

Heat Engines + Refrigerators

Goals: Basic operating principles of engines + refrigerators

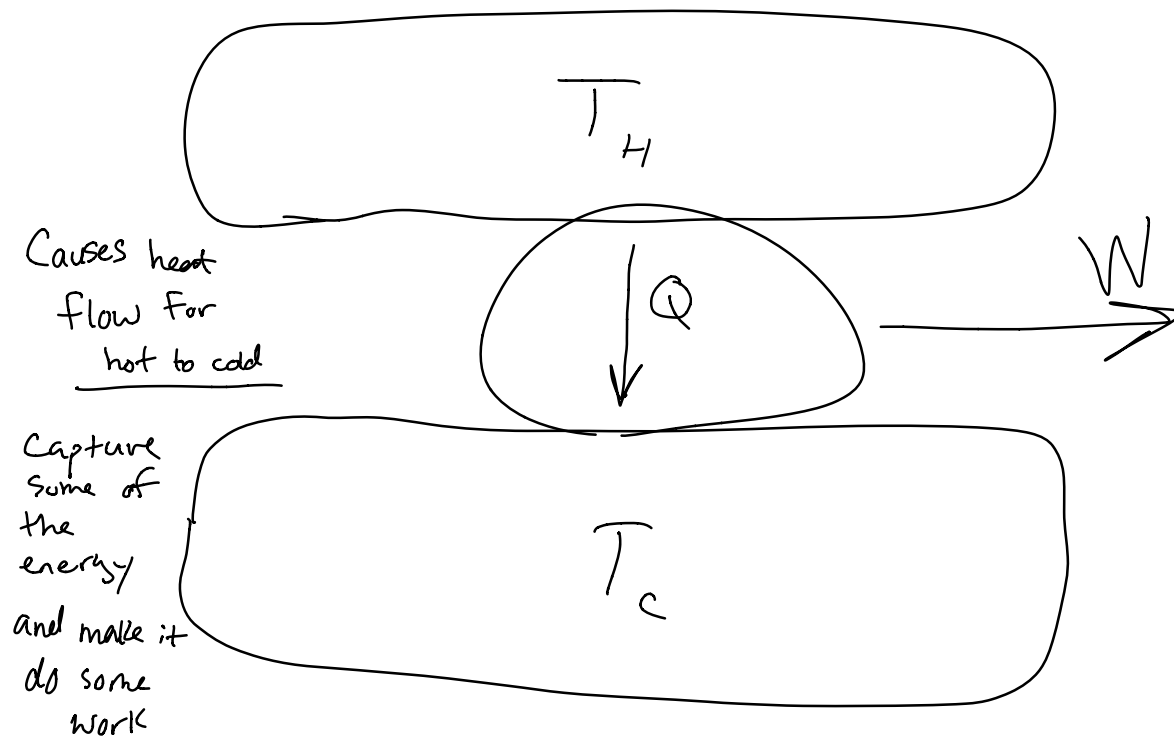
Fundamentally limited by entropy

Don't care about actual engines!

Engine: Basic Idea

Want to do some work

Need some energy



T_H : hot reservoir

T_C : cold reservoir

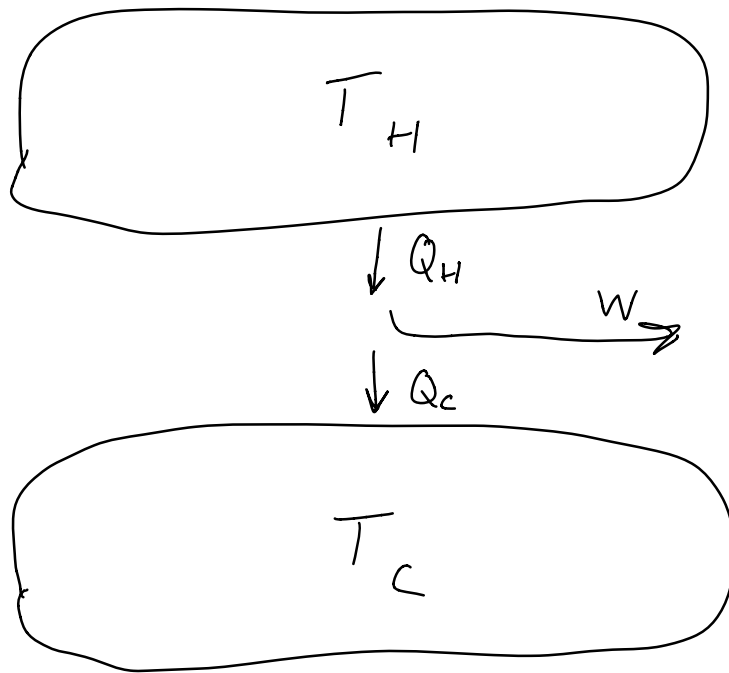
reservoir: very large material whose
temp is unaffected by heat flow

We cannot "use" all of this energy

Entropy of Hot reservoir decreases as
heat leaves

$$dU = T dS \longrightarrow dS = \frac{dU}{T} = \frac{Q}{T}$$

- There must be some "waste heat"



$$Q_H = W + Q_C$$

Efficiency: $\frac{W}{Q_H} = \epsilon$

$$\epsilon = \frac{Q_H - Q_C}{Q_H} = 1 - \frac{Q_C}{Q_H}$$

Neglecting any ΔS from Work done:

$$\Delta S = -\frac{Q_H}{T_H} + \frac{Q_C}{T_C}$$

$$2^{\text{nd}} \text{ Law: } \Delta S \geq 0$$

$$-\frac{Q_H}{T_H} + \frac{Q_C}{T_C} \geq 0$$

$$\Rightarrow \frac{Q_C}{T_C} \geq \frac{Q_H}{T_H}$$

$$\frac{Q_C}{Q_H} \geq \frac{T_C}{T_H}$$

$$e = 1 - \frac{Q_C}{Q_H}$$

$$e \leq 1 - \frac{T_C}{T_H}$$

$$\text{Ex: } T_H = 500 \text{ K}$$

$$T_C = 300 \text{ K}$$

$$e = 1 - 0.6 = 0.4$$

40% of spontaneous heat flow
is usable for work

1) Conservation of energy: $\epsilon \leq 1$

$$\epsilon = \frac{W}{Q_h} \quad \text{Can't get more out than you put in}$$

2) Second law

$$\epsilon \leq 1 - \frac{T_c}{T_h} ;$$

If $T_c = 0$ and/or $T_h = \infty$, $\epsilon = 1$

But this is impossible!

- How to cool something down to 0 K?

Need to remove energy from it

Energy flows from hotter to colder

To cool down to 0 K, we need something
colder than 0 K

$$+ T < \infty$$

First Law: can't get out than you put in

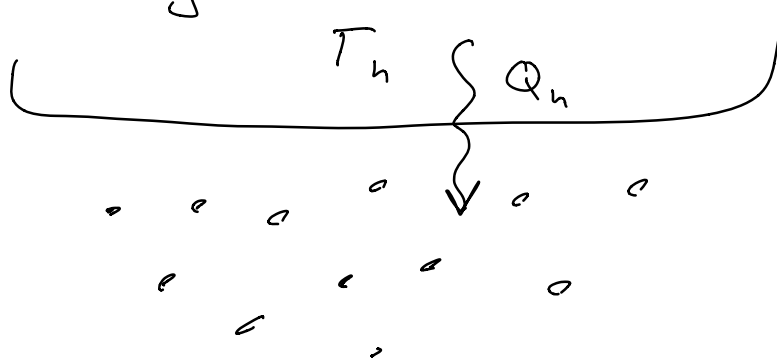
Second Law: must get less out than you put in

Can only approach $\epsilon = 1 - \frac{T_c}{T_h}$ if the rest of the engine creates minimal (0) entropy

- A theoretical engine cycle which creates no entropy is the Carnot Cycle
- Consider an Engine which uses a gas as the working material

The engine cycle consists of several steps

- 1) Transfer heat Q_h from the hot reservoir to the gas



$$\Delta S = -\frac{Q_h}{T_h} + \frac{Q_h}{T_{\text{gas}}}$$

$\Delta S = 0$ if $T_h = T_{\text{gas}}$, but then no heat flows

Want T_{gas} to be just smaller than T_h

- Need to prevent T_{gas} from increasing
as heat enters it

Let it expand isothermally

First step in cycle

isothermal expansion at hot temp

When the "wasted" heat leaves the gas

To minimize entropy when Q_c leaves the gas
for the cold reservoir, want T_{gas} to
be close to, but just above, T_c

as heat leaves gas, temp decreases
unless we compress it

isothermal compression at low temp

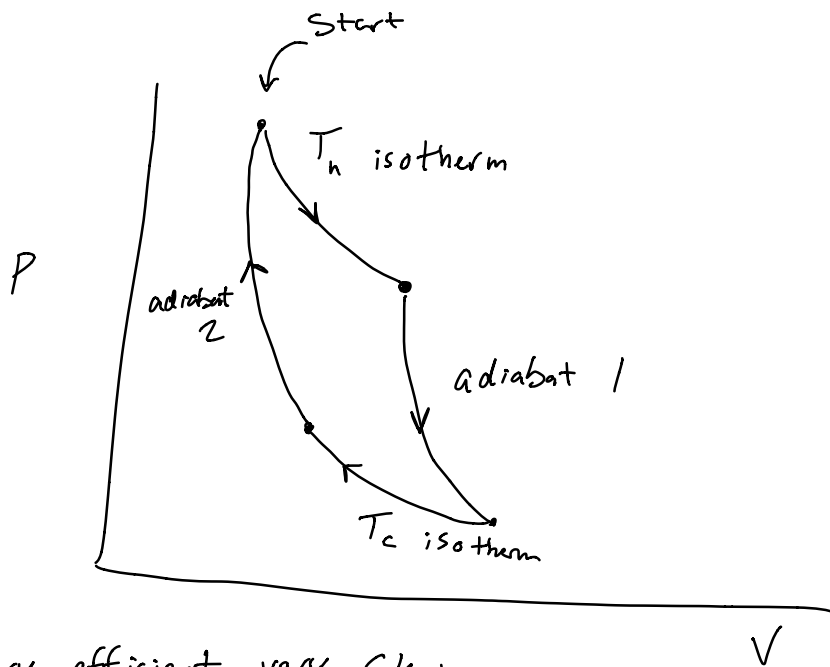
How do we get the gas from hot to cold?

- Don't want any heat exchange

Adiabatic expansion

The Carnot Cycle

- 1) Isothermal expansion near T_h
- 2) Adiabatic expansion from T_h to T_c
- 3) Isothermal compression near T_c
- 4) Adiabatic compression to get back up to T_h



very efficient, very slow