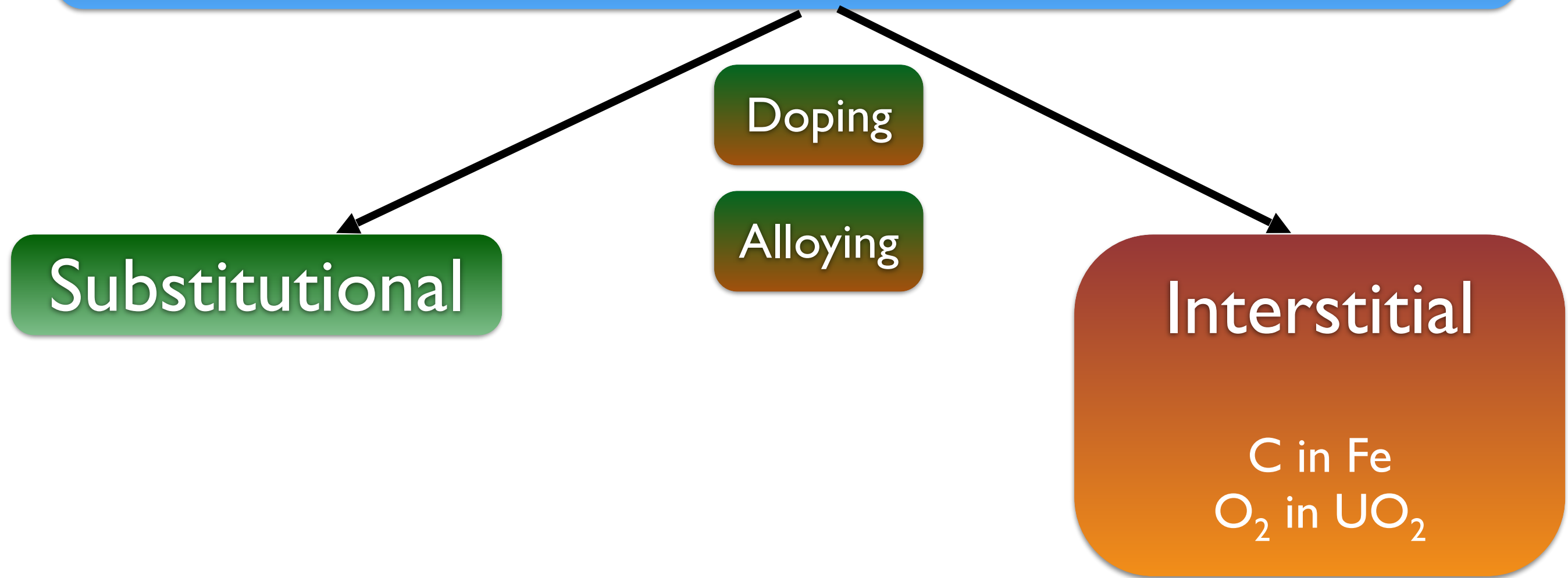
Substitutional

Doping

Alloying

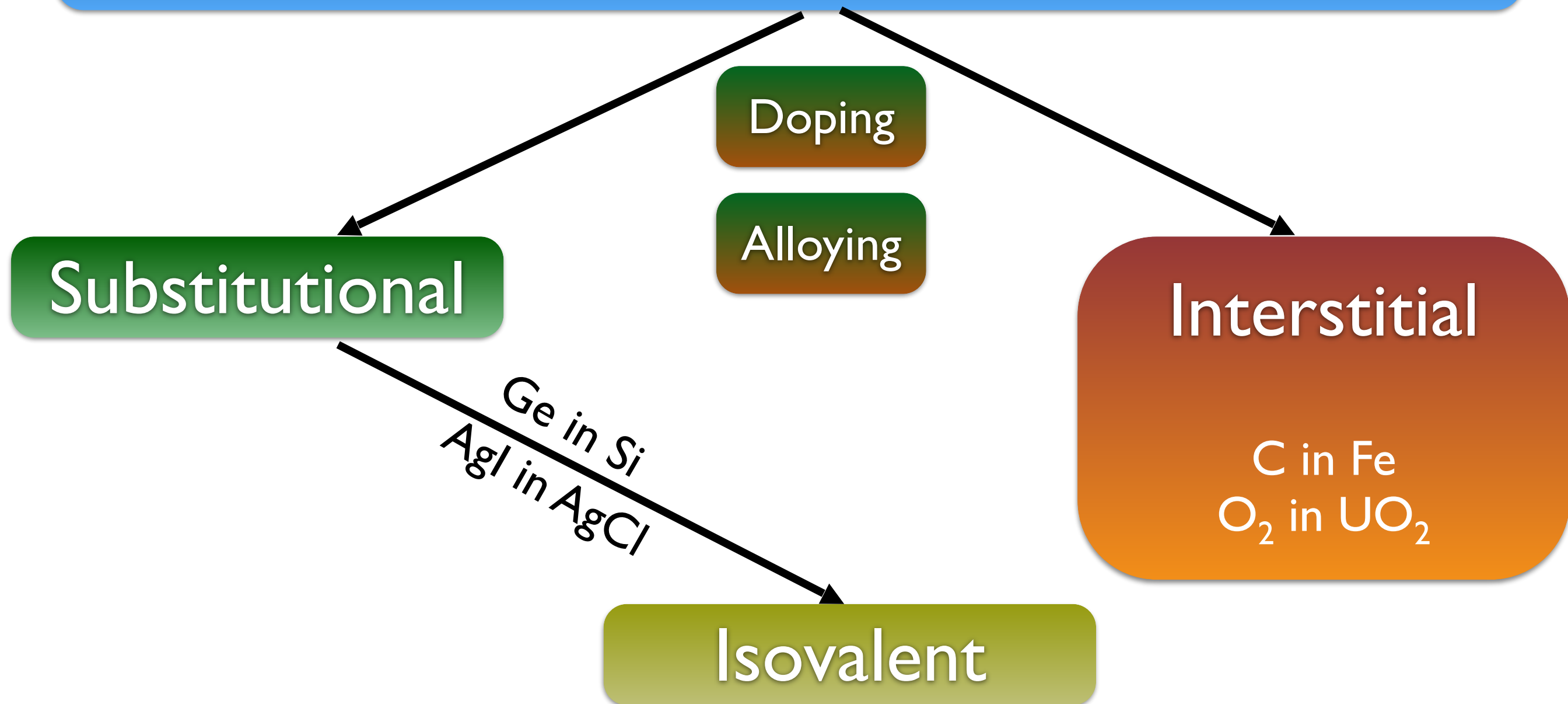
Interstitial

C in Fe  
O<sub>2</sub> in UO<sub>2</sub>





# Extrinsic defect incorporation



# Extrinsic defect incorporation

Doping

Alloying

Substitutional

Interstitial

C in Fe  
O<sub>2</sub> in UO<sub>2</sub>

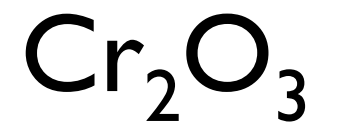
Isovalent

Aliovalent

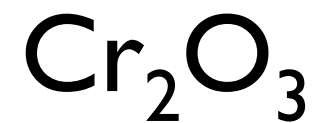
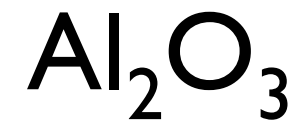
Ge in Si  
AgI in AgCl

P in Si  
CdCl<sub>2</sub> in AgCl

# Example - Isovalent Substitutional

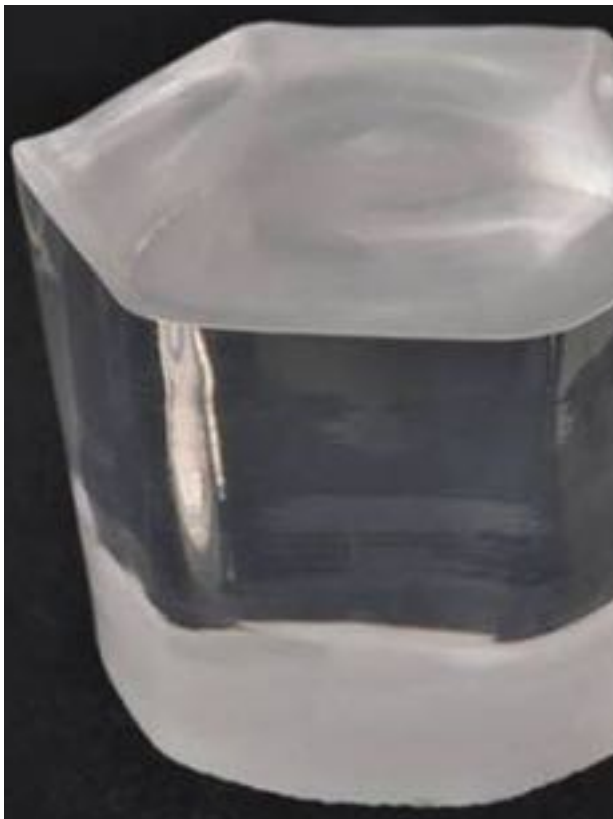
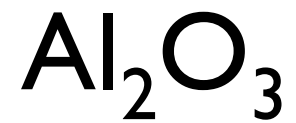


# Example - Isovalent Substitutional

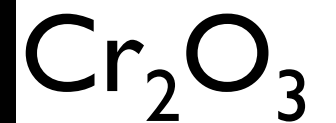


Increasing  $\text{Cr}_2\text{O}_3$  →

# Example - Isovalent Substitutional



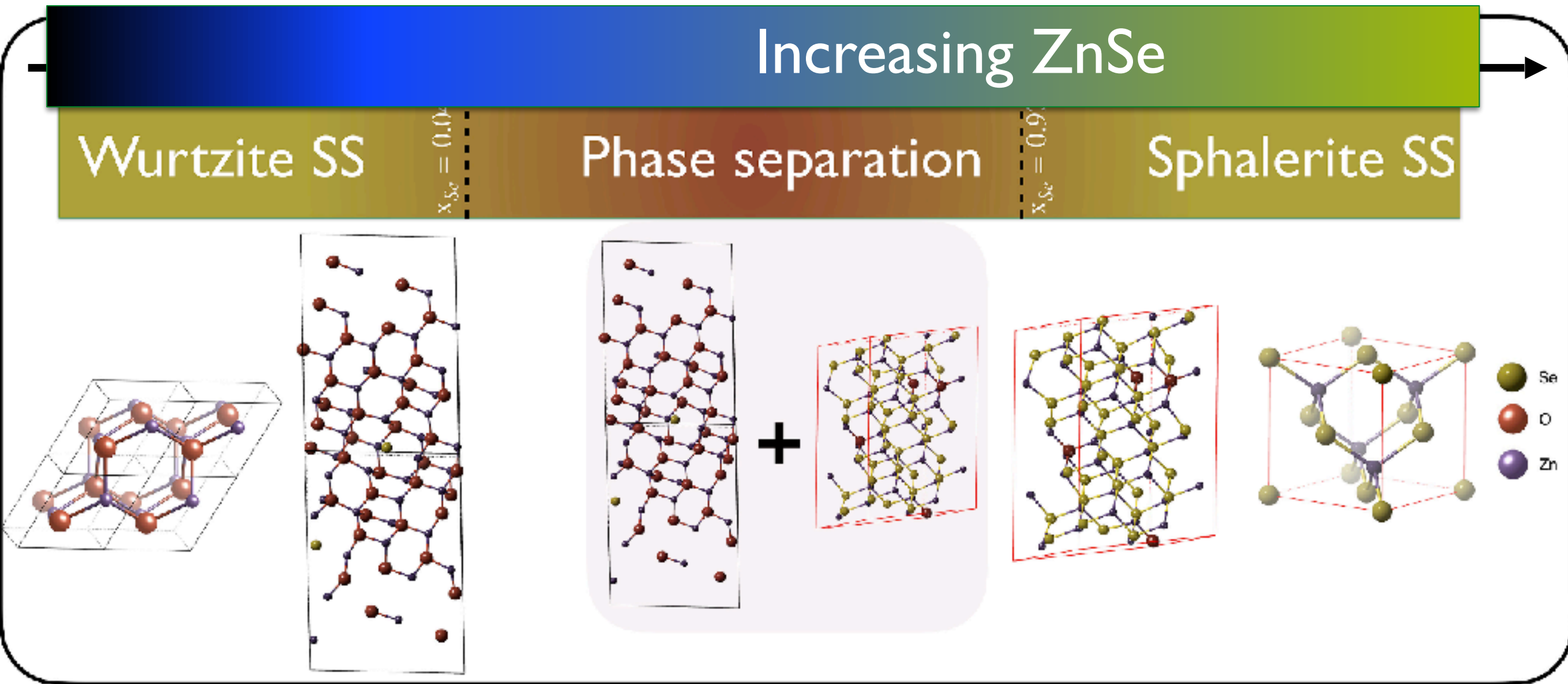
Ruby



Increasing  $\text{Cr}_2\text{O}_3$  →

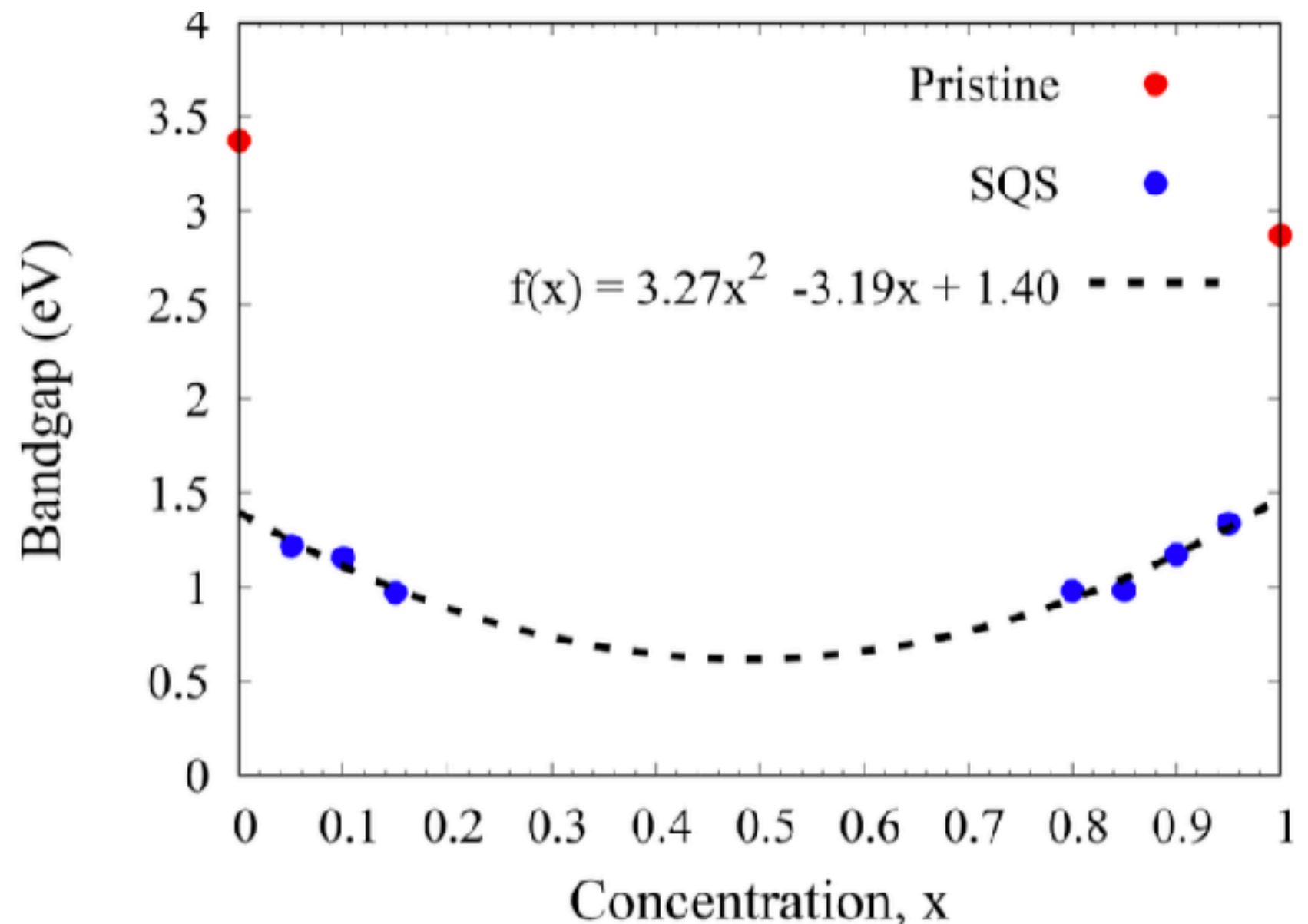
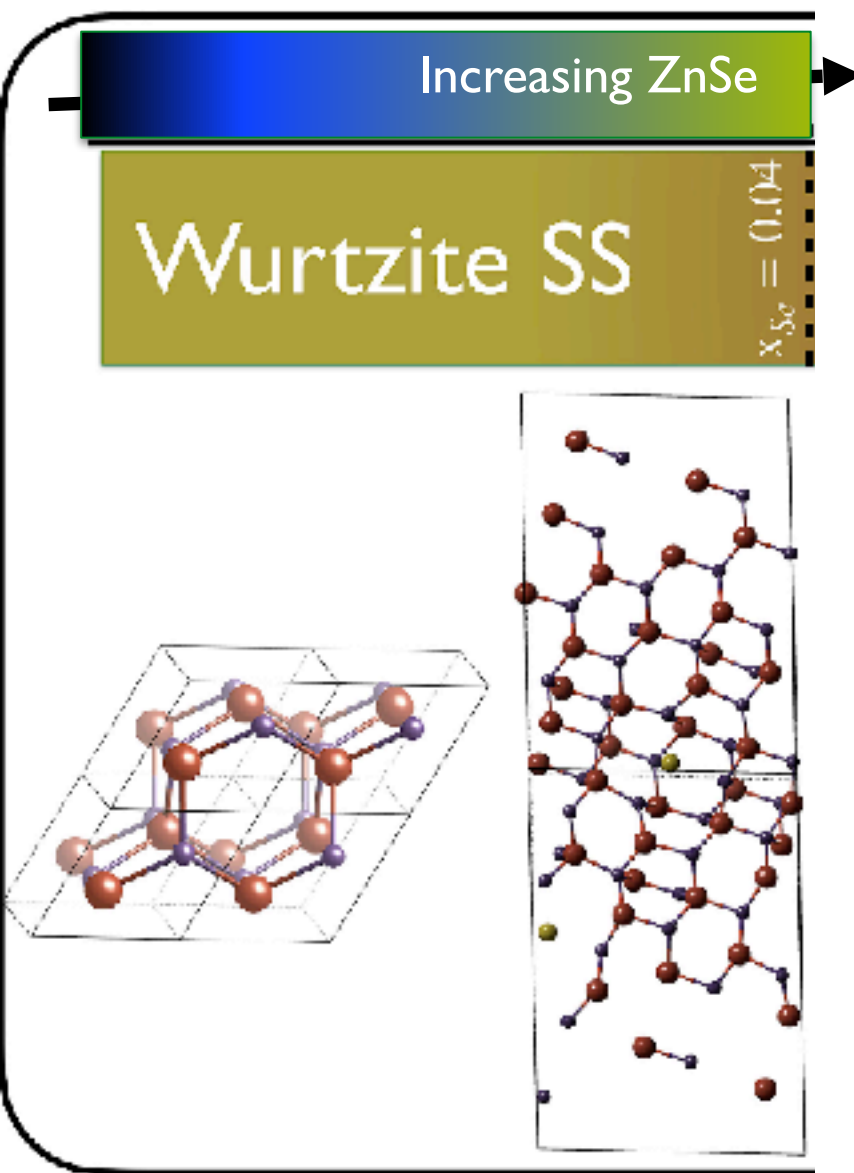


# Example - Isovalent Substitutional





# Example - Isovalent Substitutional



# Aliovalent Incorporation



Atoms with different valence than the site



Electro-neutrality

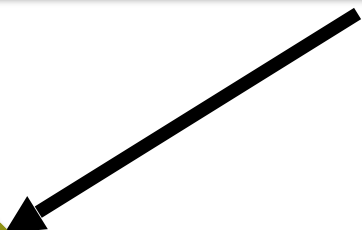
# Aliovalent Incorporation



Atoms with different valence than the site



Electro-neutrality



Ionic  
Compensation

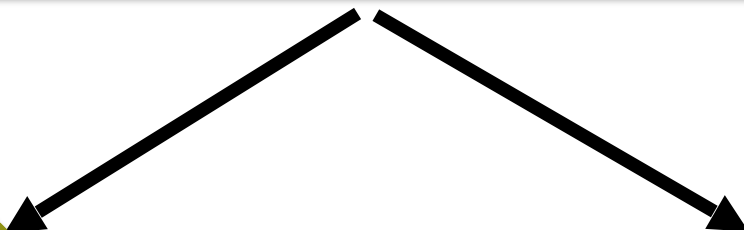
# Aliovalent Incorporation



Atoms with different valence than the site



Electro-neutrality



Ionic  
Compensation

Electronic  
Compensation

# Class Test 3

## (10 marks)

AgCl crystallizes in the cF lattice with a lattice parameter of 0.5622 nm. Cl forms the ccp framework with Ag in the octahedral interstices.

Defect	Formation enthalpy (kJ.mol <sup>-1</sup> )	Formation entropy (kJ.mol <sup>-1</sup> )
Schottky	400	9.8R
Frenkel	140	9.4R

Determine the volume of AgCl at room temperature (  $T = 300\text{ K}$  ) when you will find a single chlorine vacancy in the material.

# Defect Reactions - Rules

- *Site relation:*

- The number of M sites in a compound  $M_aX_b$  must always be in correct proportion to the number of X sites
- Total number of each type of site may change

- *Site creation:*

- Must not affect the site relation described in rule above

- *Mass balance:*

- Mass balance must be maintained as in any chemical reaction

*Note: subscript in the defect symbol indicates the site under consideration and is of no significance for the mass balance*

- *Electroneutrality:*

- The crystal must remain electrically neutral
- Only neutral atoms or molecules are exchanged with other phases outside the crystal under consideration; within the crystal neutral particles can yield two or more oppositely charged defects

- *Surface sites:*

- Atom M displaced from the bulk to surface increases the number of M sites



# Aliovalent Incorporation



Atoms with different valence than the site



Electro-neutrality

# Aliovalent Incorporation



```
graph TD; A[Aliovalent Incorporation] --> B[Atoms with different valence than the site]; B --> C[Electro-neutrality]; C --> D[Ionic Compensation];
```

Atoms with different valence than the site

Electro-neutrality

Ionic  
Compensation

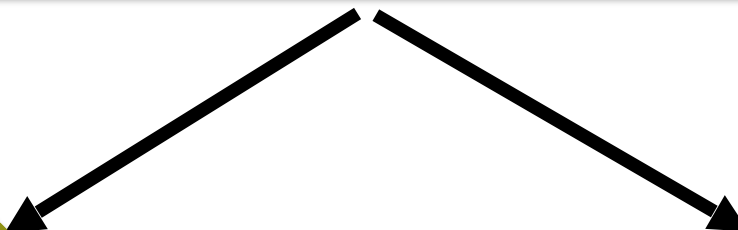
# Aliovalent Incorporation



Atoms with different valence than the site



Electro-neutrality

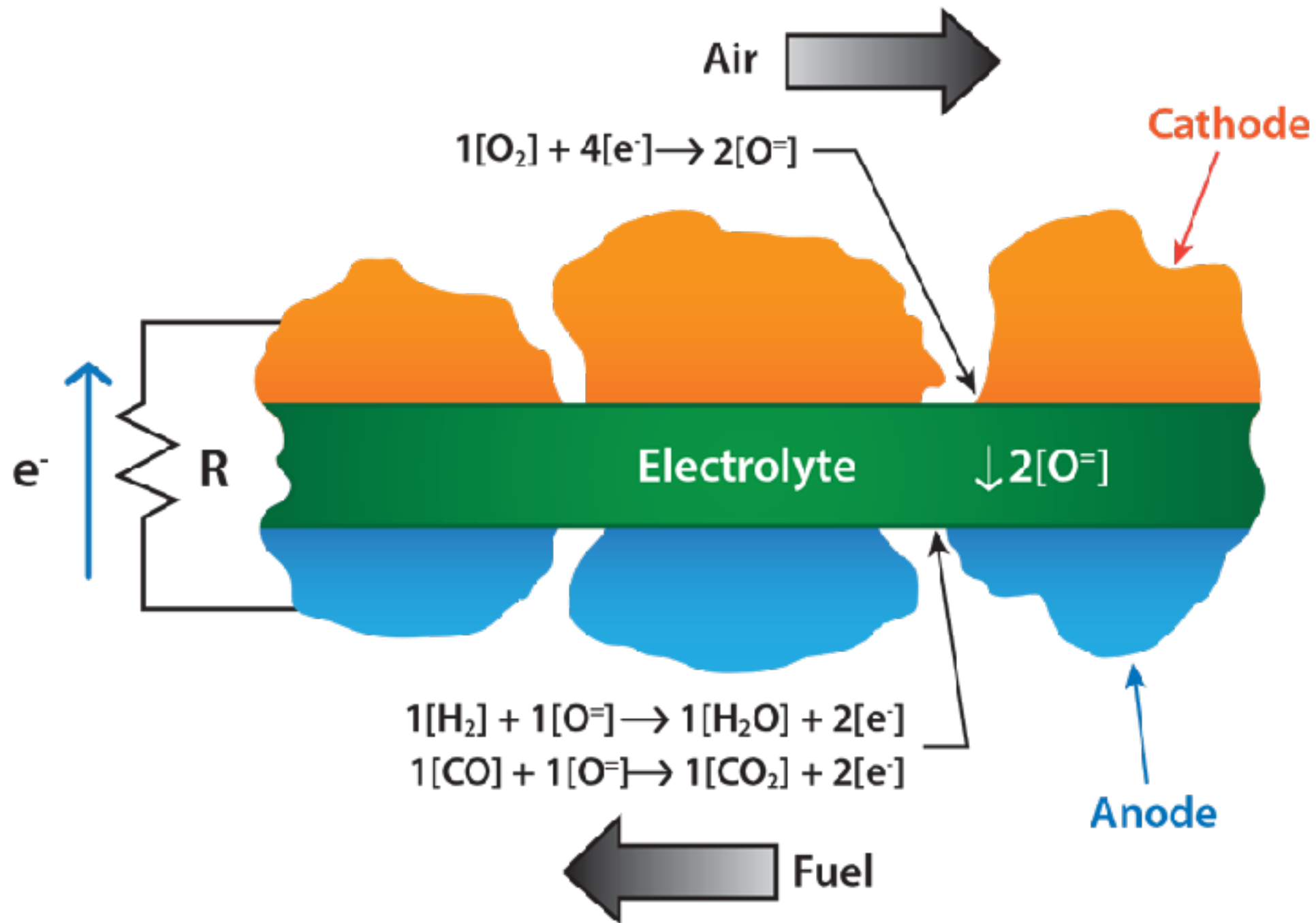


Ionic  
Compensation

Electronic  
Compensation

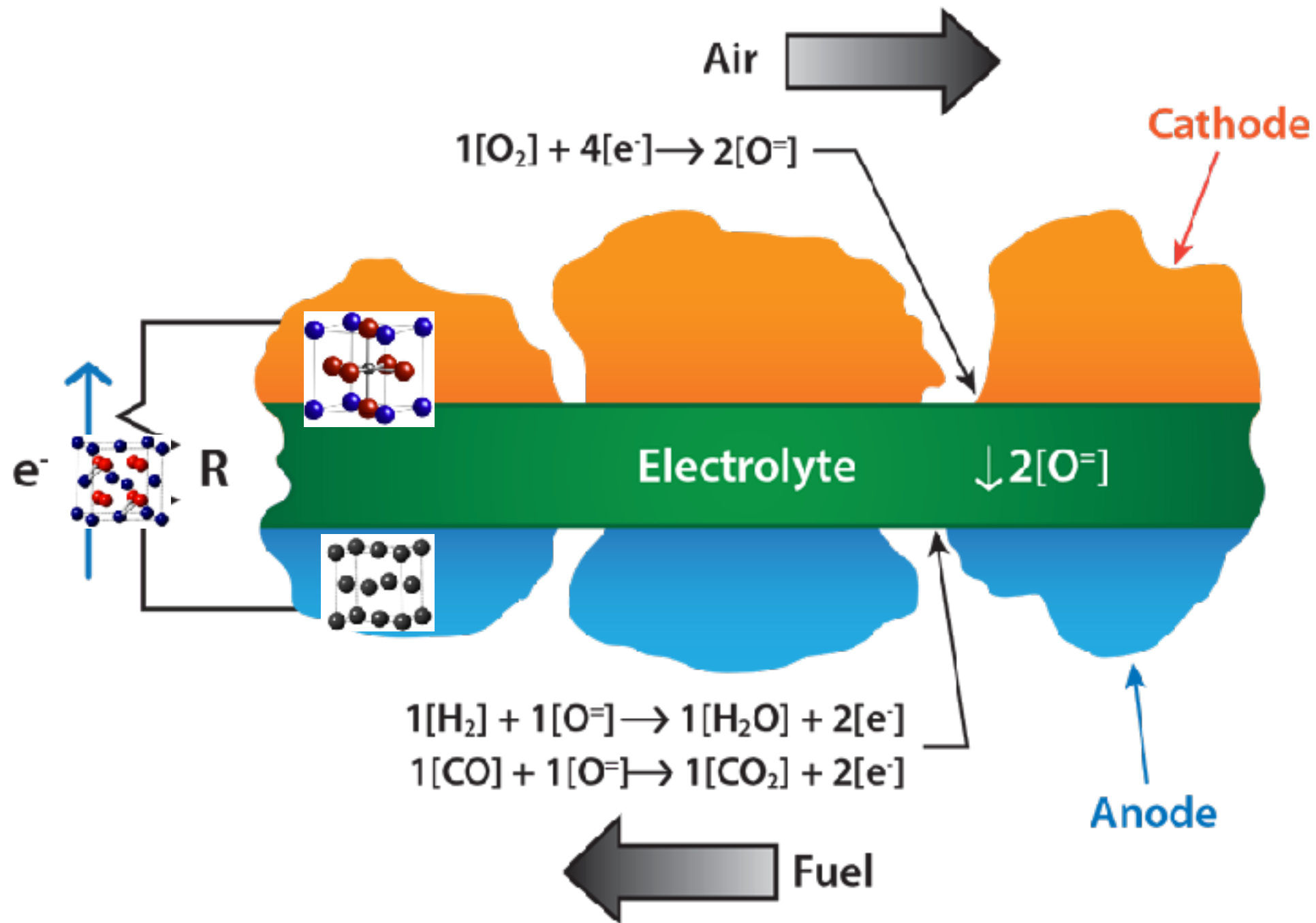
# Anion Vacancies

## ***Solid Oxide Fuel Cell electrolyte***



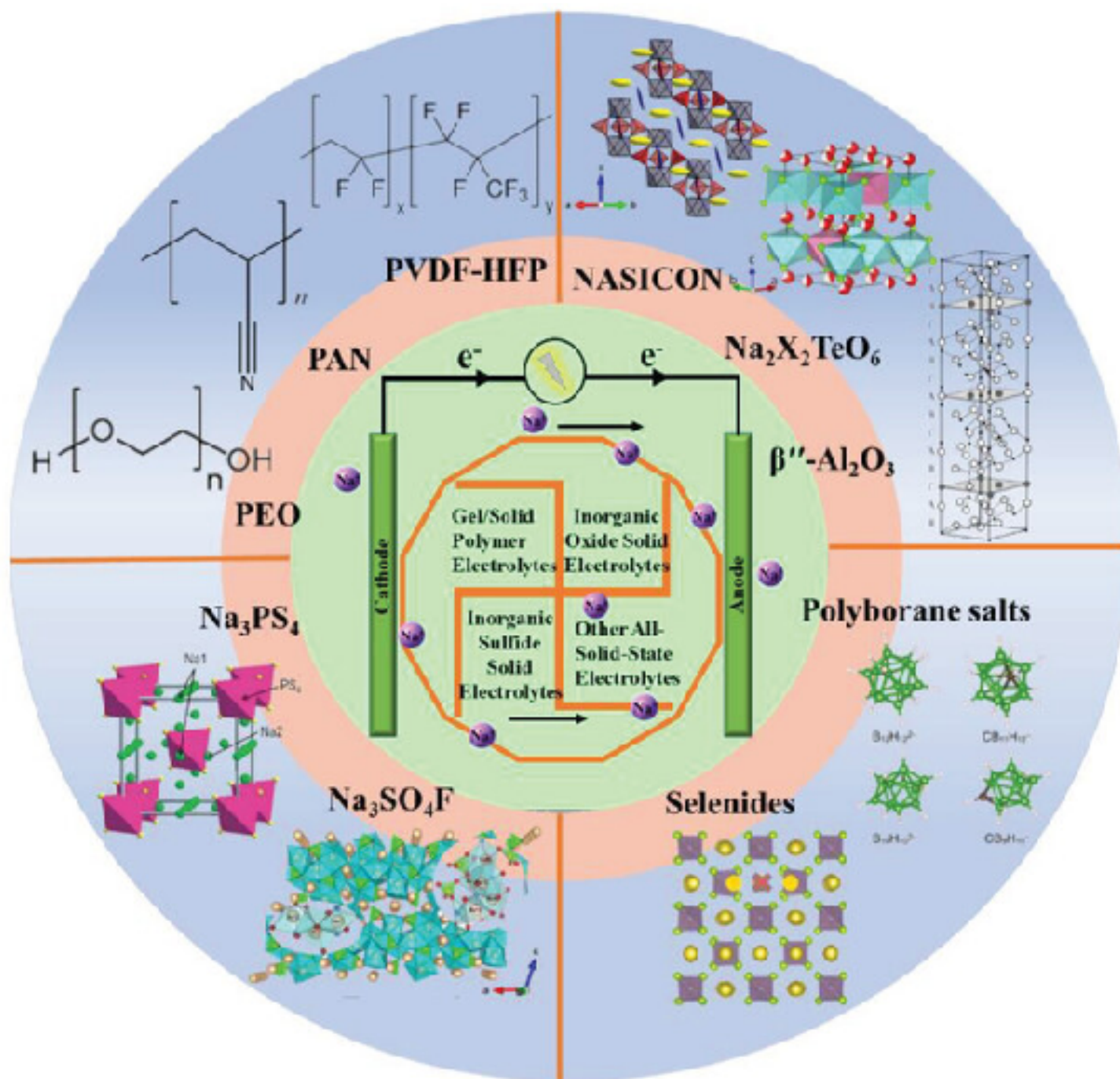
# Anion Vacancies

## ***Solid Oxide Fuel Cell electrolyte***



# Cation Interstitials

## ***Solid electrolytes for Na-ion Batteries***

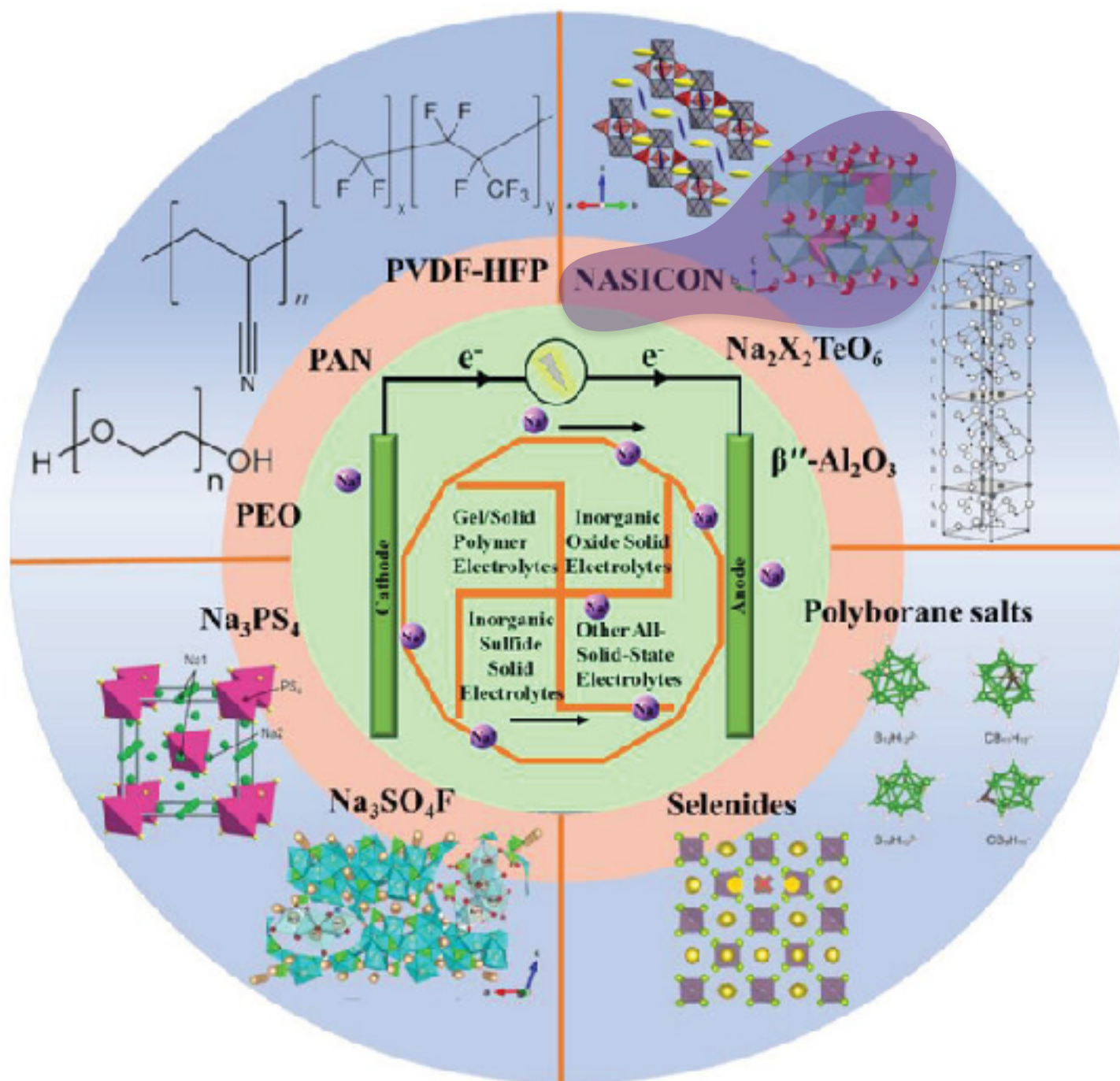




# Cation Interstitials

## ***Solid electrolytes for Na-ion Batteries***

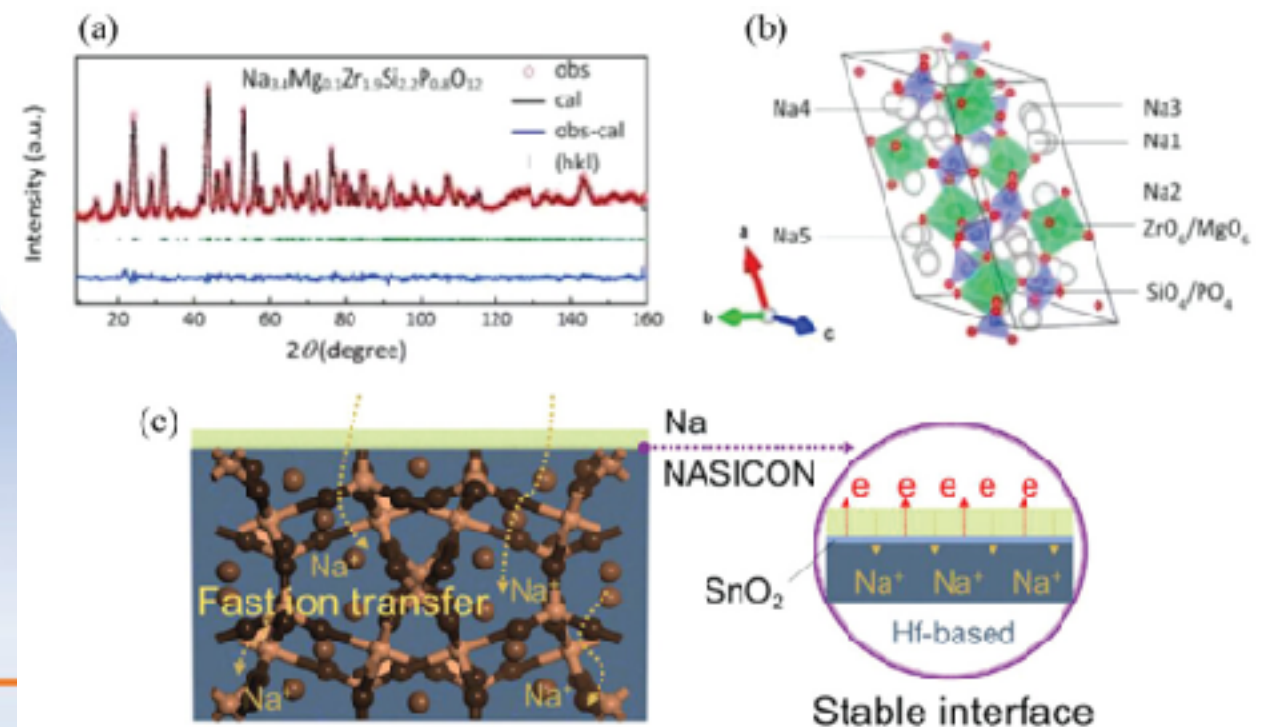
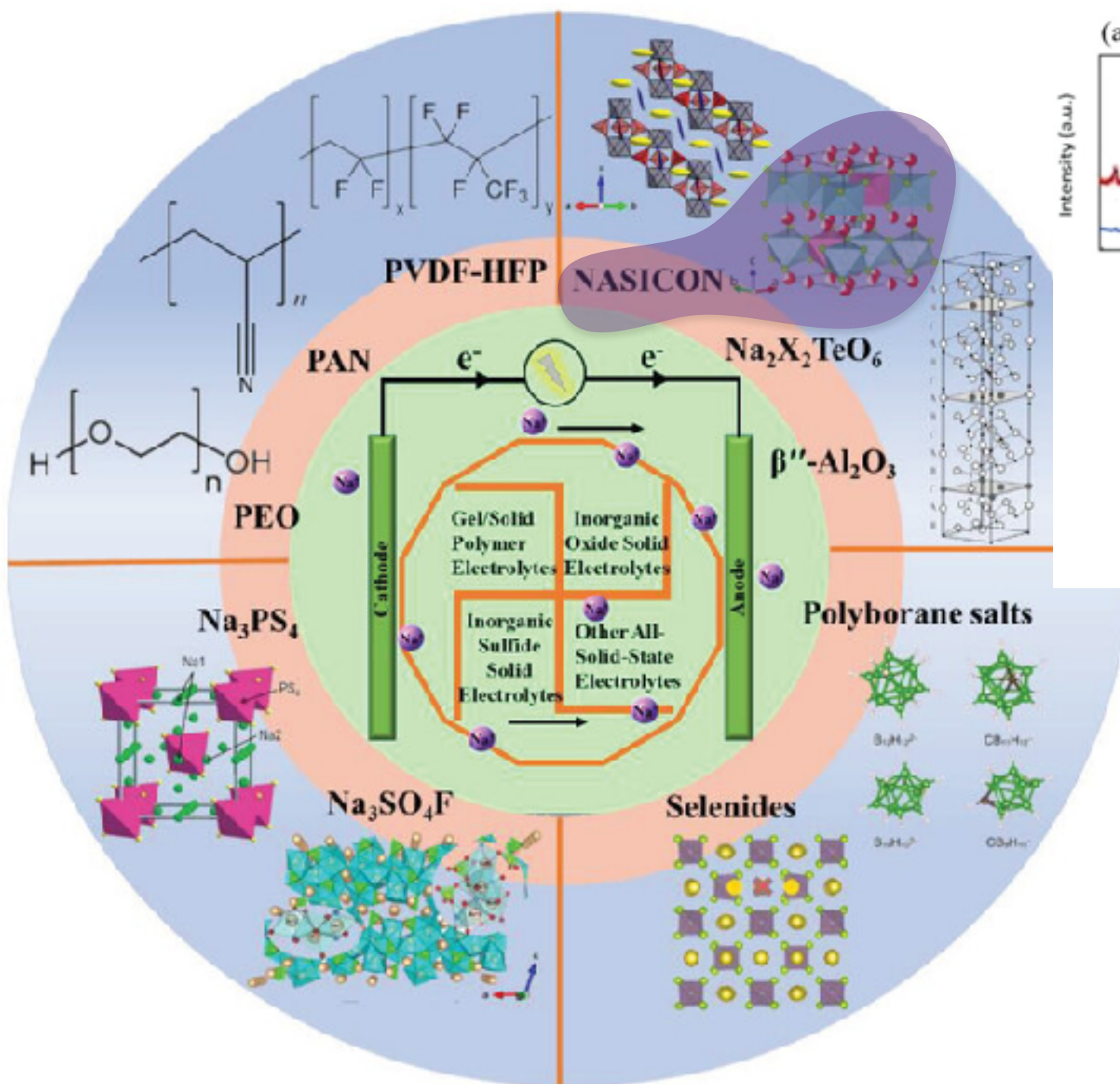
Sodium(**Na**) Super-Ionic (**SI**) Conductor (**Con**)



# Cation Interstitials

## ***Solid electrolytes for Na-ion Batteries***

### Sodium(**Na**) Super-Ionic (**SI**) Conductor (**Con**)

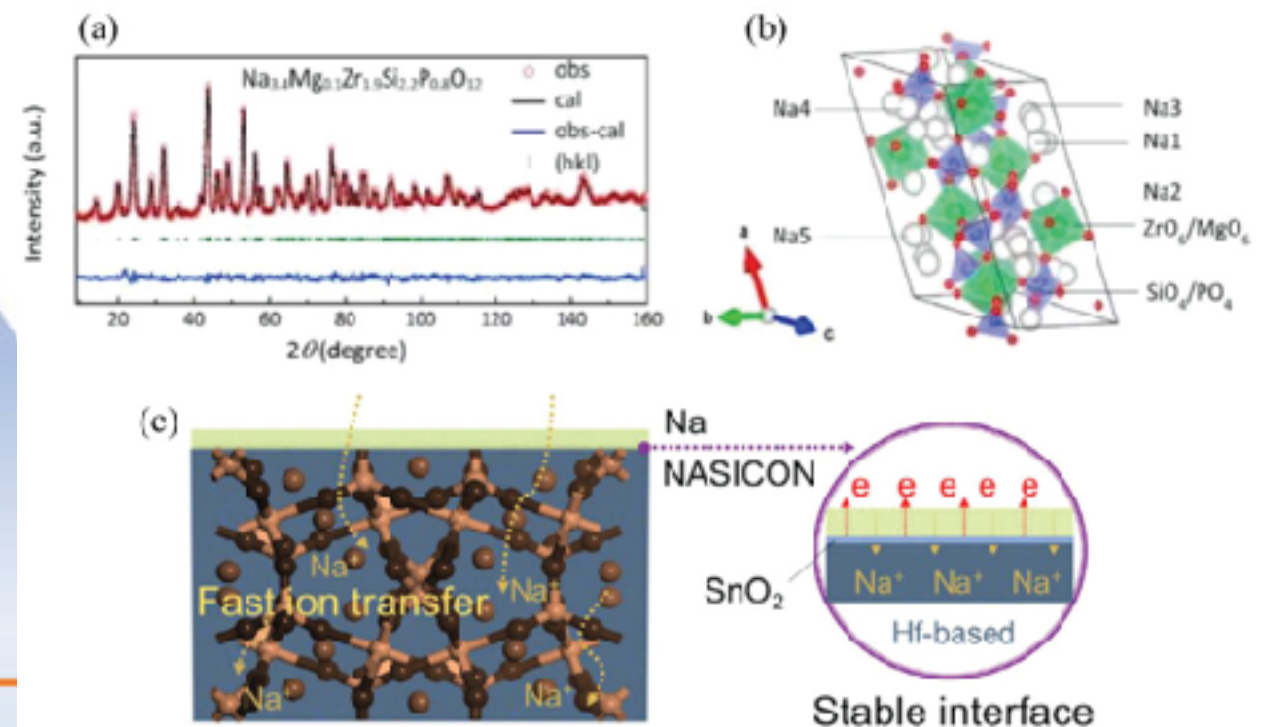
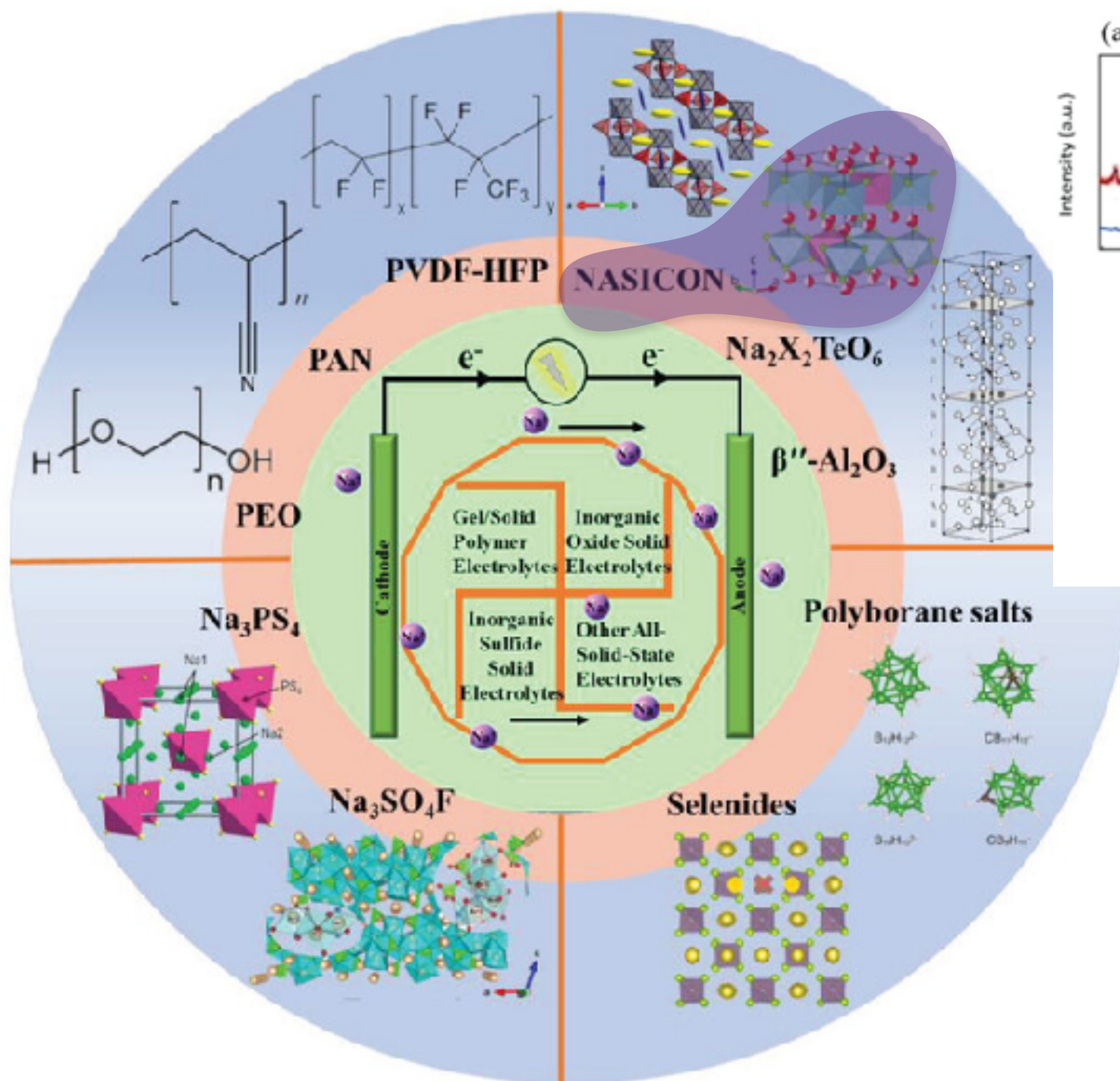




# Cation Interstitials

## ***Solid electrolytes for Na-ion Batteries***

Sodium(**Na**) Super-Ionic (**SI**) Conductor (**Con**)

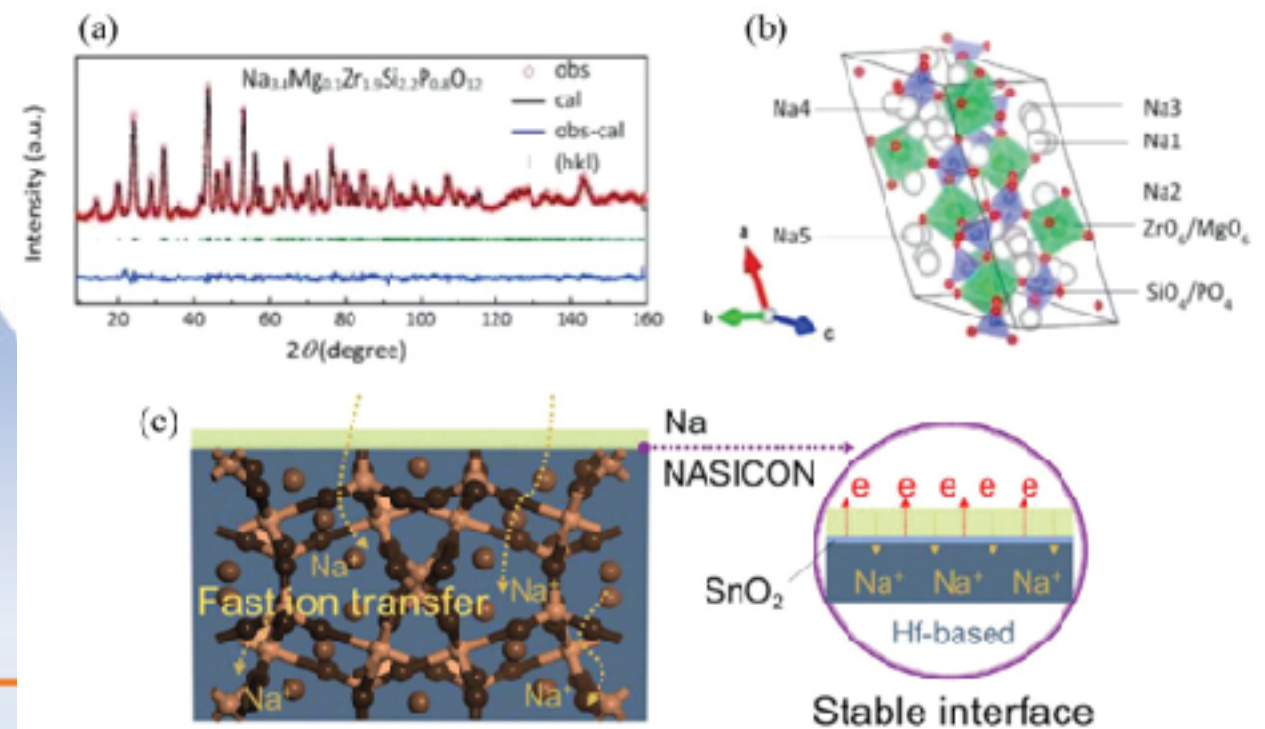
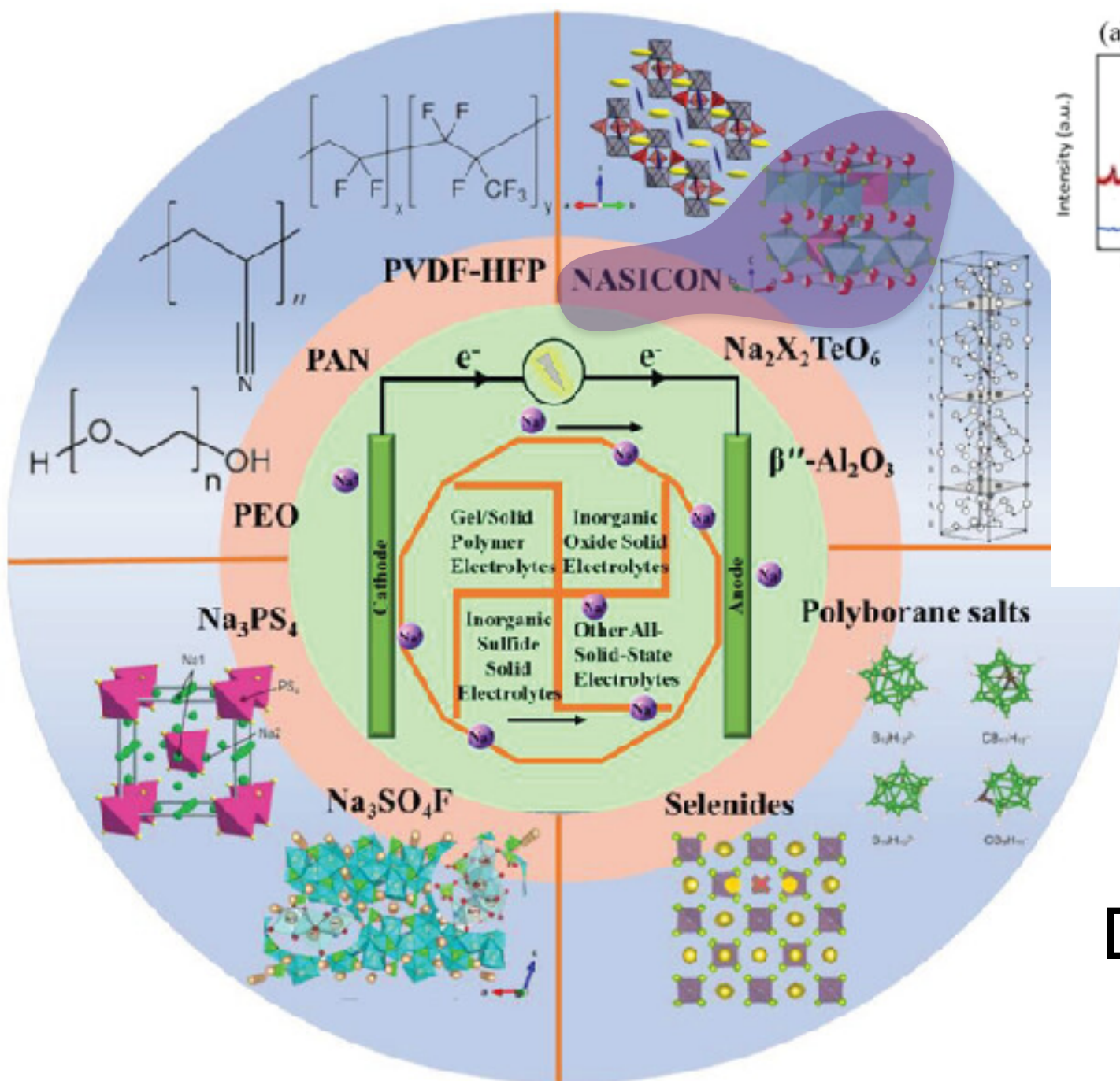


Host Material:  $\text{NaZr}_2(\text{PO}_4)_3$

# Cation Interstitials

## ***Solid electrolytes for Na-ion Batteries***

Sodium(**Na**) Super-Ionic (**SI**) Conductor (**Con**)



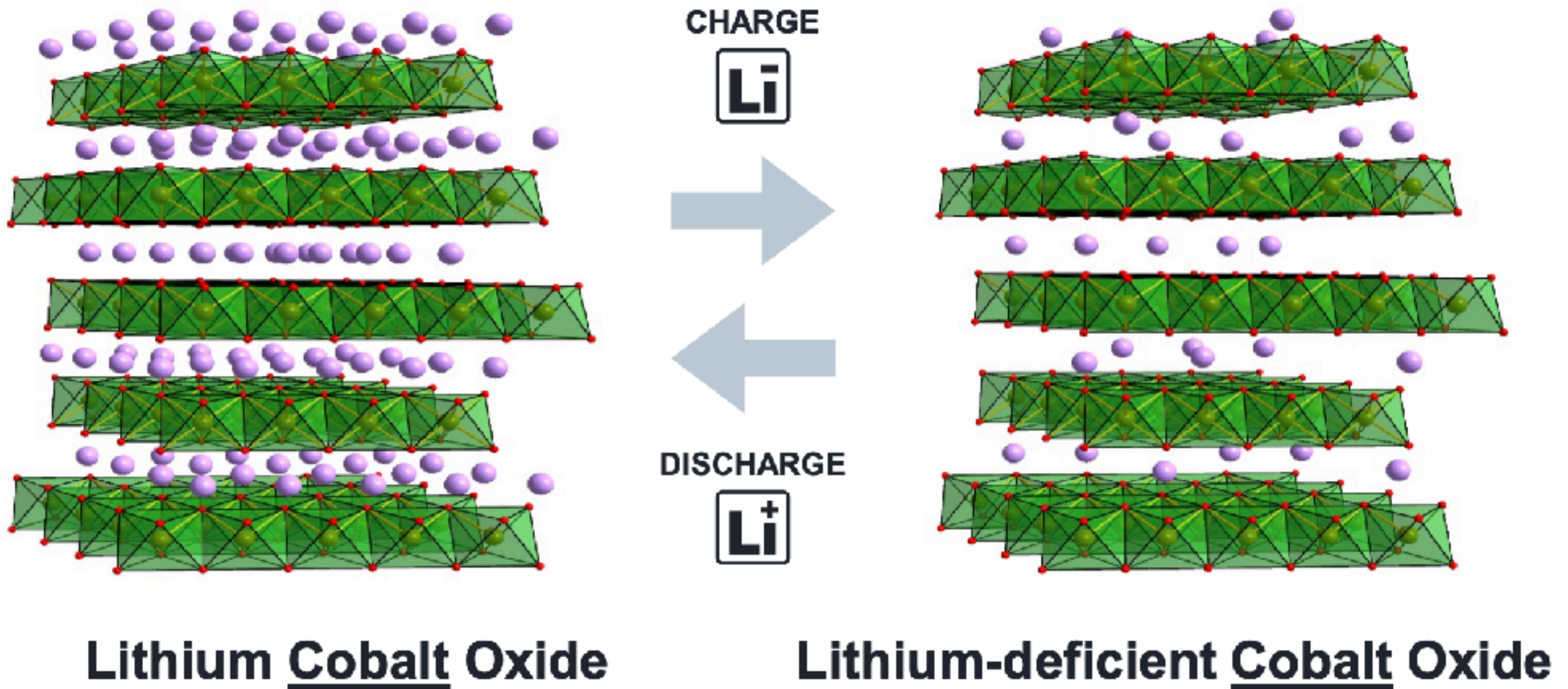
Host Material: NaZr<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub>

Dopant Material: Na<sub>4</sub>Zr<sub>2</sub>(SiO<sub>4</sub>)<sub>3</sub>



# Electronic compensation

## ***Li ion battery electrodes***



# Electronic compensation

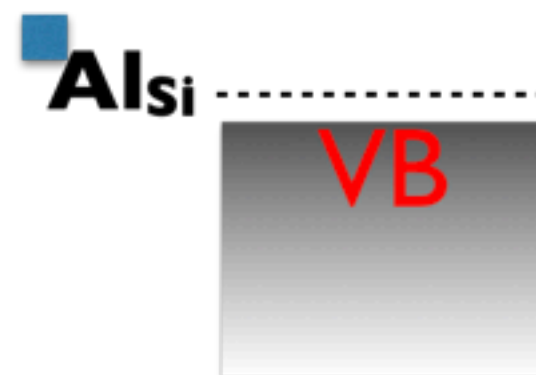
## ***Solar Photovoltaic Absorber***

Si  $\rightarrow$  Ne 3s<sup>2</sup> 3p<sup>2</sup>

P  $\rightarrow$  Ne 3s<sup>2</sup> 3p<sup>3</sup>

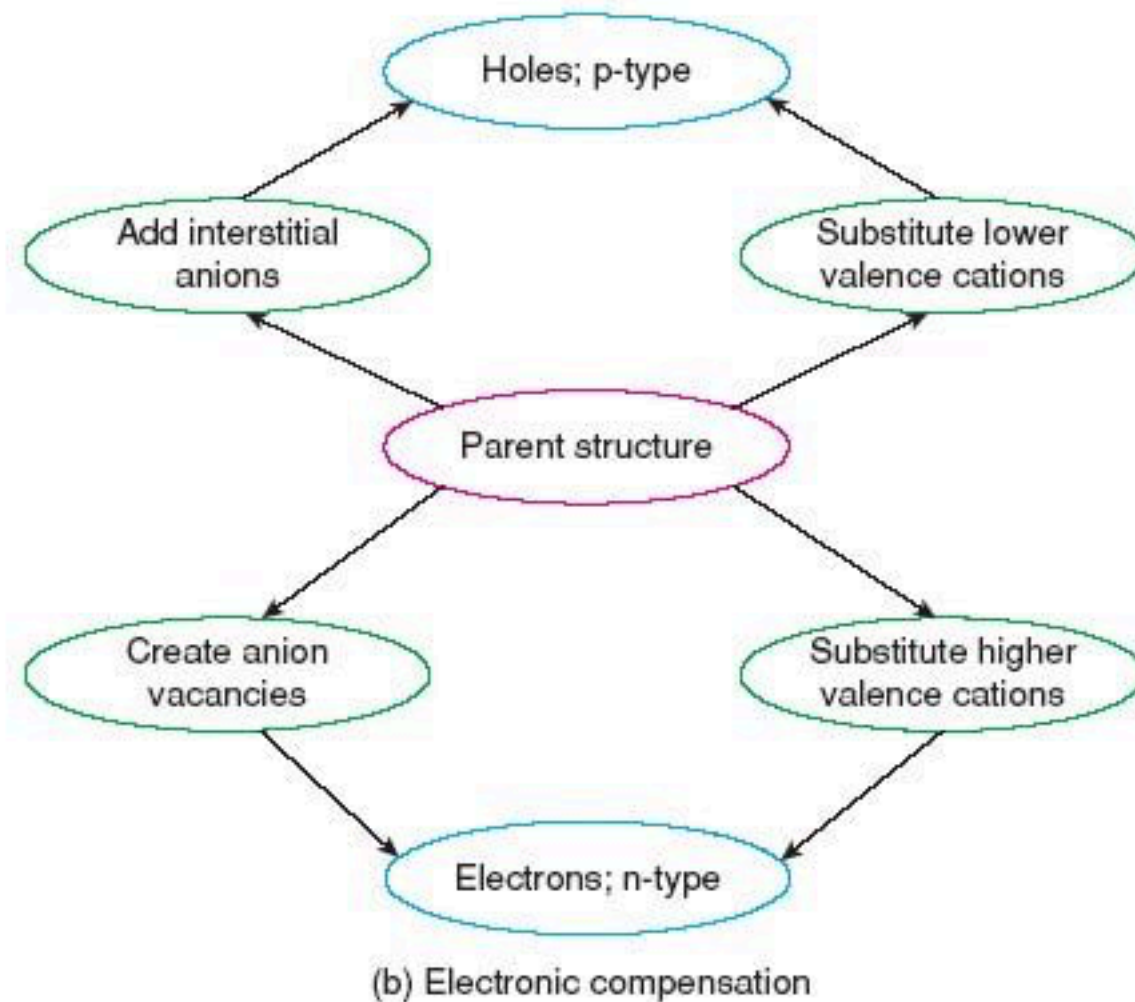
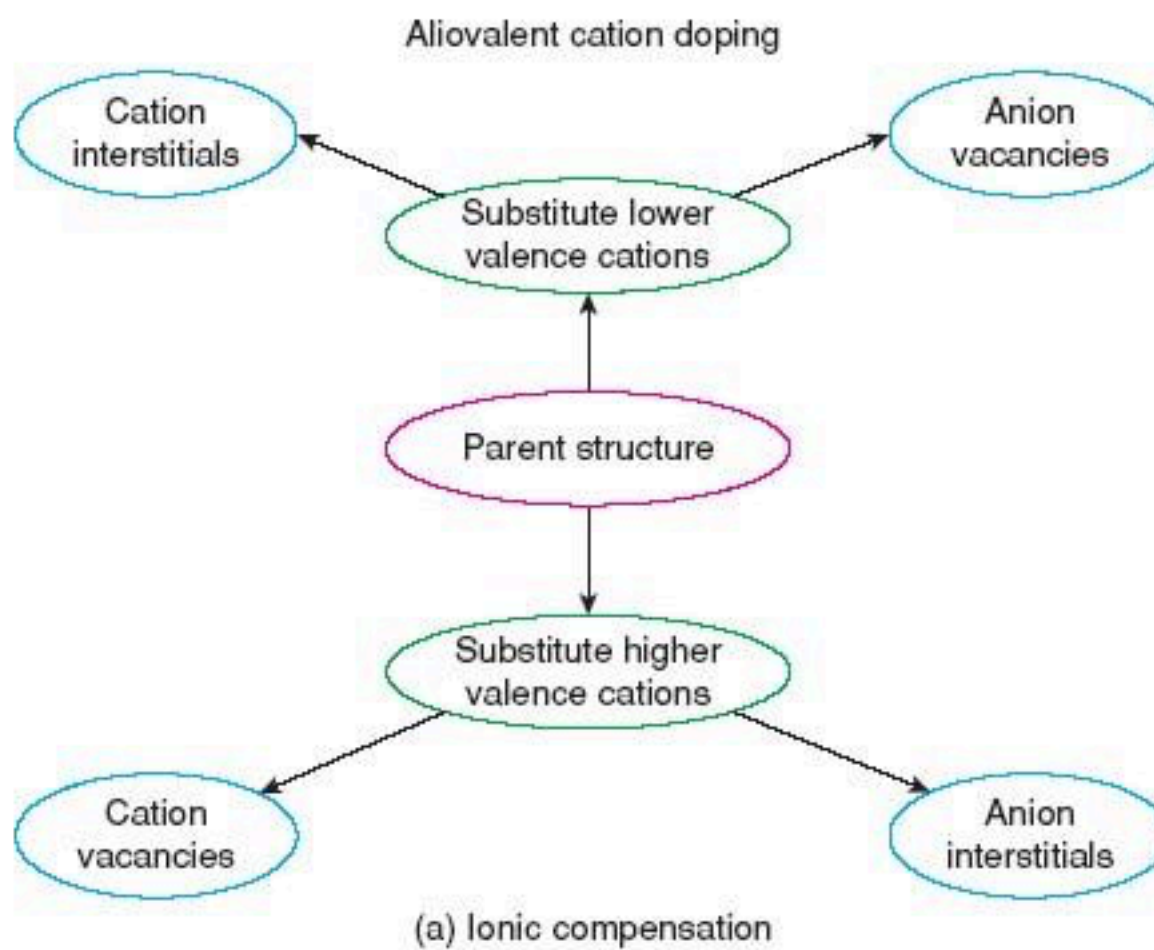
Si  $\rightarrow$  Ne 3s<sup>2</sup> 3p<sup>2</sup>

Al  $\rightarrow$  Ne 3s<sup>2</sup> 3p<sup>1</sup>



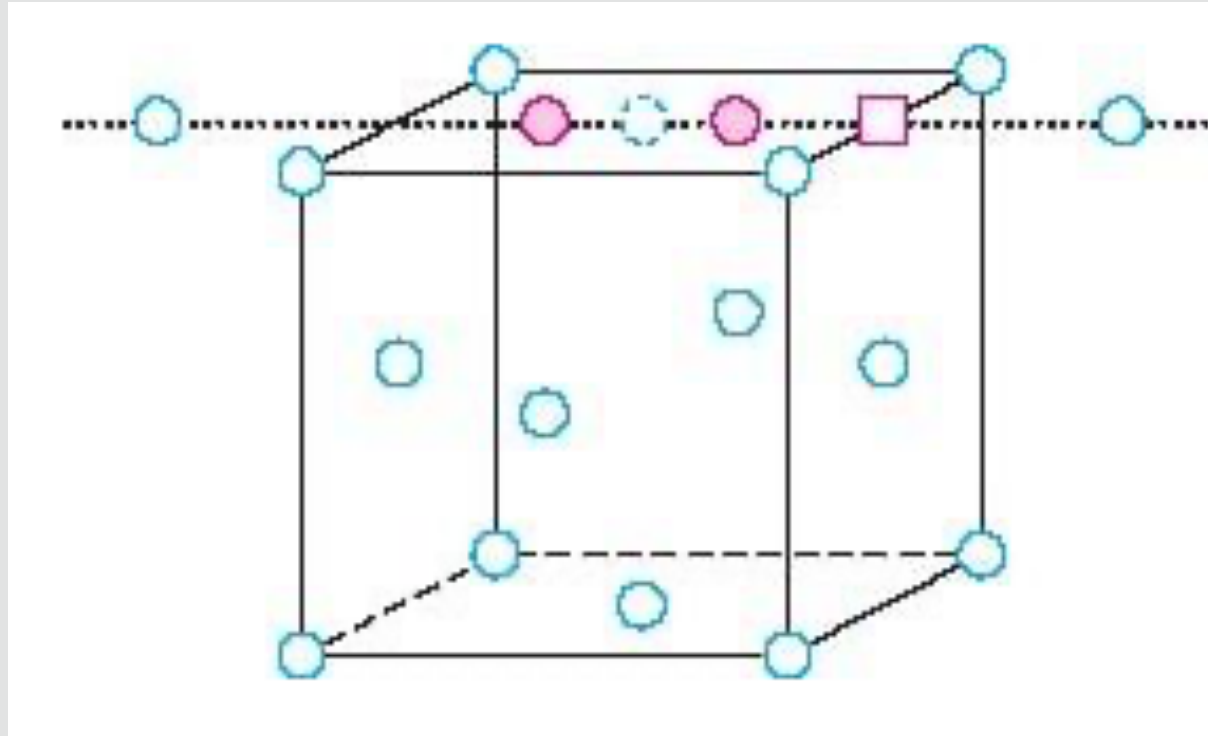


# Summary

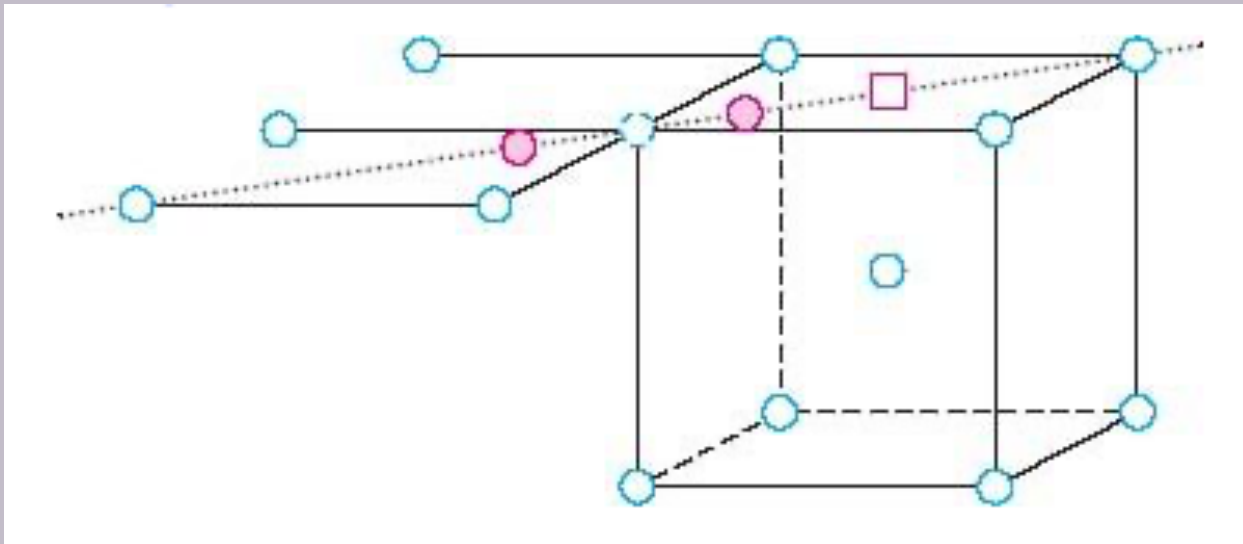


Read other examples in Section 2.3.3. of A.R. West

# Defect Clusters

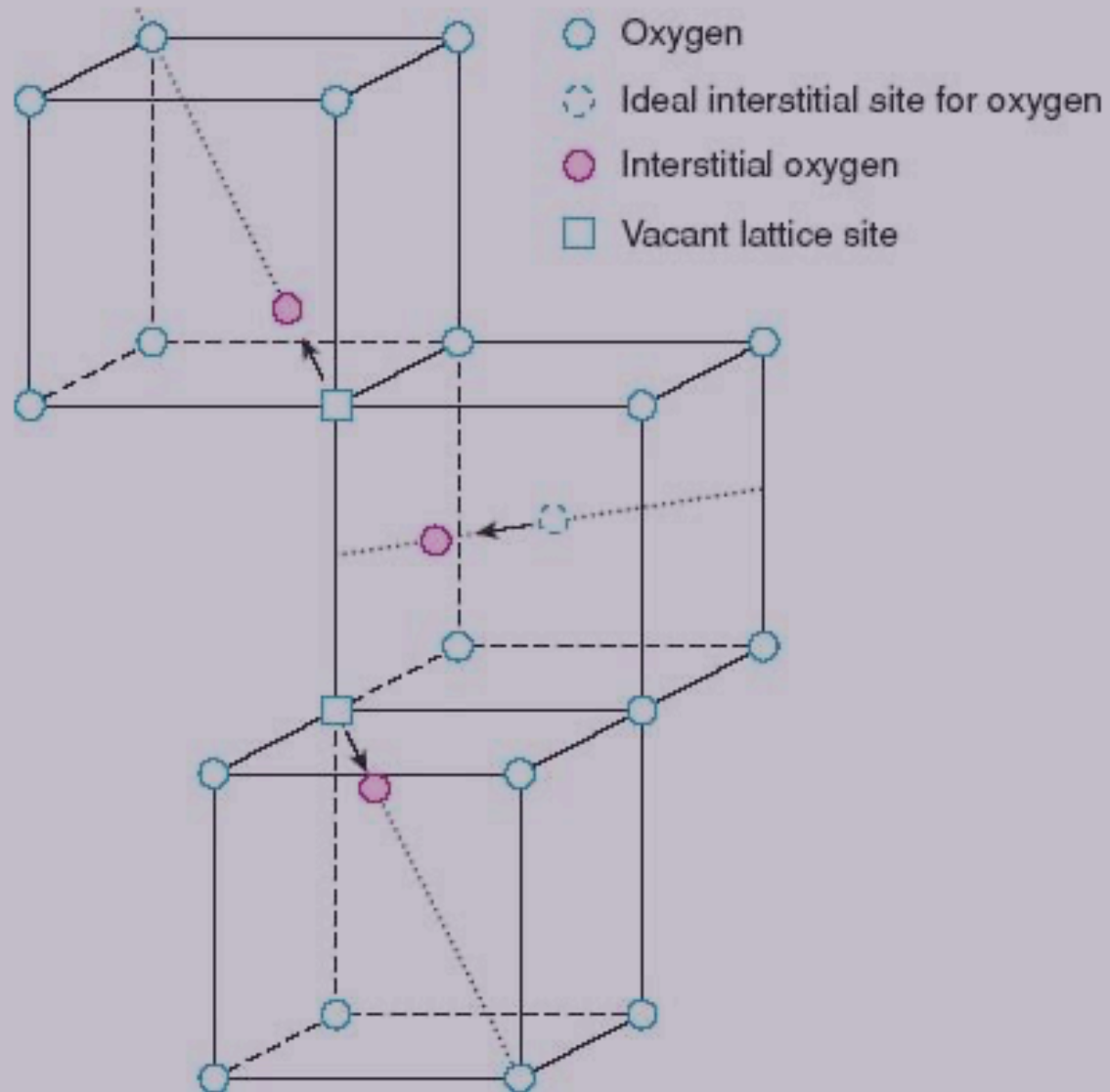


- Interstitial Pt atom at octahedral site in fcc Pt
- Displaced towards top face Pt atom
- Displaces top face Pt atom
- Two Pt atoms on distorted interstitial site - cluster



- Interstitial Fe atom at octahedral site in bcc Fe
- Displaced towards vertex Fe atom
- Displaces vertex Fe atom
- Two Fe atoms on distorted interstitial site - cluster

# Defect Complexes in Oxides – $\text{UO}_2$



- $\text{UO}_2$  - ccp  $\text{U}^{4+}$  with  $\text{O}^{2-}$  in tetrahedral interstices
- Non-stoichiometry -  $\text{UO}_{2+x}$
- Ideal interstitial site is the octahedral site
- Displaced along  $\langle 110 \rangle$
- Displaces two other site  $\text{O}^{2-}$
- 3  $\text{O}_i$  on distorted interstitial sites + 2  $\text{V}_\text{O}$  - cluster

# Electronic properties of materials

- Concept of atomic and molecular orbitals, AO and MO
- MO to bands in crystalline solids - Tight binding, Free electron, and nearly free electron models
- Metals, semiconductors, insulators
- Electrical behaviour of metals and semiconductors
- **Section 3.3, 3.4, 8.1, 8.2, 8.4 in A.R. West**