Task 1:

- a) see code in c)
- b) i): parent p of a child c

$$p = c - \lfloor \frac{c}{2} \rfloor - 1 \tag{1}$$

b) ii): left child c_l of parent p

$$c_l = 2(p+1) - 1 (2)$$

b) iii): right child c_r of parent p

$$c_l = 2(p+1) \tag{3}$$

```
1 #include <stdio.h>
 2 #include <stdlib.h>
 з #include <mpi.h>
 4 #include <math.h>
6 #define TAG_Bcast_simple 1
7 #define TAG_Bcast_tree 2
 8 #define TAG_Bcast_type 3
9 #define typeof __typeof__
10
   //simple broadcast function
11
   void Bcast_simple(void* buffer, int count, MPI_Datatype datatype,
       MPI Comm comm) {
       int i, NoP_comm, myID;
13
       MPI_Status status;
14
15
       MPI\_Comm\_size(comm,\&NoP\_comm)\;; \quad //\,\text{get comm size}
16
       MPI_Comm_rank(comm,&myID);
                                             //get own ID in comm
17
18
        if (myID==0){
                                             //only process zero is sender (
19
        i.e. 0 broadcasts)
            \begin{array}{ll} \textbf{for} & (\ i = 1; i < NoP\_comm; \ i + +) \{ \end{array}
                                             //\operatorname{exclude} 0 as it is the source
20
21
                 //send to ith process
                 MPI Send(buffer, count, datatype, i, TAG Bcast simple, comm)
22
                 printf("\nI am process %i and I sent to %i\n",myID,i);
23
24
25
26
            //reveivcer need to receive size first
27
            MPI_Probe(0, TAG_Bcast_simple, comm, & status);
28
            MPI_Get_count(&status, datatype,&count);
29
            MPI_Recv(buffer, count, datatype, 0, TAG_Bcast_simple, comm,&
30
       status);
            }
31
32
33
int get parent(int child, int num nodes){
  //compute parent node using the formula as shoow in the solution
       document
```

```
if (child!=0){ //only rank zero node doesn't have a parent
36
           return (child-floor(child/((double) 2))-1);}
37
38
       else{
39
           return -1;
40 }
41
int get_left_child(int parent,int num_nodes){
  //compute left child node using the formula as shoow in the
43
       solution document
       int child left;
44
       child_left = 2*(parent+1)-1;
45
46
47
       if (child left>num nodes-1){ //return -1 if left child is
       greater than NoP
          return -1;
48
49
       else {
           return child_left;}
50
51
  int get right child(int parent, int num nodes){
53
  //compute right child node using the formula as shoow in the
       solution document
       int child_right;
       child_right=2*(parent+1);
56
       if (child\ right>num\ nodes-1){//return\ -1} if right child is
58
       greater than NoP
59
          return -1;
       else {
60
61
           return child_right;}
62 }
63
  void Bcast tree(void* buffer, int count, MPI Datatype datatype,
64
      MPI Comm comm) {
   //function to broadcast a message using a tree structure for
       message propagation
       int myID, NoP, parent, child_left, child_right;
66
      MPI_Status status;
67
68
      MPI Comm rank(comm,&myID);
                                             //get comm size
69
      MPI_Comm_size(MPI_COMM_WORLD, &NoP); // get own ID in comm
71
       parent=get_parent(myID, NoP);
                                                 //get corresponding
      parent element
       child_left=get_left_child(myID,NoP);
73
                                                 //get left child
       child_right=get_right_child(myID, NoP);
                                                 //get right child
74
75
       /*//just for checking purposes
76
       printf("\nparent of %d is %d",myID, parent);
77
       printf("\nleft child of %d is %d",myID,child_left);
78
       printf("\nright child of %d is %d",myID,child_right);*/
79
       if (parent!=-1){ // if parent is not -1, i.e. if myID!=0
81
            /probe first to get value
82
           MPI Probe(parent, TAG Bcast tree, comm, & status);
83
           MPI_Get_count(&status, datatype,&count);
84
           MPI_Recv(buffer, count, datatype, parent, TAG_Bcast_tree, comm,
85
```

```
&status);
             //printf("\n%d:recv from parent: %d\n",myID,parent);
86
87
88
        if (child_left!=-1){
89
90
             MPI Send(buffer, count, datatype, child left, TAG Boast tree,
91
        comm);
             //\operatorname{printf}("\n\%d:send\ to\ left\ child:\m%d\n",myID,child\_left);
92
93
94
         if (child_right!=-1){
95
             MPI Send(buffer, count, datatype, child right, TAG Boast tree,
96
        comm);
             //printf("\n%d:send to right child: %d\n",myID,child_right)
97
98
99
100
101
        main(int args, char *argv[])
102
103
104
         int myRank, NoP;
        {\rm MPI\_Init(\&args\;,\;\&argv\,)}\;;
        MPI Comm rank (MPI COMM WORLD, & myRank);
106
        \label{eq:mpi_comm_size} $$ MPI\_COMM\_WORLD, \& NoP) ;
107
108
         /*test value*/
109
        int N;
111
        N=3;
        int *sd;
112
113
        sd=malloc(N*sizeof(int));
        if (myRank==0){
114
115
             sd[0]=1;
116
             sd[1]=2;
117
             sd[2]=3;
118
             {\tt Bcast\_tree} \, (\, {\tt sd} \, , {\tt N}, {\tt MPI\_INT}, {\tt MPI\_COMM\_WORLD}) \; ;
119
             //Bcast_simple(sd,N,MPI_INT,MPI_COMM_WORLD);
120
121
        else {
             Bcast tree (sd, N, MPI INT, MPI COMM WORLD);
123
             //Bcast_simple(sd,N,MPI_INT,MPI_COMM_WORLD);
             printf("\nProcess %d: %d %d %d\n",myRank, sd[0], sd[1],sd
         [2]);
127
         free(sd); //free test array
128
129
        MPI_Finalize();
130
        return 0;
132
```

Task 2: Glider Movement:

Generation 1:

	X												
		X											
X	X	X											
													•
Generation 2:													
	•												
	X		•	•	•	•	•	•	•	•	•	•	•
•	X											•	•
•	•	٠,	·	•	•	•	: .	or	٠,		•	•	•
٠	•											•	•
•		X										•	•
	•										•	٠	٠
•	x										٠	٠	٠
•	٠	٠,						•			٠	•	•
Generation 4:													
٠		•											•
•	X											•	•
•		X										•	•
•	Х	X	•			•	•	•	•	•	•	•	•
•	•	•	ユ,			· rn	+;	•		Է.	•	•	•
Generation 5:													
•	•												
•	•	X							•	•	•	•	•
•	· X	•	х Х				•		•	•	•	•	•
•	Л	А	А	•	•	٠	٠	•	٠	•	•	•	•

Code:

```
#include <stdlib.h>
#include <stdlib.h>
#include <mpi.h>
#include <string.h>
#include <math.h>

#define TAG_CycleRst 1 //tag for sending/receiving results after each cycle
#define TAG_Exchange 2 //tag for exchange of ghost points between different domains
#define TAG_CartPos 3 //tag for sending/receiving ranks in the cartesian grid

/*This program simulates Conway's game of life in parallel.

The domain is decompositioned, such that evaluation of
```

```
cells
13 can be done in parallel. This is accomplished by the
      workers.
14 A master process receives the results to facilitate
      correct
output of the result
16 For reasons of simplicity, the initial configuration
     is implied
on a process level*/
18
19 //error depends on width!
int main(int args, char *argv[])
21 {
       int myID, NoP;
22
       MPI Init(&args,&argv);
                                                 //init MPI
23
      session
      25
      of processes
26
       //init
27
      int dims[0], period[0], reorder, w, domain_size[NoP
28
      -1], k, i, j, h, r;
      MPI Status status;
29
      w=14; //board size (square board!)
30
      k=7; //number of timesteps
31
33
      //domain decomposition
34
       r=w; //remainder
35
       for ( i=0; i< NoP-2; i++){ //-2 because one is master
36
     and one will fill up the rest domain_size[i]=floor(w/(double) (NoP-1));
37
           r-=domain size[i];
38
39
       domain size [NoP-2]=r;
40
41
      dims[0] = NoP-1;
                         //number of domains, Number of
42
      process - master process
       period[0]=1;
                         //periodic boundary conditions
43
                         //reordering of processes in Cart
       reorder=1;
44
45
      int excl[0];
                         //process to exclude from new
46
      group
       excl[0] = 0;
                         //exclude master(0)
47
      \begin{array}{ll} MPI\_Group\ GroupWorker\ ,\ GroupWorld\ ;\\ MPI\_Comm\ CommWorker\ ; \end{array}
48
49
      MPI Comm group (MPI COMM WORLD, & Group World);
51
      get group of MPI_COMM_WORLD
      MPI_Group_excl(GroupWorld, 1, excl,&GroupWorker); //Create Group of worker without master
53
       //Create new communicator corresponding to group
54
      of workers
       if (myID!=0)
           MPI Comm create (MPI COMM WORLD, GroupWorker, &
56
```

```
CommWorker);
           MPI Comm create (MPI COMM WORLD, MPI GROUP EMPTY
58
      ,&CommWorker);
59
60
       if (myID!=0) {
61
62
           MPI_Comm Cart;
63
           MPT Cart create (CommWorker, 1, dims, period,
64
      reorder, & Cart);
65
            int sum, ngbor_top, ngbor_bot, jp1, jm1, crt_rank,
66
      crt rank var, mysize;
67
           MPI Comm rank(CommWorker,&crt rank); //get
68
      rank in Cart
69
            mysize=domain_size[crt_rank];
                                                      //get size
       of own domain
71
            //own domain includes ghost points (no
      distinction here) to make computation simple int myConfig[mysize+2][w], ngborConfig_top[w],
      ngborConfig bot[w], myNewConfig[mysize+2][w];
74
            //init to zero
            for (j=0; j < mysize + 2; j++){
76
                for (i=0; i < w; i++)
77
                     myConfig[j][i]=0;
78
                     myNewConfig[j][i]=0;
79
80
                }
           }
81
82
           //initial configuration for the given special
83
      case
            //0 === dead, 1==alive
84
            if (crt_rank==0){
                my\overline{C}onfig[1][0] = 0; myConfig[1][1] = 1; myConfig[1][1] = 1
86
      [1][2]=0;
                myConfig[2][0] = 0; myConfig[2][1] = 0; myConfig
87
      [2][2]=1;
                myConfig[3][0] = 1; myConfig[3][1] = 1; myConfig
      [3][2]=1;
           }
90
             get top and bottom neighbor
91
           MPI Cart shift (Cart, 0, -1, & crt rank var, &
92
      ngbor_top);
            MPI Cart_shift(Cart,0,1,&crt_rank_var,&
93
      ngbor_bot);
95
            for (i=0; i < k; i++){ //loop over number of
      generations to play
97
                /*send and recv ghost points: first send
```

```
to top and receive from bottom,
                  the vice versa, to avoid deadlocks*/MPI_Sendrecv(myConfig[1],w,MPI_INT,
99
       ngbor_top, TAG_Exchange, ngborConfig_bot, w, MPI_INT,
       ngbor_bot, TAG_Exchange, CommWorker, & status);
                  MPI_Sendrecv(myConfig[mysize],w,MPI_INT
      \begin{array}{l} ngbor\_bot\ , TA\overline{G}\_Exchange\ , ngborConfig\_top\ , w\ , MPI\_INT\ , \\ ngbor\_top\ , TAG\_Exchange\ , CommWorker\ , \&\ s\ t\ a\ t\ u\ s\ )\ ; \end{array}
                  //transfer ghost points to own domain
                 memcpy(myConfig[0],ngborConfig_top,w*
       sizeof(int));
                 memcpy(myConfig[mysize+1],ngborConfig bot,
      w*sizeof(int));
106
                  for (h=1;h\leq mysize;h++)\{ //loop over row \}
107
108
                       for (j=0; j < w; j++){
                                              //loop over every
109
        cell in row
                            //apply horizontal periodocity and
111
        find horizontal neighbors
                           sum=0;
                            if (j!=0)
113
                                jm1=j-1;
114
115
                                jm1=w-1;
117
                            if (i!=w-1)
118
119
                                jp1=j+1;
120
                                jp1 = 0;
                            //calculate the sum, because of
       binary values, the sum indicates
                            //the number of live cells
124
                           sum+=myConfig[h-1][jm1]+myConfig[h]
       -1][j]+myConfig[h-1][jp1];
                           sum+=myConfig[h][jm1]+myConfig[h][
       jp1];
                           sum+=myConfig[h+1][jm1]+myConfig[h
       +1][j]+myConfig[h+1][jp1];
128
                            //apply rules given in the task
129
                            if ((myConfig[h][j]==1) && ((sum
130
       <2) | (sum>3))
                                myNewConfig[h][j]=0;
                            else if ((myConfig[h][j]==1) \&\& ((
      sum = 2) | | (sum = 3))
                                myNewConfig[h][j]=1;
133
                            else if ((myConfig[h][j]==0) \&\& (
      sum==3)
                                myNewConfig[h][j]=1;
                           } //for j
136
137
                         //for h
                       if (i!=0){ //to print initial
139
```

```
configuration
                               for (j=0; j < mysize + 2; j++) \{ //
140
      transfer linewise
                                   memcpy(myConfig[j],
      myNewConfig[j],w*sizeof(int));
                              } //for j
142
                     } //for
143
144
145
                     //just to check whether sending worked
146
       correctly
                     /* for (h=1;h< mysize+1;h++){
147
                          for (j=0; j \le w; j++) \{
printf("%d%d", crt_rank,
148
149
      myConfig[h][j]);
150
                          printf("\n");
152
153
                     //send own rank in cartesian
154
      communicator to allow correct printing
      for (h=1;h\leq mysize;h++) //send actual
156
       data linewise (facilitates easier printing)
                          MPI_Send(myConfig[h],w,MPI INT,0,
157
      TAG_CycleRst ,MPI_COMM_WORLD);
159
160
            //free groups and communicator
           MPI_Comm_free(&CommWorker);
MPI_Group_free(&GroupWorker);
MPI_Group_free(&GroupWorld);
161
163
164
      } //endif
       else{
167
            int rk, counter, recv_size, CurConfig[w][w],
168
      RecvConfig[w];
            //int RecvConfig[recv size][w];
171
            for (i=0; i < k; i++){ //iteration over all
      generations
                counter=0;
173
174
                 for (j=1; j<NoP; j++){
175
                     recv size=domain size[j-1]; //domain
177
      of process which sends
                       receive rank
178
                     MPI_Recv(&rk, 1, MPI_INT, j, TAG_CartPos,
      MPI COMM_WORLD, & status);
180
                     for (h=0;h< recv\_size;h++){
181
      iteration over domain, receive linewise
                          MPI Recv(RecvConfig, w, MPI INT, j,
```

```
TAG\_CycleRst\ , MPI\_COMM\_WORLD, \&\ status\ )\ ;
                                       memcpy(CurConfig[counter],
183
         RecvConfig, sizeof(int)*w); //build global result counter+=1;
184
                         } //for h
} //for j
185
186
187
                         //print results
for (j=0;j<w;j++){
    for (h=0;h<w;h++){
        if (CurConfig[j][h]==0)
            printf(".");
188
190
191
193
                                               printf(" x");
194
                                } //for \dot{h}
195
                                printf("\n
196
         n");
                         \} \ // \, for \ j \\ printf(" \setminus n
197
198
         \overline{n \setminus n});
           } //else
200
201
202
         MPI_Finalize();
203
204 }
```