

Day - 5

→ mass and momentum conservation

$$\left. \frac{dm}{dt} \right|_{sys} = \frac{\partial}{\partial t} \int_{cv} \rho(\downarrow) dv + \int_{cs} \rho(\downarrow) (\vec{n} \cdot \vec{v}) dA$$

Some intensive property

$$\left. \frac{d\vec{p}}{dt} \right|_{sys} = \frac{\partial}{\partial t} \int_{cv} \rho \vec{v} dv + \int_{cs} \rho \vec{v} (\vec{n} \cdot \vec{v}) dA$$

(control volume) (control surface)

→ = 0 (for classical mechanics)

$$\rightarrow = \sum (\underbrace{\vec{F}_s}_{\substack{\text{surface} \\ \text{(pressure)}}} + \underbrace{\vec{F}_B}_{\text{body (gravity)}})$$

At steady state, the $\frac{\partial}{\partial t} \int \rho(\dots) dv$ term is 0.

Along flow direction:

$$-\rho A_1 v_{x_1}^2 + \rho A_2 v_{x_2}^2 = P_1 A_1 - P_2 A_2 + F_{shear} + F_{reac}$$