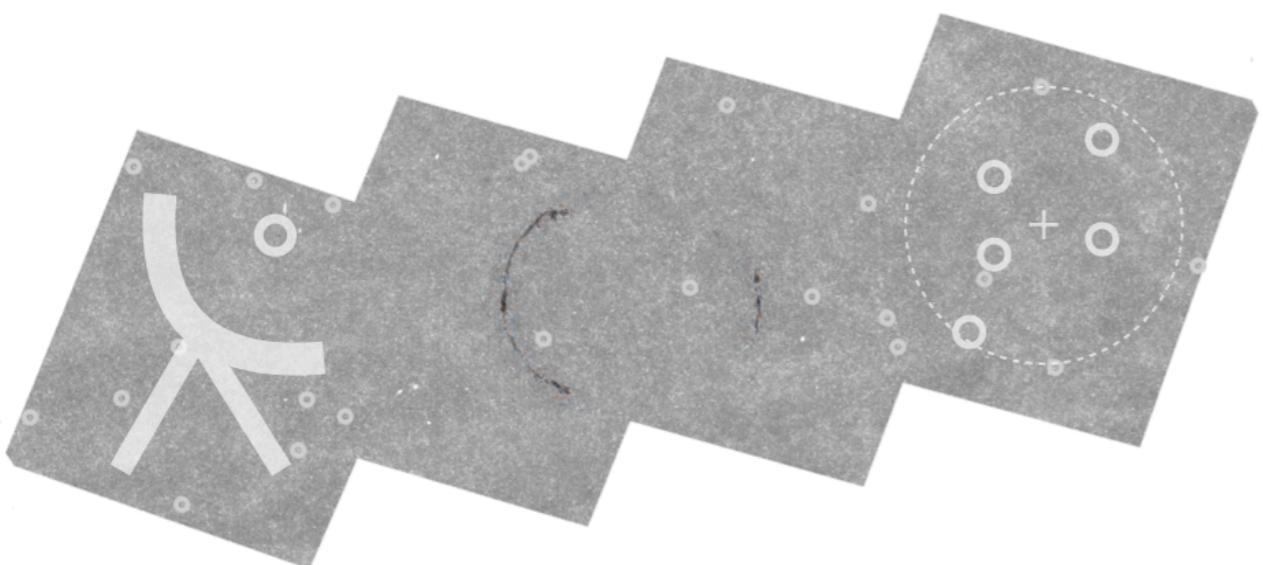


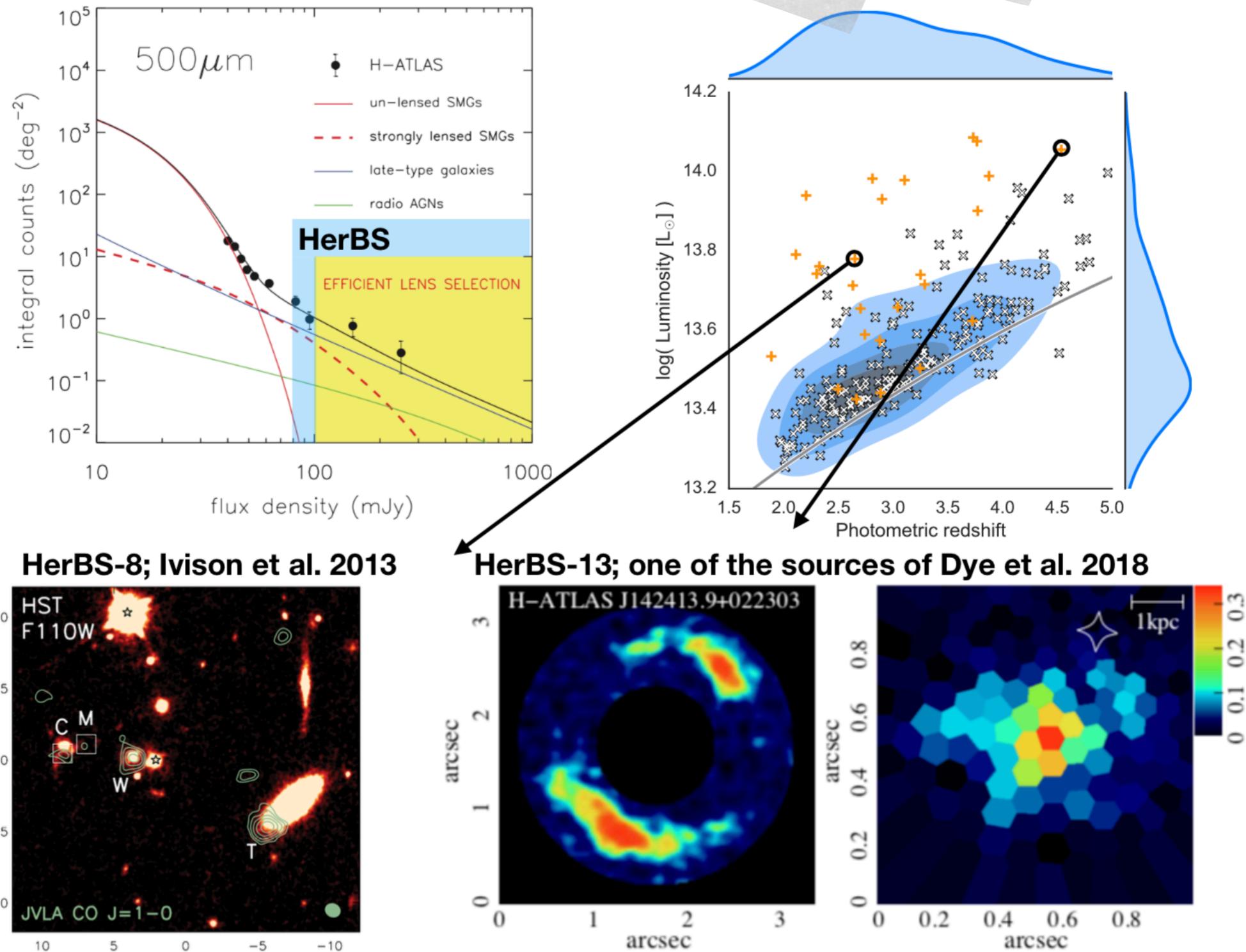
How many gravitational lenses did Herschel detect?

*Optical and near-infrared counterparts
to sub-mm sources*

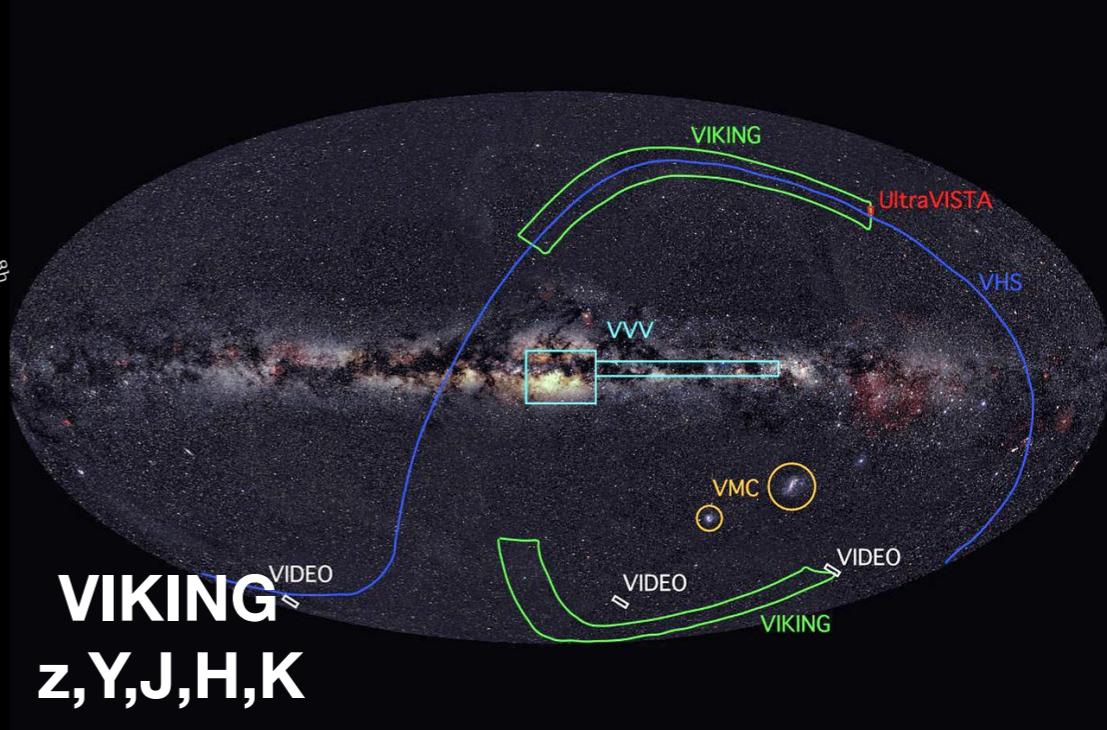
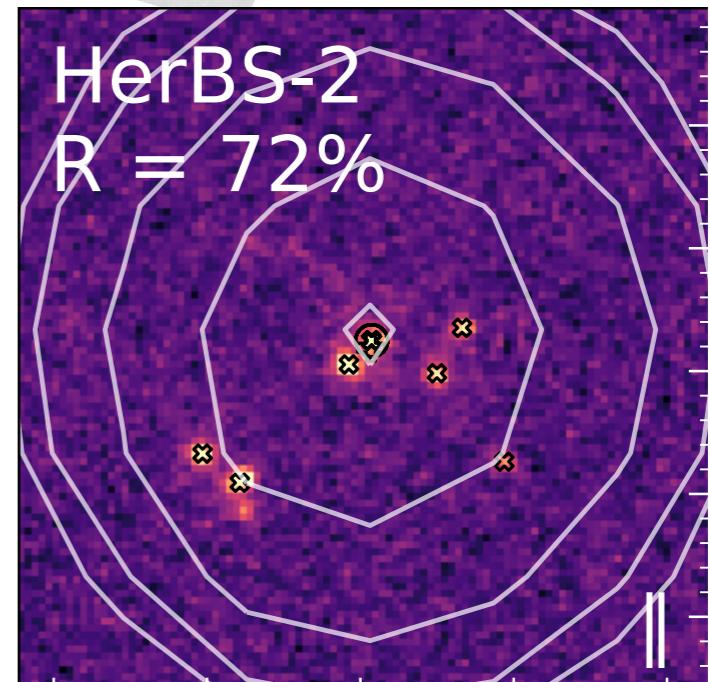
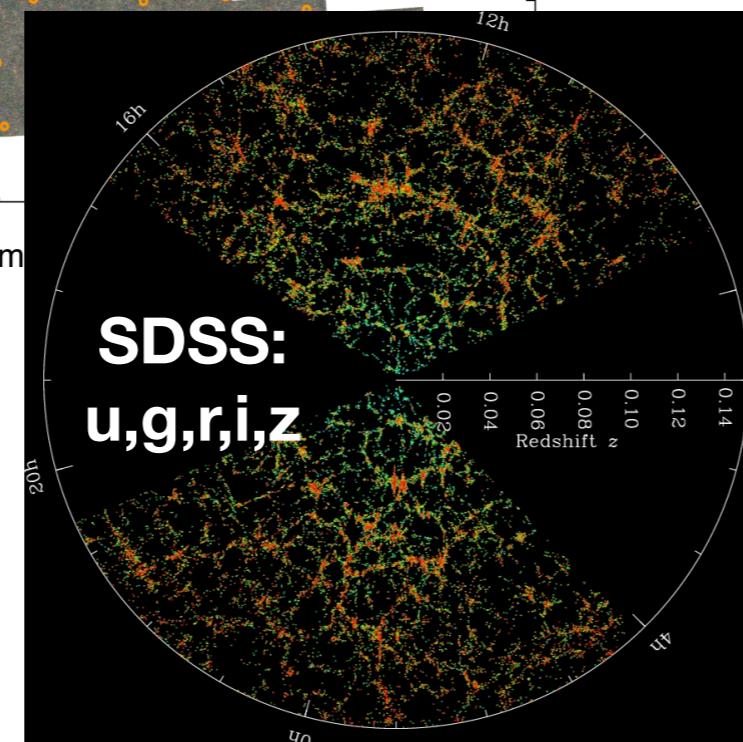
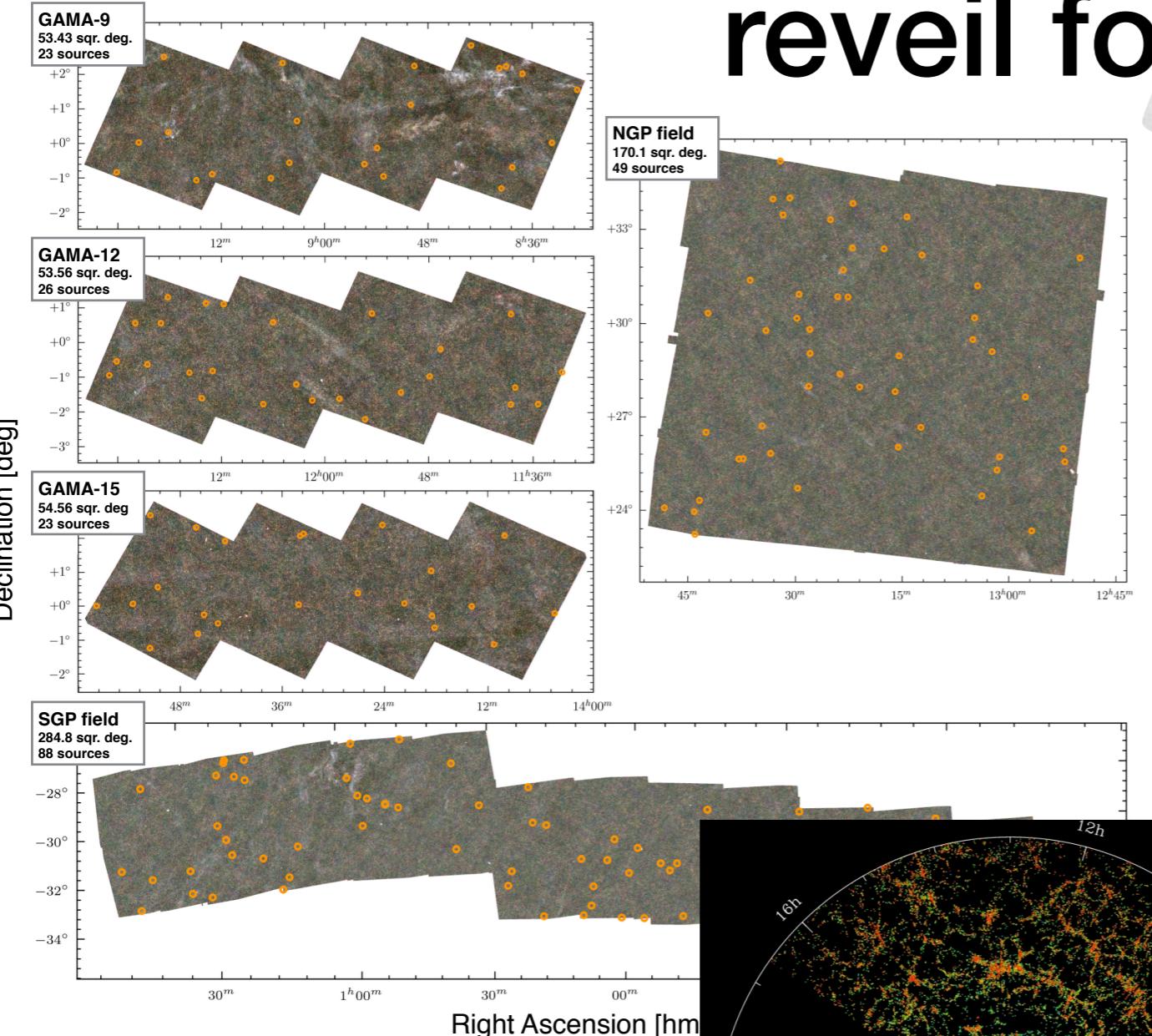


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Brightest sub-mm sources are mostly lensed



Counterparts in SDSS and VIKING reveal foreground lenses



The probability follows from two ‘simple’ equations

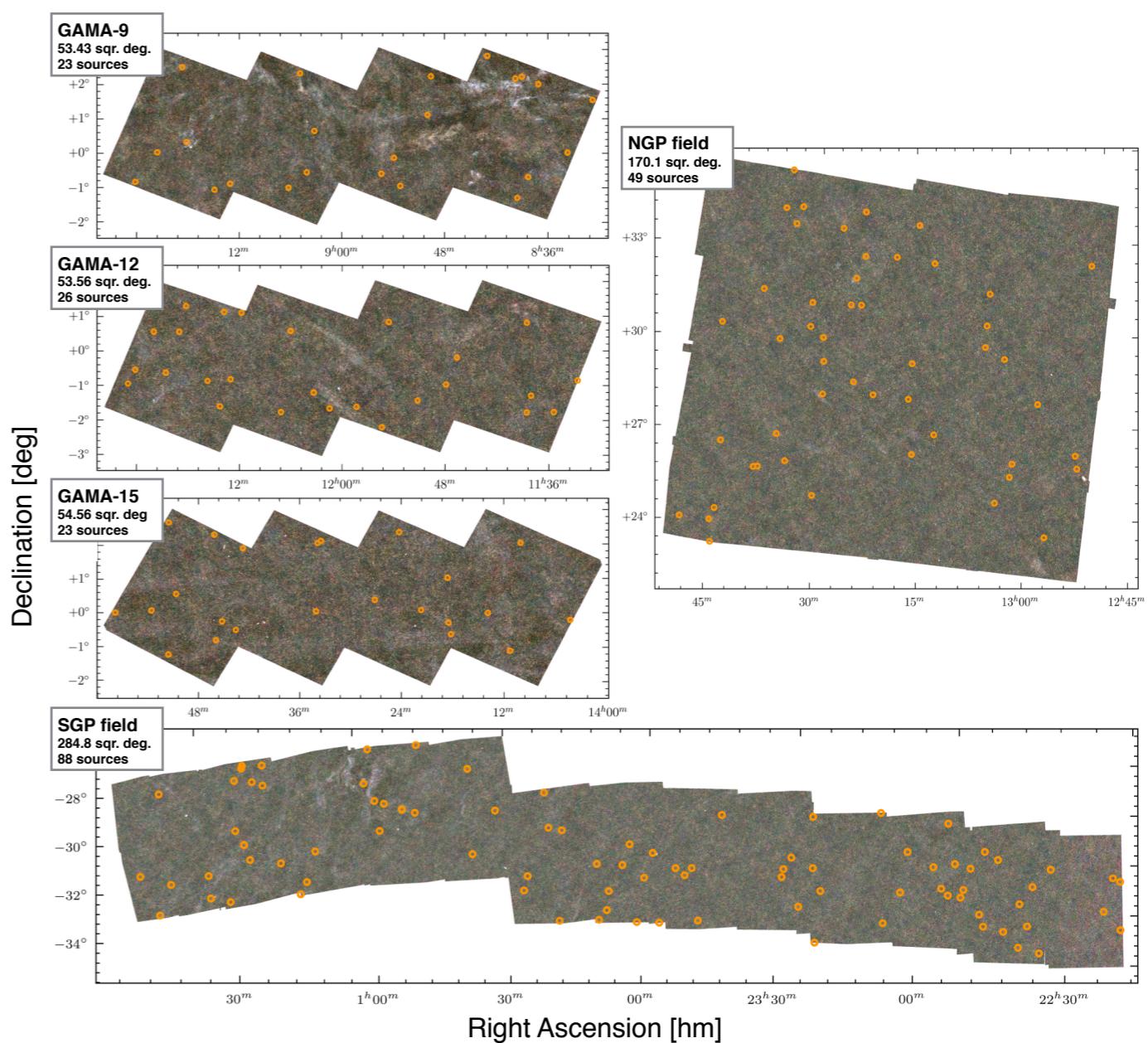
$$L = \frac{q(m)f(r)}{n(m)} \cdot \equiv \frac{\text{Chance of source (m) at distance (r)}}{\text{Chance of a random source (m)}}$$

$$R_j = \frac{L_j}{\sum_i L_i + (1 - Q_0)} \cdot \equiv \frac{\text{Probability of this source } j \text{ being a genuine counterpart}}{\text{Chance the source outside of survey depth}}$$

SDSS counterparts already exist, but finds only 35% of counterparts

Table 1. The SDSS reliabilities of Herschel sources.

R	< 0.8	> 0.8	All
GAMA	52	20	72
NGP	38	11	49
Total	90	31	121



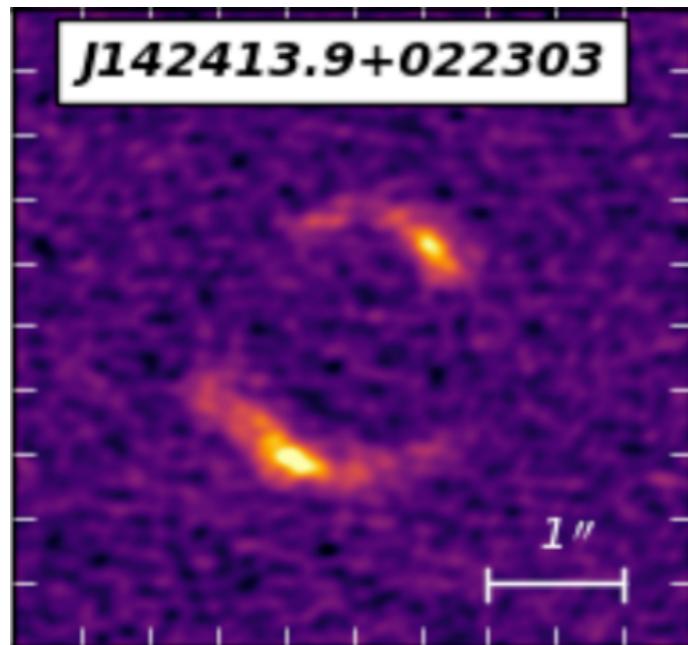
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$$L = \frac{q(m)f(r)}{n(m)} \cdot \equiv \frac{\text{Chance of source } (m) \text{ at distance } (r)}{\text{Chance of a random source } (m)}$$

$$R_j = \frac{L_j}{\sum_i L_i + (1 - Q_0)} \cdot \equiv \frac{\text{Probability of this source } j \text{ being a genuine counterpart}}{\text{Chance the source outside of survey depth}}$$



Recalculating the angular probability distribution allows us to find more lenses



Measured

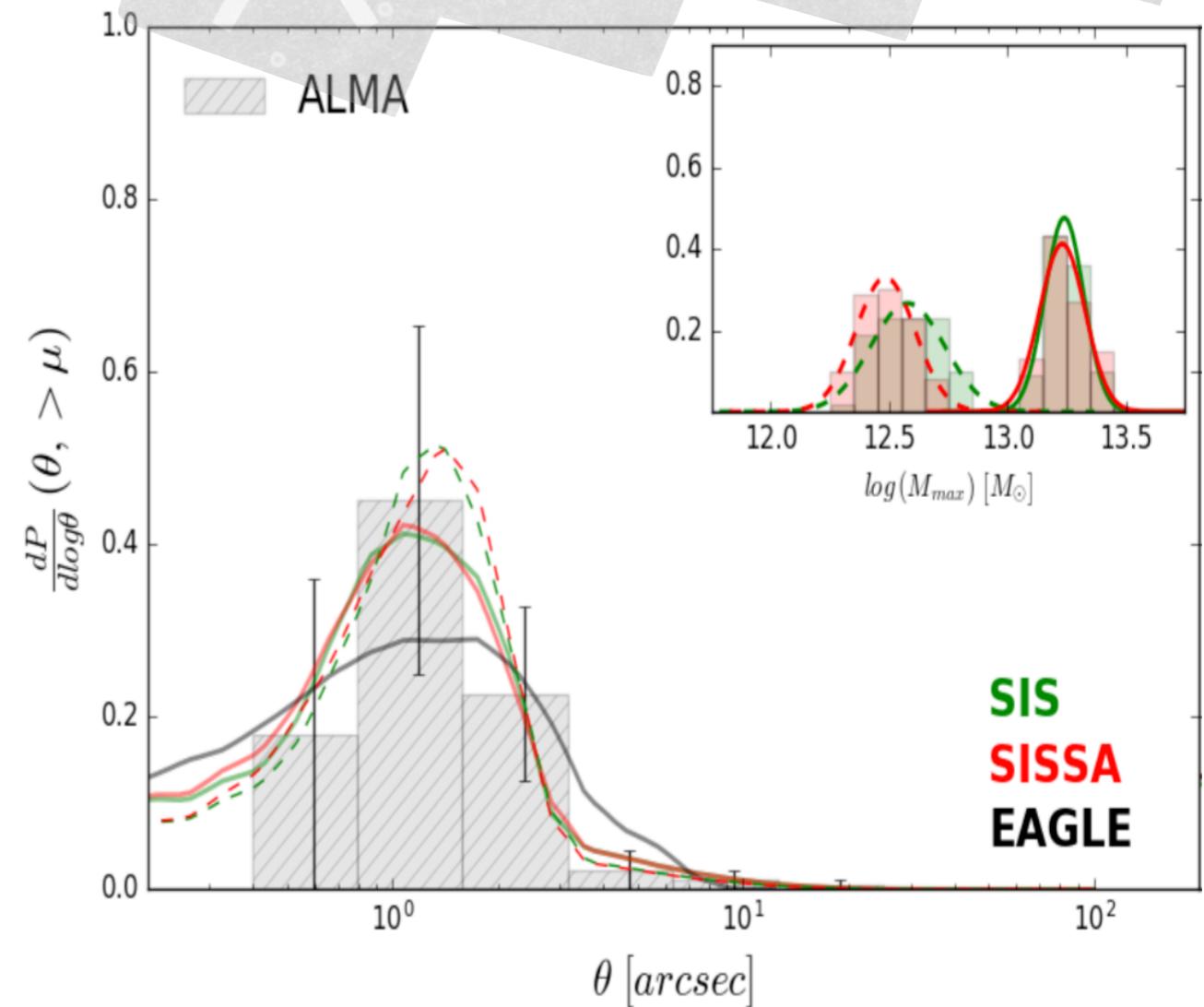
θ_{tot}

θ_{scatter}

SDSS

θ_{lens}

SPIRE

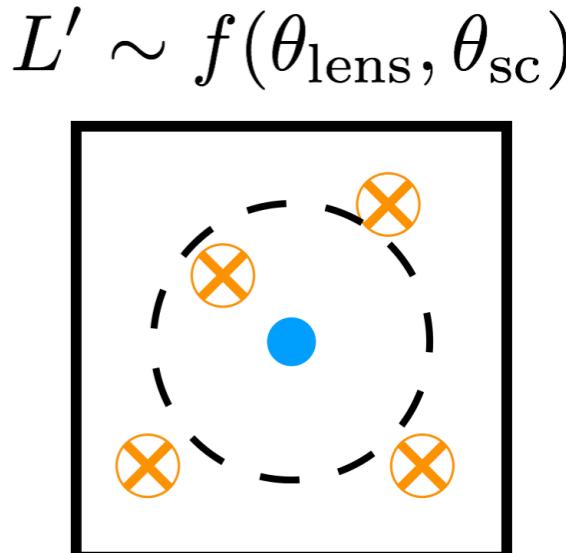
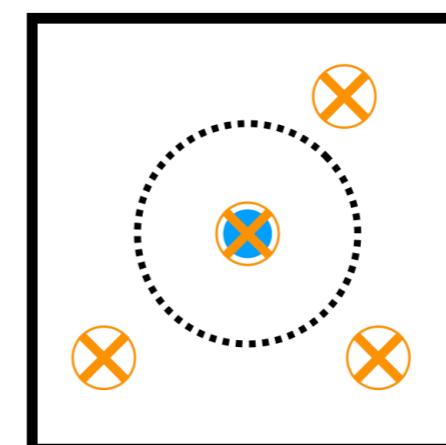
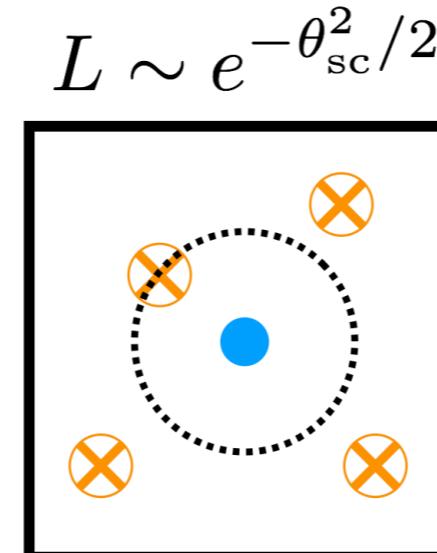
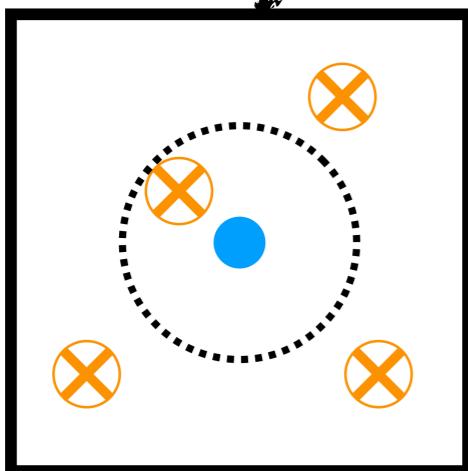


The re-analysis suggests we are missing multiple lensed sources

Model	Method 1	Method 2
No lens	31	31
Total model	32.5	41

Complete
recalculation

Statistics
on reliable
sources



$$L \sim e^{-\theta_{\text{sc}}^2/2}$$

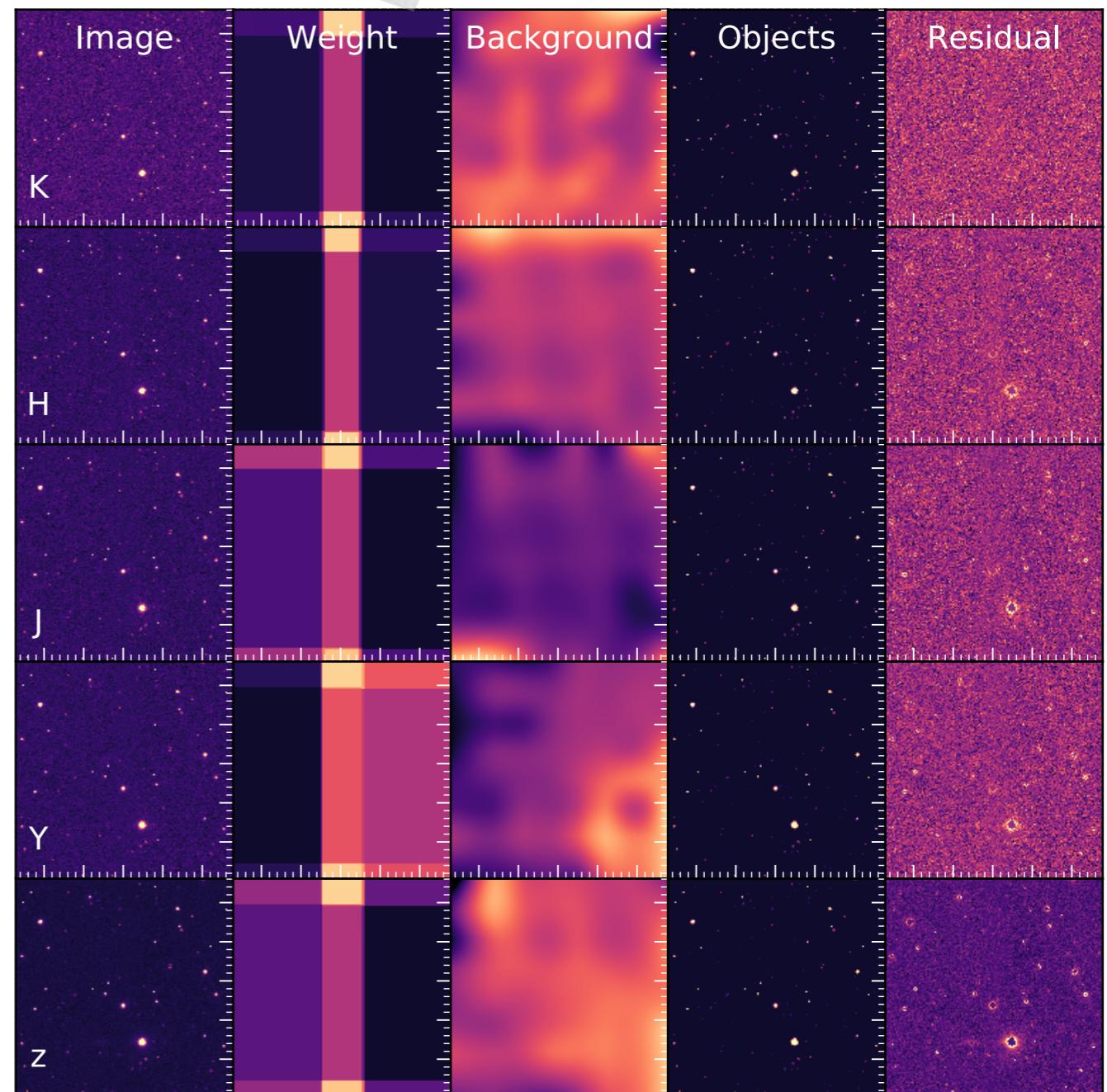
$$L_0$$

$$L' \sim f(\theta_{\text{lens}}, \theta_{\text{sc}})$$

VIKING sources are extracted by minimising the residuals

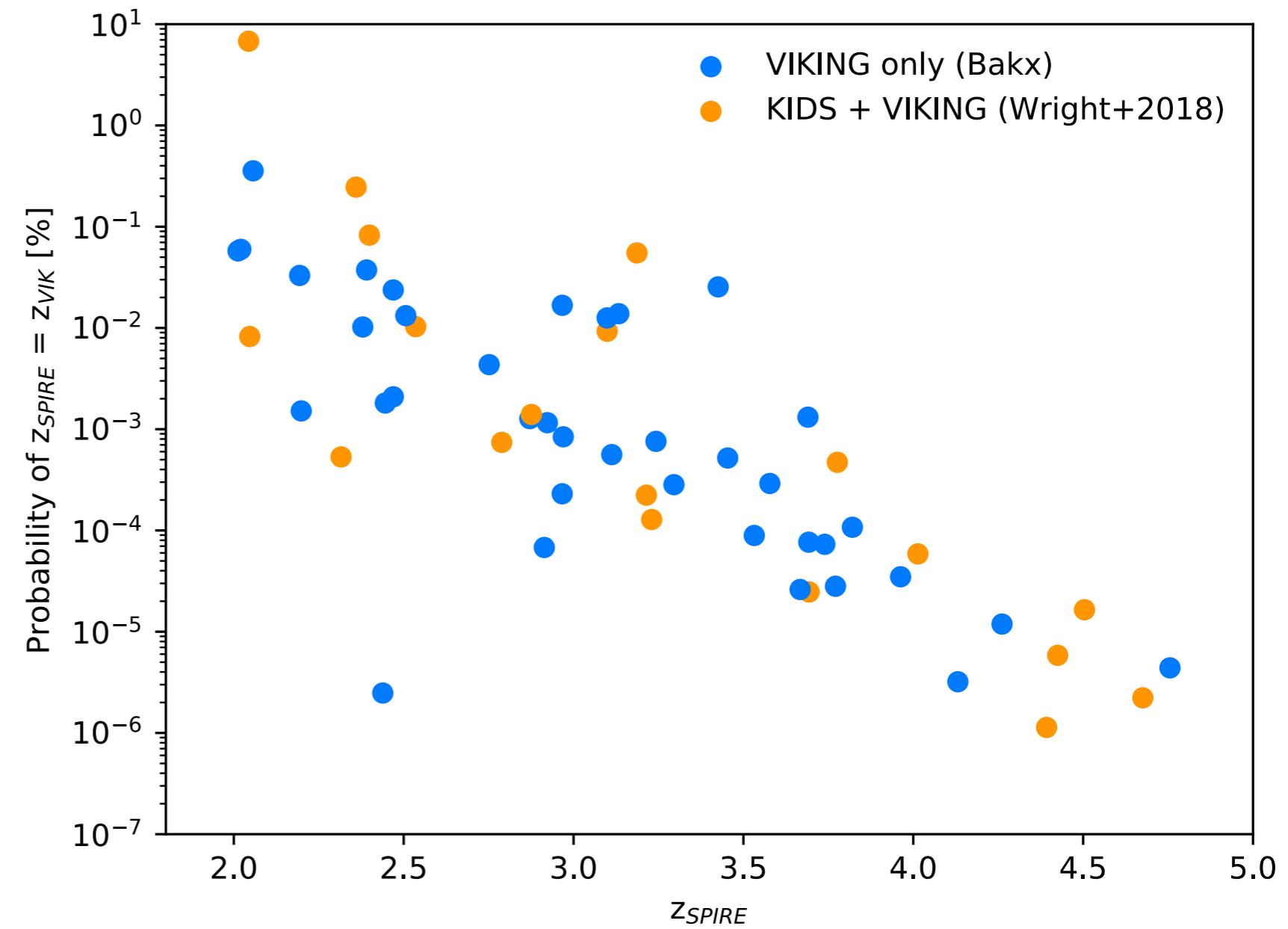
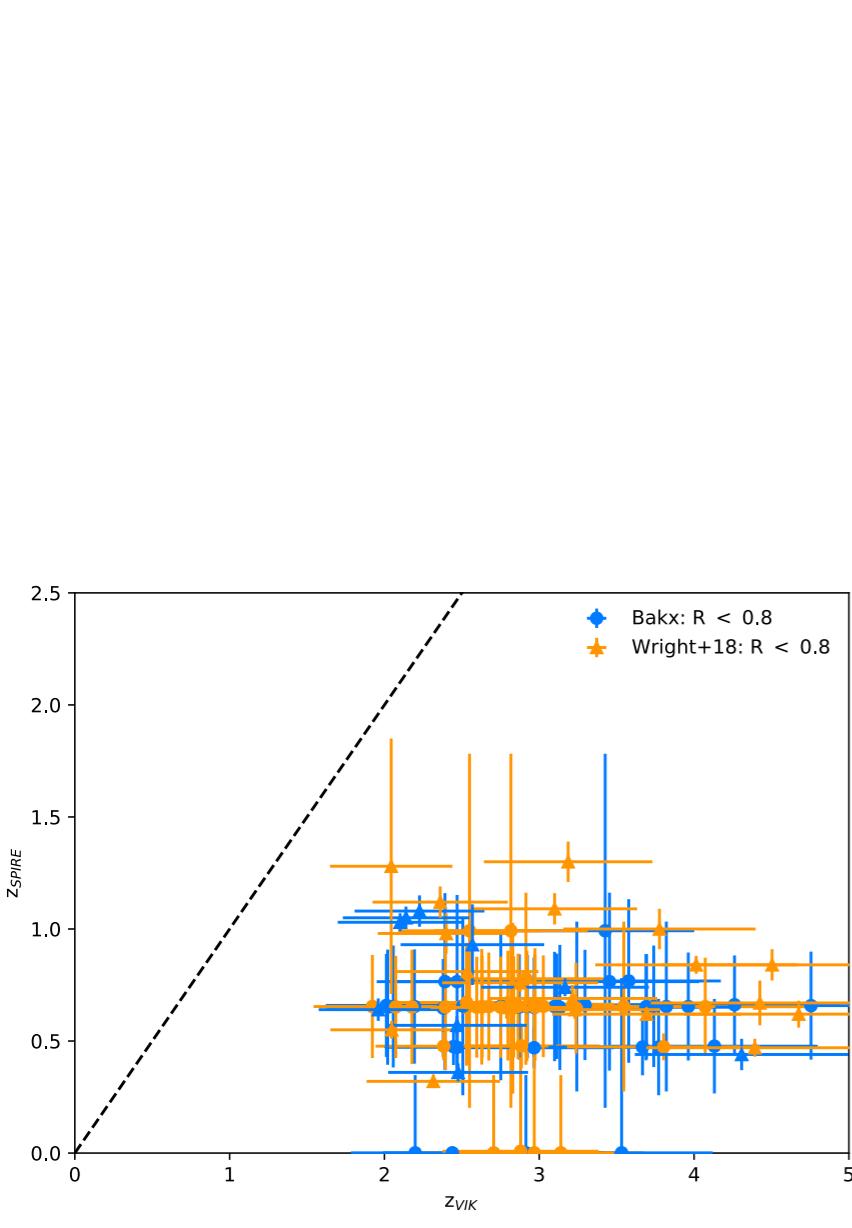
Table 3. VIKING reliabilities

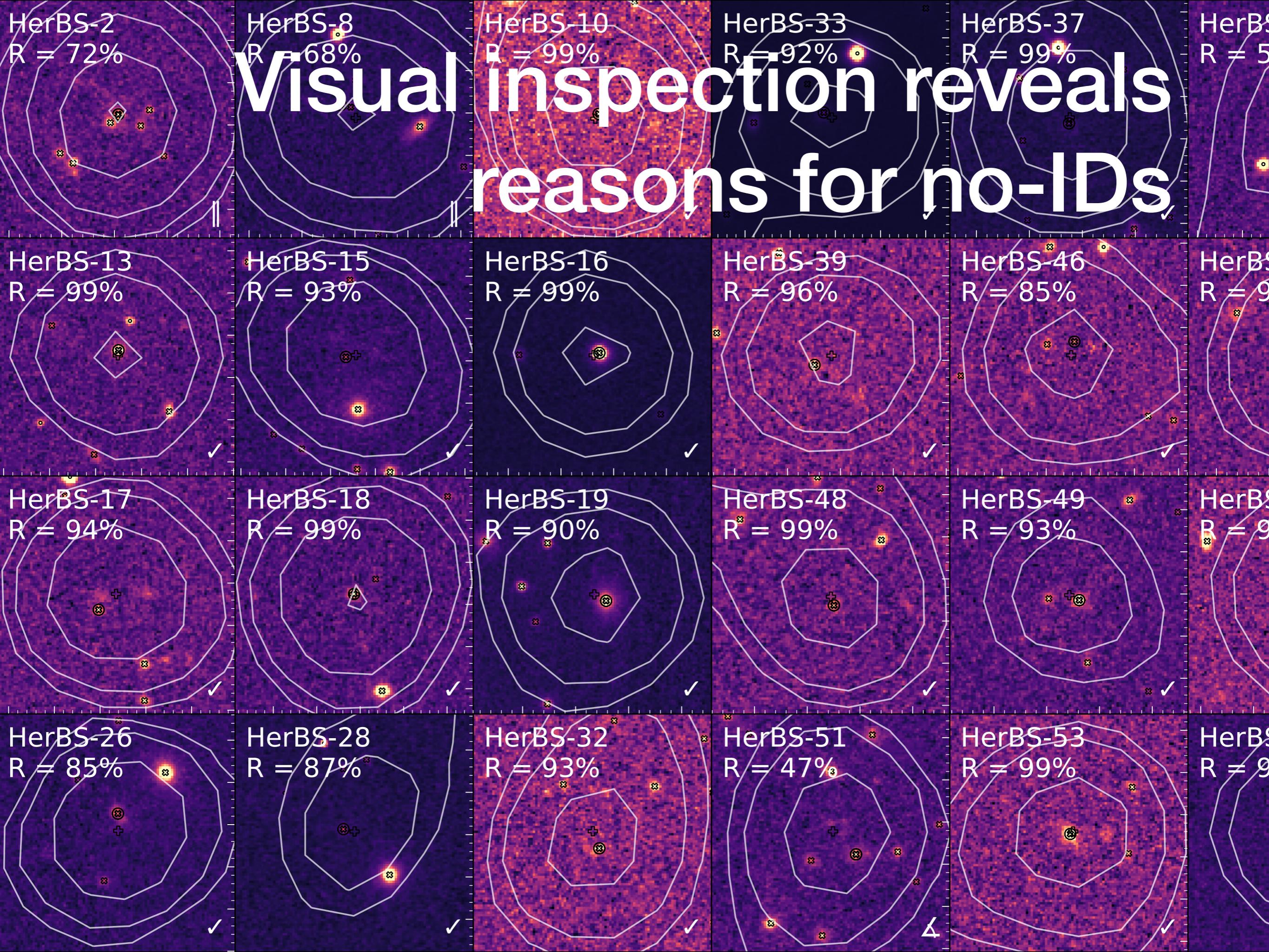
R	< 0.8	> 0.8	All
SGP	6	22	28
GAMA09	13	8	21
GAMA12	9	17	26
GAMA15	10	13	23
Total	38	60	98



Foreground sources ≠ Background sources

≠



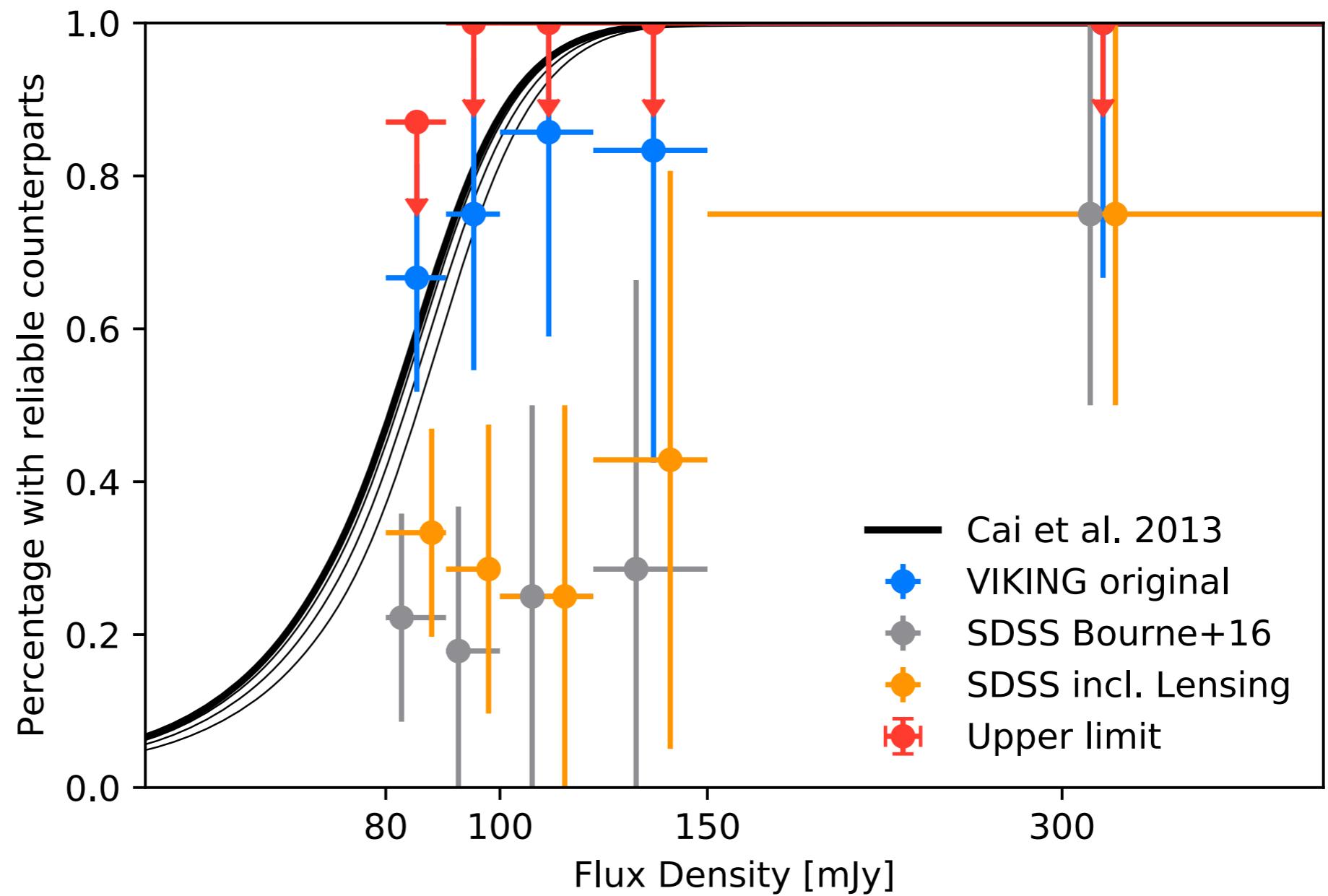


Why more is less

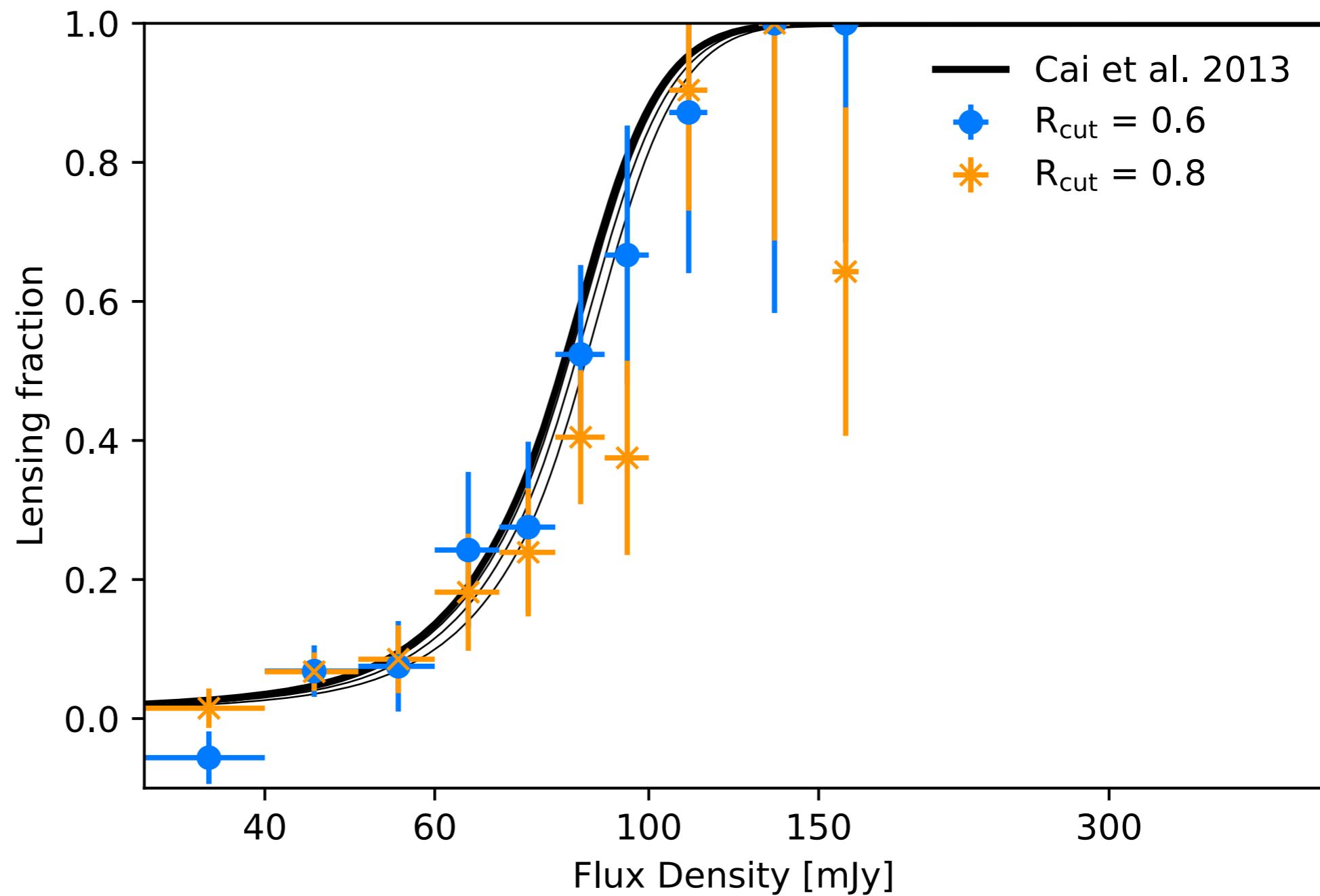
Table 4. VIKING visual inspection results

Counterpart with $R < 0.8$ because ...	Amount
... i. large angular separation	$\angle: 9$
... ii. nearby, competing sources	$\parallel: 14$
... iii. close source not picked up	$\otimes: 6$
... iv. close source with $J - K_S < 0$	$\leq: 2$
... v. nothing nearby is detected	$\emptyset: 7$

While SDSS does not see all foreground sources, VIKING appears complete

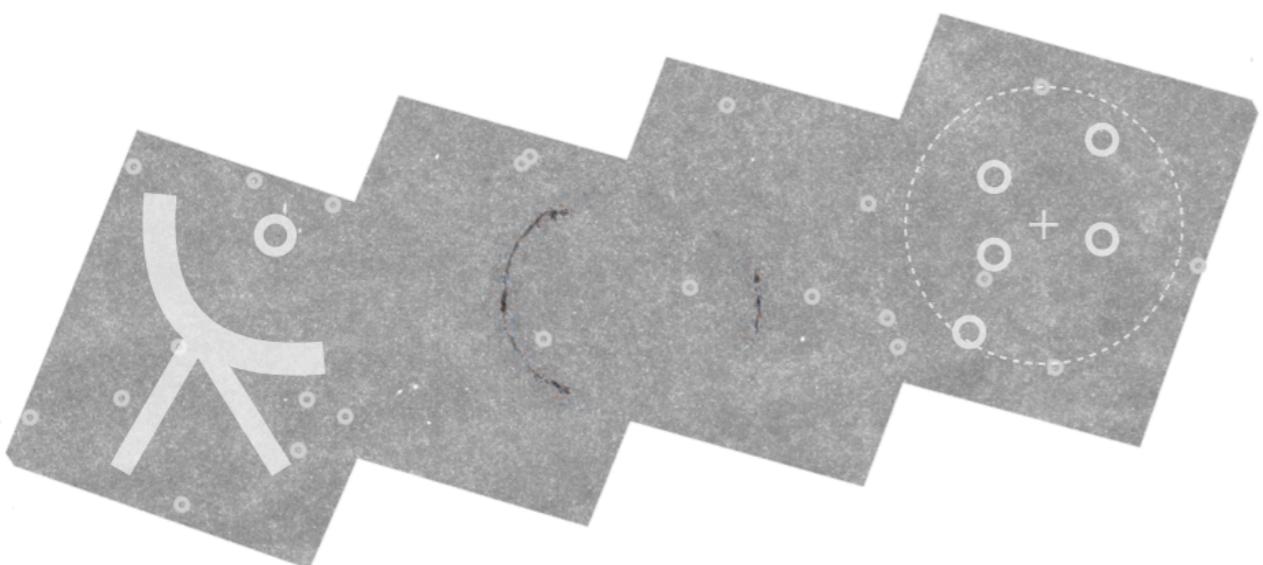


Using all Herschel sources reveals the lensing fraction



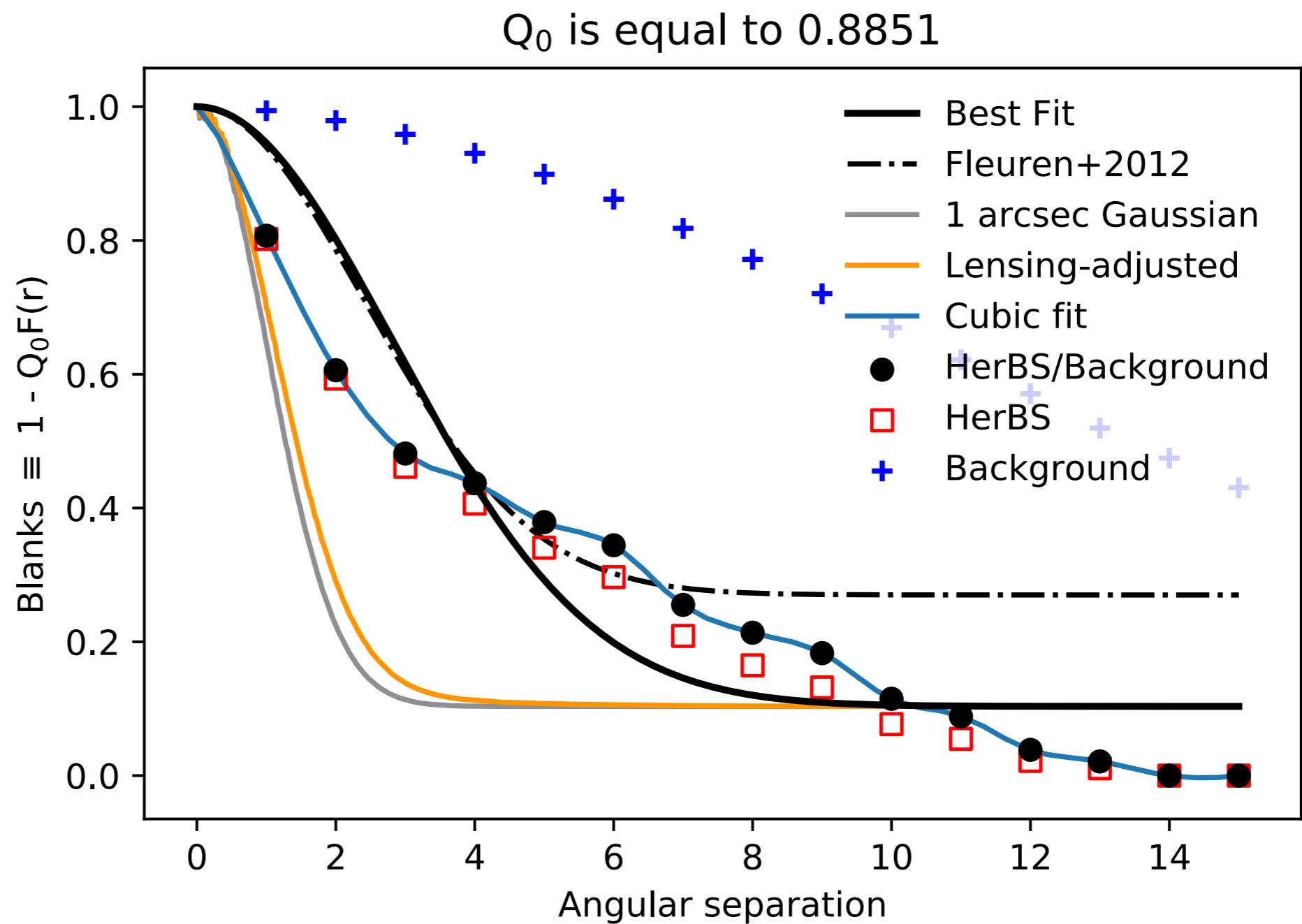
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The sources extend out to high angular scales



Recalculated angular distribution

