
LECTURE 5

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1 Degree of polynomials in fields

$K[x]/f(x)$ where $f(x)$ is irreducible. What is $[L : K]$? where $d = \deg f(x)$

$$1, \bar{x}, \bar{x}^2, \dots, \bar{x}^{d-1} \quad \text{basis for } L$$

$$\bar{1} = 1 + \langle f \rangle$$

$$\bar{x} = x + \langle f \rangle \quad \text{spn } L \text{ over } K$$

$$K[x]/\langle f \rangle \text{ is isomorphic to } L$$