

CHAPTER 22

FARADAY'S LAW

MAXWELL'S EQUATIONS

Equation	Name	Explanation
$\oint \vec{E} \cdot \hat{n} dA = \frac{1}{\epsilon_0} \sum q_{\text{inside}}$	Gauss's Law for Electricity	<ul style="list-style-type: none">▶ How charges produce electric fields▶ Used to derive Coulomb's Law
$\oint \vec{B} \cdot \hat{n} dA = 0$	Gauss's Law for Magnetism	<ul style="list-style-type: none">▶ No magnetic monopoles▶ Constrains shape of magnetic field ("curly")
$\oint \vec{E} \cdot d\vec{l} = 0$	Faraday's Law	<ul style="list-style-type: none">▶ Constrains shape of electric field (radially outward, cannot be "curly")
$\oint \vec{B} \cdot d\vec{l} = \mu_0 \sum I_{\text{inside}}$	Ampere's Law	<ul style="list-style-type: none">▶ How currents produce magnetic fields▶ Used to derive Biot-Savart Law

MAXWELL'S EQUATIONS



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MAXWELL'S EQUATIONS

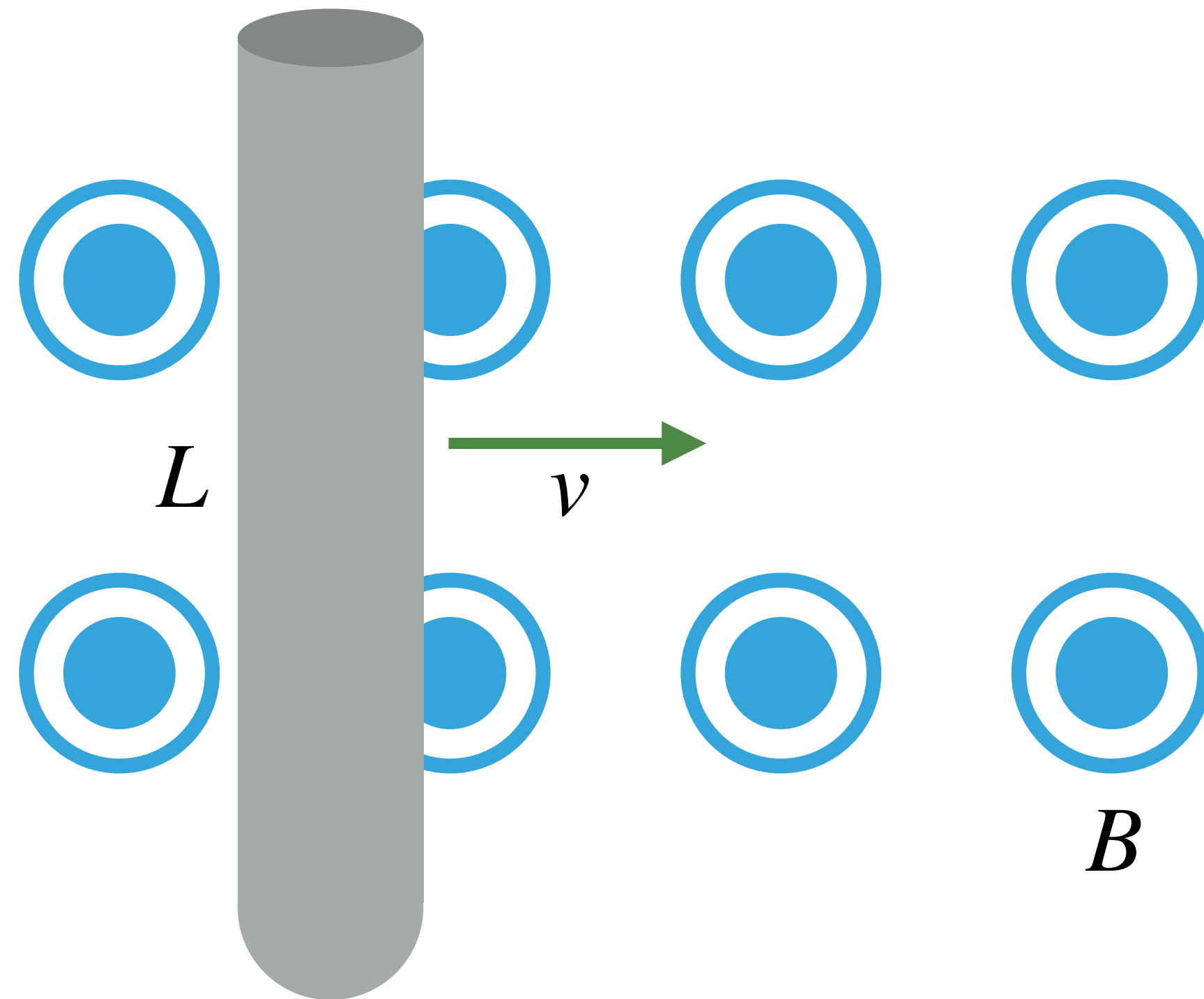
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$\oint \vec{E} \cdot d\vec{l} = 0$	Faraday's Law*	<div><div>▶ Constrains electric field (radially out)</div><div>Chapter 22</div></div>
$\oint \vec{B} \cdot d\vec{l} = \mu_0 \sum I_{\text{inside}}$	Ampere's Law*	<div><div>▶ How current produces magnetic field</div><div>Chapter 23</div></div> <div><div>▶ Used to derive Biot-Savart Law</div></div>

FARADAY'S LAW

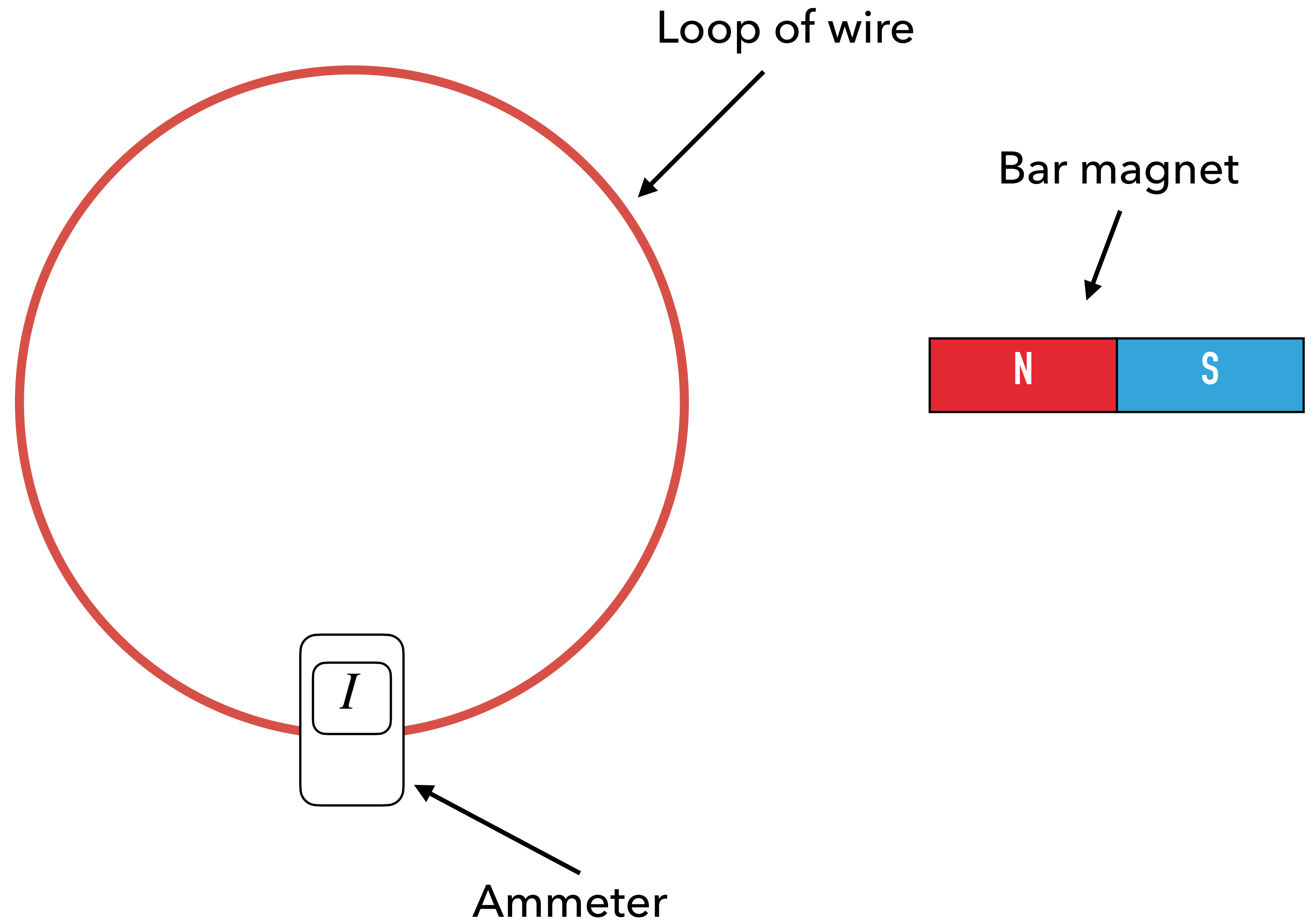
- ▶ Recall from chapter 20: motion relative to a magnetic field produces an emf
 - ▶ Motional emf
 - ▶ $\varepsilon = BLv$



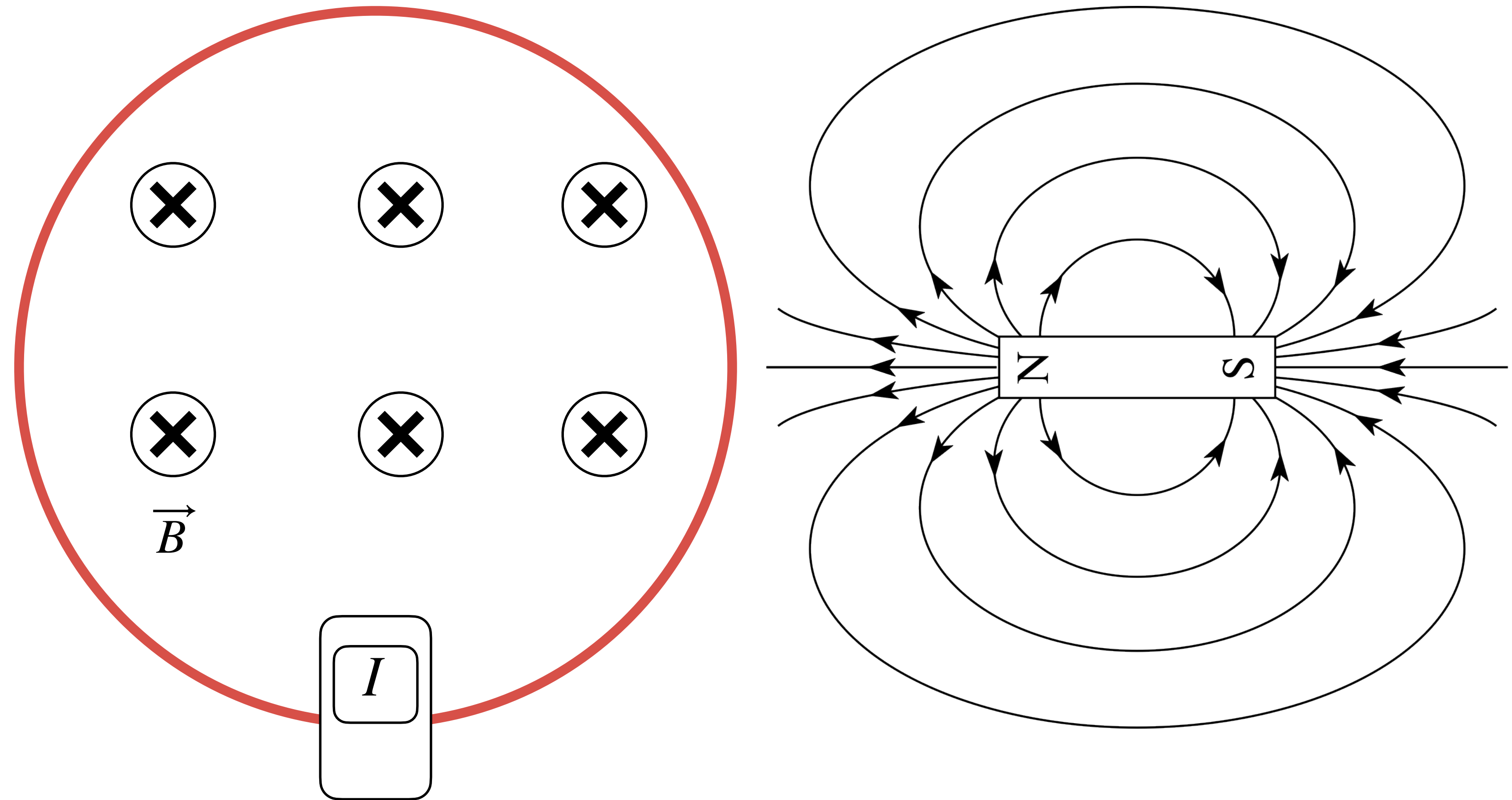
QUESTION

- ▶ How do electric charges respond to a *changing* magnetic field?

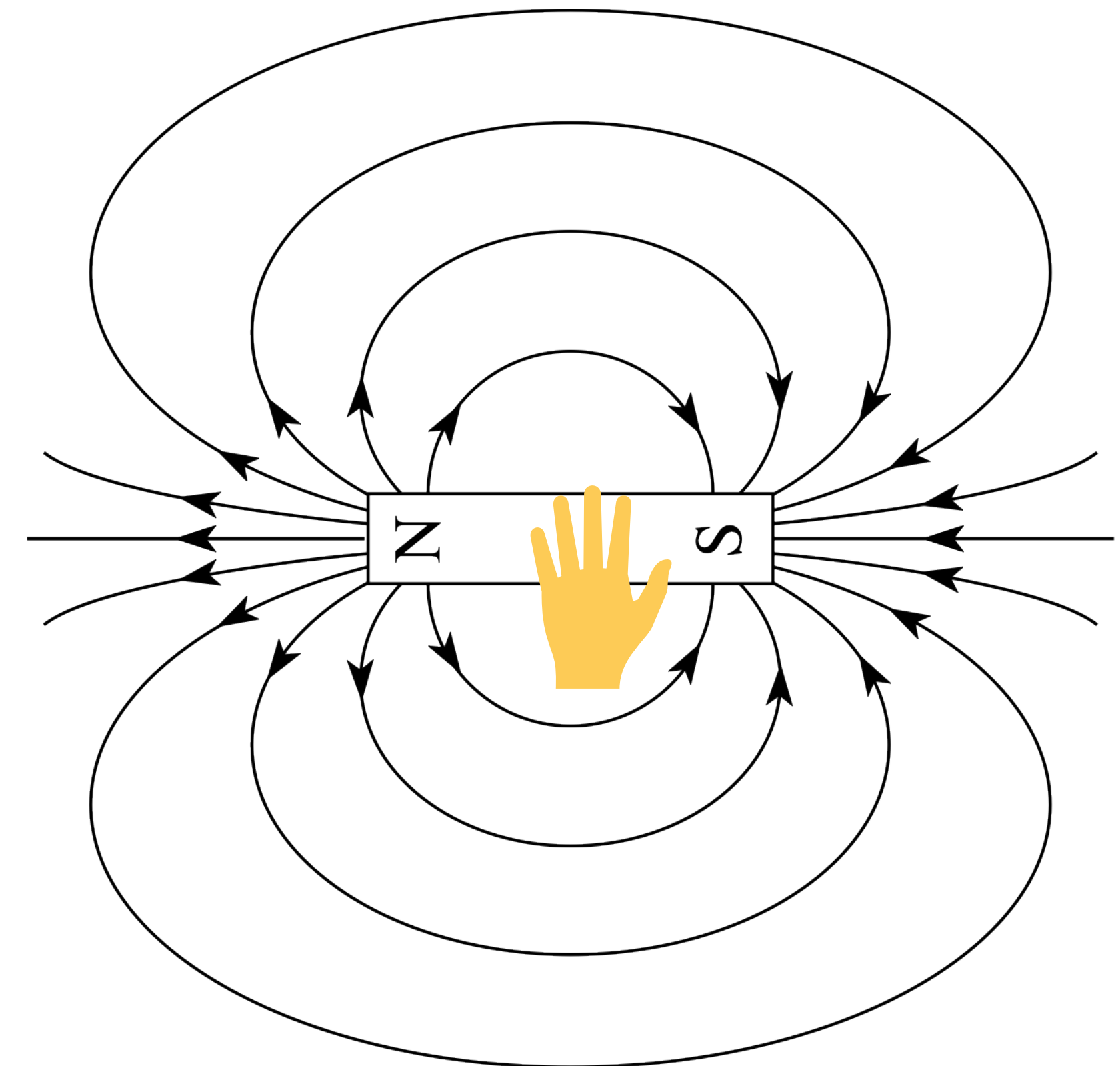
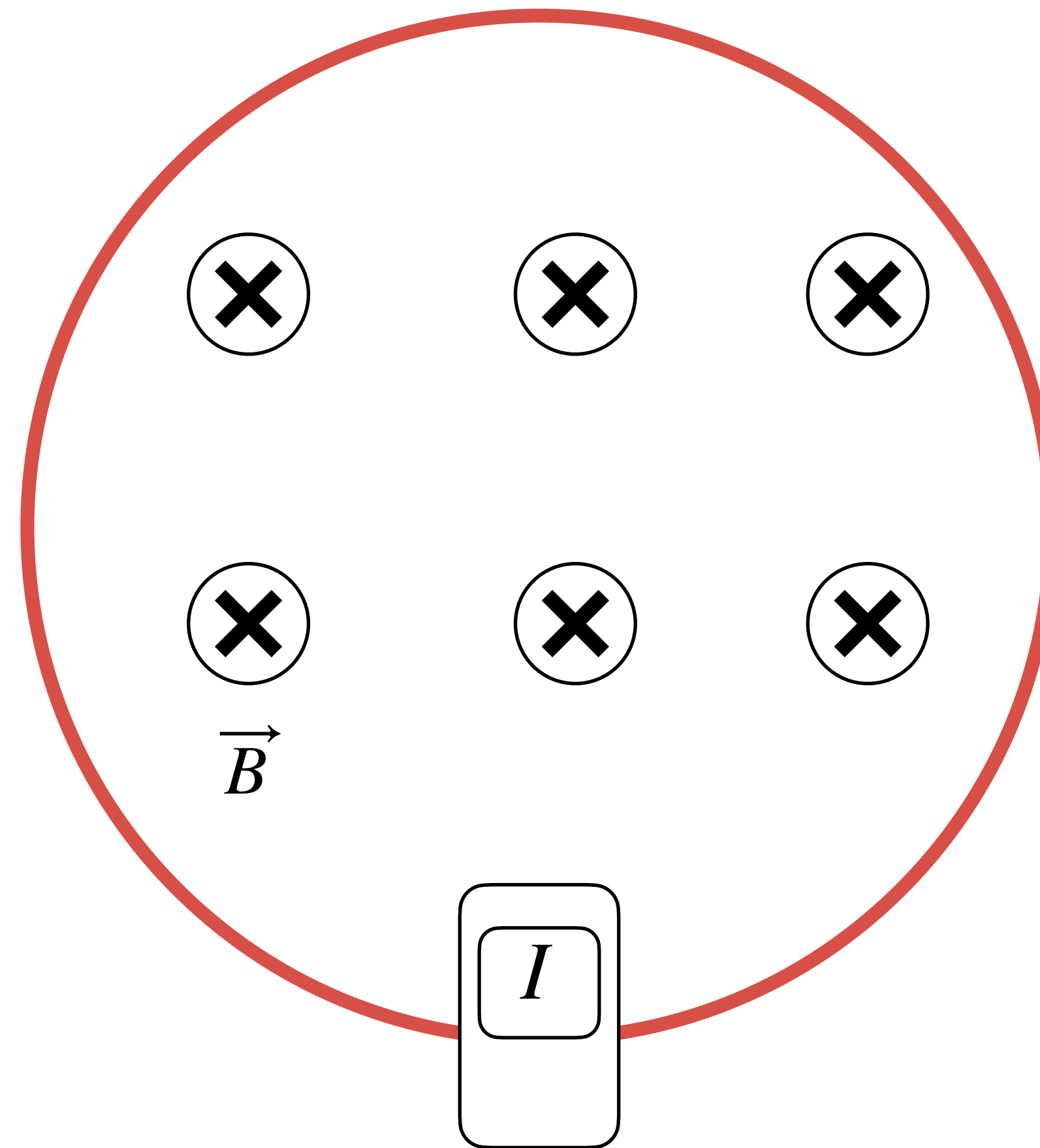
AN EXPERIMENT



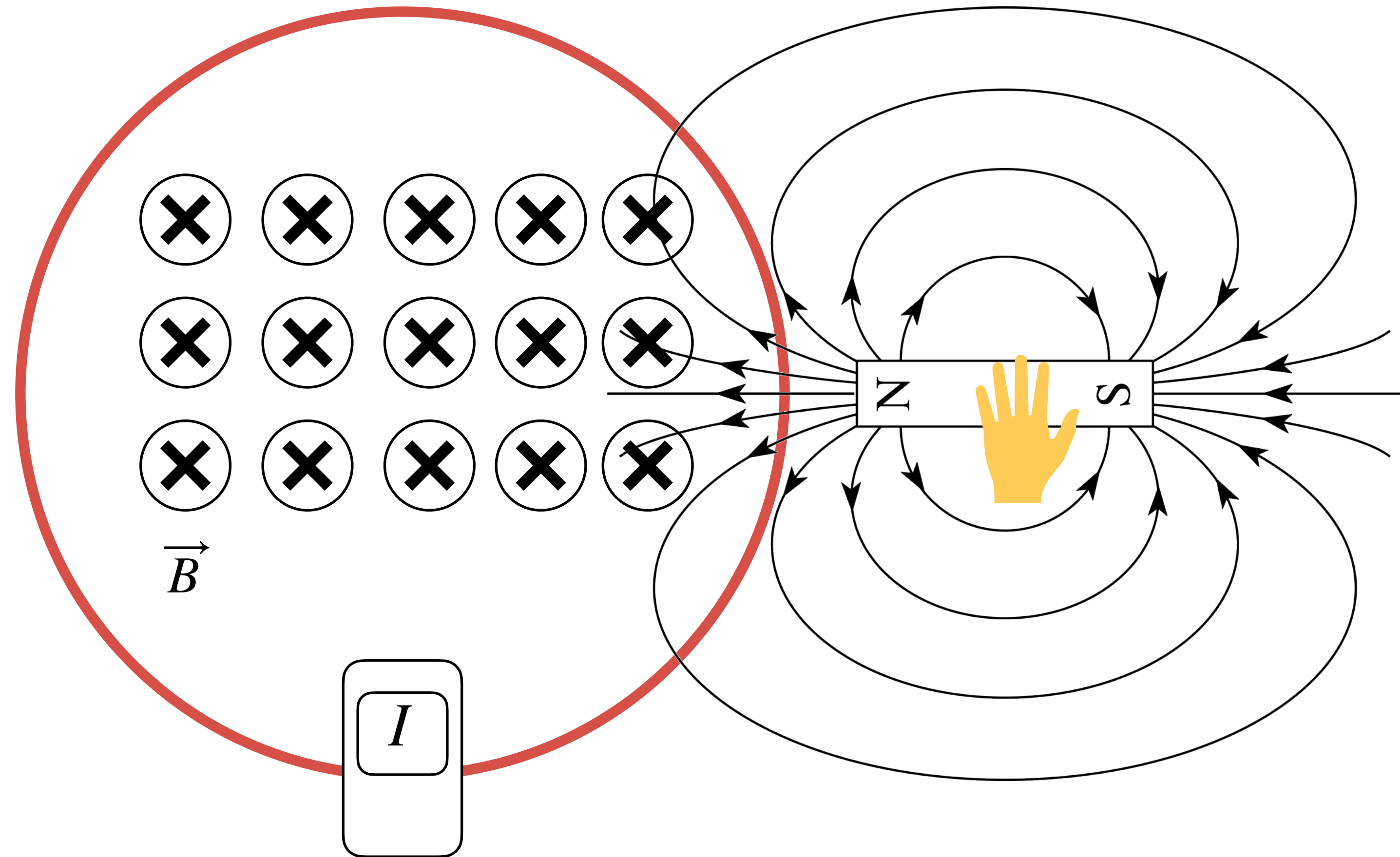
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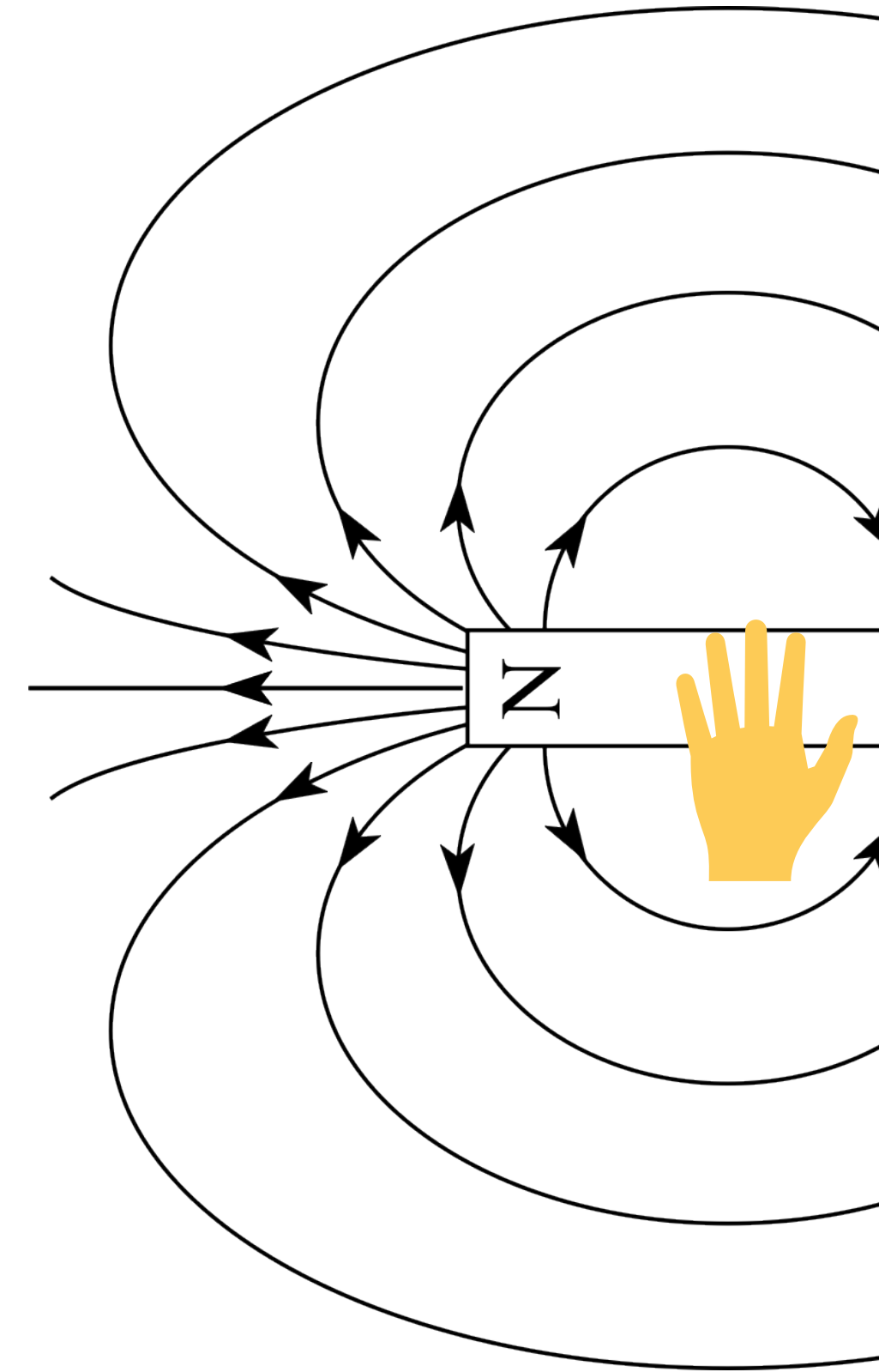
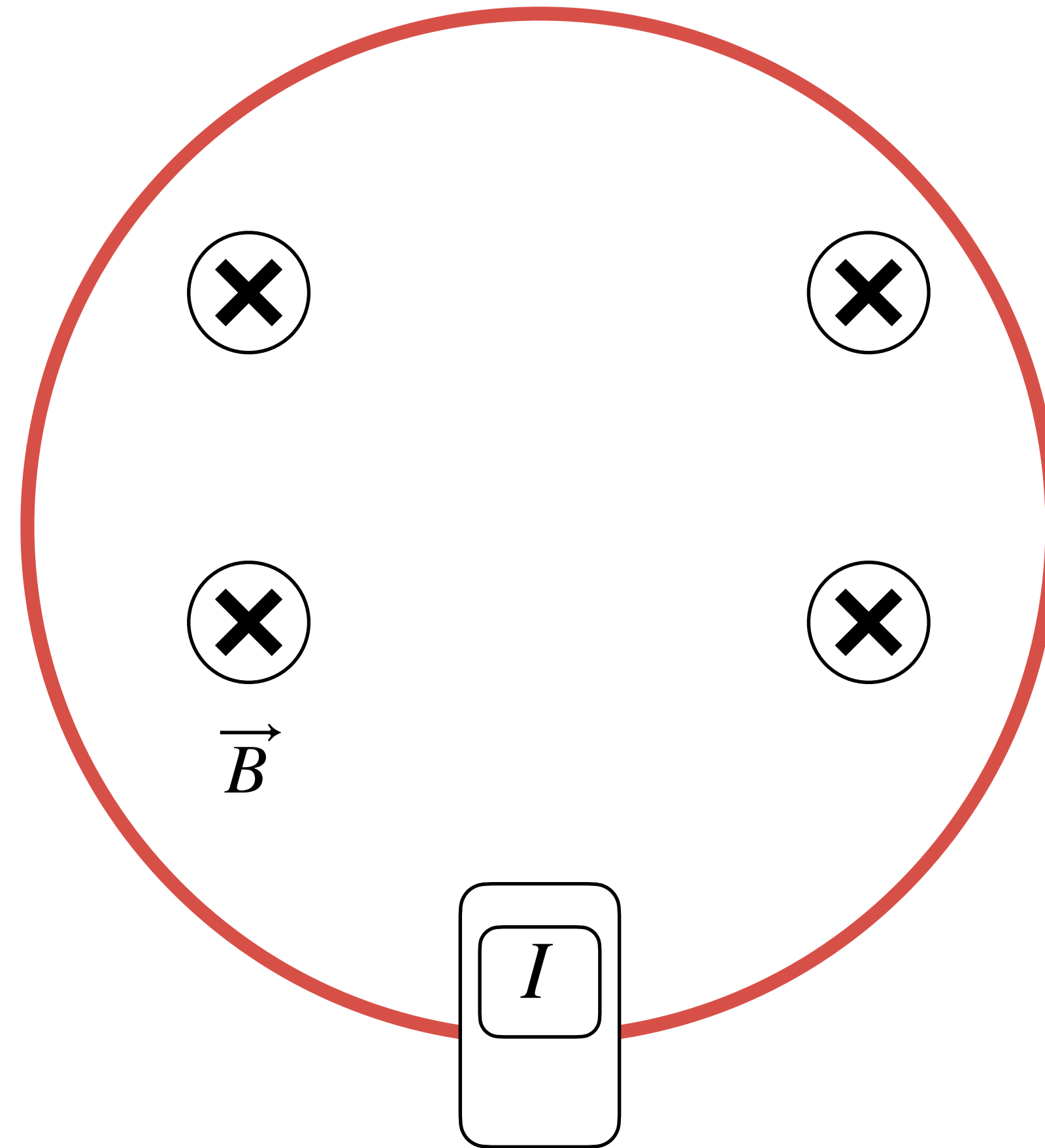
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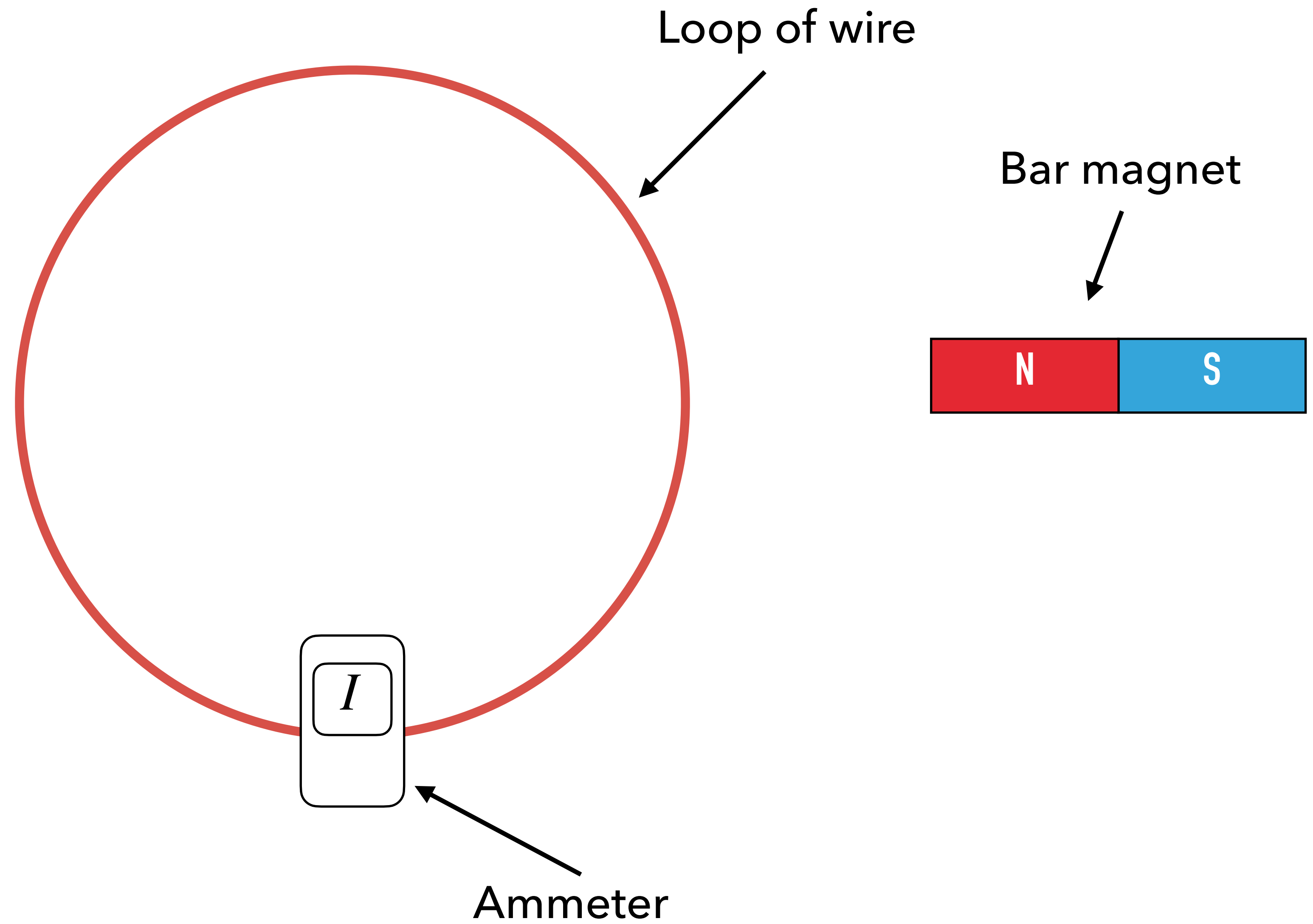
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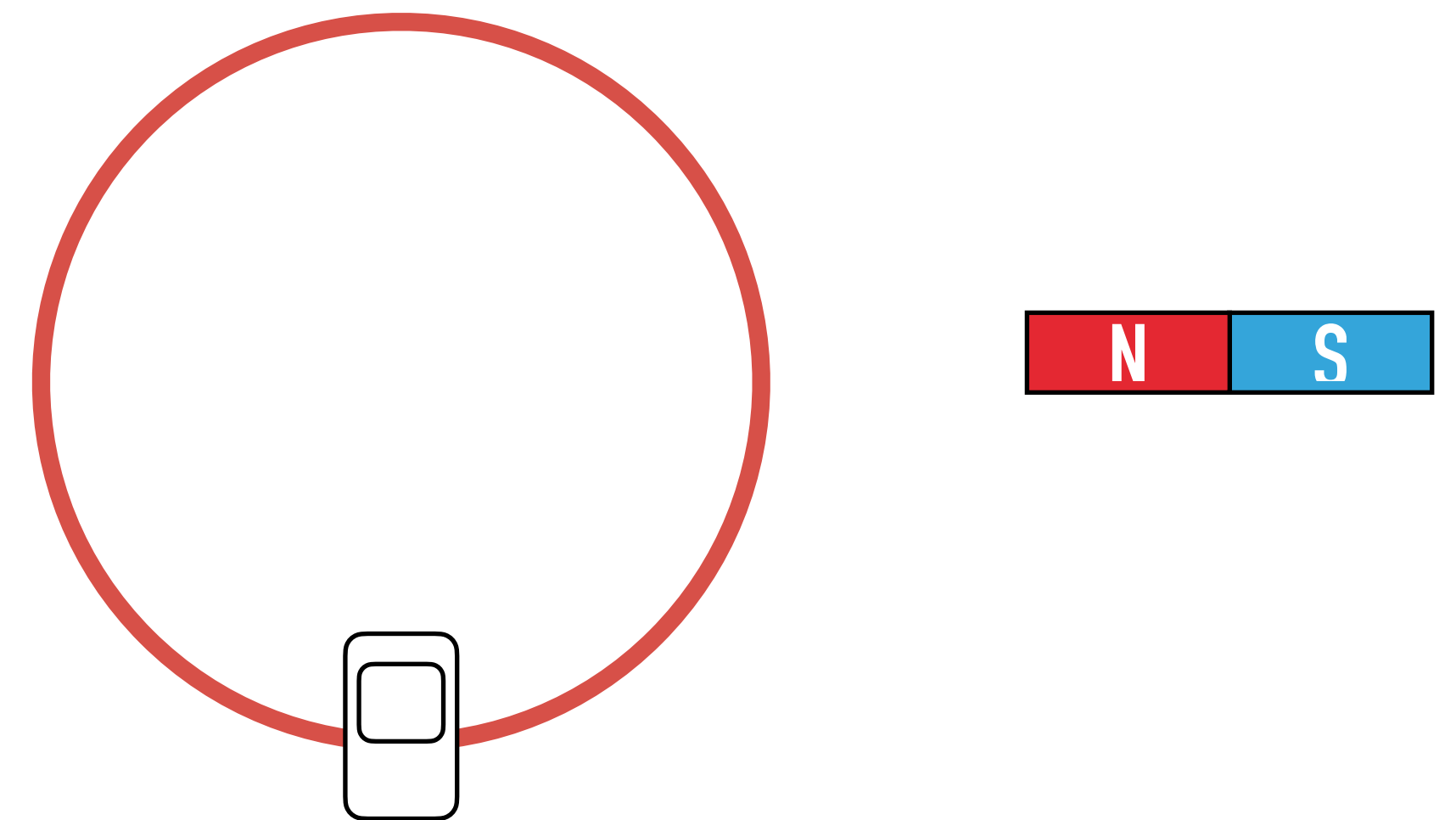


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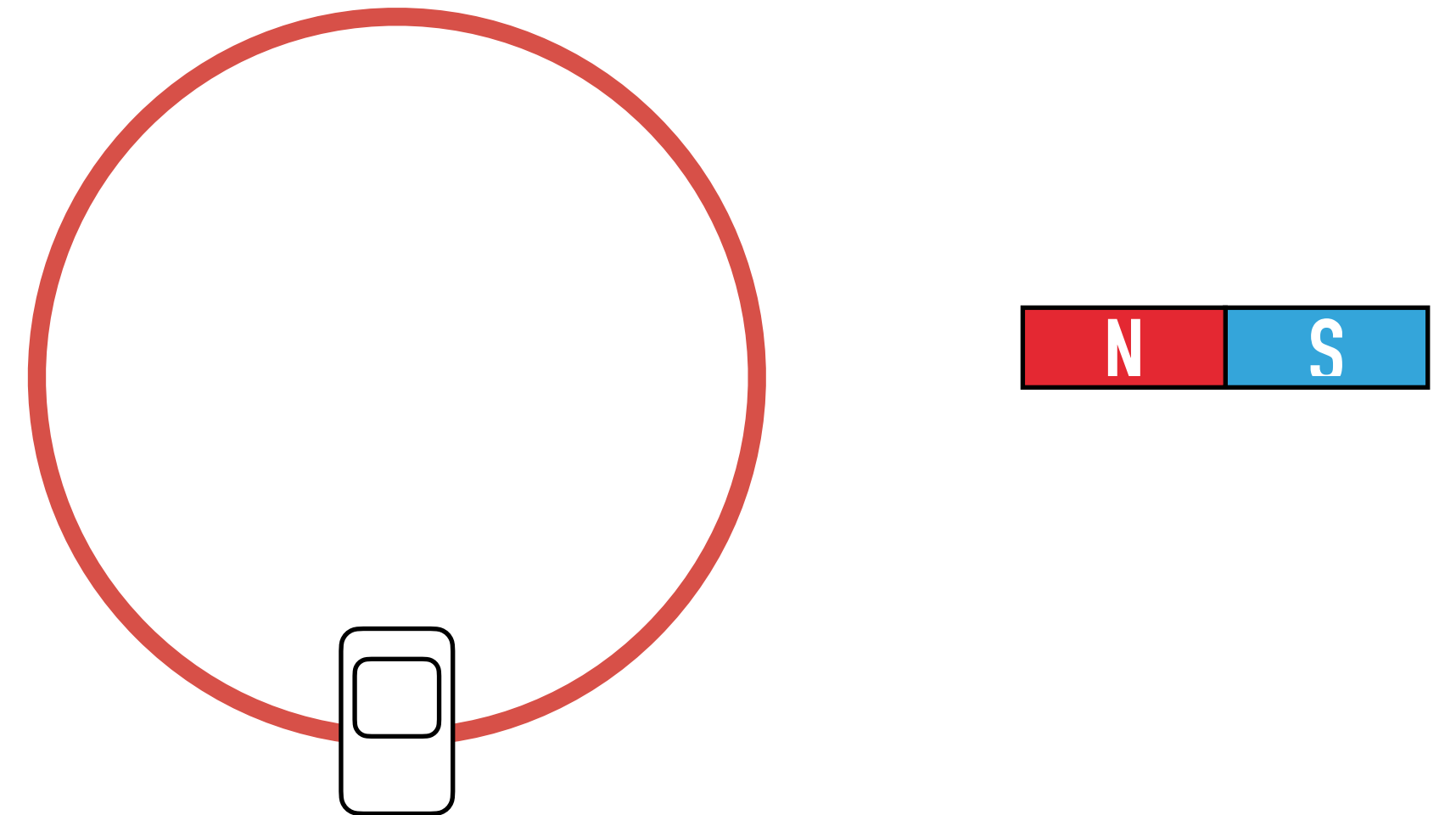
OBSERVATIONS

- 1. A changing magnetic field causes a current!**



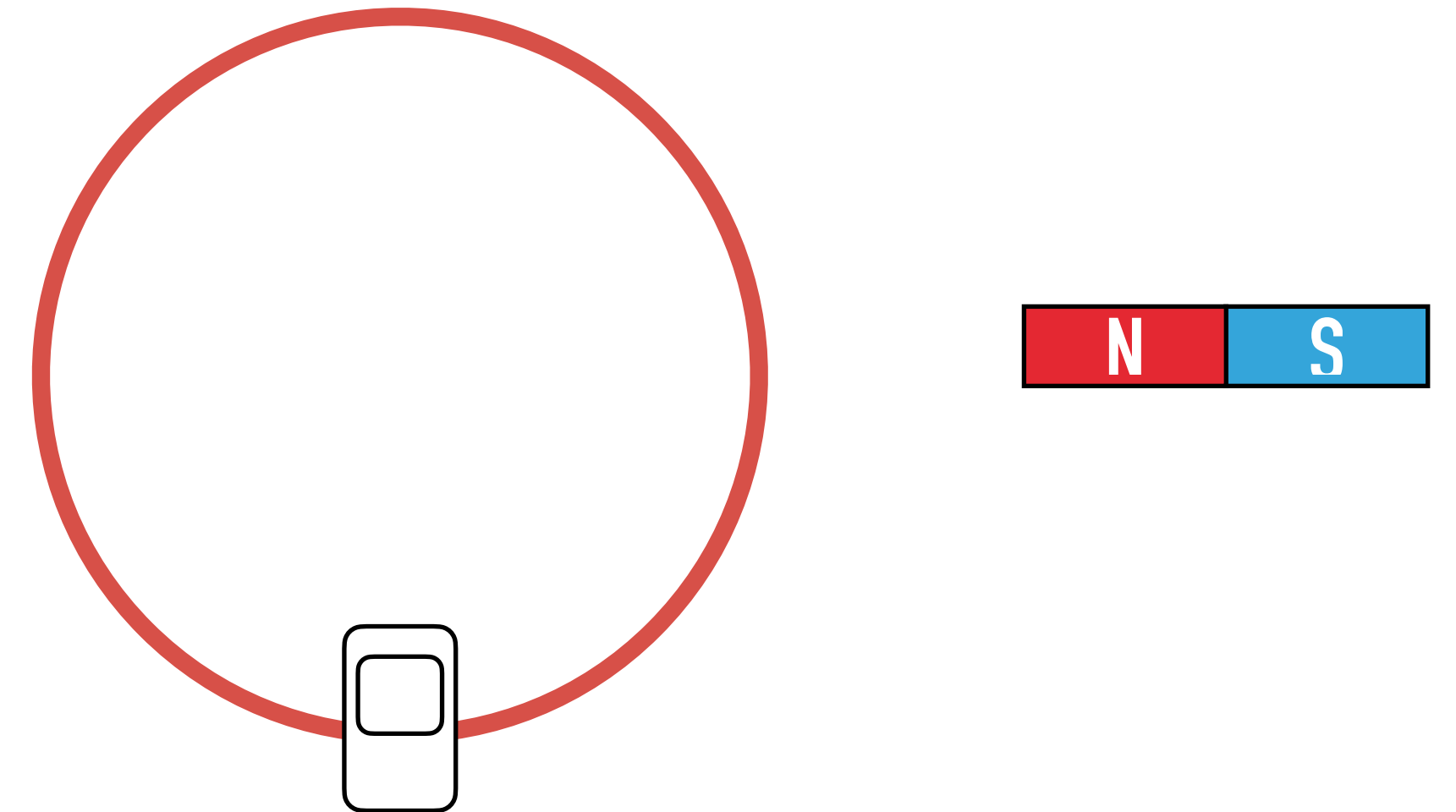
OBSERVATIONS

1. **A changing magnetic field causes a current!**
2. Unchanging magnetic field \rightarrow no current



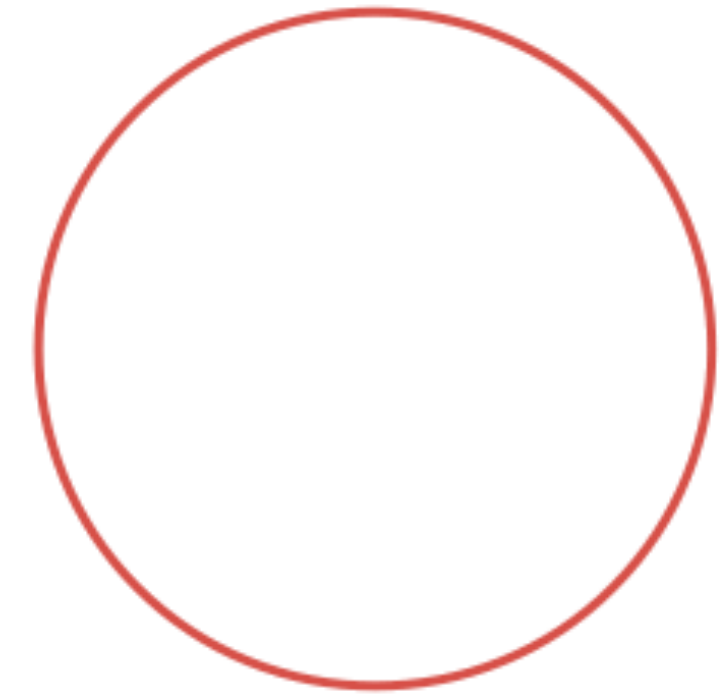
OBSERVATIONS

1. **A changing magnetic field causes a current!**
2. Unchanging magnetic field \rightarrow no current
3. Faster motion causes a larger current



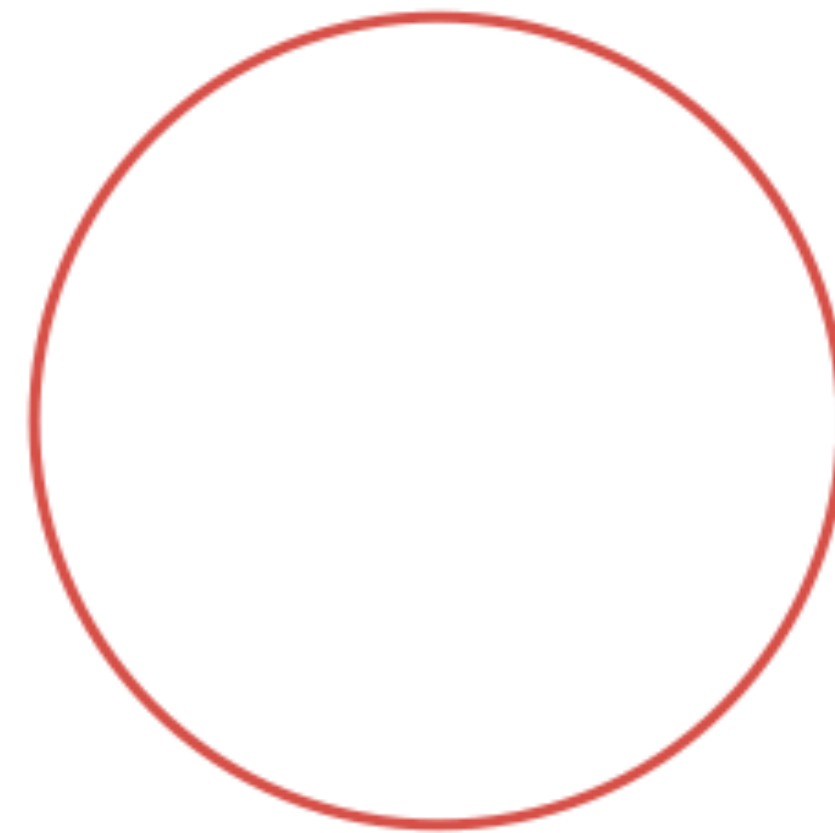
OBSERVATIONS

1. **A changing magnetic field causes a current!**
2. Unchanging magnetic field \rightarrow no current
3. Faster motion causes a larger current
4. Direction of current depends on direction of motion of magnet (and orientation!)



INDUCED EMF

- ▶ Current is caused by an emf in the wire
- ▶ Emf is caused by changing magnetic field

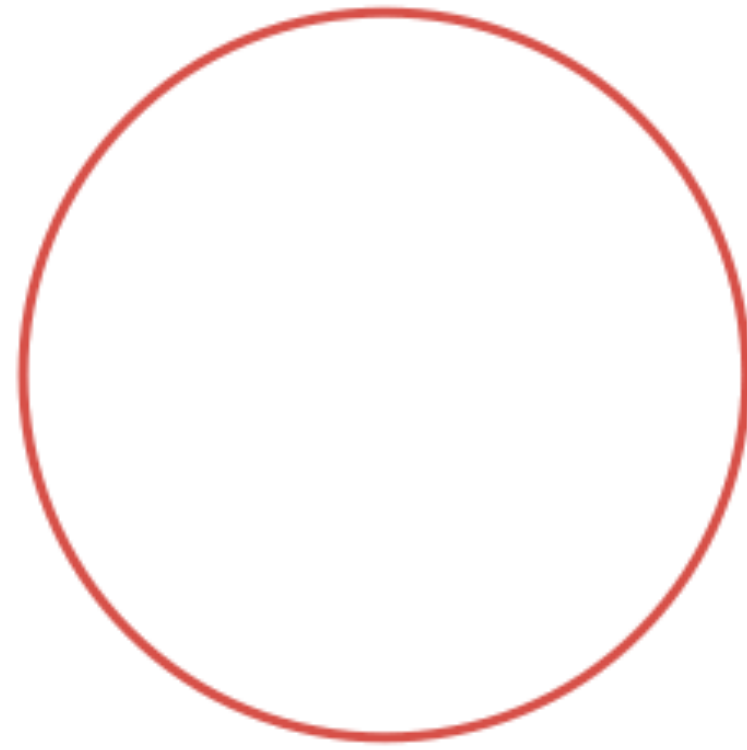


WHAT CAUSES THE EMF?

- ▶ Magnetic field *cannot do work*
- ▶ What is causing the charges in the wire to accelerate?

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- ▶ Magnetic field *cannot do work*
- ▶ What is causing the charges in the wire to accelerate?
 - ▶ It must be an *electric field*



CONCLUSION

A changing magnetic field creates an electric field!

QUANTIFYING THE RELATIONSHIP

- ▶ Changing magnetic field produces a curly electric field
- ▶ Curly electric field drives an emf ε in a loop of wire
- ▶ How is ε related to $\frac{dB}{dt}$?

OBSERVATIONS

Magnitude of induced emf in loop depends on:

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OBSERVATIONS

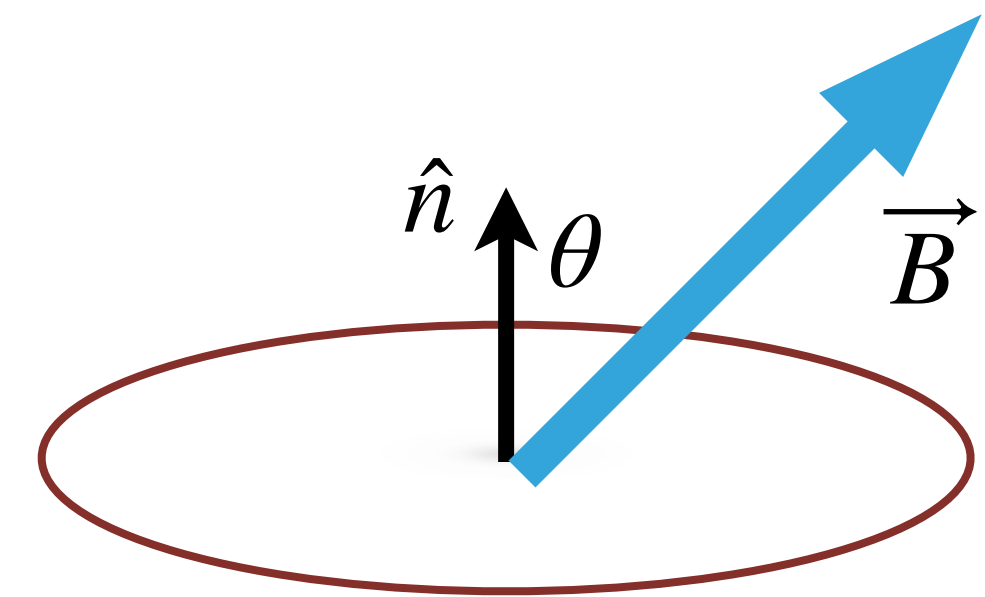
Magnitude of induced emf in loop depends on:

1. Rate of change of magnetic field (higher $\frac{dB}{dt} \rightarrow$ higher ε)
2. Area of loop (larger area \rightarrow larger ε)

OBSERVATIONS

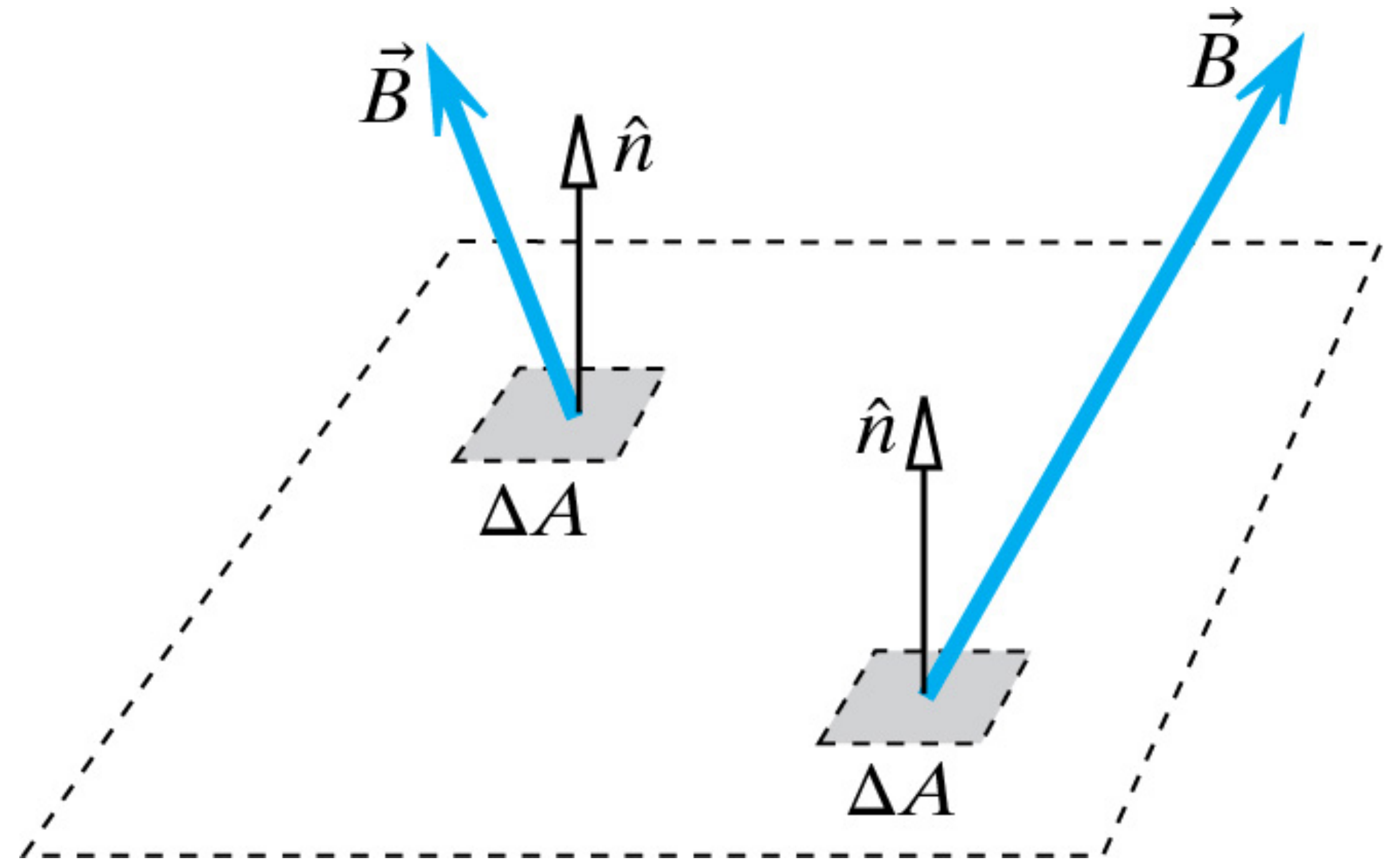
Magnitude of induced emf in loop depends on:

1. Rate of change of magnetic field (higher $\frac{dB}{dt} \rightarrow$ higher ε)
2. Area of loop (larger area \rightarrow larger ε)
3. Angle of magnetic field through loop ($\varepsilon \propto \cos \theta$)



MAGNETIC FLUX

$$\phi_B = \sum \vec{B} \cdot \hat{n} \Delta A \rightarrow \int \vec{B} \cdot \hat{n} dA$$

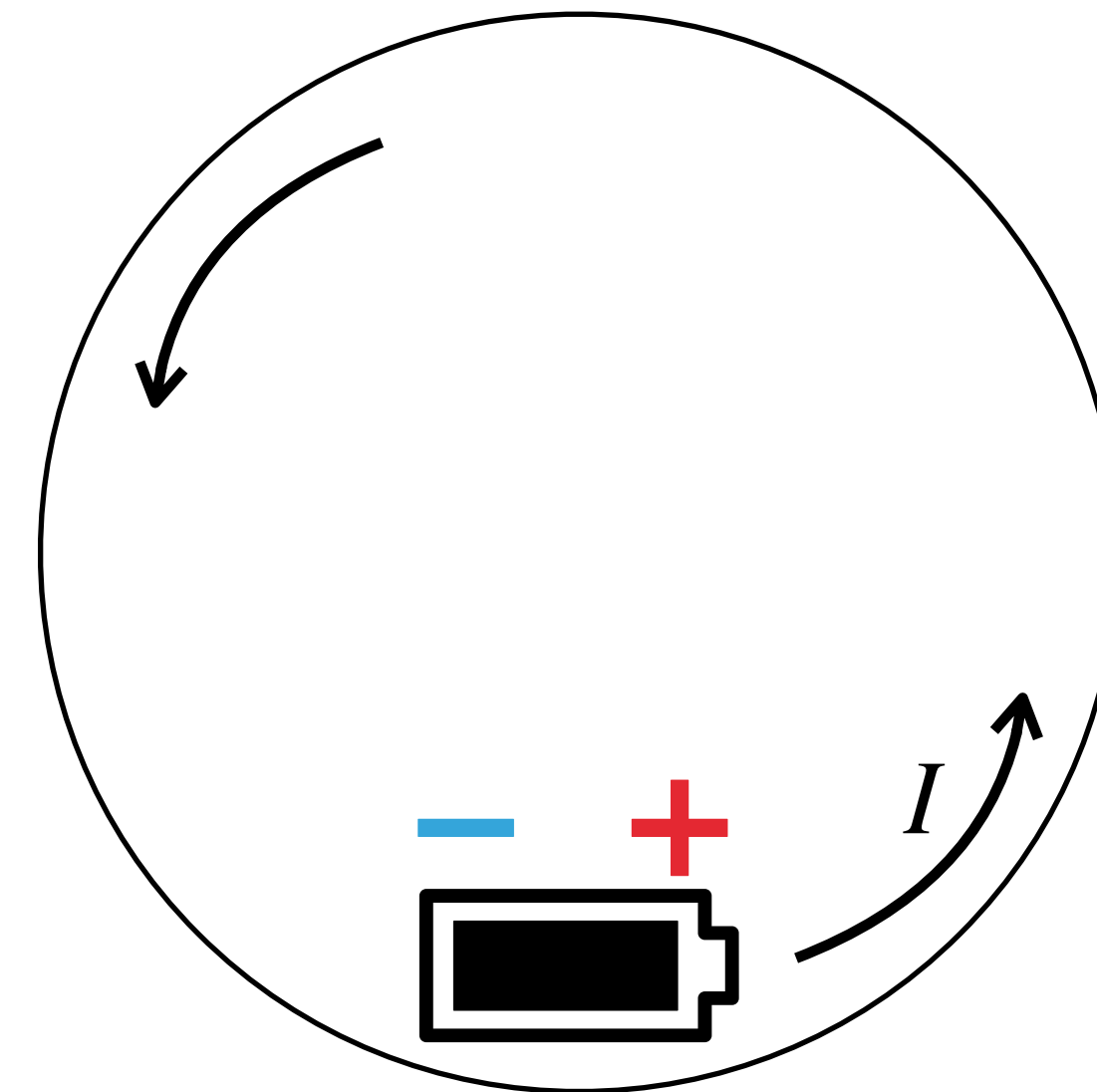


FARADAY'S LAW

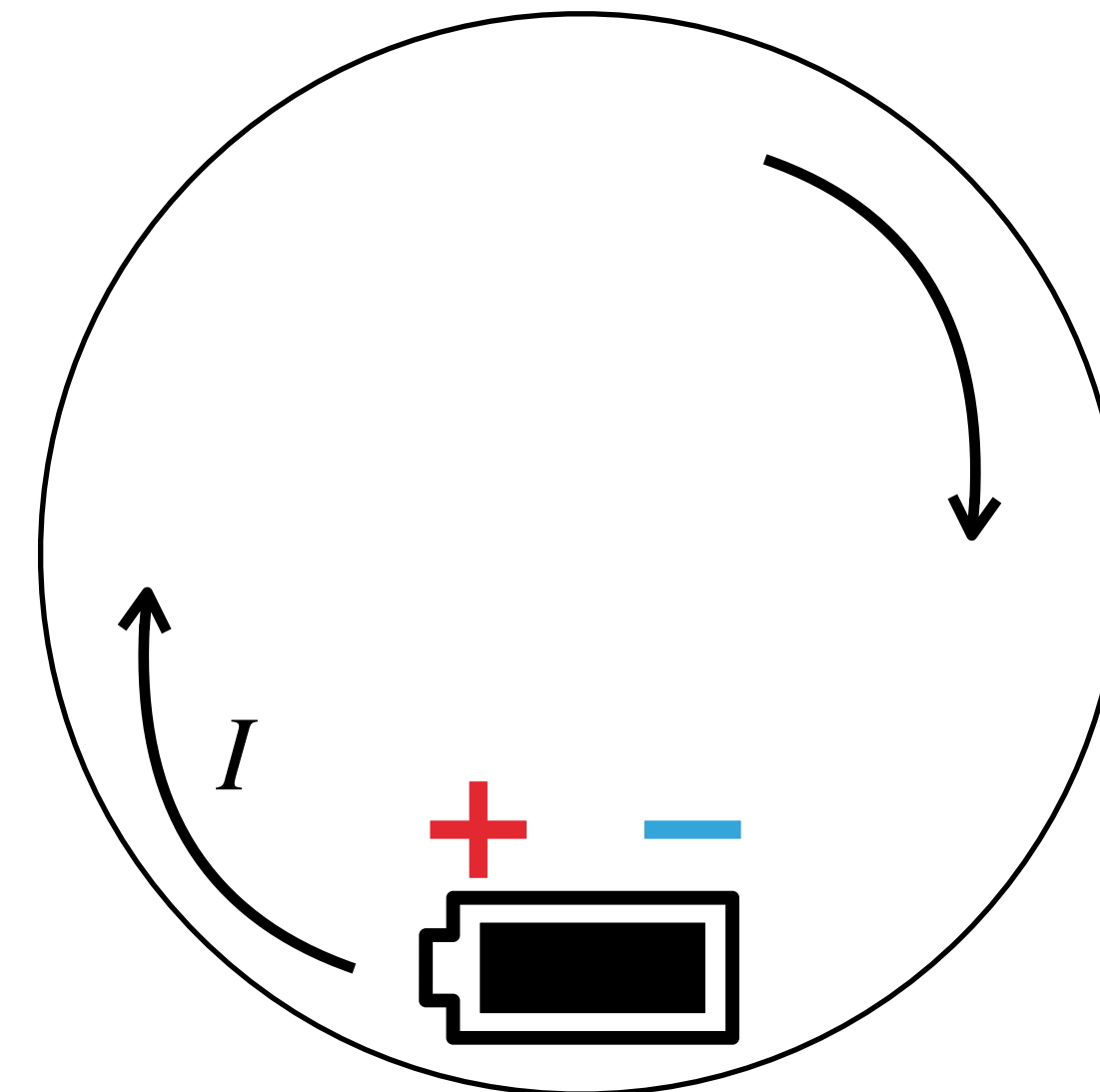
$$\mathcal{E} = - \frac{d\phi_B}{dt}$$

THE SIGN (POLARITY) OF THE EMF

- ▶ How to determine the polarity of the induced emf?



OR



FARADAY'S LAW (FORMAL VERSION)

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d}{dt} \int \vec{B} \cdot \hat{n} dA$$

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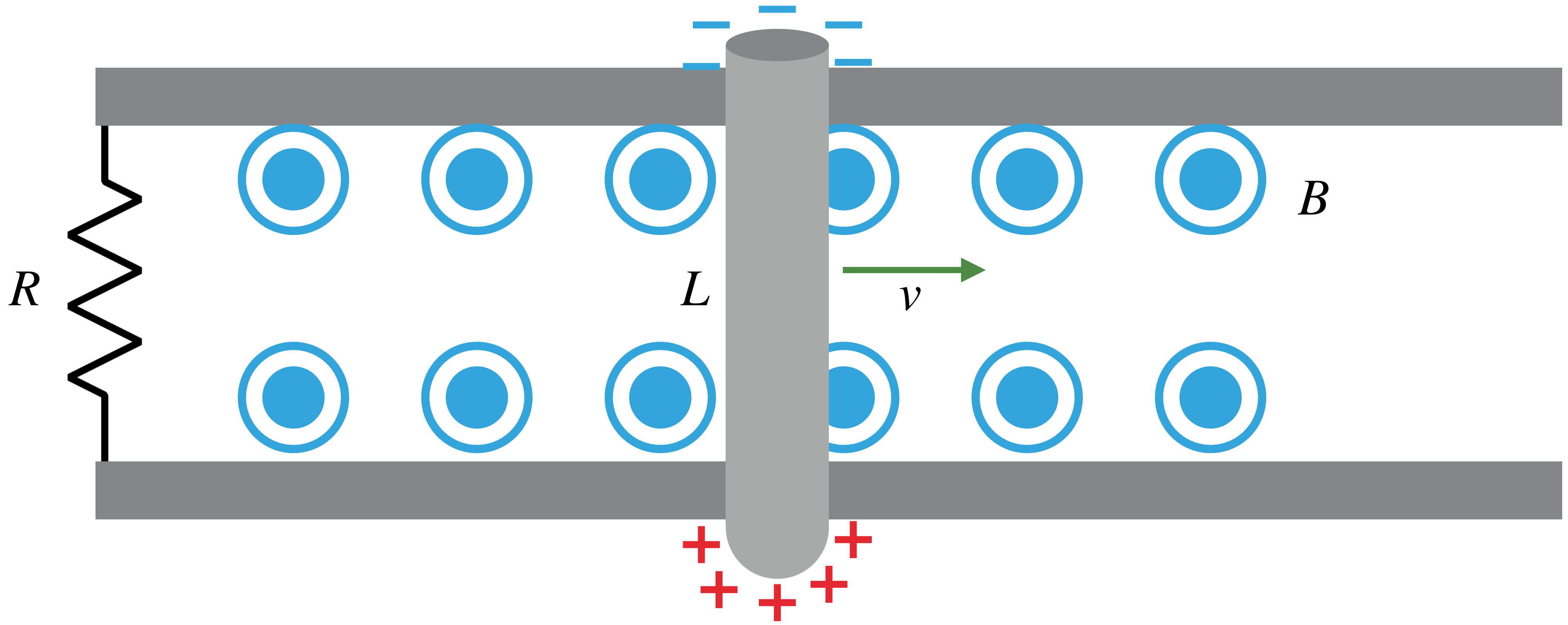
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$\oint \vec{E} \cdot d\vec{l} = - \int \vec{B} \cdot \hat{n} dA$	Faraday's Law 	<ul style="list-style-type: none">▶ Curly electric field produced by time-varying magnetic field
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FARADAY'S LAW AND MOTIONAL EMF

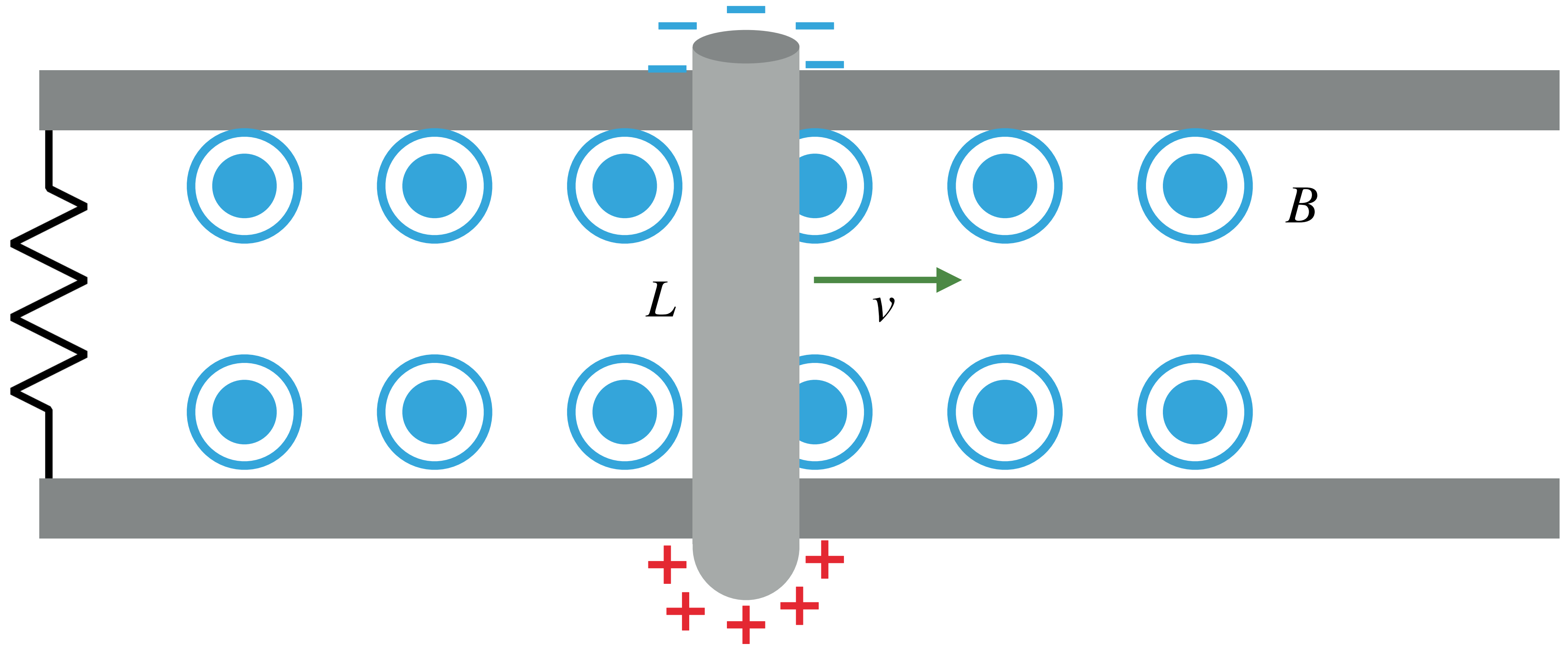
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conducting
bar sliding in
presence of
magnetic
field

- ▶ $\varepsilon = BLv$



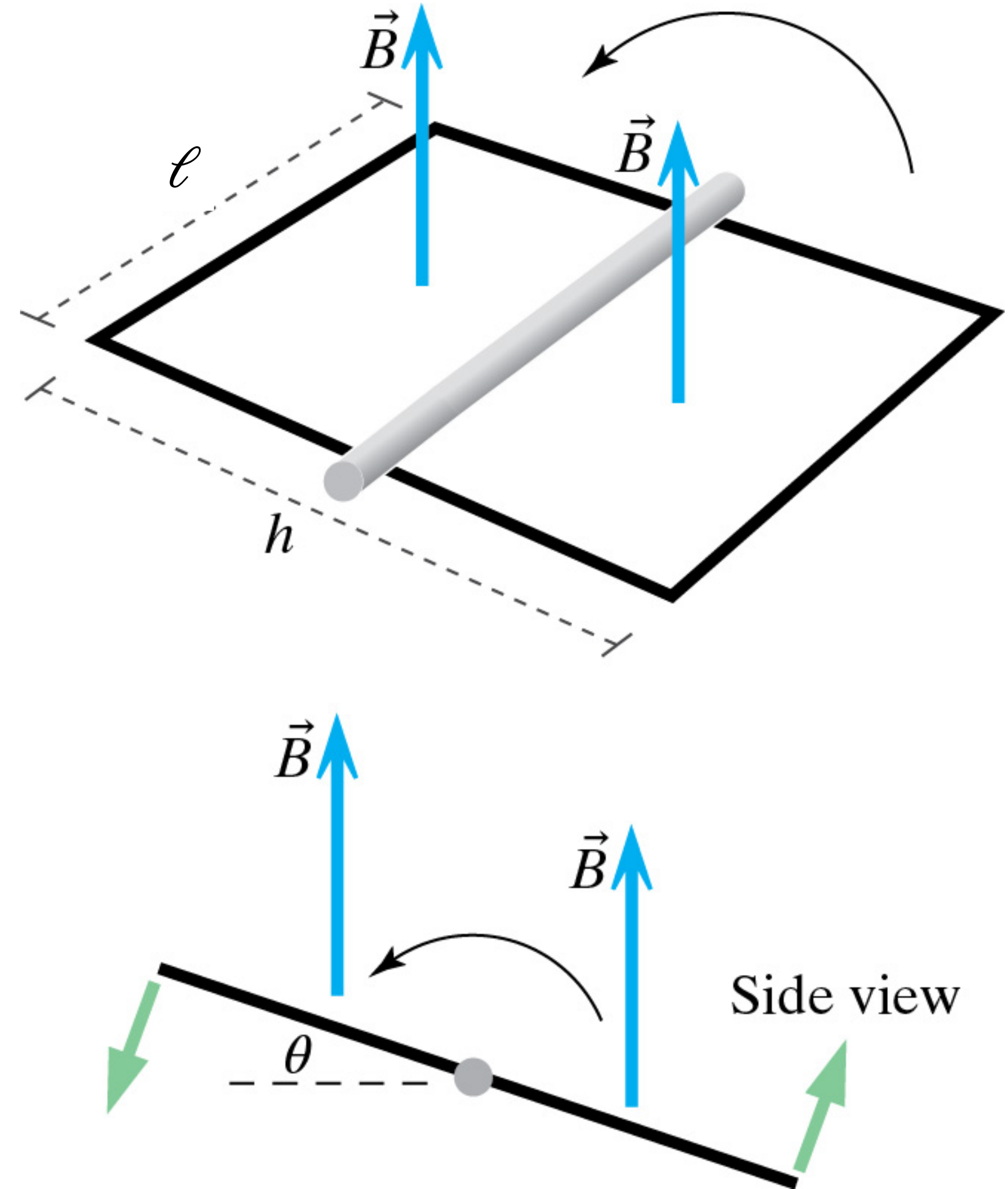
FARADAY'S LAW AND MOTIONAL EMF

- ▶ Recall:
conducting
bar sliding in
presence of
magnetic field B
- ▶ $\mathcal{E} = BLv$
- ▶ Can derive
with Faraday's
Law

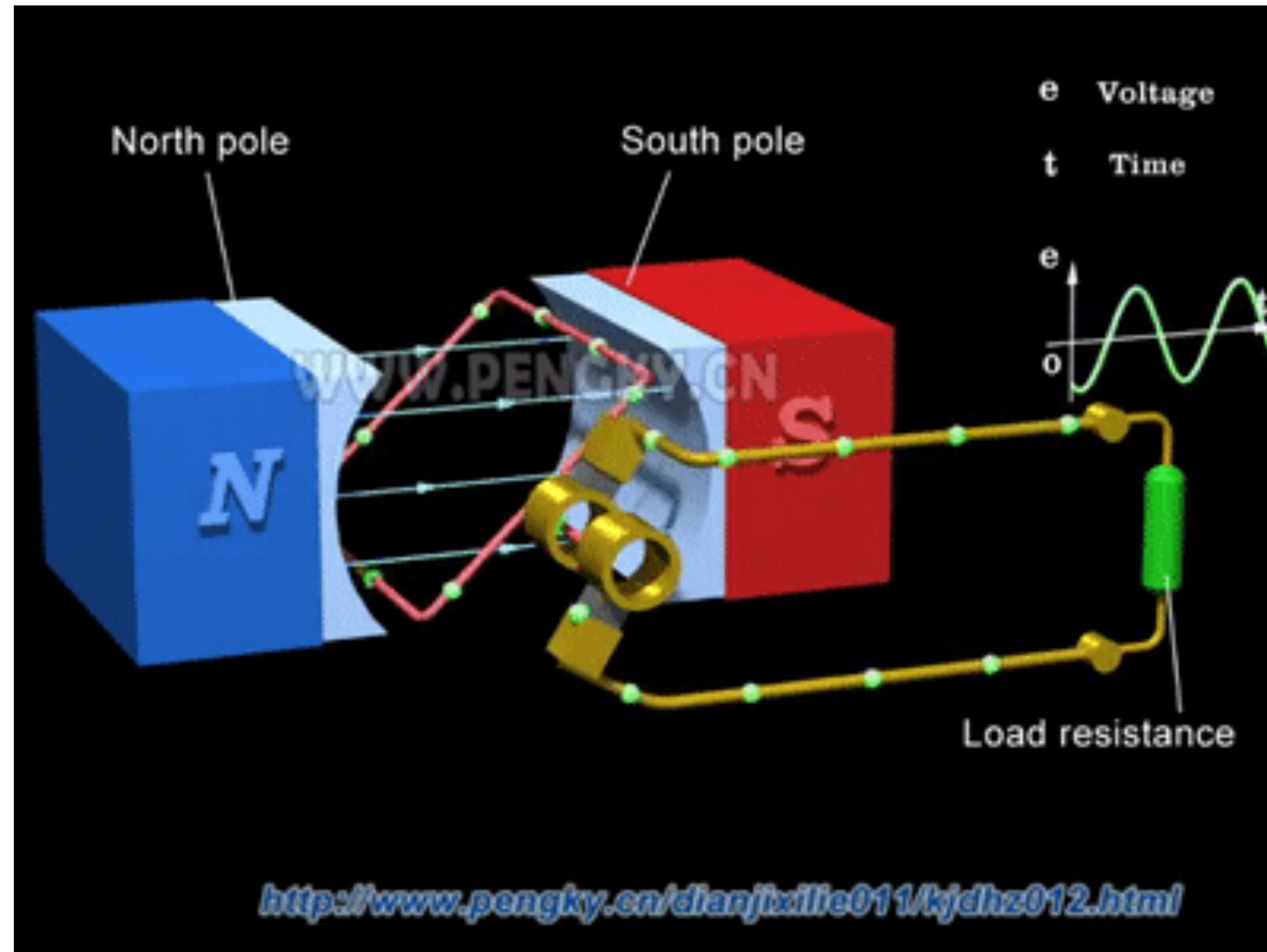


EXAMPLE

- ▶ Rotating loop of wire in presence of steady magnetic field
- ▶ Rotating at constant angular speed $\omega = \frac{d\theta}{dt}$



GENERATORS



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