

## Lab 05 Systems and mixed FEM (step-20)

### Computational Methods for PDEs Summer School 2019

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1. The topic of this lab session is a version of step-20. The original program with documentation can be found here: [https://www.dealii.org/current/doxygen/deal.II/step\\_20.html](https://www.dealii.org/current/doxygen/deal.II/step_20.html)
2. After running the program, open the solution and inspect the three different variables of the solution ( $u_x$ ,  $u_y$ ,  $p$ ). Then visualize the velocity as a vector field using the “Glyph” filter.
3. To check convergence rates for  $h$  going to zero, go into `run()` and implement a loop that repeatedly assembles, solves, and refines the mesh globally.  
You probably want to move the call to `hyper_cube()` in `make_grid_and_dofs()` outside this new for loop.
4. With this, run the program for RT0, RT1, and RT2 and check the L2 errors. Verify that the convergence rates make sense.
5. Now change the permeability field to the random field discussed in [https://www.dealii.org/current/doxygen/deal.II/step\\_20.html#Morerealisticpermeabilityfields](https://www.dealii.org/current/doxygen/deal.II/step_20.html#Morerealisticpermeabilityfields).  
Why do the errors not converge anymore?