

Table of Distributions

Distribution	Notation	Probability Function	Mean	Variance	Moment-Generating Function
<i>Discrete Distributions</i>					
Binomial	$\text{Bin}(n, p)$	$p_X(k) = \binom{n}{k} p^k (1-p)^{n-k}, \quad k = 0, 1, \dots, n$	np	$np(1-p)$	$[pe^t + (1-p)]^n$
Geometric	$\text{Geom}(p)$	$p_X(k) = p(1-p)^{k-1}, \quad k = 1, 2, \dots$	$\frac{1}{p}$	$\frac{1-p}{p^2}$	$\frac{pe^t}{1 - (1-p)e^t}$
Negative Binomial	$\text{NegBin}(r, p)$	$p_X(k) = \binom{k-1}{r-1} p^r (1-p)^{k-r}, \quad k = r, r+1, \dots$	$\frac{r}{p}$	$\frac{r(1-p)}{p^2}$	$\left[\frac{pe^t}{1 - (1-p)e^t} \right]^r$
HyperGeometric	$\text{Hyp}(N, r, n)$	$p_X(k) = \frac{\binom{r}{k} \binom{N-r}{n-k}}{\binom{N}{n}}, \quad k = 0, 1, \dots, \min(n, r)$	$\frac{nr}{N}$	$\left(\frac{nr}{N}\right) \left(\frac{N-r}{N}\right) \left(\frac{N-n}{N-1}\right)$	
Poisson	$\text{Pois}(\lambda)$	$p_X(k) = e^{-\lambda} \frac{\lambda^k}{k!}, \quad k = 0, 1, 2, \dots$	λ	λ	$\exp \{ \lambda (e^t - 1) \}$
<i>Continuous Distributions</i>					
Uniform	$U(a, b)$	$f_X(x) = \frac{1}{b-a}, \quad a < x < b$	$\frac{a+b}{2}$	$\frac{(b-a)^2}{12}$	$\frac{e^{tb} - e^{ta}}{t(b-a)}$
Normal	$\mathcal{N}(\mu, \sigma^2)$	$f_X(x) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left[-\frac{(x-\mu)^2}{2\sigma^2} \right], \quad -\infty < x < \infty$	μ	σ^2	$\exp \left(\mu t + \frac{t^2 \sigma^2}{2} \right)$
Exponential	$\text{Exp}(\beta)$	$f_X(x) = \frac{1}{\beta} \exp(-x/\beta), \quad x > 0$	β	β^2	$(1-t\beta)^{-1}, \quad t < 1/\beta$
Gamma	$G(\alpha, \beta)$	$f_X(x) = \frac{1}{\Gamma(\alpha)\beta^\alpha} x^{\alpha-1} e^{-x/\beta}, \quad x > 0$	$\alpha\beta$	$\alpha\beta^2$	$(1-t\beta)^{-\alpha}, \quad t < 1/\beta$
Chi-Squared	χ_ν^2	$f_X(x) = \frac{1}{\Gamma(\nu/2)2^{\nu/2}} x^{\frac{\nu}{2}-1} e^{-\frac{x}{2}}, \quad x > 0$	ν	2ν	$(1-2t)^{-\nu/2}, \quad t < 1/2$
Beta	$\text{Beta}(\alpha, \beta)$	$f_X(x) = \frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}, \quad 0 < x < 1$	$\frac{\alpha}{\alpha+\beta}$	$\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$	does not exist