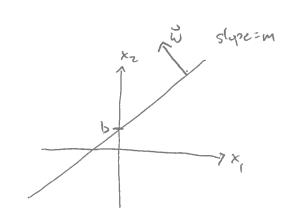
Support Vector Machines (SVM)

One way to write the equation for a line in a plane is

In higher dimensions, it is more convenient to write

$$\begin{pmatrix} -m \\ 1 \end{pmatrix} \circ \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = 6$$

$$\frac{1}{2} \circ x_2 = 6$$

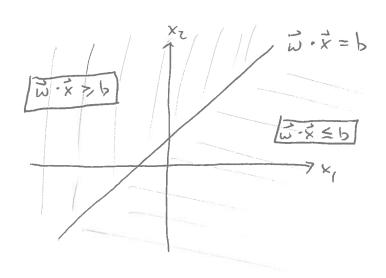


Note: it is perpendentar our normal to the line.

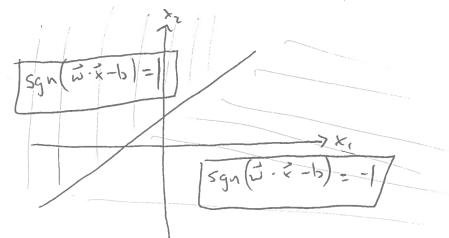
In 2-dimensions, the set of pts. satisfying $\vec{w} \cdot \vec{x} = b$ is a line. In 3-dim, its a plane. The vector \vec{w} is normal to the plane. In n-dim, its an n-1dim hyperplane

How do we describe the set of pts. above the line, $\vec{\omega} \cdot \vec{x} = b$, in Z-dim? It is the healf-space of pts. \vec{x} satisfying

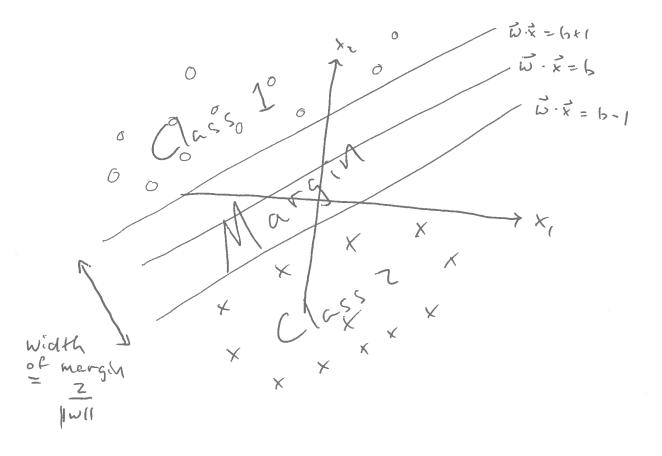
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If I know $\vec{\omega}$ and \vec{b} , I can define a classifier by $\vec{x} \mapsto \vec{y} = \vec{x} \cdot \vec{x} + \vec{b}$



If I take b >> b+1 or b >> b+1, I get Z
move lines parallel to the first.



Idea: maxim: Ze I WII

S.t. $\vec{w} \cdot \vec{x}_i \neq b+1$ \(\times \text{i belonging to class } \)
\(\vec{w} \cdot \vec{x}_i \leq \text{b-1} \)
\(\vec{v} \cdot \vec{x}_i \leq \text{b-1} \)
\(\vec{v} \cdot \vec{v} \text{belonging to class } \vec{z} \).

It can be shown that this is equivalent to

minimize | | W|| W, b

5.t. Y: (2.x; -6) > (4:.

From the picture, the max-margin hyperplane

will touch some of the x: (otherwise, we could take

Will to be smaller). These xi are called support

vectors.