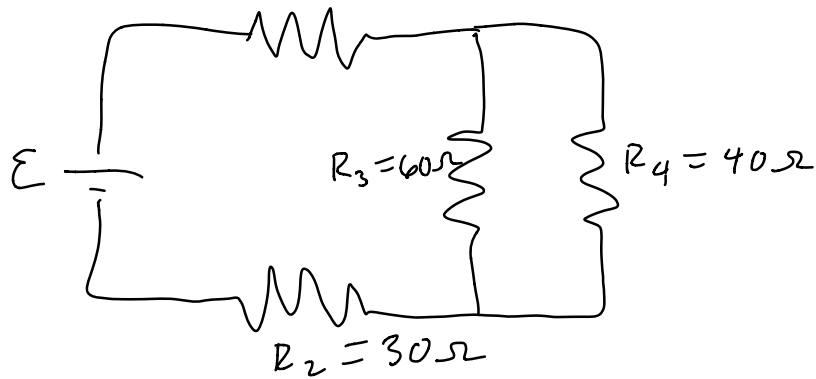
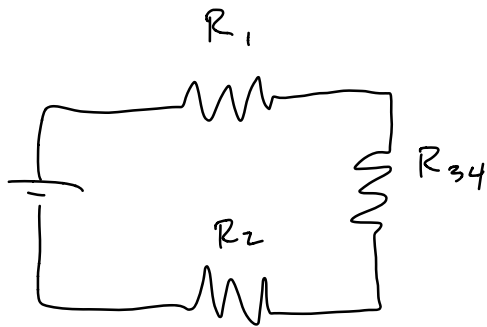


Example:

$$R_1 = 20\ \Omega$$



What is  $R_{eq}$ ?



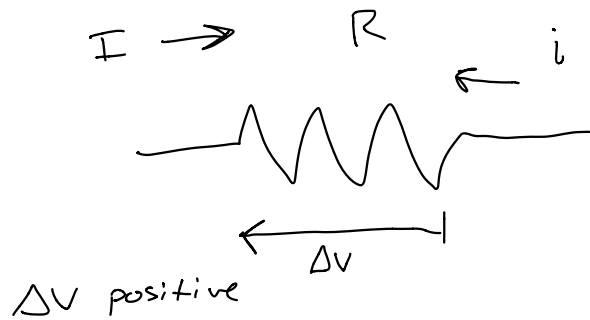
$$R_{eq} = R_1 + R_2 + R_{34}$$

$$\frac{1}{R_{34}} = \frac{1}{R_3} + \frac{1}{R_4} = \frac{1}{60} + \frac{1}{40} = \frac{1}{24}, \quad R_{34} = 24\ \Omega$$

$$R_{eq} = 20\ \Omega + 24\ \Omega + 30\ \Omega = 74\ \Omega$$

Question:

Energy dissipated in a resistor



$$\Delta U = -e\Delta V$$
$$\Delta K = 0$$

$\Delta U$  goes into heat

Energy gained by resistor =  $\Delta E = e\Delta V$

$$\text{Power} = \frac{\Delta E}{\Delta t} = \frac{I \Delta t \Delta V}{\Delta t} = I \Delta V$$

$$P = I \Delta V$$

$$\Delta V = IR, \quad P = I^2 R$$

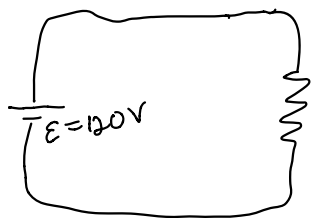
Unit: Watt  $\left(\frac{\text{J}}{\text{s}}\right)$

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Example: A 60 W light bulb

What is the current?

USA outlets:  $\Delta V = 120 \text{ V}$



$$P = I \Delta V$$

$$\mathcal{E} - \Delta V = 0$$

$$\frac{P}{\Delta V} = I, \quad \frac{60}{120} = I = 0.5 \text{ A}$$

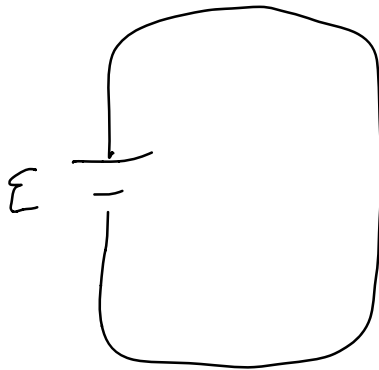
Resistance?

$$I = \frac{\Delta V}{R} \Rightarrow R = \frac{\Delta V}{I} = \frac{120}{0.5} = 240 \Omega$$

Resistance of a 150 W bulb?

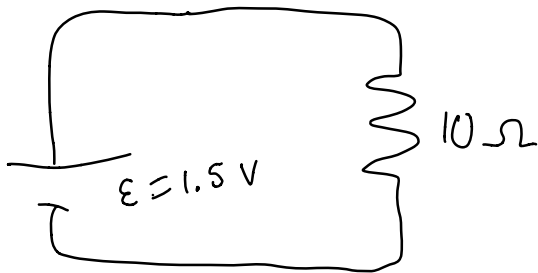
$$R = \frac{\Delta V}{I} = \frac{\mathcal{E}}{I} = \frac{\mathcal{E}}{P/\mathcal{E}} = \frac{\mathcal{E}^2}{P} = \frac{120^2}{150} = 96 \Omega$$

$$P = I\mathcal{E}, \quad I = \frac{P}{\mathcal{E}}$$



$$I = \frac{\mathcal{E}}{R} = \infty$$

$$R = 10^{-3} \Omega$$



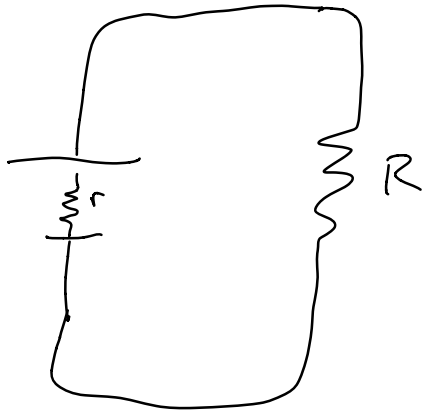
What is  $I$ ?

$$I = \frac{\mathcal{E}}{R} = 0.15 \text{ A}$$

$$I_{\text{meas}} = 0.146 \text{ A}$$

What is going on?

Resistance inside the battery



$$\Delta V_{\text{BAT}} = \mathcal{E} - Ir$$

$$\mathcal{E} - Ir - IR = 0, \quad I = \frac{\mathcal{E}}{r+R}$$

Even if  $R$  is 0,  $I < \infty$

Short Circuit:

$$I_{\text{max}} = \frac{\mathcal{E}}{r}$$

Above example:

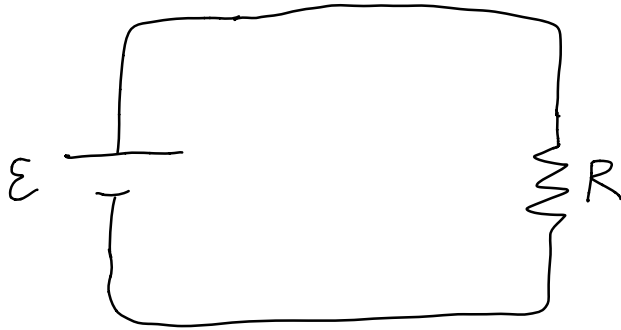
$$I_{\text{obs}} = 0.146 = \frac{1.5}{r+10}$$

$$r = 0.25 \Omega$$

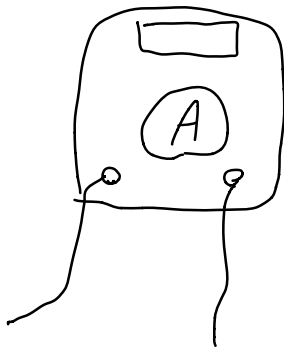
For copper,  $R$  of  $1\text{m} \approx 10^{-3}$

$$I_{\text{max}} = \frac{1.5}{0.25} = 6.0 \text{ A}$$

How to measure current?

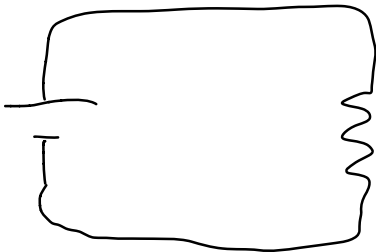


- Compass deflection / magnetic field
- Measure  $\Delta V$  across a known resistor  $R_1$   
+  $I = \frac{\Delta V}{R_1}$

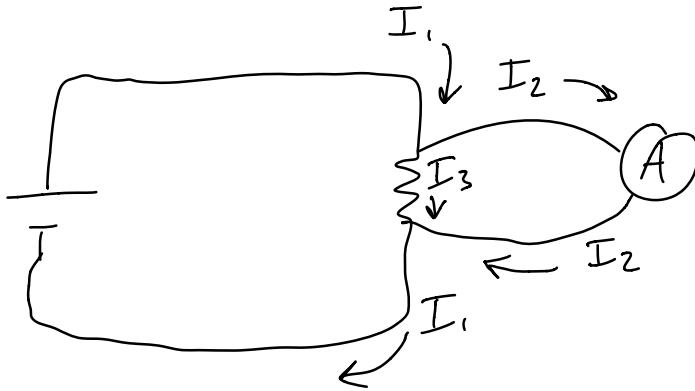


How to connect?

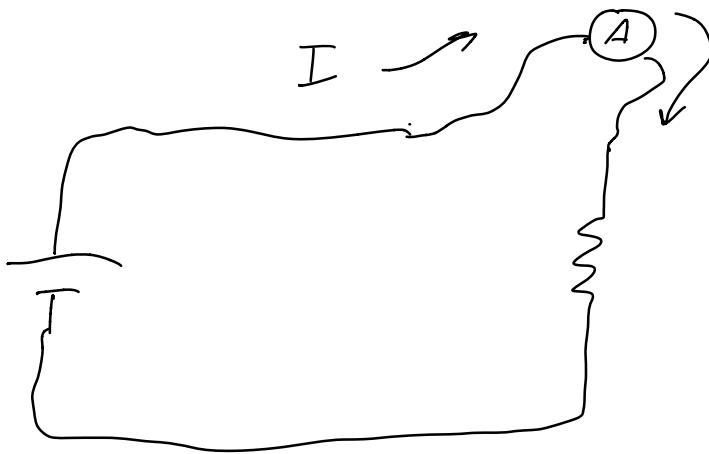
Series or parallel?



## Ammeter in Parallel



## Ammeter in Series



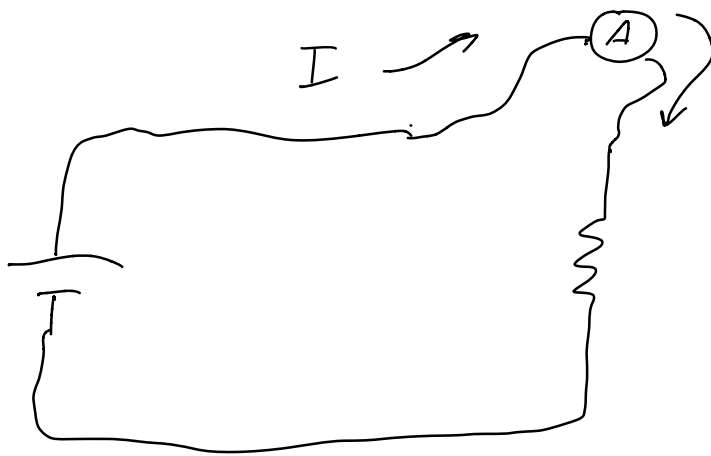
$$I = \frac{\mathcal{E}}{R + R_A}, \quad R_A \text{ should be small!}$$

What about a voltmeter?

If I know the resistance of  
the ammeter, I can use

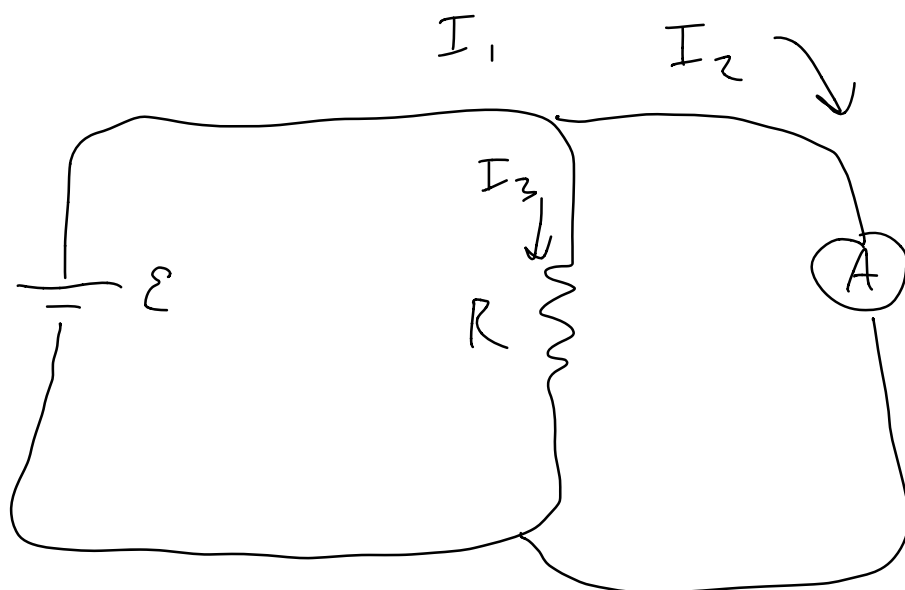
$$\Delta V = IR_A$$

CANT have it in series



$$\mathcal{E} - IR_A - IR = 0$$



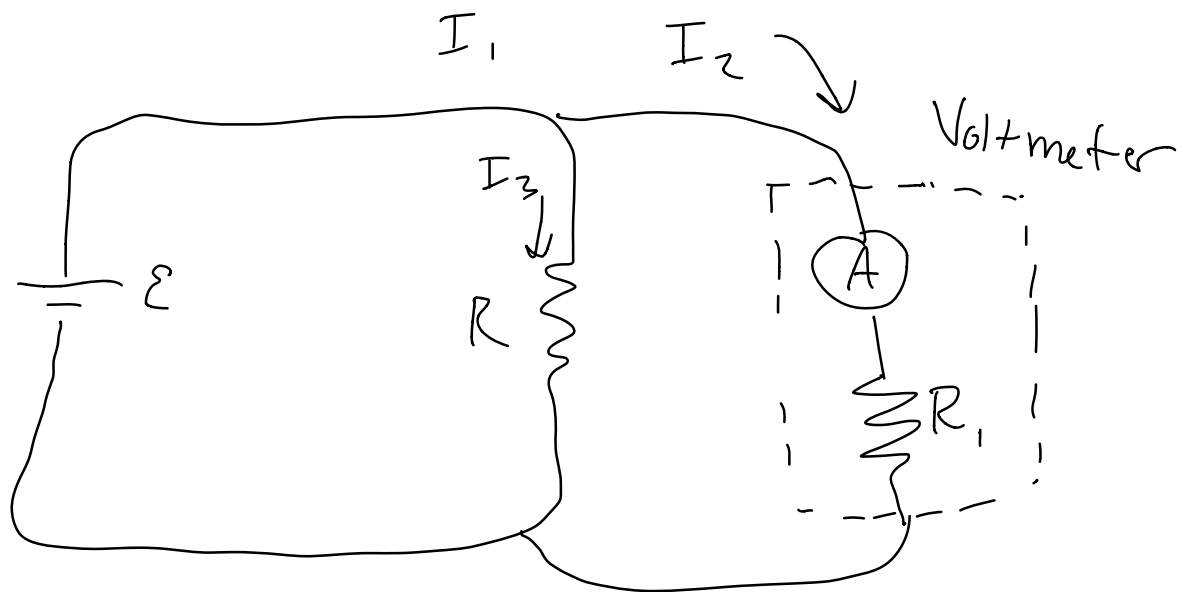


$$I_1 = I_2 + I_3$$

$$I_3 R = I_2 R_A$$

$$I_2 = \frac{R}{R_A} I_3$$

$$\frac{R}{R_A} \gg 1$$



$$I_3 R = I_2 (R_A + R_1)$$

$$I_2 = \frac{R}{R_A + R_1} I_3$$

$$R_1 \gg R$$

$$I_2 \approx 0$$

Voltmeters need very high resistance

	Ammeter	Voltmeter
Circuit Connection	Series	Parallel
Resistance	Low	High