

## Day-7

→ Lattice Planes ↓

Hyperplane → 1D lower than  $n$ -D plane

→ Directions in a lattice → line, plane

→ Boundary Surfaces — extension of crystallographic hyperplane

→ Crystallographic hyperplane —

3 non-collinear points: all the lattice vectors that exist between these points

Nomenclature or a notation to identify/name these planes → in line with what was developed for directions.

Let us consider a triclinic lattice ( $a, b, c$ ).  
A 3D object is formed by the intersection of planes.

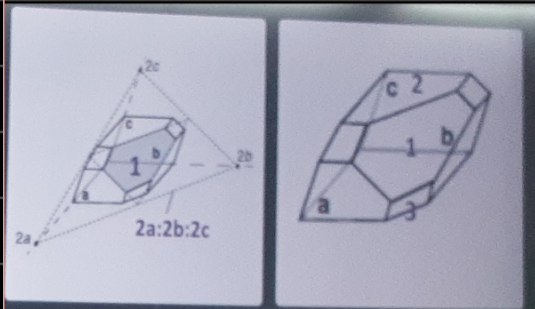
consistent approach to nomenclature.

1.) Extend this plane so that the crystallographic axes intersect this plane → intercepts.

~~2x~~ ~~2y~~ ~~2z~~

2 2 2 written as → (2 2 2)

differentiate from  
writing a vector.



Lattice plane  
nomenclature:  
Miller Indices

2.) Plane 2 || to  $\vec{a}\vec{b}$  plane.  
intercepts the c-axis  
at  $1 \times c$ .

$$(\infty \quad \infty \quad 1)$$

↓ to get rid of  $\infty$   
(take reciprocal)

$$\left(\frac{1}{\infty} \quad \frac{1}{\infty} \quad \frac{1}{1}\right)$$

↓

$$(0 \quad 0 \quad 1)$$

Do the same for  $(2 \quad 2 \quad 2)$

↓ (keep universal)

$$\left(\frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2}\right)$$

↓ convert to integers

$$(1 \quad 1 \quad 1)$$

3.) Plane 3:  $\frac{7a}{4} \quad 2b \quad \infty c$

$$\left(\frac{4}{7} \quad 2 \quad \infty\right)$$

↓ reciprocal

$$\left(\frac{4}{7} \quad \frac{1}{2} \quad 0\right)$$

↓ Integers

$$(8 \quad 7 \quad 0)$$

→ what if plane passes origin?

- Displace it along its normal.
- Determine the intercepts of the plane with the 3 crystallographic axes  $(a, b, c)$ . Let them be  $s_1, s_2, s_3$ .
- Take reciprocal:  $\left(\frac{1}{s_1} \quad \frac{1}{s_2} \quad \frac{1}{s_3}\right)$
- multiply by Lcm to convert them to integers.  
 $(h \ k \ l)$

→  $(h \ k \ l) \rightarrow$  determine distance from origin  $(d)$ .

Along normal, by 'd', shift the plane; we get a set of planes

→ Symmetry related or family of planes

CP:  $(110)$   $\xrightarrow{\text{related}}$   $(101)$   $\xrightarrow{\text{obtained by rotation}}$

IP:  $(110)$   $(101)$

$\xrightarrow{\text{not related}}$

$\downarrow$   
degeneration

CP:  $(110), (101), (011),$

$(1\bar{1}0), (10\bar{1}), (01\bar{1})$

$\times 2 = 12$

$\downarrow$   
degeneracy



Denoted by  $\{110\} \rightarrow$  set of symmetry-related planes

