

Assignment - 2

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Abstract—This document contains the solution to Exercise 3.30(b) of Oppenheim.

Problem 1. Determine the inverse z -transform of

$$X(z) = \log_2\left(\frac{1}{2} - z\right), \quad |z| < \frac{1}{2} \quad (1)$$

(b) by using the power series

Solution: For the ROC $|z| < \frac{1}{2}$

$$nx[n] \leftrightarrow -z \frac{d}{dx} \log(1 - 2x) = -z \left(\frac{1}{1 - 2z} \right) (-2) = z^{-1} \left(\frac{-1}{1 - \frac{1}{2}z^{-1}} \right) \quad (2)$$

$$nx[n] = \left(\frac{1}{2}\right)^n u[-n - 1] \quad (3)$$

$$x[n] = \frac{1}{n} \left(\frac{1}{2}\right)^n u[-n - 1] \quad (4)$$