EECS 498: Reinforcement Learning Homework 3 Responses

Tejas Jha tjha

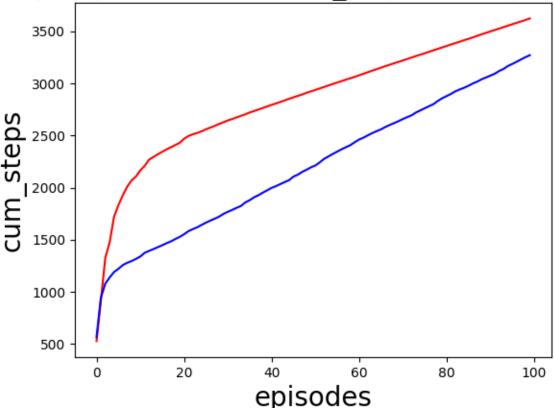
November 5, 2018

This document includes my responses to Homework 3 questions. Responses that involved the use of coding will provide references to specific lines of code to provide a better overview of how the problem was approached. The code can either be referenced in the Appendix or in the accompanied python script submitted with this assignment.

Question 1

(a) The dynaq algorithm was implemented following the pseudocode shown on page 164 of the textbook. In the below plot, the red curve corresponds to the use the Q-learning algorithm and the blue curve represents the use of dynaq algorithm. As can be seen by the images, there curve for dynaq appears to apprach a constant slope earlier than the curve for Q-learning, indicating a faster approach towards an optimal policy with the optimal number of steps required in an episode to reach the terminal state.

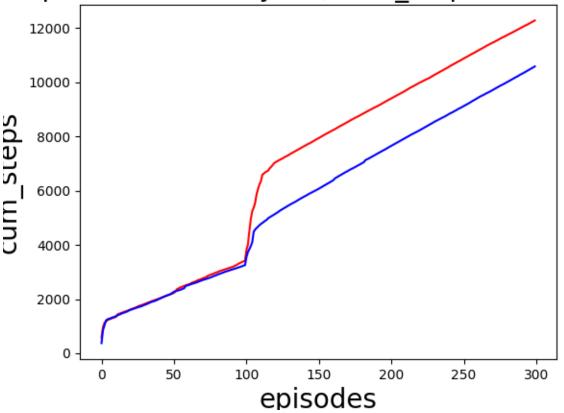
Dynaq and Q-learn cum_steps over episodes



(b) In the case where the environment switches from "Taxi-v4" to "Taxi-v5" after the initial 100 episodes, the length of each episode drastically increased as the algorithm needed more iterations to adjust the model and action-values to the new environment. As the algorithm was able to iterate and better learn the new environment, the length of each episode begins to converge to a constant as represented by a straight line. In order to better account for the change in the environment, I have modified the use of the algorithm to use a lower discount rate (γ) . In my case, I used a discout factor of 0.5, which would help in a faster adjustment to the new environment by reducing the weight placed on already learned Q values. As a result, the algorithm is affected less by future expected returns and more by the immediate rewards, which greatly boosts immediate learning to a changing environment. Note that a similar change can be seen by decreasing alpha, the step size, as well as a combination of both.

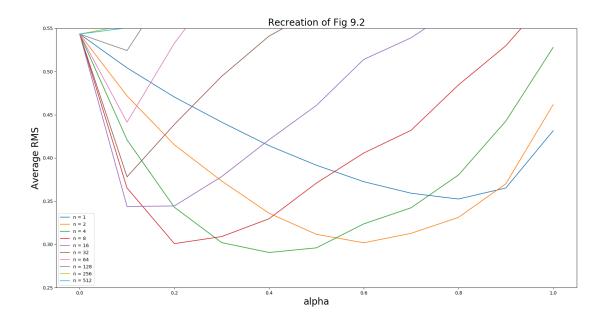
The plot below displays this difference with the two curves. The red curve is the original algorithm prom part (a) reacting to the change in the environment. The blue curve represents the modified algorithm as described above.

naq and Modified DynaQ cum_steps over episo



Question 2

Below is the plot produced in an attempt to reproduce the right plot in Figure 9.2 of the textbook.



Appendix: Relevant Code - tjha.py

```
1 # Tejas Jha
2 # 5 November 2018
3 # EECS 498 — Reinforcement Learning HW 3
4 #
5 #
```

- 6 # The code below implements a modified version of "Tabular Dyna-Q" as well as
- 7 # implementation modifications to adapt to changes in the environemnt faster.
- 8 # This file also contains the code used to implement n-step semi-gradient TD estimation
- 10 # The functions below expand on the starter code provided that help generate the
- 11 # states, actions, and rewards using Taxi-v4 and Taxi-v5 on openAi gym 12 #
- 13
 14 import numpy as np
 15 import gym
 16 import copy
 17 import mytaxi

```
18 import math
19 import matplotlib.pyplot as plt
20
21 # Environment for Taxi-v4
22 ENV4 = gym. make('Taxi-v4'). unwrapped
23 # Einvironment for Taxi-v5
24 \text{ ENV5} = \text{gym.make}('Taxi-v5').unwrapped
25 # Possible actions that can be taken
26 \text{ ACTIONS} = [0, 1, 2, 3, 4, 5]
27
28 # Helpers to choose best action given probability distributions
29 \operatorname{def}_{-\operatorname{greedy}}(Q, s):
        qmax = np.max(Q[s])
30
31
        actions = []
32
        for i,q in enumerate(Q[s]):
33
            if q == qmax:
34
                 actions.append(i)
35
        return actions
36
37
   def greedy (Q, s):
38
        return np.random.choice(_greedy(Q,s))
39
40
   def ep_greedy (Q, s, ep):
41
        if np.random.rand() < ep:</pre>
42
            return np.random.choice(len(Q[s]))
43
        else:
44
            return greedy (Q, s)
45
46 \# Part(a) - Tabular Dyna-Q:
47 # Function implementation of dynag to handle the stochastic nature of
       the environment
48 # returns Q and cum_steps - list of the cumulatative number of steps
       counted from the
49 # first episode to the end of each episode.
50 def dynaq (env, n=10, gamma=1, alpha=1, epsilon=0.1, runs=1, episodes=100):
        for run in range(runs):
51
            # Update kept on cumulative number of steps
52
53
            cum_steps = np.zeros(episodes)
            Q = np.zeros((env.nS,env.nA))
54
            # Using deterministic model
55
56
            Model = \{\}
            for s in range(env.nS):
57
58
                 Model[s] = \{\}
59
                 for a in range (env.nA):
60
                     Model[s][a] = (-1, s)
61
            # Loop over episodes
62
            for idx in range(episodes):
                 visited_states = []
63
```

```
64
                  taken\_actions = \{\}
 65
                  s = env.reset()
                  visited_states.append(s)
 66
                  done = False
 67
 68
                  counter = 0
                  while not done:
 69
 70
                      a = ep_greedy(Q, s, epsilon)
71
                      if s in taken_actions:
72
                           if a not in taken_actions[s]:
73
                               taken_actions[s].append(a)
74
                      else:
75
                           taken_actions[s] = []
 76
                           taken_actions[s].append(a)
77
                      ss, r, done, = env.step(a)
 78
                      Q[s,a] = Q[s,a] + alpha * (r + gamma * np.max(Q[ss]) -
                         Q[s,a]
79
                      Model[s][a] = (r, ss)
 80
                      s = ss
 81
                      for i in range(n):
 82
                           rand_s = np.random.choice(visited_states, size=1)
                           rand_s = rand_s[0]
 83
                           rand_a = np.random.choice(taken_actions[rand_s],
 84
                              size = 1)
 85
                           rand_a = rand_a[0]
 86
                           tup = Model[rand_s][rand_a]
87
                           Q[rand_s, rand_a] = Q[rand_s, rand_a] + alpha * (tup)
                              [0] + \operatorname{gamma} * \operatorname{np.} \operatorname{max}(Q[\operatorname{tup}[1]]) - Q[\operatorname{rand}_s],
                              rand_a])
 88
                      counter += 1
 89
                      visited_states.append(s)
 90
                  if idx == 0:
 91
                      cum_steps[idx] = counter
 92
                  else:
 93
                      cum_steps[idx] = counter + cum_steps[idx - 1]
 94
         return Q, cum_steps
95
 96 # Part (a) — adaptation of qlearn from hw2 to compare with Tabular Dyna
97 # Key difference is 100 episodes instead of 500 by default
98 # Also, steps are now everaged through multiple callings of function
    def qlearn (env, gamma=1, alpha=0.9, ep=0.05, runs=1, episodes=100):
99
         #np.random.seed(3)
100
         \#env.seed(5)
101
         nS = env.nS
102
103
         nA = env.nA
104
         rew_alloc = []
105
         for run in range(runs):
106
             Q = np.zeros((nS,nA))
```

```
107
             rew_list = np.zeros(episodes)
108
             cum_steps = np.zeros(episodes)
109
             for idx in range(episodes):
                 s = env.reset()
110
                 done = False
111
                 counter = 0
112
113
                 cum_rew = 0
114
                 while not done:
                     a = ep_greedy(Q, s, ep)
115
116
                     ss, r, done, = env.step(a)
                     O[s,a] = O[s,a] + alpha * (r + gamma * np.max(O[ss]) -
117
                        O[s,a]
118
                     s = ss
119
                     cum_rew += gamma**counter * r
120
                     counter += 1.
                 rew_list[idx] = cum_rew
121
122
                 if idx == 0:
123
                     cum_steps[idx] = counter
124
                 else:
                     cum_steps[idx] = counter + cum_steps[idx - 1]
125
             rew_alloc.append(rew_list)
126
         rew_list = np.mean(np.array(rew_alloc), axis=0)
127
128
        return Q, cum_steps
129
130 # Modified versions of the algorithms above for usage in random change
       to v5 environment after 100 episodes
    \mathbf{def} original_dynaq (env1, env2, n=10,gamma=1,alpha=1,epsilon=0.1,runs=1,
131
       episodes = 300):
        for run in range(runs):
132
133
             # Update kept on cumulative number of steps
134
             cum_steps = np.zeros(episodes)
            Q = np.zeros((env1.nS,env1.nA))
135
136
             # Using deterministic model
137
             Model = \{\}
             for s in range(env1.nS):
138
                 Model[s] = \{\}
139
                 for a in range(env1.nA):
140
141
                     Model[s][a] = (-1, s)
142
             env = env1
143
             # Loop over episodes
             for idx in range(episodes):
144
                 if idx == 100:
145
                     env = env2
146
                 visited_states = []
147
148
                 taken_actions = \{\}
149
                 s = env.reset()
150
                 visited_states.append(s)
151
                 done = False
```

```
152
                  counter = 0
153
                  while not done:
154
                      a = ep_greedy(Q, s, epsilon)
155
                      if s in taken_actions:
                           if a not in taken_actions[s]:
156
157
                               taken_actions[s].append(a)
158
                      else:
159
                           taken_actions[s] = []
160
                           taken_actions[s].append(a)
161
                      ss, r, done, = env.step(a)
162
                      Q[s,a] = Q[s,a] + alpha * (r + gamma * np.max(Q[ss]) -
                         O[s,a]
                      Model[s][a] = (r, ss)
163
164
                      s = ss
165
                      for i in range(n):
                           rand_s = np.random.choice(visited_states, size=1)
166
167
                           rand_s = rand_s[0]
                           rand_a = np.random.choice(taken_actions[rand_s],
168
                              size = 1)
169
                           rand_a = rand_a[0]
                           tup = Model[rand_s][rand_a]
170
                          Q[rand_s, rand_a] = Q[rand_s, rand_a] + alpha * (tup)
171
                              [0] + \operatorname{gamma} * \operatorname{np.max}(Q[\operatorname{tup}[1]]) - Q[\operatorname{rand_s}],
                              rand_a 1)
172
                      counter += 1
173
                      visited_states.append(s)
174
                  if idx == 0:
175
                      cum_steps[idx] = counter
176
                  else:
177
                      cum_steps[idx] = counter + cum_steps[idx - 1]
178
         return Q, cum_steps
179
180
    # Modified improvement for dynag to account for environment change
181
    def modified_dynaq (env1, env2, n=10,gamma=0.5, alpha=1, epsilon=0.1, runs
       =1, episodes =300):
         for run in range(runs):
182
             # Update kept on cumulative number of steps
183
184
             cum_steps = np.zeros(episodes)
             Q = np.zeros((env1.nS,env1.nA))
185
             # Using deterministic model
186
187
             Model = \{\}
             for s in range(env1.nS):
188
189
                 Model[s] = \{\}
190
                  for a in range(env1.nA):
191
                      Model[s][a] = (-1, s)
192
             env = env1
193
             # Loop over episodes
194
             for idx in range(episodes):
```

```
195
                 if idx == 100:
196
                     env = env2
197
                 visited_states = []
198
                 taken\_actions = \{\}
                 s = env.reset()
199
200
                 visited_states.append(s)
201
                 done = False
202
                 counter = 0
203
                 while not done:
204
                     a = ep_greedy(Q, s, epsilon)
                     if s in taken_actions:
205
206
                          if a not in taken_actions[s]:
207
                              taken_actions[s].append(a)
208
                     else:
209
                          taken_actions[s] = []
210
                          taken_actions[s].append(a)
211
                     ss, r, done, = env.step(a)
212
                     Q[s,a] = Q[s,a] + alpha * (r + gamma * np.max(Q[ss]) -
                        Q[s,a]
213
                     Model[s][a] = (r, ss)
214
                     s = ss
215
                     for i in range(n):
216
                          rand_s = np.random.choice(visited_states, size=1)
217
                          rand_s = rand_s[0]
218
                          rand_a = np.random.choice(taken_actions[rand_s],
                             size = 1)
219
                          rand_a = rand_a[0]
220
                          tup = Model[rand_s][rand_a]
                         Q[rand_s, rand_a] = Q[rand_s, rand_a] + alpha * (tup)
221
                             [0] + gamma * np.max(Q[tup[1]]) - Q[rand_s],
                             rand_a 1)
222
                     counter += 1
223
                     visited_states.append(s)
224
                 if idx == 0:
225
                     cum_steps[idx] = counter
226
                 else:
227
                     cum_steps[idx] = counter + cum_steps[idx - 1]
228
        return Q, cum_steps
229
230
    class ValueFunction:
        def __init__(self, num_of_groups):
231
             self.num_of_groups = num_of_groups
232
233
             self.group_size = 1000 // num_of_groups
             self.params = np.zeros(num_of_groups)
234
235
236
        def value (self, state):
             if state in [0,1001]:
237
238
                 return 0
```

```
239
             group\_index = (state - 1) // self.group\_size
240
             return self.params[group_index]
241
242
        def update (self, delta, state):
             group\_index = (state - 1) // self.group\_size
243
244
             self.params[group_index] += delta
245
246
    def get_action():
247
        if np.random.binomial(1, 0.5) == 1:
248
             return 1
249
        return -1
250
    def step(state, action):
251
         step = np.random.randint(1, 100 + 1)
252
253
         step *= action
254
         state += step
255
         state = max(min(state, 1001), 0)
256
         if state == 0:
257
             reward = -1
         elif state == 1001:
258
259
             reward = 1
260
         else:
261
             reward = 0
262
        return state, reward
263
264 # other
    def randomWalk2(value_function, n, alpha):
265
         state = 500
266
         states = [state]
267
268
        rewards = [0]
269
        time = 0
270
271
        # the length of this episode
272
        T = float('inf')
273
        while True:
274
             # go to next time step
             time += 1
275
276
             if time < T:
277
278
                 # choose an action randomly
279
                 action = get_action()
                 next_state , reward = step(state , action)
280
281
                 # store new state and new reward
282
283
                 states.append(next_state)
284
                 rewards.append(reward)
285
286
                 if next_state in [0, 1001]:
```

```
287
                     T = time
288
289
             # get the time of the state to update
290
             update\_time = time - n
             if update_time >= 0:
291
292
                 returns = 0.0
293
                 # calculate corresponding rewards
294
                 for t in range(update_time + 1, min(T, update_time + n) +
                    1):
295
                     returns += rewards[t]
296
                 # add state value to the return
297
                 if update_time + n <= T:</pre>
                     returns += value_function.value(states[update_time + n
298
                         1)
299
                 state_to_update = states[update_time]
300
                 # update the value function
301
                 if not state_to_update in [0,1001]:
                     delta = alpha * (returns - value_function.value(
302
                         state_to_update))
                     value_function.update(delta, state_to_update)
303
             if update_time == T - 1:
304
                 break
305
306
             state = next_state
307
308
309
    if __name__ == '__main__':
310
311
        # Part (a)
        print ("Training _ using _ Tabular _ Dyna-Q_ for _ 100 _ episodes _ using _ Taxi-v4
312
313
        # Average results over 20 runs
314
        dynaq_Qavg = 0
315
        qlearn_Q_avg = 0
316
317
        dynaq_cum_steps_avg = np.zeros(shape=(100,))
        qlearn_cum_steps_avg = np.zeros(shape=(100,))
318
319
320
        for i in range (20):
             print("Performing_run:_" + str(i + 1))
321
             # Randomize seeds so runs are independent
322
             np.random.seed(i)
323
            ENV4. seed (i)
324
             _{-}, dynaq_cum_steps = dynaq(ENV4)
325
             _, qlearn_cum_steps = qlearn(ENV4)
326
327
             # Update averages
328
             \#dynaq_Q_avg += dynaq_Q / 20.0
329
             \#qlearn_Q_avg += qlearn_Q / 20.0
330
             dynaq_cum_steps_avg += np.divide(dynaq_cum_steps, 20.0)
```

```
331
            qlearn_cum_steps_avg += np.divide(qlearn_cum_steps, 20.0)
332
333
        # Compare results with O learning implementation used in hw2 in
334
        # Generate plots for Question 1 Part(a)
335
        episodes = np.arange(len(qlearn_cum_steps_avg))
        plt.plot(episodes, qlearn_cum_steps_avg, 'r')
336
        plt.plot(episodes, dynaq_cum_steps_avg, 'b')
337
        plt.xlabel("episodes", fontdict={'fontname':'DejaVu_Sans', 'size':'
338
           20'})
339
        plt.ylabel("cum_steps", fontdict={'fontname': 'DejaVu_Sans', 'size':
            '20'})
        plt.title("Dynaq_and_Q-learn_cum_steps_vs._episodes", fontdict={'
340
           fontname': 'DejaVu_Sans', 'size': '20'})
        plt.savefig("Figure1")
341
342
343
344
        dynaq_cum_steps_avg1 = np.zeros(shape=(300,))
345
        dynaq_cum_steps_avg2 = np.zeros(shape=(300,))
346
        for i in range(5):
            print("Performing_run:_" + str(i + 1))
347
            # Randomize seeds so runs are independent
348
349
            np.random.seed(i)
            ENV4. seed(i)
350
351
            ENV5. seed(i)
            _, dynaq_cum_steps1 = original_dynaq (ENV4, ENV5)
352
            _, dynaq_cum_steps2 = modified_dynaq(ENV4, ENV5)
353
            # Update averages
354
            \#dynaq_Q_avg += dynaq_Q / 20.0
355
356
            \#qlearn_Q_avg += qlearn_Q / 20.0
            dynaq_cum_steps_avg1 += np.divide(dynaq_cum_steps1, 5.0)
357
358
            dynaq_cum_steps_avg2 += np.divide(dynaq_cum_steps2, 5.0)
359
360
        episodes = np.arange(len(dynaq_cum_steps_avg1))
361
        plt.plot(episodes, dynaq_cum_steps_avg1, 'r')
        plt.plot(episodes, dynaq_cum_steps_avg2, 'b')
362
        plt.xlabel("episodes", fontdict={'fontname':'DejaVu_Sans', 'size':'
363
           20'})
        plt.ylabel("cum_steps", fontdict={'fontname': 'DejaVu_Sans', 'size':
364
            '20'})
        plt.title("Original/Modified_DynaQ_cum_steps_vs._episodes",
365
           fontdict={'fontname': 'DejaVu_Sans', 'size': '20'})
366
        plt.savefig("Figure2")
367
        plt.figure(figsize = (20,10))
368
369
        alphas = np.arange(0, 1.1, 0.1)
370
        ns = np.power(2, np.arange(0, 10))
371
        tsv = np.load('trueStateValue.npy')
```

```
372
373
        print(ns)
374
        print(alphas)
375
376
        # # dynaq_cum_steps_avg = np.zeros(shape=(100,))
377
        # # episodes = np.arange(len(dynaq_cum_steps_avg))
378
        # # for n in ns:
379
        # #
                 print(n)
380
        # #
                 lab = "n=" + str(n)
381
        # #
                 errorset = []
                 for alph in alpha:
382
        # #
        # #
383
                     print(alph)
384
        # #
                     rms = randomWalk(alph, n, tsv)
385
        # #
                     errorset.append(rms)
386
        # #
                 plt.plot(alpha, errorset, label=lab)
        # #
                 break
387
388
        # # plt.legend(bbox_to_anchor = (1.05, 1), loc = 2, borderaxespad = 0.)
        # # plt. savefig("FigureX")
389
390
391
392
        #track the errors for each (step, alpha) combination
393
        errors = np.zeros((len(ns), len(alphas)))
394
        for run in range (100):
395
            for step_ind, n in zip(range(len(ns)), ns):
                 for alpha_ind , alpha in zip(range(len(alphas)), alphas):
396
397
                     # we have 20 aggregations in this example
                     value_function = ValueFunction(20)
398
399
                     for ep in range (0, 10):
                         randomWalk2(value_function, n, alpha)
400
401
                         # calculate the RMS error
402
                         state_value = np.asarray([value_function.value(i)
                             for i in np.arange(1, 1001)])
403
                         errors [step_ind, alpha_ind] += np.sqrt(np.sum(np.
                            power(state_value - tsv[1: -1], 2)) / 1000)
404
            print(run)
405
        # take average
        errors /= 10 * 100
406
407
        # truncate the error
408
        for i in range(len(ns)):
             plt.plot(alphas, errors[i, :], label='n=' + str(ns[i]))
409
        plt.xlabel("alpha", fontdict={'fontname': 'DejaVu_Sans', 'size': '20'
410
           })
        plt.ylabel("Average_RMS", fontdict={'fontname':'DejaVu_Sans', 'size
411
            ':'20'})
412
        plt.title("Recreation_of_Fig_9.2", fontdict={'fontname':'DejaVu_
           Sans', 'size':'20'})
413
        plt.ylim ([0.25, 0.55])
414
        plt.legend()
```

plt.savefig("FigureY")