Problem Q4.2. Seeing that $\det(L) \neq 0$, we know that there does not exist any zero eigenvalue since $\det(L) = \prod_{i=1}^n \lambda_i$ if L has n eigenvalues.