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**intermediate value theorem**

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## 1 Conway base 13 function

## 2 some case functions

$f(x) = 1$  for some  $x$  in  $\mathbb{Q}$  and  $0$  for some  $x$  in  $\mathbb{Q}$

$$f(x) = \begin{cases} 1 & \text{if } x \in \mathbb{Q} \\ 0 & \text{if } x \notin \mathbb{Q} \end{cases}$$

is it continuous? prove  $f$  not continuous anywhere

*Proof.* discontinuous at  $x$  if  $\exists \epsilon > 0$  such that  $\forall \delta > 0$  there exists  $y$  such that  $|x - y| < \delta$  and  $|f(x) - f(y)| \geq \epsilon$  □