## Lab 04 Convergence and computing errors (step-4)

## Computational Methods for PDEs Summer School 2019

- 1. The topic of this lab session is a **modified** version of step-4 made available for you <a href="https://www.dealii.org/current/doxygen/deal.II/step\_4.html">https://www.dealii.org/current/doxygen/deal.II/step\_4.html</a>
- 2. For more information about computing errors see step-7 (it is a bit more complicated though) https://www.dealii.org/current/doxygen/deal.II/step\_7.html
- 3. Run the program and check the graphical and text output. Note that the L2 errors are not converging. Where is the right-hand side defined and where do the boundary conditions come from?
- 4. Fix the right-hand side and boundary conditions to get the manufactured solution

$$u(x) = \sin(\pi x) \cdot \cos(\pi y)$$

and make sure the L2 errors are converging.

- 5. Increase the polynomial degree of the finite element space and check the convergence rates of the L2 error.
- 6. Implement the computation of the H1 error. For this you need to compute the gradient of the manufactured solution and implement it (see commented out code for a start).
- 7. Bonus: Implement a suitable 3d manufactured solution and test the convergence.