

Root Finding: Redlich-Kwong Equation

The Redlich-Kwong equation of state is given by:

$$p = \frac{RT}{v - b} - \frac{a}{v(v + b)\sqrt{T}}$$

where R = gas constant, T = absolute temperature (K), p = absolute pressure (kPa), and v = specific volume (m^3/kg). The parameters a and b are calculated by:

$$a = 0.427 \frac{R^2 T_c^{2.5}}{p_c}, \quad b = 0.0866 R \frac{T_c}{p_c}$$

For methane, $R = 0.518 \text{ kJ}/(\text{kg}\cdot\text{K})$, and the critical pressure and temperature are $p_c = 4580 \text{ kPa}$, and $T_c = 191 \text{ K}$ respectively. As a chemical engineer, you are asked to determine the amount of methane fuel that can be held in a $V=3 \text{ m}^3$ tank at a temperature of 223 degrees K with a pressure of 65,000 kPa.

- Estimate v using the graphical method.
- Estimate v using `fzero()`.
- Compare the specific volume using the Redlich-Kwong equation of state to the ideal gas law $Pv=RT$. Are the results similar?