NBA

24 July 2020

Explaining Relationships Using Regression Analysis

A regression model can be used for two different purposes. It can be used to explain how one variable (y) depends on another variable (x). Indeed, here we are often trying to identify causal inferences, to explain how a system works. It can also be used to make forecasts about future outcomes.

During this week we are going to focus on the first purpose, thinking about potential causal links in the performance of professional sports teams. We are going to focus on the performance of teams across an entire season, in terms of either win percentage or league position.

The main input to any team is, of course, the players themselves. Teams compete to hire the best players and player agents seek to find the best financial deal for their clients. It is reasonable to expect, therefore, that team expenditure on player salaries should be an important factor in determining team performance. To be clear, the logic of this is NOT that paying higher salaries will make players perform better. At the top level of professional sports, all players are highly motivated, and salary probably does not play a significant motivational role. Rather, competition for players means that salaries are likely to reflect relative abilities. Better players command higher salaries, and as a result the aggregate pay of players on the team is likely to be a good predictor of team performance.

There are a number of sources for player salary data. In the North American major leagues, salary negotiations are framed by collective bargaining agreements with player unions, which often publish individual player salary data. In European soccer leagues, aggregate salary data is to be found in audited financial statements of professional clubs, which are often available to the public (notably in England). Cricket players in the Indian Premier League have their salaries determined in a public auction.

This week we are going to examine the wage-performance relationship in four different leagues - the NBA, the English Premier League, Major League Baseball and the National Hockey League. While our focus is on the role of salaries, we will also consider other factors that might be relevant, which will help us to think about some of the issues that arise in regression analysis.

We start with the NBA.

```
# As usual, we begin by loading the packages we will need
library("readxl",quietly = TRUE)
library("tidyverse",quietly = TRUE)
```

```
# Now we load the data
NBA = read_excel("NBA pay and performance.xlsx")
NBA %>% summary()
##
        Team
                             season
                                                               salaries
                                               wpc
##
    Length:210
                                                                    : 28938902
                         Min.
                                 :2012
                                         Min.
                                                 :0.1060
                                                            Min.
    Class : character
                         1st Qu.:2013
                                         1st Qu.:0.3780
                                                            1st Qu.: 59376595
##
    Mode : character
                         Median:2015
                                         Median : 0.5120
                                                            Median: 73728186
##
                         Mean
                                 :2015
                                         Mean
                                                 :0.4978
                                                            Mean
                                                                    : 78253392
                         3rd Qu.:2017
##
                                                            3rd Qu.: 95642974
                                         3rd Qu.:0.6060
##
                                 :2018
                                                                    :142560102
                         Max.
                                         Max.
                                                 :0.8900
                                                            Max.
NBA %>% str()
## Classes 'tbl df', 'tbl' and 'data.frame':
                                                    210 obs. of 4 variables:
               : chr
                       "Atlanta Hawks" "Atlanta Hawks" "Atlanta Hawks" "Atlanta Hawks"
    $ Team
                      2012 2013 2014 2015 2016 ...
##
    $ season
               : num
##
    $ wpc
                      0.606 0.537 0.463 0.732 0.585 0.524 0.293 0.591 0.506 0.305 ...
               : num
    $ salaries: num
                      55503683 60437642 58841508 62487671 82337675 ...
If salaries reflect player ability, then the success of a team should depend on how much
more or less it pays than its rivals. However, if we look at salaries paid out in different
seasons, there is clearly inflation in player salaries. We can see this if we use the group_by()
command to look at total salaries over the seven seasons:
```

```
Sumsal <- NBA %>%
  group_by(season)%>%
  dplyr::summarise(salaries = sum(salaries))%>%rename(allsal = salaries)
Sumsal
```

```
## # A tibble: 7 x 2
##
     season
                 allsal
##
      <dbl>
                  <dbl>
       2012 1438650614
## 1
## 2
       2013 1837810750
## 3
       2014 1976549213
       2015 2153667904
## 4
       2016 2523411764
## 5
## 6
       2017 3159860863
## 7
       2018 3343261288
```

We can see that salaries in 2018 were more than double the level in 2012, and increased consistently from year to year. This does not imply that the players were gettign better from season to season. Rather, this is a reflection of the growing revenues of the NBA, and the ability of players to bargain for a more or less constant share of this growing revenue.

So, if we now want to account for team performance in terms of salaries, we need to make sure we compare like with like. What \$1 million would buy in 2012 was not the same as what it would buy in 2018. It's easy to adjust for this. We simply divide the salary of each team in each season by the total spending of all teams in that season, so that we have a measure of salary spending relative to the competition.

To do this we first use left_join() to add the aggregate salaries for each season to our original dataframe:

```
NBA <- left_join(NBA, Sumsal, by="season")</pre>
head(NBA)
## # A tibble: 6 x 5
##
     Team
                                  salaries
                    season
                                                allsal
                             wpc
##
     <chr>
                     <dbl> <dbl>
                                      <dbl>
                                                 <dbl>
## 1 Atlanta Hawks
                      2012 0.606
                                  55503683 1438650614
## 2 Atlanta Hawks
                      2013 0.537
                                  60437642 1837810750
## 3 Atlanta Hawks
                      2014 0.463
                                  58841508 1976549213
## 4 Atlanta Hawks
                      2015 0.732
                                  62487671 2153667904
## 5 Atlanta Hawks
                      2016 0.585
                                  82337675 2523411764
## 6 Atlanta Hawks
                      2017 0.524 105882053 3159860863
tail(NBA)
## # A tibble: 6 x 5
##
     Team
                                       salaries
                                                     allsal
                         season
                                  wpc
##
     <chr>
                          <dbl> <dbl>
                                           <dbl>
                                                      <dbl>
## 1 Washington Wizards
                           2013 0.354
                                       58296629 1837810750
## 2 Washington Wizards
                           2014 0.537
                                       66615345 1976549213
## 3 Washington Wizards
                           2015 0.561
                                       74590100 2153667904
## 4 Washington Wizards
                           2016 0.5
                                       83380073 2523411764
## 5 Washington Wizards
                           2017 0.598 105042249 3159860863
## 6 Washington Wizards
                           2018 0.524 126304371 3343261288
```

We can now create a variable which we call 'relsal', which measures the share of team's salary spend in the total spending of all teams in that season:

```
# Here we create the variable 'relsal' for the NBA
NBA[,'relsal'] = NBA[,'salaries']/NBA[,'allsal']
head(NBA)
## # A tibble: 6 x 6
##
     Team
                   season
                                  salaries
                                               allsal relsal
                             wpc
##
     <chr>
                    <dbl> <dbl>
                                     <dbl>
                                                <dbl> <dbl>
## 1 Atlanta Hawks
                     2012 0.606
                                  55503683 1438650614 0.0386
## 2 Atlanta Hawks
                                  60437642 1837810750 0.0329
                     2013 0.537
## 3 Atlanta Hawks
                     2014 0.463
                                  58841508 1976549213 0.0298
```

```
## 4 Atlanta Hawks 2015 0.732 62487671 2153667904 0.0290

## 5 Atlanta Hawks 2016 0.585 82337675 2523411764 0.0326

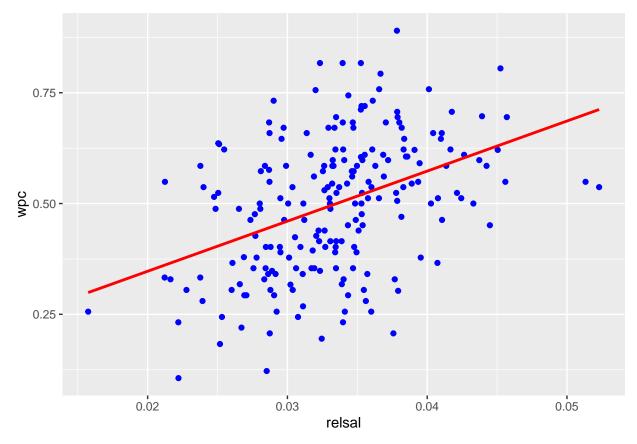
## 6 Atlanta Hawks 2017 0.524 105882053 3159860863 0.0335

tail(NBA)
```

```
## # A tibble: 6 x 6
##
     Team
                        season
                                 wрс
                                      salaries
                                                    allsal relsal
##
     <chr>
                         <dbl> <dbl>
                                          <dbl>
                                                     <dbl> <dbl>
                          2013 0.354 58296629 1837810750 0.0317
## 1 Washington Wizards
## 2 Washington Wizards
                          2014 0.537
                                      66615345 1976549213 0.0337
## 3 Washington Wizards
                          2015 0.561
                                      74590100 2153667904 0.0346
## 4 Washington Wizards
                          2016 0.5
                                       83380073 2523411764 0.0330
                          2017 0.598 105042249 3159860863 0.0332
## 5 Washington Wizards
## 6 Washington Wizards
                          2018 0.524 126304371 3343261288 0.0378
```

Before running a regression, we use ggplot() to look at the relationship between salaries and win percentage on a chart.

```
ggplot(data = NBA,aes(x = relsal,y = wpc )) + geom_point(color='blue') +
  geom_smooth(method = "lm", se = FALSE,color = "red")
```



It's clear from the data that there is a positive correlation between relsal and wpc, as shown by the regression line which regplot adds to the scatter diagram. We now run a regression

using lm() in order to derive the coefficients of the regression and other diagnostic statistics.

```
wpcsal1 lm = lm(formula = 'wpc ~ relsal', data = NBA)
wpcsal1_lm %>% summary()
##
## Call:
## lm(formula = "wpc ~ relsal", data = NBA)
##
## Residuals:
##
        Min
                       Median
                                     3Q
                                             Max
                  1Q
## -0.33885 -0.09912 -0.00710
                                0.09068
                                        0.34130
```

2.086

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

0.0382 *

6.577 3.81e-10 ***

Estimate Std. Error t value Pr(>|t|)

0.05809

1.71823

Residual standard error: 0.1405 on 208 degrees of freedom
Multiple R-squared: 0.1722, Adjusted R-squared: 0.1682
F-statistic: 43.26 on 1 and 208 DF, p-value: 3.811e-10

0.12114

11.30094

Coefficients:

(Intercept)

Signif. codes:

relsal

##

##

The first things to look at in any regression are the coefficients of the explanatory variables and their statistical significance. We can see here that the coefficient on relsal is 11.3009. This means that every one percentage (0.01) increase in the share of the team in total salaries leads to and $11.3 \times .01$ increase in win percentage - that is roughly .11, or eleven percentage points. That is a very large increase, but not that the share of salaries, as can be seen on the x axis of the chart above, ranges from around .02 (2%) to .05 (5%). Thus going from the lowest salary to the highest share (from 2% to 5%) will produce a $3 \times .11 = .33$ increase in win percentage - from around roughly 33% to 66%.

This estimate is statistically significant. The coefficient estimate is more than six times larger than its standard error (this ratio is called the t- statistic (6.577). The p-value (P>|t|) tells us the probability of observing such estimate if the true value were actually zero. The p-value here is shown as "0.000" - however, it can never be exactly zero. It is just that, in this case, it is so small that is does not register up to three decimal places. The usual standard for statistical significance is a p-value below 0.05. Clearly, in this case the estimate clearly beats that standard.

How much of the variation in team performance is captured by this relsal? We can see this from the R-squared coefficient which is 0.172, or 17.2%. Clearly, there is much else to team performance than salaries alone.

Is the coefficient estimate plausible? Our regression estimate is the best estimate we have of the effect, but only under the assumption that our regression includes all of the relevant

variables. If there are other variables which influence performance other than salary share, then our regression estimate will be biased, either upward or downward. This is the problem known as "omitted variable bias" (OVB). There is no way to be certain that OVB is not a problem, it requires good judgment and careful thought to decide on whether there are other variables that should be included.

The fact that the R-squared value was only 0.172 might give one to think that there are other factors to include, but it is always possible that the remainder is just random - the effect of luck, which no doubt plays a role in every game.

But in this case, it is possible to think of other factors that might be relevant and therefore should be included. One such is "lagged dependent variable", which here means the value of win percentage in the previous season. While the salary level should capture many aspects of team quality, salaries are not renegotiated every year, and many aspects of team quality would have been in pace in the previous season. So we can add this lagged dependent variable to our regression, and then see if this changes our estimate of the impact of salaries.

We create this variable in two stages. First, we sort the data by team, and then by season, using arrange() function.

Self test

Based on this model, what would be the win percentage of a team for whom the value of relsal was 4%?

```
NBA <- NBA %>% arrange(Team, season)
head(NBA)
## # A tibble: 6 x 6
##
     Team
                   season
                             wpc
                                  salaries
                                                allsal relsal
     <chr>
                     <dbl> <dbl>
                                                 <dbl>
##
                                     <dbl>
                                                        <dbl>
## 1 Atlanta Hawks
                     2012 0.606
                                  55503683 1438650614 0.0386
## 2 Atlanta Hawks
                     2013 0.537
                                  60437642 1837810750 0.0329
## 3 Atlanta Hawks
                     2014 0.463
                                  58841508 1976549213 0.0298
## 4 Atlanta Hawks
                     2015 0.732
                                  62487671 2153667904 0.0290
## 5 Atlanta Hawks
                     2016 0.585
                                  82337675 2523411764 0.0326
                     2017 0.524 105882053 3159860863 0.0335
## 6 Atlanta Hawks
tail(NBA)
```

```
## # A tibble: 6 x 6
##
     Team
                         season
                                  wpc
                                       salaries
                                                     allsal relsal
##
     <chr>
                                          <dbl>
                          <dbl> <dbl>
                                                      <dbl>
                                                             <dbl>
                                       58296629 1837810750 0.0317
## 1 Washington Wizards
                           2013 0.354
## 2 Washington Wizards
                           2014 0.537
                                       66615345 1976549213 0.0337
## 3 Washington Wizards
                           2015 0.561
                                       74590100 2153667904 0.0346
## 4 Washington Wizards
                           2016 0.5
                                       83380073 2523411764 0.0330
                           2017 0.598 105042249 3159860863 0.0332
## 5 Washington Wizards
```

```
2018 0.524 126304371 3343261288 0.0378
## 6 Washington Wizards
NBA <- NBA %>%
      group_by(Team)%>%
      mutate(wpc_lag = dplyr::lag(wpc))%>%
      ungroup()
head(NBA)
## # A tibble: 6 x 7
##
     Team
                  season
                            wpc salaries
                                              allsal relsal wpc_lag
##
                    <dbl> <dbl>
                                               <dbl>
                                                     <dbl>
                                                              <dbl>
     <chr>
                                    <dbl>
## 1 Atlanta Hawks
                    2012 0.606 55503683 1438650614 0.0386 NA
## 2 Atlanta Hawks
                    2013 0.537 60437642 1837810750 0.0329
                                                              0.606
## 3 Atlanta Hawks 2014 0.463 58841508 1976549213 0.0298
                                                              0.537
## 4 Atlanta Hawks 2015 0.732 62487671 2153667904 0.0290
                                                              0.463
## 5 Atlanta Hawks 2016 0.585 82337675 2523411764 0.0326
                                                              0.732
## 6 Atlanta Hawks 2017 0.524 105882053 3159860863 0.0335
                                                              0.585
tail(NBA)
## # A tibble: 6 x 7
##
     Team
                        season
                                wpc salaries
                                                   allsal relsal wpc lag
##
     <chr>>
                         <dbl> <dbl>
                                         <dbl>
                                                    <dbl> <dbl>
                                                                   <dbl>
## 1 Washington Wizards 2013 0.354 58296629 1837810750 0.0317
                                                                   0.303
## 2 Washington Wizards 2014 0.537 66615345 1976549213 0.0337
                                                                   0.354
## 3 Washington Wizards 2015 0.561 74590100 2153667904 0.0346
                                                                   0.537
## 4 Washington Wizards 2016 0.5
                                      83380073 2523411764 0.0330
                                                                   0.561
## 5 Washington Wizards
                         2017 0.598 105042249 3159860863 0.0332
                                                                   0.5
## 6 Washington Wizards
                         2018 0.524 126304371 3343261288 0.0378
                                                                   0.598
We now run our regression again, but adding wpc_lag into the regression equation:
wpcsal2 lm = lm(formula = 'wpc ~ wpc lag + relsal', data = NBA)
wpcsal2 lm %>% summary()
##
## Call:
## lm(formula = "wpc ~ wpc_lag + relsal", data = NBA)
##
## Residuals:
       Min
                      Median
                                    3Q
                                            Max
                  1Q
## -0.33064 -0.07005 0.00118 0.08533 0.26500
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
               0.12925
                           0.05444
                                     2.374
                                             0.0187 *
## (Intercept)
## wpc lag
                                     9.125
                                             <2e-16 ***
                0.60310
                           0.06609
## relsal
                2.01650
                         1.86111
                                    1.083
                                            0.2801
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1186 on 176 degrees of freedom
## (31 observations deleted due to missingness)
## Multiple R-squared: 0.4164, Adjusted R-squared: 0.4097
## F-statistic: 62.78 on 2 and 176 DF, p-value: < 2.2e-16</pre>
```

The result of this change is quite dramatic. Not only has the coefficient on relsal fallen to only 2.0165, but it is not statistically insignificant (p_value is 0.28, greater than the critical value of .05). Last year's win percentage is highly significant and the R-squared of the regression has risen to 0.416.

It is quite usual for the lagged dependent variable to be significant in situations such as these-history matters. But should we now abandon our theory that wages influence performance? One should also be cautious about a theory that relies only on the lagged dependent variable - while history matters, one should also expect there to be specific, quantifiable factors that drive history.

While the omission of the lagged dependent variable in the first regression suggests that there may have been OVB that biased the estimate upwards, there is also the possibility that OVB can bias the estimate downwards.

Clearly, not all teams are identical, while our regression estimates thus far treat each team as if it were, in the sense that spending would affect the performance of each team in the same way, and that last year's win percentage would imact this year's in the same way. In our regression specification we want to find balance between treating each team as if it were identical, and treating each team as if it were completely unique. The truth is likely to be that there are common factors affecting all teams, but that there are also idiosyncrasies. This is often described as heterogeneity.

One way we can introduce heterogeneity is through fixed effects. Fixed effects are dummy variables. For each team there is a fixed effect, equal to one if the row relates to the team in question, and zero otherwise. Each team can have its own fixed effects. Estimation of fixed effects allows us to identify differences between the teams that are independent of the impact of salaries or of the lagged dependent variable.

Adding fixed effects is very easy in R. The variable 'Team' identifies the team names, and if we add "factor(Team)" to the regression formula, R will estimate a fixed effect for each team.

We now run the regression with the lagged dependent variable and fixed effects, to see what impact this has on the estimate of the salary coefficient.

Self test

Based on this model, what would be the win percentage of a team that (a) had 0.5 win percentage last season and (b) had a value of relsal equal to 3%?

```
wpcsal3_lm <- lm(wpc ~ wpc_lag + relsal + factor(Team),</pre>
                    data = NBA)
wpcsal3 lm %>% summary()
##
## Call:
## lm(formula = wpc ~ wpc_lag + relsal + factor(Team), data = NBA)
##
## Residuals:
##
         Min
                           Median
                                         30
                    1Q
                                                  Max
                        0.002725
                                   0.063521
##
  -0.294627 -0.067238
                                             0.315694
##
## Coefficients:
##
                                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                        0.2333450
                                                                3.140
                                                                       0.00204
                                                    0.0743186
## wpc lag
                                        0.2353017
                                                    0.0854354
                                                                2.754
                                                                       0.00663
## relsal
                                        4.9387798
                                                    2.1020799
                                                                2.349
                                                                       0.02013
## factor(Team)Boston Celtics
                                        0.0178757
                                                   0.0634989
                                                                0.282
                                                                       0.77871
## factor(Team)Brooklyn Nets
                                                               -2.060
                                       -0.1430698
                                                    0.0694556
                                                                       0.04117
## factor(Team)Charlotte Bobcats
                                       -0.0254028
                                                   0.0647996
                                                               -0.392
                                                                       0.69561
## factor(Team)Chicago Bulls
                                       -0.0293438
                                                   0.0636228
                                                               -0.461
                                                                       0.64533
## factor(Team)Cleveland Cavaliers
                                        0.0063372
                                                   0.0659487
                                                                0.096
                                                                       0.92358
## factor(Team)Dallas Mavericks
                                       -0.0349739
                                                   0.0635606
                                                               -0.550
                                                                       0.58299
## factor(Team)Denver Nuggets
                                       -0.0070167
                                                    0.0634787
                                                               -0.111
                                                                       0.91214
## factor(Team)Detroit Pistons
                                                              -0.936
                                       -0.0607367
                                                    0.0649100
                                                                       0.35096
## factor(Team)Golden State Warriors
                                                    0.0638705
                                                                2.635
                                                                       0.00932
                                        0.1682771
## factor(Team)Houston Rockets
                                        0.1155091
                                                   0.0632127
                                                                1.827
                                                                       0.06968
## factor(Team)Indiana Pacers
                                       -0.0168743
                                                   0.0635887
                                                               -0.265
                                                                       0.79110
## factor(Team)Los Angeles Clippers
                                        0.0641937
                                                    0.0644623
                                                                0.996
                                                                       0.32097
## factor(Team)Los Angeles Lakers
                                       -0.1530379
                                                    0.0673842
                                                               -2.271
                                                                       0.02459
## factor(Team) Memphis Grizzlies
                                       -0.0114011
                                                    0.0640422
                                                               -0.178
                                                                       0.85895
## factor(Team)Miami Heat
                                                                0.222
                                        0.0144919
                                                    0.0653730
                                                                       0.82487
## factor(Team)Milwaukee Bucks
                                       -0.0502629
                                                    0.0643936
                                                               -0.781
                                                                       0.43632
## factor(Team)Minnesota Timberwolves -0.0782858
                                                               -1.192
                                                                       0.23509
                                                    0.0656635
## factor(Team)New Orleans Hornets
                                       -0.0585614
                                                   0.0665339
                                                               -0.880
                                                                       0.38020
## factor(Team)New York Knicks
                                       -0.1144296
                                                    0.0666855
                                                               -1.716
                                                                       0.08828
## factor(Team)Oklahoma City Thunder
                                        0.0649010
                                                    0.0642279
                                                                1.010
                                                                       0.31393
## factor(Team)Orlando Magic
                                       -0.1411094
                                                    0.0652435
                                                               -2.163
                                                                       0.03217
## factor(Team)Philadelphia 76ers
                                                               -1.797
                                       -0.1193238
                                                    0.0663928
                                                                       0.07435
## factor(Team)Phoenix Suns
                                                               -1.643
                                       -0.1058937
                                                    0.0644483
                                                                       0.10250
## factor(Team)Portland Trail Blazers
                                        0.0360544
                                                   0.0634828
                                                                0.568
                                                                       0.57094
## factor(Team)Sacramento Kings
                                                              -1.711
                                       -0.1125413
                                                    0.0657910
                                                                       0.08927
## factor(Team)San Antonio Spurs
                                        0.1328336
                                                   0.0644003
                                                                2.063
                                                                       0.04091
```

```
0.0778177 0.0635339
## factor(Team)Toronto Raptors
                                                              1.225 0.22260
## factor(Team)Utah Jazz
                                       0.0034318 0.0634856
                                                               0.054 0.95696
## factor(Team)Washington Wizards
                                      -0.0009162 0.0644252 -0.014 0.98867
##
## (Intercept)
                                      **
## wpc lag
                                      **
## relsal
## factor(Team)Boston Celtics
## factor(Team)Brooklyn Nets
## factor(Team)Charlotte Bobcats
## factor(Team)Chicago Bulls
## factor(Team)Cleveland Cavaliers
## factor(Team)Dallas Mavericks
## factor(Team)Denver Nuggets
## factor(Team)Detroit Pistons
## factor(Team)Golden State Warriors
## factor(Team)Houston Rockets
## factor(Team)Indiana Pacers
## factor(Team)Los Angeles Clippers
## factor(Team)Los Angeles Lakers
## factor(Team)Memphis Grizzlies
## factor(Team)Miami Heat
## factor(Team)Milwaukee Bucks
## factor(Team)Minnesota Timberwolves
## factor(Team)New Orleans Hornets
## factor(Team)New York Knicks
## factor(Team)Oklahoma City Thunder
## factor(Team)Orlando Magic
## factor(Team)Philadelphia 76ers
## factor(Team)Phoenix Suns
## factor(Team)Portland Trail Blazers
## factor(Team)Sacramento Kings
## factor(Team)San Antonio Spurs
## factor(Team)Toronto Raptors
## factor(Team)Utah Jazz
## factor(Team)Washington Wizards
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1094 on 147 degrees of freedom
     (31 observations deleted due to missingness)
## Multiple R-squared: 0.5851, Adjusted R-squared: 0.4976
## F-statistic: 6.686 on 31 and 147 DF, p-value: 5.878e-16
```

There are 30 fixed effects listed in the output, one for each team. A positive fixed effect means

that in some way the team was able to perform above average, and a negative fixed effect implies below average performance. However, most of the fixed effects are not statistically significant. The significant fixed effects are: The Brooklyn Nets (negative), the Golden State Warriors (positive), The LA Lakers (negative), Orlando Magic (negative), San Antonio Spurs (positive).

Looking at our main variable of interest, relsal, it is clear that this variable is once again statistically significant with the addition of the fixed effects. Thus, we might conclude that the absence of the fixed effects biased the coefficient estimate downwards. The coefficient is statistically significant at the 5% level, and the value of 4.9388 implies that increasing salary share in the NBA by 1 percentage point (e.g. from 2% to 3%) will lead to an increase in win percentage of almost 5%. This is smaller than our original estimate, but also because of the presence of the lagged dependent variable, spending which increases win percentage this season will also have an effect, albeit a smaller one, on the following season. Indeed, an increase in spending today will create a ripple effect which will be discernible in performance for a number of years into the future.

Also note that the size of the lagged dependent variable is smaller once we add the fixed effects. Finally, with this third specification the R-squared of the regression has now risen to 0.585 (close to 60%), which accounts for significant fraction of the overall variation.

We should never expect to explain 100% of the variation of outcomes in sport - if we could do that then each game would be perfectly predictable - and then what would be the point of watching?

Self test

Run the regression of win percentage on relsal with fixed effects but without the lagged depedent variable. Compare your output results. Compare this to the previous three regressions. Which do you think is the best representation of the data. Why?

Conclusion

In this notebook we have explored the possibility of using regression analysis to explore the validity of a causal explanation of team success. That causal explanation was itself not derived from the data, but based on a theory that player quality will be reflected in salaries and therefore salaries will predict team success.

You might be wondering about why this works at all with the NBA, since the league operates a salary cap system which is intended to equalize resources among the teams. If each team spent the same amount of money on players, our theory predicts that each team can expect to win 50% of its games, and team performances will vary randomly around this mean. However, the NBA cap is a "soft cap", meaning that there are many exemptions, so teams spend varying amounts in reality. Some leagues, such as the NFL, operate a hard cap, which strictly prohibit spending above the cap. The NFL also has a salary floor, which prevents teams from

spending a lot less than average. When looking at NFL data, therefore, it is much harder to identify the effect of wage spending on performance.

We next turn to look at the salary performance relationship in the English Premier League.