

Using Euclidean proofs

$$|CD|^2 = |AC|^2 + |AD|^2 + 2*|AC|*|AD| \text{ (prop 2.4)}$$

$$|CB|^2 = |CD|^2 + |DB|^2 \text{ (prop 1.47)}$$

$$|AB|^2 = |AD|^2 + |DB|^2 \text{ (prop 1.47)}$$

C

$$|CB|^2 = |AC|^2 + |AD|^2 + 2*|AC|*|AD| + |DB|^2$$

$$|CB|^2 = |AC|^2 + |AB|^2 + 2*|AC|*|AD|$$

In Trigonometry

$$|CB|^2 = |AC|^2 + |AB|^2 + 2*|AC|*|AB|\cos(\pi - \alpha)$$

$$|CB|^2 = |AC|^2 + |AB|^2 + 2*|AC|*|AB|(-\cos(\alpha))$$

$$|CB|^2 = |AC|^2 + |AB|^2 - 2*|AC|*|AB|\cos(\alpha)$$

In Vector

$$|CB|^2 = (AC - AB)^2$$

$$|CB|^2 = |AC|^2 + |AB|^2 - 2*|AC|*|AB|\cos(\alpha)$$

$$(AC - AB)^2 = |AC|^2 + |AB|^2 - 2*|AC|*|AB|\cos(\alpha)$$

$$(AC - AB)(AC - AB) = |AC|^2 + |AB|^2 - 2*|AC|*|AB|\cos(\alpha)$$

$$AC^2 + AB^2 - 2*AC*AB = |AC|^2 + |AB|^2 - 2*|AC|*|AB|\cos(\alpha)$$

$$AC*AB = |AC|*|AB|\cos(\alpha)$$

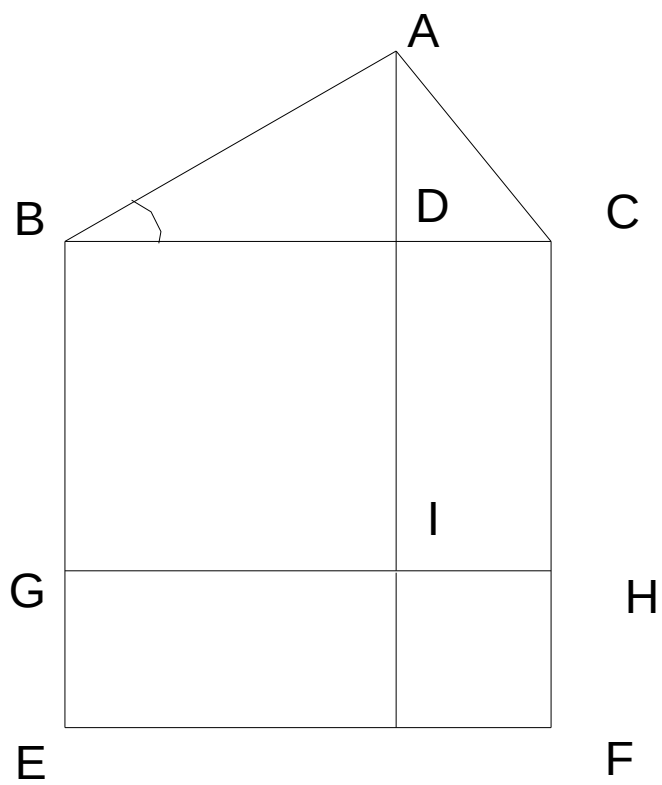
What is $AC*AB$?

$$AC*AB = |AC|*|AB|\cos(\alpha) = -|AC|*|AD|$$

$$AD = AB*\cos(\pi - \alpha)$$

What is AD ?

$$\text{How come } |AC| * |AD| = C_x * B_x + C_y * B_y$$



$$CB^2 + BD^2 = 2 \cdot CB \cdot BD + CD^2 \text{ (prop 2.7)}$$

$$AB^2 = BD^2 + DA^2$$

$$AC^2 = DC^2 + DA^2$$

$$CB^2 = DB^2 + DC^2 + 2 \cdot DB \cdot DC$$

$$DC^2 = CB^2 + BD^2 - 2 \cdot CB \cdot BD$$

$$DA^2 = AB^2 - BD^2$$

$$AC^2 = CB^2 + BD^2 - 2 \cdot CB \cdot BD + AB^2 - BD^2$$

$$AC^2 = CB^2 + AB^2 - 2 \cdot CB \cdot BD$$