Numerical Methods with Python

Numerical Integration

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- Example: $W = \int_{x_i}^{x_f} F_x(x)dx$

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- It is just the **area under the curve**

Example: a triangle