15-213: Midterm Review Session

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Agenda

- **■** Review midterm problems
 - **■**Cache
 - Assembly
 - **■Stack**
 - **■Floats, Arrays, Structs**
- Q&A for general midterm problems

Reminders

- We may or may not be holding office hours over the break.
- If you would like for us to have them, please fill out the survey on Canvas
 - If you need any help with midterm questions after today, please make a <u>public</u> Piazza post (and specify exactly which question!)
- Cheat sheet: ONE 8½ x 11 in. sheet, both sides.

- Typical questions asked
 - Given a function, look at assembly to fill in missing portions
 - Given assembly of a function, intuit the behavior of the program
 - (More rare) Compare different chunks of assembly, which one implements the function given?
- Important things to remember/put on your cheat sheet:
 - Memory Access formula: D(Rb,Ri,S)
 - Distinguish between mov/lea instructions,
 - instructions that alter control flows: cmp Src, Dest, test,...etc

Consider the following x86-64 code (Recall that %cl is the low-order byte of %rcx):

```
# On entry:
#
    %rdi = x
#
    %rsi = y
#
    %rdx = z
4004f0 <mysterious>:
  4004f0:
                    $0x0, %eax
            mov
                    -0x1(%rsi),%r9d
  4004f5:
            lea
  4004f9:
                    400510 <mysterious+0x20>
            jmp
  4004fb:
            lea
                    0x2(%rdx),%r8d
  4004ff:
                    %esi,%ecx
            mov
  400501:
            shl
                    %cl,%r8d
  400504:
            mov
                    %r9d,%ecx
  400507:
                    %cl,%r8d
            sar
  40050a:
            add
                    %r8d, %eax
  40050d:
                    $0x1, %edx
            add
                    %edx, %edi
  400510:
            CMP
  400512:
                    4004fb <mysterious+0xb>
            ja
  400514:
            reta
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i = Z ; ; ; ; ; )){
    e = i + 2;
    e = ;
    e = ;
    d = ;
}
return ;
}
```

```
# On entry:
   rdi = x
   %rsi = v
   rdx = z
4004f0 <mysterious>:
  4004f0:
           mov
                  $0x0, %eax
  4004f5:
           lea
                  -0x1(%rsi),%r9d
  4004f9:
           jmp
                  400510 <mysterious+0x20>
  4004fb:
                  0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                  %esi,%ecx
  400501:
           shl
                  %cl,%r8d
  400504:
                  %r9d,%ecx
           mov
  400507:
                  %cl,%r8d
           sar
  40050a:
           add
                  %r8d, %eax
  40050d:
           add
                  $0x1, %edx
  400510:
                  %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

```
int mysterious(int x, int y, int z){
                                                                                   # On entry:
  unsigned i;
                                                                                      rdi = x
                                                                                      %rsi = v
  int d = 0;
                                                                                      rdx = z
  int e;
                                                                                   4004f0 <mysterious>:
                                                 j++
  for(i =
               Z
                                                                                     4004f0:
                                                                                                    $0x0, %eax
                                                                                             mov
     e = i + 2;
                                                                                     4004f5:
                                                                                             lea
                                                                                                    -0x1(%rsi),%r9d
                                                                                     4004f9:
                                                                                             jmp
                                                                                                    400510 <mysterious+0x20>
     e =
                                                                                     4004fb:
                                                                                                    0x2(%rdx),%r8d
                                                                                             lea
                                                                                     4004ff:
                                                                                             mov
                                                                                                    %esi,%ecx
     e =
                                                                                     400501:
                                                                                             shl
                                                                                                    %cl,%r8d
     d =
                                                                                     400504:
                                                                                             mov
                                                                                                    %r9d, %ecx
                                                                                     400507:
                                                                                                    %cl,%r8d
                                                                                             sar
                                                                                                    %r8d,%eax
                                                                                    40050a:
                                                                                             add
                                                                                    40050d:
                                                                                             add
                                                                                                    $0x1, %edx
  return
                                                                                    400510:
                                                                                                    %edx,%edi
                                                                                             cmp
                                          Loop end: add 1, compare, iterate
                                                                                    400512:
                                                                                             ja
                                                                                                    4004fb <mysterious+0xb>
                                                                                     400514:
                                                                                             retq
```

```
int mysterious(int x, int y, int z){
                                                                                 # On entry:
  unsigned i;
                                                                                     rdi = x
                                                                                     %rsi = v
  int d = 0;
                                                                                     rdx = z
  int e;
                              x > i
                                                                                 4004f0 <mysterious>:
                                                j++
  for(i =
               Z
                                                                                   4004f0:
                                                                                                  $0x0, %eax
                                                                                            mov
     e = i + 2;
                                                                                   4004f5:
                                                                                            lea
                                                                                                  -0x1(%rsi),%r9d
                                                                                   4004f9:
                                                                                            jmp
                                                                                                  400510 <mysterious+0x20>
     e =
                                                                                   4004fb:
                                                                                            lea
                                                                                                  0x2(%rdx),%r8d
                                                                                   4004ff:
                                                                                            mov
                                                                                                  %esi,%ecx
     e =
                                                                                   400501:
                                                                                            shl
                                                                                                  %cl,%r8d
     d =
                                                                                   400504:
                                                                                            mov
                                                                                                  %r9d, %ecx
                                                                                   400507:
                                                                                                  %cl,%r8d
                                                                                            sar
                                                                                                  %r8d,%eax
                                                                                   40050a:
                                                                                            add
                                                                                   40050d:
                                                                                            add
                                                                                                  $0x1, %edx
  return
                                                                                   400510:
                                                                                                  %edx,%edi
                                                                                            cmp
                                                                                   400512:
                                                                                            jа
                                                                                                  4004fb <mysterious+0xb>
            cmp %edx, %edi => (%edi - %edx > 0), same as x > i
                                                                                   400514:
                                                                                            retq
```

```
int mysterious(int x, int y, int z){
                                                                                    # On entry:
  unsigned i;
                                                                                       rdi = x
                                                                                       %rsi = v
  int d = 0;
                                                                                       rdx = z
  int e;
                                                                                    4004f0 <mysterious>:
  for(i =
                                                             ) {
               Ζ
                                  x > i
                                                    i++
                                                                                     4004f0:
                                                                                                     $0x0, %eax
                                                                                              mov
     e = i + 2;
                                                                                     4004f5:
                                                                                              lea
                                                                                                     -0x1(%rsi),%r9d
                                                                                     4004f9:
                                                                                                     400510 <mysterious+0x20>
     e =
                                                                                     4004fb:
                                                                                              lea
                                                                                                     0x2(%rdx),%r8d
                                                                                     4004ff:
                                          %r8d = 2 + %rdx (i), e = %r8d
                                                                                              mov
                                                                                                     %esi,%ecx
     e =
                                                                                     400501:
                                                                                              shl
                                                                                                     %cl,%r8d
     d =
                                                                                     400504:
                                                                                                     %r9d,%ecx
                                                                                              mov
                                                                                     400507:
                                                                                                     %cl,%r8d
                                                                                              sar
                                                                                     40050a:
                                                                                              add
                                                                                                     %r8d, %eax
                                                                                     40050d:
                                                                                              add
                                                                                                     $0x1, %edx
  return
                                                                                     400510:
                                                                                                     %edx,%edi
                                                                                              cmp
                                                                                     400512:
                                                                                              ja
                                                                                                     4004fb <mysterious+0xb>
                                                                                     400514:
                                                                                              retq
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i =
                                      j++
                         x > i
                                                ){
            Z
        i + 2;
    e =
    e =
                         We know that e = %r8d...
    e =
    d =
 return
```

```
# On entry:
   rdi = x
   %rsi = v
   rdx = z
4004f0 <mysterious>:
  4004f0:
           mov
                   $0x0, %eax
  4004f5:
           lea
                   -0x1(%rsi),%r9d
  4004f9:
           jmp
                   400510 <mysterious+0x20>
  4004fb:
                   0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                   %esi,%ecx
  400501:
           shl
                   %cl,%r8d
  400504:
                   %r9d,%ecx
           mov
  400507:
                   %cl,%r8d
           sar
  40050a:
           add
                   %r8d, %eax
  40050d:
           add
                   $0x1, %edx
  400510:
                   %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

```
int mysterious(int x, int y, int z){
                                                                                    # On entry:
  unsigned i;
                                                                                       rdi = x
                                                                                       %rsi = v
  int d = 0;
                                                                                       rdx = z
  int e;
                                                                                    4004f0 <mysterious>:
  for(i =
                                x > i
                                                 j++
                                                             ) {
               Ζ
                                                                                      4004f0:
                                                                                                     $0x0, %eax
                                                                                               mov
          i + 2;
                                                                                      4004f5:
                                                                                               lea
                                                                                                     -0x1(%rsi),%r9d
                                                                                      4004f9:
                                                                                               jmp
                                                                                                     400510 <mysterious+0x20>
     e =
             e << v
                                                                                      4004fb:
                                                                                                     0x2(%rdx),%r8d
                                                                                               lea
                                                                                     4004ff:
                                                                                                     %esi,%ecx
                                                                                               mov
     e =
                                                                                      400501:
                                                                                               shl
                                                                                                     %cl,%r8d
     d =
                                                                                      400504:
                                                                                                     %r9d,%ecx
                                                                                               mov
                                                                                                     %cl,%r8d
                                                                                      400507:
                                                                                               sar
                                                                                      40050a:
                                                                                               add
                                                                                                     %r8d,%eax
                                                                                      40050d:
                                                                                               add
                                                                                                     $0x1, %edx
  return
                                                                                      400510:
                                                                                                     %edx,%edi
                                                                                               cmp
                                                                                      400512:
                                                                                               ja
                                                                                                     4004fb <mysterious+0xb>
                                                                                      400514:
                                                                                               retq
  Where did %cl come from?
                                      %есх
                                                               %ch
                                                       &CX
                                                                         %cl
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i = Z ; x > i ; i++ ){
    e = i + 2;
    e = e << y ;
    e = ; Again, e = %r8d...
    d = ;
}
return ;
}</pre>
```

```
# On entry:
    rdi = x
   %rsi = v
   rdx = z
4004f0 <mysterious>:
  4004f0:
                   $0x0, %eax
           mov
  4004f5:
           lea
                   -0x1(%rsi),%r9d
  4004f9:
           jmp
                   400510 <mysterious+0x20>
  4004fb:
                   0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                   %esi,%ecx
  400501:
           shl
                   %cl,%r8d
  400504:
                   %r9d,%ecx
           mov
  400507:
                   %cl,%r8d
           sar
  40050a:
           add
                   %r8d, %eax
  40050d:
           add
                   $0x1, %edx
  400510:
                   %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

```
int mysterious(int x, int y, int z){
                                                                                     # On entry:
  unsigned i;
                                                                                         rdi = x
                                                                                         %rsi = v
  int d = 0;
                                                                                         rdx = z
  int e;
                                                                                     4004f0 <mysterious>:
  for(i =
                                                  j++
                                x > i
                                                              ) {
                Ζ
                                                                                       4004f0:
                                                                                                       $0x0, %eax
                                                                                                mov
          i + 2;
                                                                                       4004f5:
                                                                                                lea
                                                                                                       -0x1(%rsi),%r9d
                                                                                       4004f9:
                                                                                                       400510 <mysterious+0x20>
                                                                                                jmp
     e =
              e << v
                                                                                       4004fb:
                                                                                                       0x2(%rdx),%r8d
                                                                                                lea
                                                                                       4004ff:
           e >> (y - 1)
                                                                                                mov
                                                                                                       %esi,%ecx
                                                                                       400501:
                                                                                                shl
                                                                                                       %cl,%r8d
                                                                                       400504:
     d =
                                                                                                       %r9d,%ecx
                                                                                                mov
                                                                                       400507:
                                                                                                       %cl,%r8d
                                                                                                sar
                                                                                       40050a:
                                                                                                add
                                                                                                       %r8d,%eax
                                                                                       40050d:
                                                                                                add
                                                                                                       $0x1, %edx
  return
                                                                                       400510:
                                                                                                       %edx,%edi
                                                                                                cmp
                                                                                       400512:
                                                                                                ja
                                                                                                       4004fb <mysterious+0xb>
                                                                                       400514:
                                                                                                retq
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i = Z ; x > i ; i++ ){
    e = i + 2;
    e = e << y ;
    e = e >> (y - 1);
    d = ; What's left?
}
return ;
}
```

```
# On entry:
    rdi = x
    %rsi = v
    rdx = z
4004f0 <mysterious>:
  4004f0:
                   $0x0, %eax
           mov
  4004f5:
           lea
                   -0x1(%rsi),%r9d
  4004f9:
           jmp
                   400510 <mysterious+0x20>
  4004fb:
                   0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                   %esi,%ecx
  400501:
           shl
                   %cl,%r8d
 400504:
                   %r9d,%ecx
           mov
  400507:
                   %cl,%r8d
           sar
  40050a:
           add
                   %r8d, %eax
  40050d:
           add
                   $0x1, %edx
  400510:
                   %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

```
int mysterious(int x, int y, int z){
                                                                                   # On entry:
  unsigned i;
                                                                                       rdi = x
                                                                                      %rsi = y
  int d = 0;
                                                                                       rdx = z
  int e;
                                                                                   4004f0 <mysterious>:
  for(i =
                               x > i
                                                 j++
                                                             ) {
              Z
                                                                                     4004f0:
                                                                                                    $0x0,%eax
                                                                                              mov
     e = i + 2;
                                                                                     4004f5:
                                                                                              lea
                                                                                                    -0x1(%rsi),%r9d
                                                                                                    400510 <mysterious+0x20>
                                                                                     4004f9:
                                                                                              jmp
             e << v
                                                                                     4004fb:
                                                                                                    0x2(%rdx),%r8d
                                                                                              lea
                                                                                     4004ff:
           e >> (y - 1)
                                                                                              mov
                                                                                                    %esi,%ecx
                                                                                     400501:
                                                                                              shl
                                                                                                    %cl,%r8d
     d =
              e + d
                                                                                     400504:
                                                                                                    %r9d,%ecx
                                                                                              mov
                                                                                     400507:
                                                                                                    %cl,%r8d
                                                                                              sar
                                                                                     40050a:
                                                                                                    %r8d, %eax
                                                                                              add
                                                                                     40050d:
                                                                                              add
                                                                                                    $0x1, %edx
  return
                                                                                     400510:
                                                                                                    %edx,%edi
                                                                                              cmp
                                                                                     400512:
                                                                                                    4004fb <mysterious+0xb>
                                                                                              jа
                                                                                     400514:
                                                                                              retq
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i = z ; x>i ; i++ ){
    e = i + 2;
    e = e << y ;
    e = e >> (y-1);
    d = e + d ;
}
return ;
}
```

```
# On entry:
    rdi = x
   %rsi = v
    rdx = z
4004f0 <mysterious>:
  4004f0:
                  $0x0, %eax
           mov
  4004f5:
           lea
                  -0x1(%rsi),%r9d
  4004f9:
           jmp
                  400510 <mysterious+0x20>
  4004fb:
                  0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                  %esi,%ecx
  400501:
           shl
                  %cl,%r8d
  400504:
                  %r9d,%ecx
           mov
  400507:
                  %cl,%r8d
           sar
  40050a:
           add
                  %r8d, %eax
  40050d:
           add
                  $0x1, %edx
  400510:
                  %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

```
int mysterious(int x, int y, int z){
                                                                                    # On entry:
  unsigned i;
                                                                                        rdi = x
                                                                                        %rsi = v
  int d = 0;
                                                                                        rdx = z
  int e;
                                                                                    4004f0 <mysterious>:
  for(i =
                                x > i
                                                 j++
                                                             ) {
               Z
                                                                                      4004f0:
                                                                                                     $0x0, %eax
                                                                                               mov
     e = i + 2;
                                                                                      4004f5:
                                                                                               lea
                                                                                                     -0x1(%rsi),%r9d
                                                                                      4004f9:
                                                                                               jmp
                                                                                                     400510 <mysterious+0x20>
             e << v
                                                                                      4004fb:
                                                                                                     0x2(%rdx),%r8d
                                                                                               lea
                                                                                      4004ff:
           e >> (y - 1)
                                                                                               mov
                                                                                                     %esi,%ecx
                                                                                      400501:
                                                                                               shl
                                                                                                     %cl,%r8d
     d =
                                                                                      400504:
                                                                                                     %r9d,%ecx
               e + d
                                                                                               mov
                                                                                      400507:
                                                                                                     %cl,%r8d
                                                                                               sar
                                                                                      40050a:
                                                                                               add
                                                                                                     %r8d, %eax
                                                                                      40050d:
                                                                                               add
                                                                                                     $0x1, %edx
  return
                                                                                      400510:
                                                                                                     %edx,%edi
                                                                                               cmp
                                                                                      400512:
                                                                                               ja
                                                                                                     4004fb <mysterious+0xb>
                                                                                      400514:
                                                                                               retq
```

```
int mysterious(int x, int y, int z){
  unsigned i;
  int d = 0;
  int e;
  for(i =
                         x > i
                                        j++
                                                 ) {
            Z
    e = i + 2;
           e << v
         e >> (y - 1)
    d =
            e + d
              d
 return
```

```
# On entry:
    rdi = x
   %rsi = v
   rdx = z
4004f0 <mysterious>:
  4004f0:
                  $0x0, %eax
           mov
  4004f5:
           lea
                  -0x1(%rsi),%r9d
  4004f9:
           jmp
                  400510 <mysterious+0x20>
  4004fb:
                  0x2(%rdx),%r8d
           lea
  4004ff:
           mov
                  %esi,%ecx
  400501:
           shl
                  %cl,%r8d
  400504:
                  %r9d,%ecx
           mov
  400507:
                  %cl,%r8d
           sar
  40050a:
           add
                  %r8d, %eax
  40050d:
           add
                  $0x1, %edx
  400510:
                  %edx,%edi
           cmp
  400512:
           ja
                   4004fb <mysterious+0xb>
  400514:
           retq
```

- **■** Important things to remember:
 - Stack grows <u>DOWN!</u>
 - %rsp = stack pointer, always point to "top" of stack
 - Push and pop, call and ret
 - Stack frames: how they are allocated and freed
 - Which registers used for arguments? Return values?
 - **Little endianness**
- ALWAYS helpful to draw a stack diagram!!
- Stack questions are like Assembly questions on steroids

Consider the following code:

```
void foo(char *str, int a) {
  int buf[2];
  if (a != 0xdeadbeef) {
    foo(str, 0xdeadbeef);
    return;
  }
  strcpy((char*) buf, str);
}
void caller() {
  foo("midtermexam", 0x15213);
}
```

```
caller:
foo:
        subq
                $24, %rsp
                                                 subq
                                                         $8, %rsp
        cmpl
                $0xdeadbeef, %esi
                                                movl
                                                         $86547, %esi
        je
                                                         $.LCO, %edi
                .L2
                                                 mov1
        movl
                $0xdeadbeef, %esi
                                                call
                                                         foo
        call
                foo
                                                addq
                                                         $8, %rsp
        jmp
                .L1
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
                                                                 .rodata.str1.1, "aMS", @progbits, 1
        call
                strcpy
                                                 .section
.L1:
                                         .LCO:
                $24, %rsp
                                                 .string "midtermexam"
        addq
        ret
```

Hints:

- strcpy(char *dst, char *src) copies the string at address src (including the terminating '\0' character) to address dst.
- Keep endianness in mind!
- Table of hex values of characters in

"midtermexam"

Assumptions:

- %rsp = 0x800100 just before caller() calls foo()
- .LC0 is at address 0x400300

Consider the following code:

```
caller:
foo:
        subq
                 $24, %rsp
                                                 subq
                                                          $8, %rsp
        cmpl
                 $0xdeadbeef, %esi
                                                 movl
                                                         $86547, %esi
        je
                                                          $.LCO, %edi
                 .L2
                                                 mov1
        movl
                $0xdeadbeef, %esi
                                                 call
                                                          foo
                                                                          % rsp = 0x800100
        call
                 foo
                                                 addq
                                                         $8, %rsp
        jmp
                 .L1
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
                                                                  .rodata.str1.1, "aMS", @progbits, 1
        call
                strcpy
                                                 .section
.L1:
                                         .LC0 := 0 \times 400300
        adda
                 $24, %rsp
                                                 .string "midtermexam"
        ret
```

Hints:

- strcpy(char *dst, char *src) copies the string at address src (including the terminating '\0' character) to address dst.
- Keep endianness in mind!
- Table of hex values of characters in

"midtermexam"

Assumptions:

- %rsp = 0x800100 just
 before caller() calls
 foo()
- .LC0 is at address 0x400300

Question 1: What is the hex value of %rsp just <u>before</u> strcpy() is called for the first time in foo()?

```
foo:
                                        caller:
        subq
                $24, %rsp
                                                suba
                                                        $8, %rsp
                $0xdeadbeef, %esi
                                                        $86547, %esi
        cmpl
                                                movl
        je
                .L2
                                                movl
                                                        $.LCO, %edi
                                                                         %rsp = 0x800100
                $0xdeadbeef, %esi
                                          Start call
        movl
                                                        foo
        call
                foo
                                                addq
                                                        $8, %rsp
                .L1
        dmi
                                                ret
.L2:
        movq
                %rdi, %rsi
                %rsp, %rdi
        movq
   End call
                                                .section
                                                                 .rodata.str1.1, "aMS", @progbits, 1
                strcpy
                                        .Lco: = 0x400300
.L1:
        addq
                $24, %rsp
                                                .string "midtermexam"
        ret
```

Hints:

- Step through the program instruction by instruction from start to end
- Draw a stack diagram!!!
- Keep track of registers too

Arrow is instruction that will execute NEXT

```
void foo(char *str, int a) {
                                      void caller() {
                                                                                                0x800100
                                                                                0x800100
                                                                        %rsp
   int buf[2];
                                         foo("midtermexam", 0x15213);
   if (a != 0xdeadbeef) {
                                                                                                0x8000f8
                                                                        %rdi
                                                                                .LCO
      foo(str, 0xdeadbeef);
      return;
                                                                                                0x8000f0
                                                                        %rsi
                                                                                0 \times 15213
   strcpy((char*) buf, str);
                                                                                                0x8000e8
                                                                                                0x8000e0
foo:
                                     caller:
       suba
               $24, %rsp
                                             suba
                                                     $8, %rsp
               $0xdeadbeef, %esi
                                                     $86547, %esi
       cmpl
                                             movl
                                                                                                0x8000d8
       ie
               .L2
                                             movl
                                                     $.LCO, %edi
                                                                    % rsp = 0x800100
               $0xdeadbeef, %esi
       movl
                                             call
                                                     foo
                                                                                                0x8000d0
       call
               foo
                                             addq
                                                     $8, %rsp
               .L1
       dmi
                                             ret
.L2:
                                                                                                0x8000c8
               %rdi, %rsi
       movq
               %rsp, %rdi
       movq
                                                                                                0x8000c0
   End call
                                             .section
                                                             .rodata.str1.1, "aMS", @progbits, 1
               strcpy
                                      .Lco: = 0x400300
.L1:
       addq
               $24, %rsp
                                             .string "midtermexam"
                                                                                                0x8000b8
       ret
```

%rsp	0x8000f8	
%rdi	.LCO	
%rsi	0x15213	

0x800100	?
0x8000f8	ret address for foo()
0x8000f0	
0x8000e8	
0x8000e0	
0x8000d8	
0x8000d0	
0x8000c8	
0x8000c0	
0x8000b8	

```
foo:
                                        caller:
        subq
                $24, %rsp
                                                suba
                                                         $8, %rsp
                $0xdeadbeef, %esi
                                                         $86547, %esi
        cmpl
                                                movl
        je
                .L2
                                                         $.LCO, %edi
                                                movl
                $0xdeadbeef, %esi
        movl
                                                call
                                                         foo
        call
                foo
                                                addq
                                                         $8, %rsp
                .L1
        dmi
                                                ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
   End call
                                                 .section
                                                                 .rodata.str1.1, "aMS", @progbits, 1
                strcpy
                                         .Lco: = 0x400300
.L1:
        addq
                $24, %rsp
                                                 .string "midtermexam"
        ret
```

Hint: \$24 in decimal = 0x18

%rsp	0x8000e0
%rdi	.LCO
%rsi	0x15213

0x800100	?
0x8000f8	ret address for foo()
0x8000f0	?
0x8000e8	?
0x8000e0	?
0x8000d8	
0x8000d0	
0x8000c8	
0x8000c0	
8d0008x0	

foo:			caller:		
	subq	\$24, %rsp		subq	\$8, %rsp
	cmpl	\$0xdeadbeef, %esi		movl	\$86547, %esi
•	je	.L2		movl	\$.LCO, %edi
	movl	\$0xdeadbeef, %esi		call	foo
	call	foo		addq	\$8, %rsp
	jmp	.L1		ret	
.L2:					
	movq	%rdi, %rsi			
	movq	%rsp, %rdi			
End	call	strcpy		.sectio	n .rodata.str1.1,"aMS",@progbits,1
.L1:			.LC0: =	0x4003	800
	addq	\$24, %rsp		.string	"midtermexam"
	ret				

%rsp	0x8000e0
%rdi	.LCO
%rsi	0xdeadbeef

0x800100	?
0x8000f8	ret address for foo()
0x8000f0	?
0x8000e8	?
0x8000e0	?
0x8000d8	
0x8000d0	
0x8000c8	
0x8000c0	
0x8000b8	

foo:			caller:	
	subq	\$24, %rsp	subq \$8, %rsp	_
	cmpl	\$0xdeadbeef, %esi	movl \$86547, %esi	
	je	.L2	movl \$.LCO, %edi	
	movl	\$0xdeadbeef, %esi	call foo	
	call	foo	addq \$8, %rsp	
Ť	jmp	.L1	ret	_
.L2:			III.	
	movq	%rdi, %rsi		
	movq	%rsp, %rdi		
End	call	strcpy	.section .rodata.str1.1, "aMS", @progbits, 1	
.L1:			$-$ LC0: = 0×400300	-
	addq	\$24, %rsp	.string "midtermexam"	
	ret			

Question 1: What is the hex value of %rsp just before strcpy() is called for the first time in foo()?

%rsp	0x8000d8
%rdi	.LCO
%rsi	0xdeadbeef

0x8000f8	ret address for foo()
0x8000f0	?
0x8000e8	?
0x8000e0	?
8b0008x0	ret address for foo()
0x8000d0	
0x8000c8	
0x8000c0	
0x8000b8	

0x800100

foo:			caller:
	subq	\$24, %rsp	subq \$8, %rsp
	cmpl	\$0xdeadbeef, %esi	movl \$86547, %esi
	je	.L2	movl \$.LCO, %edi
	movl	\$0xdeadbeef, %esi	call foo
	call	foo	addq \$8, %rsp
	jmp	.L1	ret
.L2:			
	movq	%rdi, %rsi	
	movq	%rsp, %rdi	
End	call	strcpy	.section .rodata.str1.1,"aMS",@progbits,1
.L1:			.Lco: = 0x400300
	addq ret	\$24, %rsp	.string "midtermexam"

%rsp	0x8000c0
%rdi	.LCO
%rsi	0xdeadbeef

foo:			caller:		
	subq	\$24, %rsp		subq	\$8, %rsp
	cmpl	\$0xdeadbeef, %esi		movl	\$86547, %esi
	je	.L2		movl	\$.LC0, %edi
	movl	\$0xdeadbeef, %esi		call	foo
	call	foo		addq	\$8, %rsp
	jmp	.L1		ret	
.L2:					
	movq	%rdi, %rsi			
	movq	%rsp, %rdi			
End	call	strcpy		.sectio	n .rodata.str1.1,"aMS",@progbits,1
.L1:			.LC0: =	0x4003	800
	addq	\$24, %rsp		.string	"midtermexam"
	ret				

0x800100	?
0x8000f8	ret address for foo()
0x8000f0	?
0x8000e8	?
0x8000e0	?
0x8000d8	ret address for foo()
0x8000d0	?
0x8000c8	?
0x8000c0	?

%rsp	0x8000c0
%rdi	.LCO
%rsi	0xdeadbeef

foo:			caller:		
	subq	\$24, %rsp		subq	\$8, %rsp
	cmpl	\$0xdeadbeef, %esi		movl	\$86547, %esi
	je	.L2		movl	\$.LCO, %edi
	movl	\$0xdeadbeef, %esi		call	foo
	call	foo		addq	\$8, %rsp
	jmp	.L1		ret	
.L2:					
	movq	%rdi, %rsi			
	movq	%rsp, %rdi			
End	call	strcpy		.section	on .rodata.str1.1,"aMS",@progbits,
.L1:			.LC0: =	0x400	300
	addq	\$24, %rsp		.string	ng "midtermexam"
	ret				

0x800100	?
0x8000f8	ret address for foo()
0x8000f0	?
0x8000e8	?
0x8000e0	?
0x8000d8	ret address for foo()
0x8000d0	?
0x8000c8	?
0x8000c0	?
0x8000b8	

int if (f r	<pre>void foo(char *str, int a) { int buf[2]; if (a != 0xdeadbeef) { foo(str, 0xdeadbeef); return; }</pre>		foo("midtermexam", 0x15213);) {		%rsp 0x8000c0 %rdi 0x8000c0 %rsi .LC0		0x800100 0x8000f8 0x8000f0	? ret address for foo() ?
-	cpy((cha	r*) buf, str);			0131	.1100	0x8000e8	?
foo:	subq	\$24, %rsp	caller:	oq \$8, %rsp			0x8000e0	?
	cmpl je	\$0xdeadbeef, %esi	mov mov	/l \$86547, %esi			0x8000d8	ret address for foo()
	movl call	<pre>\$0xdeadbeef, %esi foo .L1</pre>	cal add	lq \$8, %rsp			0x8000d0	?
.L2:	jmp	%rdi, %rsi	ret	•			0x8000c8	?
End	movq call	%rsp, %rdi strcpy	.se .Lco: = 0x		tr1.1,"aM	S",@progbits,1	0x8000c0	?
.L1:	addq ret	\$24, %rsp		ring "midtermexam"			0x8000b8	

Question 2: What is the hex value of buf[0] when strcpy() returns?

```
void foo(char *str, int a) {
                                      void caller() {
                                                                                                 0x800100
                                                                                0x8000c0
                                                                        %rsp
   int buf[2];
                                         foo("midtermexam", 0x15213);
   if (a != 0xdeadbeef) {
                                                                                                 0x8000f8
                                                                                                                ret address for foo()
                                                                                0x8000c0
                                                                        %rdi
      foo(str, 0xdeadbeef);
      return;
                                                                                                 0x8000f0
                                                                        %rsi
                                                                                 .LC0
   strcpy((char*) buf
                                                                                                                            ?
                                                                                                 0x8000e8
                                                                                                 0x8000e0
foo:
                                      caller:
       suba
               $24, %rsp
                                             suba
                                                     $8, %rsp
               $0xdeadbeef, %esi
                                                     $86547, %esi
       cmpl
                                             movl
                                                                                                 0x8000d8
                                                                                                                ret address for foo()
       je
               .L2
                                                     $.LCO, %edi
                                             movl
               $0xdeadbeef, %esi
       movl
                                             call
                                                     foo
                                                                                                                            ?
                                                                                                 0x8000d0
       call
               foo
                                             addq
                                                     $8, %rsp
               .L1
       dmi
                                             ret
.L2:
                                                                                                 0x8000c8
               %rdi, %rsi
       movq
               %rsp, %rdi
       movq
                                                                                                0x8000c0
       call
                                              .section
                                                             .rodata.str1.1, "aMS", @progbits, 1
               strcpy
                                      .LC0: = 0 \times 400300
.L1:
        addq
               $24, %rsp
                                              .string "midtermexam"
                                                                                                 0x8000b8
        ret
```

%rsp 0x8000c0 %rdi 0x8000c0

Question 2: What is the hex value of buf[0] when strcpy() returns?

```
foo:
                                         caller:
        subq
                $24, %rsp
                                                 suba
                                                          $8, %rsp
                $0xdeadbeef, %esi
                                                 movl
                                                          $86547, %esi
        cmpl
        je
                .L2
                                                 movl
                                                          $.LCO, %edi
                $0xdeadbeef, %esi
                                                 call
        movl
                                                          foo
        call
                foo
                                                 addq
                                                          $8, %rsp
                 .L1
        dmi
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
        call
                                                  .section
                                                                   .rodata.s
                strcpy
                                         .LC0: = 0 \times 400300
.L1:
        addq
                $24, %rsp
                                                  .string "midtermexam"
        ret
```

0x800100	?		
0x8000f8	ret address for foo()		
0x8000f0	?		
0x8000e8	?		
0x8000e0	?		
0x8000d8	ret address for foo()		
0x8000d0	?		
0x8000c8			
0x8000c0	·d'	ʻi'	'm'
0x8000b8	c7 c2	c1	c0

addq

ret

\$24, %rsp

%rsp 0x8000c0 %rdi 0x8000c0 %rsi .LC0

Question 2: What is the hex value of buf[0] when strcpy() returns?

.string "midtermexam"

```
void foo(char *str, int a) {
                                         void caller() {
   int buf[2];
                                            foo("midtermexam", 0x15213);
   if (a != 0xdeadbeef) {
      foo(str, 0xdeadbeef);
      return;
foo:
                                        caller:
        subq
                $24, %rsp
                                                suba
                                                         $8, %rsp
                $0xdeadbeef, %esi
                                                         $86547, %esi
        cmpl
                                                movl
        je
                .L2
                                                movl
                                                         $.LCO, %edi
                $0xdeadbeef, %esi
                                                call
        movl
                                                         foo
        call
                foo
                                                addq
                                                         $8, %rsp
                .L1
        dmi
                                                ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
        call
                                                 .section
                                                                  .rodata.s
                strcpy
                                        .LC0: = 0 \times 400300
.L1:
```

0x800100				,	?			
0x8000f8			ret a	address	s for fo	00()		
0x8000f0				,	?			
0x8000e8				,	?			
0x8000e0				•	?			
0x8000d8			ret a	address	s for fo	00()		
0x8000d0					?			
0x8000c8	?	?	?	?	'\0'	'm'	ʻa'	'x'
0x8000c0	'e'	'm'	ʻr'	'e'	't'	'd'	ʻi'	'm'
0x8000b8	с7					с2	c1	c0

void foo(char *str, int a) {

Question 2: What is the hex value o buf[0] when strcpy() returns?

void caller() {

```
%rsp 0x8000c0
%rdi 0x8000c0
%rsi .LC0
```

```
int buf[2];
                                            foo("midtermexam", 0x15213);
   if (a != 0xdeadbeef) {
      foo(str, 0xdeadbeef);
      return;
foo:
                                         caller:
        subq
                $24, %rsp
                                                 suba
                                                         $8, %rsp
                $0xdeadbeef, %esi
                                                         $86547, %esi
        cmpl
                                                 movl
        je
                .L2
                                                 movl
                                                         $.LCO, %edi
                $0xdeadbeef, %esi
                                                 call
        movl
                                                         foo
        call
                foo
                                                 addq
                                                         $8, %rsp
                 .L1
        dmi
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
        call
                                                 .section
                                                                  .rodata.s
                strcpy
                                         .LC0: = 0 \times 400300
.L1:
        addq
                $24, %rsp
                                                 .string "midtermexam"
        ret
```

0x800100				1	?							
0x8000f8		ret address for foo()										
0x8000f0		?										
0x8000e8		?										
0x8000e0				1	?							
0x8000d8			ret a	address	for fo	00()						
0x8000d0				1	?							
0x8000c8	?	?	?	?	'\0'	'm'	'a'	ʻx'				
0x8000c0	'e'	'm'	ʻr'	'e'	't'	'd'	ʻi'	'm'				
0x8000b8					с3	buf	[0]	c0				

$$(as int) = 0x7464696d$$

Char	Hex	Char	Hex
a	61	m	6d
d	64	r	72
e	65	t	74
i	69	X	78

0x800100		?									
0x8000f8		ret address for foo()									
0x8000f0		?									
0x8000e8		?									
0x8000e0		?									
0x8000d8			ret a	address	for fo	0()					
0x8000d0					?						
0x8000c8	?	?	?	?	'\0'	'm'	'a'	ʻx'			
0x8000c0	'e'	'm'	ʻr'	'e'	'ť'	'd'	ʻi'	'm'			
0x8000b8						buf	[0]				

0x8000c0

0x8000c0

.LCO

%rsp

%rdi

%rsi

Problem 2: Stack

```
Question 3: What is the hex value of buf[1] when strcpy() returns?
 void foo(char *str, int a) {
                                void caller() {
```

```
int buf[2];
                                       foo("midtermexam", 0x15213);
if (a != 0xdeadbeef) {
   foo(str, 0xdeadbeef);
   return;
```

```
foo:
                                         caller:
        subq
                $24, %rsp
                                                 suba
                                                          $8, %rsp
                $0xdeadbeef, %esi
                                                          $86547, %esi
        cmpl
                                                 movl
        je
                 .L2
                                                 movl
                                                          $.LCO, %edi
                $0xdeadbeef, %esi
                                                 call
        movl
                                                          foo
        call
                 foo
                                                 addq
                                                          $8, %rsp
                 .L1
        dmi
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
        call
                                                  .section
                                                                   .rodata.s
                 strcpy
                                         .LC0: = 0 \times 400300
.L1:
                                                  .string "midtermexam"
        addq
                $24, %rsp
        ret
```

0x8000b8	c7 buf[1] C4 buf[0]									
0x8000c0	'e'	'm'	ʻr'	'e'	't'	'd'	ʻi'	'm'		
0x8000c8	?	?	?	?	'\0'	'm'	ʻa'	'x'		
0x8000d0					?					
0x8000d8		ret address for foo()								
0x8000e0		?								
0x8000e8		?								
0x8000f0		?								
0x8000f8			ret a	address	for fo	0()				
0x800100	?									

$$(as int) = 0x656d7265$$

Char	Hex	Char	Hex
a	61	m	6d
d	64	r	72
e	65	t	74
i	69	X	78

0x800100	?							
0x8000f8		ret address for foo()						
0x8000f0		?						
0x8000e8		?						
0x8000e0		?						
0x8000d8		ret address for foo()						
0x8000d0		?						
0x8000c8	?	? ? ? ? '\0' 'm' 'a' 'x'						'x'
0x8000c0	'e'	'e' 'm' 'r' 'e' 't' 'd' 'i' 'm'						'm'
0x8000b8	buf[1]							

jmp

movq

movq call

addq

ret

.L2:

.L1:

.L1

%rdi, %rsi

%rsp, %rdi

\$24, %rsp

strcpy

Question 4: What is the hex value of %rdi at the point where foo() is called recursively in the successful arm of the if statement?

.rodata.str1.1, "aMS", @progbits, 1

```
void foo(char *str, int a) {
                                       void caller() {
   int buf[2];
                                          foo("midtermexam", 0x15213);
   if (a != 0xdeadbeef) {
      foo(str, 0xdeadbeef);
      return;
   strcpy((char*) buf, str);
foo:
                                        caller:
        subq
                $24, %rsp
                                                subq
                                                        $8, %rsp
                $0xdeadbeef, %esi
        cmpl
                                                movl
                                                        $86547, %esi
        je
                                                movl
                                                        $.LCO, %edi
                .L2
                $0xdeadbeef, %esi
        movl
                                                call
                                                        foo
        call
                foo
                                                addq
                                                        $8, %rsp
```

ret

.section .Lco: = 0x400300

.string "midtermexam"

This is before the recursive call to foo()

void foo(char *str, int a) {

int buf[2];

ret

Question 4: What is the hex value of %rdi at the point where foo() is called recursively in the successful arm of the if statement?

```
if (a != 0xdeadbeef) {
      foo(str, 0xdeadbeef);
      return;
   strcpy((char*) buf, str);
foo:
                                        caller:
        subq
                $24, %rsp
                                                suba
                                                         $8, %rsp
                $0xdeadbeef, %esi
        cmpl
                                                movl
                                                         $86547, %esi
                                                                              loaded %rdi
                                                movl
                                                         $.LCO, %edi
        ie
                .L2
                $0xdeadbeef, %esi
        movl
                                                call
                                                         foo
        call
                                                         $8, %rsp
                foo
                                                addq
        jmp
                .L1
                                                 ret
.L2:
                %rdi, %rsi
        movq
                %rsp, %rdi
        movq
        call
                                                                 .rodata.str1.1, "aMS", @progbits, 1
                strcpy
                                         Lco: = 0x400300
.L1:
        addq
                $24, %rsp
                                                 .string "midtermexam"
```

void caller() {

foo("midtermexam", 0x15213);

- This is before the recursive call to foo()
- Going backwards, %rdi was loaded in caller()
- %rdi = \$.LC0 =
 0x400300
 (based on hint)

Question 5: What part(s) of the stack will be corrupted by invoking caller()? Check all that apply.

- return address from foo() to caller()
- return address from the recursive call to foo()
- strcpy()'s return address
- there will be no corruption

Question 5: What part(s) of the stack will be corrupted by invoking caller()?

Check all that apply.

return address from foo() to caller()

- return address from the recursive call to foo()
- strcpy()'s return address
- there will be no corruption

The strcpy didn't overwrite any return addresses, so there was no corruption!

riapted by inventing carrer ().								
0x800100		?						
0x8000f8			ret a	address	s for fo	00()		
0x8000f0				,	?			
0x8000e8				,	?			
0x8000e0		?						
0x8000d8			ret a	address	s for fo	00()		
0x8000d0					?			
0x8000c8	?	? ? ? ? '\0' 'm' 'a' 'x'						'x'
0x8000c0	'e' 'm' 'r' 'e' 't' 'd' 'i' 'm'						'm'	
0x8000b8								

- Things to remember/put on a cheat sheet because please don't try to memorize all of this:
 - Direct mapped vs. n-way associative vs. fully associative
 - Tag/Set/Block offset bits, how do they map depending on cache size?
 - LRU policies, write-back, write-through, write-allocate...
 - **■** cache misses types: cold miss, conflict miss, capacity miss

- A. Assume you have a cache of the following structure:
 - a. 32-byte blocks
 - b. 2 sets
 - c. Direct-mapped
 - d. 8-bit address space
 - e. The cache is cold prior to access
- B. What does the address decomposition look like? (S, E, B, m), (s, b)

0000000

- A. Assume you have a cache of the following structure:
 - a. 32-byte blocks
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 - c. Direct-mapped
 - d. 8-bit address space
 - e. The cache is cold prior to access
- B. What does the address decomposition look like? (S, E, B, m), (s, b)

0000000

Address	Set	Tag	н/м	Evict? Y/N
0 x 56				
0x6D				
0x49				
0x3A				

Address	Set	Tag	н/м	Evict? Y/N
0101 0110				
0110 1101				
0100 1001				
0011 1010				

Address	Set	Tag	н/м	Evict? Y/N
0101 0110	0	01	M	N
0110 1101				
0100 1001				
0011 1010				

Address	Set	Tag	н/м	Evict? Y/N
0101 0110	0	01	M	N
0110 1101	1	01	M	N
0100 1001				
0011 1010				

Address	Set	Tag	н/м	Evict? Y/N
0101 0110	0	01	M	N
0110 1101	1	01	M	N
0100 1001	0	01	Н	N
0011 1010				

Address	Set	Tag	н/м	Evict? Y/N
0101 0110	0	01	M	N
0110 1101	1	01	M	N
0100 1001	0	01	Н	N
0011 1010	1	00	M	Y

- A. Assume you have a cache of the following structure:
 - a. 2-way associative
 - b. 4 sets, 64-byte blocks
- B. What does the address decomposition look like?

 \dots 0 0 0 0 0 0 0 0 0 0 0 0 0 0

- A. Assume you have a cache of the following structure:
 - a. 2-way associative
 - b. 4 sets, 64-byte blocks
- B. What does the address decomposition look like?

 \dots 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0

- B. Assume A and B are128 ints andcache-aligned.
 - a. What is the miss rate of pass 1?
 - b. What is the miss rate of pass 2?

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

B. Pass 1: Only going through 64 ints with step size 4. Since our cache size is 64 bytes. Each miss loads 16 ints into a cache line, giving us 3 more hits before loading into a new line.

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

B. Pass 1: 25% miss

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

B. Pass 2: Our cache is the same size as our working set! Due to cache alignment, we won't evict anything from A, but still get a 1:3 miss:hit ratio for B.

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

B. Pass 2: For every 4 loop iterations, we get all hits for accessing A and 1 miss for accessing B, which gives us 1/8 miss.

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

B. Pass 2: 12.5% miss

```
int get prod and copy(int *A, int *B) {
    int length = 64;
    int prod = 1;
    // pass 1
    for (int i = 0; i < length; i+=4) {
        prod*=A[i];
    // pass 2
    for (int j = length-1; j > 0; j-=4) {
        A[\dot{j}] = B[\dot{j}];
    return prod;
```

- Things to remember/put on your cheat sheet:
 - Floating point representation (-1)^s * M * 2^E
 - Values of M in normalized vs denormalized
 - Difference between normalized, denormalized and special floating point numbers
 - Rounding
 - Bit values of smallest and largest normalized and denormalized numbers

A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.

a) 31/8

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8

 Step 1: Convert the fraction into the form (-1)^s * M * 2^E

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 0$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 0$$

M = 31/16 (M should be put in the range [1.0, 2.0) initially)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 0$$

M = 31/16 (M should be put in the range [1.0, 2.0) initially)

$$E = 1$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

```
=> (-1)^0 * 31/16 * 2^1
```

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

 $E = \exp - bias$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

$$exp = E + bias$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

$$exp = E + bias$$

bias = 2^{k-1} - 1 (k is the number of exponent bits)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

$$exp = E + bias$$

bias =
$$2^{k-1}$$
 - 1 = 2^{2-1} - 1 = 1

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

$$exp = E + bias = 1 + 1 = 2$$

bias =
$$2^{k-1} - 1 = 2^{2-1} - 1 = 1$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 2: Find exponent bits (exp)

$$exp = E + bias => 10$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
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 Step 3: Convert M into binary and find fraction bits

$$M = 31/16$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16$$

Need to represent M as $\sum_{i} 1/2^{i}$ First split 1 from improper fraction

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16 = 16/16 + 15/16$$

Need to represent M as $\sum_{i} 1/2^{i}$ First split 1 from improper fraction

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16 = 1 + 8/16 + 4/16 + 2/16 + 1/16$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16 = 1/2^0 + 1/2^1 + 1/2^2 + 1/2^3 + 1/2^4$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16 \Rightarrow 1.1111_{2}$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3: Convert M into binary and find fraction bits

$$M = 31/16 \Rightarrow 1.1111_2$$

1.1111₂ => fraction bits are 1111

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 3.5: Collect sign, exponent and fraction bits

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 3.5</u>: Collect sign, exponent and fraction bits

sign bit = 0

exponent bits = 10

fraction bits = 1111

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 4</u>: Take care of rounding issues

Fraction bits are 1111

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 4</u>: Take care of rounding issues

Fraction bits are BBGRXXX

Fraction bits are BBGRXXX

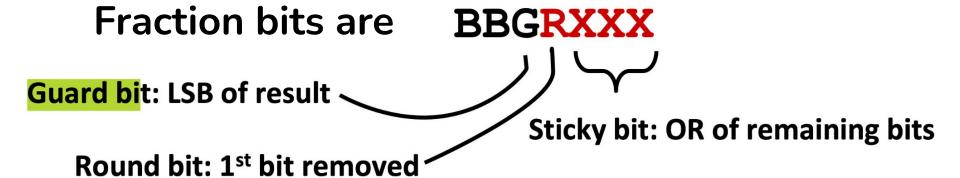
Fraction bits are BBGRXXX

Guard bit: LSB of result <

Fraction bits are BBGRXXX

Guard bit: LSB of result

Round bit: 1st bit removed



- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 4</u>: Take care of rounding issues

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

Fraction bits are 1111 <= excess bit

- **Guard bit = 1**

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

- Guard bit = 1
- Round bit = 1

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

- **Guard bit = 1**
- Round bit = **1**
- No sticky bit (so we can just think of it as just 0)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

- Guard bit = 1
- Round bit = 1
- No sticky bit (so we can just think of it as just 0) Round up! (truncate the excess bits, then add 1)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 4</u>: Take care of rounding issues

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

Fraction bits are 111
$$\frac{+ \quad 1}{\text{overflow}} > 1000$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

Adding 1 overflows the fraction bits, so we increment the exponent bits by 1 and set the fraction bits to all zeros

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

sign bit = 1

exponent bits = 10

fraction bits = 1111

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 Step 4: Take care of rounding issues

```
sign bit = 1
```

exponent bits = 10 => 11

fraction bits = 1111 => 000

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 5</u>: Put together your final result

A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.

a) 31/8
<u>Step 5</u>: Put together your final result

Result: 0 11 000

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- a) 31/8
 <u>Step 5</u>: Put together your final result

Result: 0 11 000 <= Positive Infinity!

A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.

b) -7/8

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 1$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 1$$

M = 7/8 (M is in correct range [0.0, 1.0) for denormalized)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

$$s = 1$$

M = 7/8 (M is in correct range [0.0, 1.0) for denormalized

E = -1 (denormalized exponent)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 1</u>: Convert the fraction into the form (-1)^s * M * 2^E

```
=> (-1)^1 * 7/8 * 2^{-1}
```

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 2</u>: Find exponent bits (exp)

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 2</u>: Find exponent bits (exp)

We know we have a denormalized number

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 2</u>: Find exponent bits (exp)

We know we have a denormalized number

$$=> \exp = 00_2$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

M = 7/8

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

$$M = 7/8$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

$$M = 7/8 = 4/8 + 2/8 + 1/8$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

$$M = 7/8 = 1/2^1 + 1/2^2 + 1/2^3$$

Need to represent M as $\sum_{i} 1/2^{i}$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

$$M = 7/8 \Rightarrow 0.111_{2}$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3: Convert M into binary and find fraction bits

$$M = 7/8 \Rightarrow 0.111_{2}$$

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 Step 3.5: Collect sign, exponent and fraction bits

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 <u>Step 3.5</u>: Collect sign, exponent and fraction bits

sign bit = 1

exponent bits = 00

fraction bits = 111

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 4</u>: Take care of rounding issues

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8

 <u>Step 4</u>: Take care of rounding issues

None!

- A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.
- b) -7/8
 <u>Step 5</u>: Put together your final result

A. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following number into its floating point representation.

b) -7/8

<u>Step 5</u>: Put together your final result

Result: 1 00 111

B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.

a) 0 10 101

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 1: Find E from exponent bits

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 Step 1: Find E from exponent bits

exponent bits = 10 (normalized)

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 1: Find E from exponent bits

exponent bits = 10 (normalized)

E = exp - bias

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

Step 1: Find E from exponent bits

exponent bits = 10 (normalized)

E = exp - bias

bias = $2^{k-1} - 1$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101
 Step 1: Find E from exponent bits

exponent bits = 10 (normalized)

E = exp - bias

bias =
$$2^{k-1}$$
 - 1 = 2^{2-1} - 1 = 1

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 Step 1: Find E from exponent bits

exponent bits = 10 (normalized)

$$E = \exp - bias = 10_2 - 1 = 1$$

bias =
$$2^{k-1}$$
 - 1 = 2^{2-1} - 1 = 1

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 1: Find E from exponent bits

$$=> E = 1$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 2: Find M from fraction bits and exponent bits

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 <u>Step 2</u>: Find M from fraction bits and exponent bits

fraction bits = 101

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 <u>Step 2</u>: Find M from fraction bits and exponent bits

fraction bits = 101

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 2: Find M from fraction bits and exponent bits

fraction bits = 101

$$M = 1.101_{2}$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101
 Step 2: Find M from fraction bits and exponent bits

fraction bits = 101

$$M = 1.101_2 = 1/2^0 + 1/2^1 + 1/2^3$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 2: Find M from fraction bits and exponent bits

fraction bits = 101

$$M = 1.101_2 = 8/8 + 4/8 + 1/8$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 Step 2: Find M from fraction bits and exponent bits

fraction bits = 101

$$M = 1.101_2 = 13/8$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101

 <u>Step 2</u>: Find M from fraction bits and exponent bits

$$=> M = 13/8$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 <u>Step 3</u>: Put sign bit, M and E into the form (-1)^s * M * 2^E

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 <u>Step 3</u>: Put sign bit, M and E into the form (-1)^s * M * 2^E

sign bit
$$= 0$$

$$M = 13/8$$

$$E = 1$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 <u>Step 3</u>: Put sign bit, M and E into the form (-1)^s * M * 2^E

$$=> (-1)^0 * 13/8 * 2^1$$

- B. Consider a floating point representation with 1 sign bit, 2 exponent bits and 3 fraction bits. Convert the following floating point representation into its base 10 number.
- a) 0 10 101 Step 4: Simplify the form $(-1)^s * M * 2^E$ to get the final result

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$$(-1)^0 * 13/8 * 2^1$$

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- a) 0 10 101 Step 4: Simplify the form $(-1)^s * M * 2^E$ to get the final result

$$(-1)^0 * 13/8 * 2^1$$

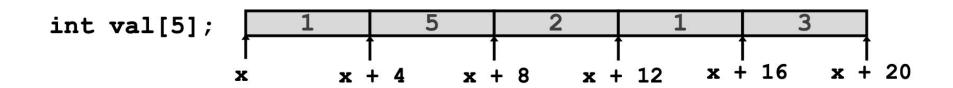
Result: 13/4

<u>IMPORTANT POINTS + TIPS:</u>

- Remember your indexing rules! They'll take you 95% of the way there.
- Be careful about addressing (&) vs. dereferencing (*)
- You may be asked to look at assembly!
- Feel free to put lecture/recitation/textbook examples in your cheatsheet.



val + i



Type Value
val
val[2]
*(val + 2)
&val[2]
val + 2

```
int val[5]; 1 5 2 1 3

x x + 4 x + 8 x + 12 x + 16 x + 20
```



```
Type Value
val int * x
val[2]
*(val + 2)
&val[2]
val + 2
val + i
```

```
int val[5]; 1 5 2 1 3

x x + 4 x + 8 x + 12 x + 16 x + 20
```

```
Type Value

val int * x

val[2] int 2

*(val + 2)

&val[2]

val + 2

val + i
```

```
int val[5]; 1 5 2 1 3

x x + 4 x + 8 x + 12 x + 16 x + 20
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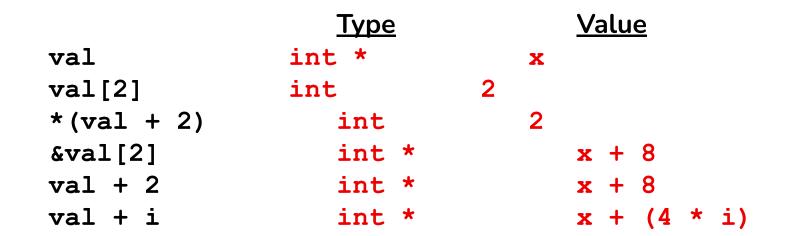
```
Value
                    Type
val
                 int *
                                  X
val[2]
                 int
*(val + 2)
                    int
&val[2]
                    int *
                                     x + 8
val + 2
                    int *
                                     x + 8
val + i
```

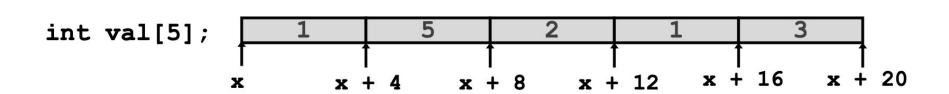


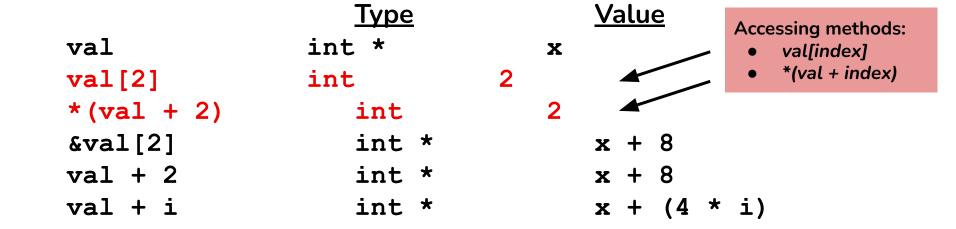


```
int val[5]; 1 5 2 1 3

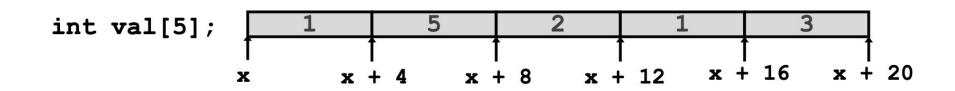
x x + 4 x + 8 x + 12 x + 16 x + 20
```

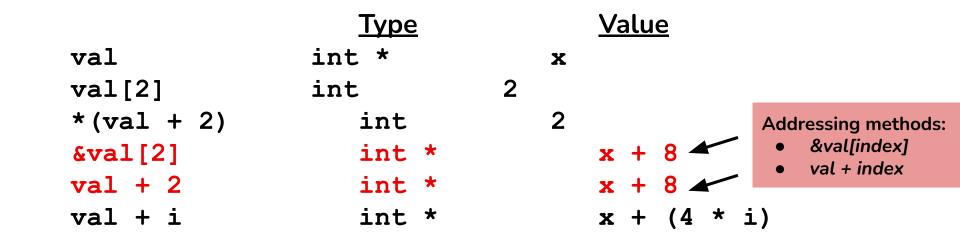










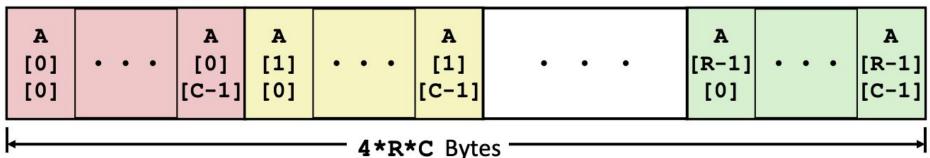


 Contiguous chunk of space (think of multiple arrays lined up next to each other)



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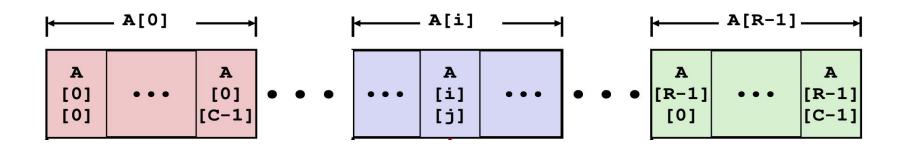




A[i][j] is element of type T, which requires K bytes

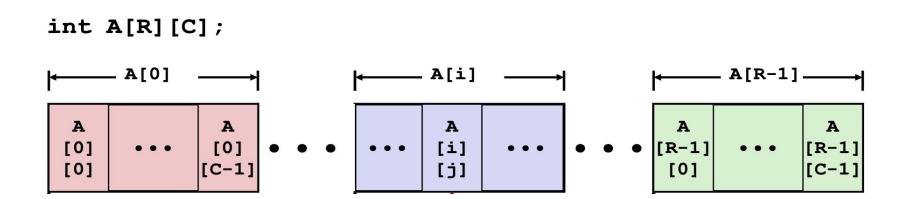


A[i][j] is element of type T, which requires K bytes



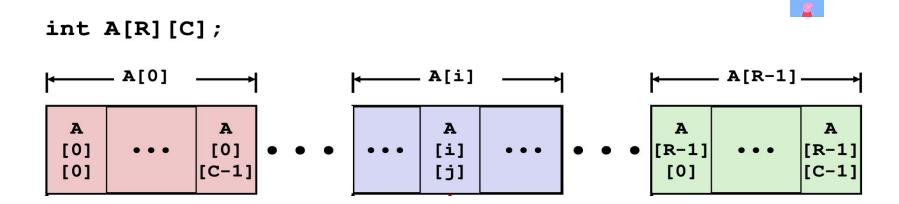
 $\mathbf{A}[\mathbf{i}][\mathbf{j}]$ is element of type T, which requires K bytes





 $\mathbf{A}[\mathbf{1}][\mathbf{j}]$ is element of type T, which requires K bytes

Address $\mathbf{A} + \mathbf{i} * (\mathbf{C} * \mathbf{K}) + \mathbf{j} * \mathbf{K}$



 $\mathbf{A}[\mathbf{i}][\mathbf{j}]$ is element of type T, which requires K bytes

Address
$$\mathbf{A} + \mathbf{i} * (\mathbf{C} * \mathbf{K}) + \mathbf{j} * \mathbf{K}$$

$$= \mathbf{A} + (\mathbf{i} * \mathbf{C} + \mathbf{j}) * \mathbf{K}$$
int $\mathbf{A}[R][C]$;
$$\longleftarrow \mathbf{A}[0] \longrightarrow \longleftarrow \mathbf{A}[1] \longrightarrow \longleftarrow \mathbf{A}[R-1] \longrightarrow$$

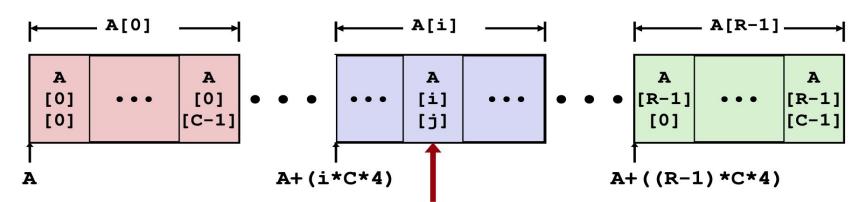
$$\begin{bmatrix} \mathbf{A} & \cdots & \mathbf{A} \\ [0] & \cdots & [0] \\ [0] & \cdots & [0] \\ [0] & \cdots & [0] \end{bmatrix} \bullet \bullet \bullet$$

 $\mathbf{A}[\mathbf{i}][\mathbf{j}]$ is element of type T, which requires K bytes

Address
$$A + i * (C * K) + j * K$$

= $A + (i * C + j) * K$

int A[R][C];



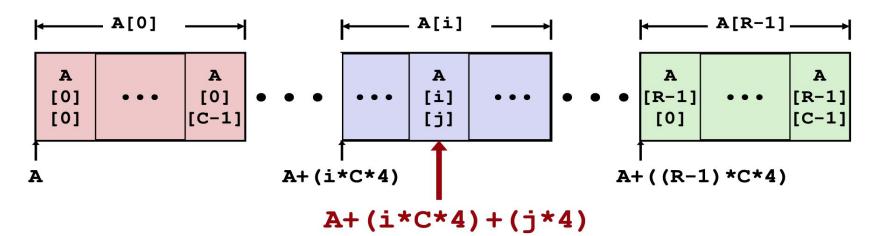


 $\mathbf{A}[\mathbf{i}][\mathbf{j}]$ is element of type T, which requires K bytes

Address
$$A + i * (C * K) + j * K$$

= $A + (i * C + j) * K$

int A[R][C];



```
Compiles Bad Deref? Size (bytes)
int A1[3][5]
int *A2[3][5]
int (*A3)[3][5]
int *(A4[3][5])
int (*A5[3])[5]
```





```
int A1[3][5]
int *A2[3][5]
int (*A3)[3][5]
int *(A4[3][5])
int (*A5[3])[5]
```

```
Compiles Bad Deref? Size (bytes)
Y
N
3*5*(4) = 60
```

```
int A1[3][5]
int *A2[3][5]
int (*A3)[3][5]
int *(A4[3][5])
int (*A5[3])[5]
```

```
        Compiles
        Bad Deref?
        Size (bytes)

        Y
        N
        3*5*(4) = 60

        Y
        N
        3*5*(8) = 120
```



```
int A1[3][5]
int *A2[3][5]
int (*A3)[3][5]
int *(A4[3][5])
int (*A5[3])[5]
```

Compiles	Bad Deref?	Size (bytes)
Y	N	3*5*(4) = 60
Y	N	3*5*(8) = 120
Y	N	1*8 = 8



int	A1[3][5]
int	*A2[3][5]
int	(*A3)[3][5]
int	*(A4[3][5])
int	(*A5[3])[5]

Bad Deref?	Size (bytes)
N	3*5*(4) = 60
N	3*5*(8) = 120
N	1*8 = 8
N	3*5*(8) = 120
	N N N



Consider accessing elements of A....

int	A1[3][5]
int	*A2[3][5]
int	(*A3)[3][5]
int	*(A4[3][5])
	(*A5[3])[5]

Compiles	Bad Deref?	Size (bytes)
Y	N	3*5*(4) = 60
Y	N	3*5*(8) = 120
Y	N	1*8 = 8
Y	N	3*5*(8) = 120

A4 is a pointer to a 3x5 (int *) element array

Consider accessing elements of A....

int	A1[3][5]
int	*A2[3][5]
int	(*A3)[3][5]
int	*(A4[3][5]) (*A5[3])[5]
int	(*A5[3])[5]

Compiles	Bad Deref?	Size (bytes)
Y	N	3*5*(4) = 60
Y	N	3*5*(8) = 120
Y	N	1*8 = 8
Y	N	3*5*(8) = 120
Y	N	3*8 = 24

A4 is a pointer to a 3x5 (int *) element array



Decl		An			*An			**An	
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3][5]	Y	N	60	Y	N	20	Y	N	4
int *A2[3][5]	Y	N	120	Y	N	40	Y	N	8
int (*A3)[3][5]	Y	N	8	Y	Y	60	Y	Y	20
int *(A4[3][5])	Y	N	120	Y	N	40	Y	N	8
int (*A5[3])[5]	Y	N	24	Y	N	8	Y	Y	20

ex., A3: pointer to a 3x5 int array

*A3: 3x5 int array (3 * 5 elements * each 4 bytes = 60)

**A3: BAD, but means stepping inside one of 3 "rows" c



Decl	An		*An			**An			
	Cmp	Bad	Size	Cmp	Bad	Size	Cmp	Bad	Size
int A1[3][5]	Y	N	60	Y	N	20	Y	N	4
int *A2[3][5]	Y	N	120	Y	N	40	Y	N	8
int (*A3)[3][5]	Y	N	8	Y	Y	60	Y	Y	20
int *(A4[3][5])	Y	N	120	Y	N	40	Y	N	8
int (*A5[3])[5]	Y	N	24	Y	N	8	Y	Y	20

ex., A5: array of 3 (int *) pointers

*A5: 1 (int *) pointer, points to an array of 5 ints

**A5: BAD, means accessing 5 individual ints of the pointer

(stepping inside "row")



Sample assembly-type questions

```
1 5 2 1 3 1 5 2 1
                                7 1 5 2 2 1
        0
                                 int *get pgh zip(int index)
                      pgh[2]
pgh
                                   return pgh[index];
   # %rdi = index
```

```
# %rdi = index
leaq (%rdi,%rdi,4),%rax # 5 * index
leaq pgh(,%rax,4),%rax # pgh + (20 * index)
```

Nested Array Row Access Code

```
1 5 2 0 6 1 5 2 1 3 1 5 2 1 7 1 5 2 2 1

pgh

pgh[2] int *get_pgh_zip(int index)
{
    return pgh[index];
}
```

```
# %rdi = index
leaq (%rdi,%rdi,4),%rax # 5 * index
leaq pgh(,%rax,4),%rax # pgh + (20 * index)
```

Row Vector

- pgh[index] is array of 5 int's
- Starting address pgh+20*index

Machine Code

- Computes and returns address
- Compute as pgh + 4* (index+4*index)



Nested Array Element Access Code

```
1 5 2 0 6 1 5 2 1 3 1 5 2 1 7 1 5 2 2 1

pgh

pgh[1][1] int get_pgh_digit(int index, int dig)

{
    return pgh[index][dig];
}
```

```
leaq (%rdi,%rdi,4), %rax  # 5*index
addl %rax, %rsi  # 5*index+dig
movl pgh(,%rsi,4), %eax  # M[pgh + 4*(5*index+dig)]
```

Array Elements

- pgh[index][dig] is int
- Address: pgh + 20*index + 4*dig
 = pgh + 4*(5*index + dig)

Bonus! Another Cache problem

- Consider you have the following cache:
 - 64-byte capacity
 - Directly mapped
 - You have an 8-bit address space

- A. How many tag bits are there in the cache?
 - Do we know how many set bits there are? What about offset bits? $2^6 = 64$
 - If we have a 64-byte direct-mapped cache, we know the number of s + b bits there are total!
 - **■** Then $t + s + b = 8 \rightarrow t = 8 (s + b)$
 - ■Thus, we have 2 tag bits!

- B. Fill in the following table, indicating the set number based on the hit/miss pattern.
 - a. By the power of guess and check tracing through, identify which partition of s + b bits matches the H/M pattern.

Load	Binary Address	Set	н/м
1	1011 0011		М
2	1010 0111		M
3	1101 1001		M
4	1011 1100		Н
5	1011 1001		Н

- B. Fill in the following table, indicating the set number based on the hit/miss pattern.
 - a. By the power of guess and check tracing through, identify which partition of s + b bits matches the H/M pattern.

Load	Binary Address	Set	H/M
1	1011 0011		M
2	1010 0111		M
3	11 01 1001		M
4	1011 1100		Н
5	1011 1001		Н

- B. Fill in the following table, indicating the set number based on the hit/miss pattern.
 - a. By the power of guess and check tracing through, identify which partition of s + b bits matches the H/M pattern.

Load	Binary Address	Set	H/M
1	10 <u>11</u> 0011		M
2	10 <u>10</u> 0111		М
3	11 <u>01</u> 1001		М
4	10 <u>11</u> 1100		Н
5	10 <u>11</u> 1001		Н

- B. Fill in the following table, indicating the set number based on the hit/miss pattern.
 - a. By the power of guess and check tracing through, identify which partition of s + b bits matches the H/M pattern.

Load	Binary Address	Set	H/M
1	10 <u>11</u> 0011	3	M
2	10 <u>10</u> 0111	2	М
3	11 <u>01</u> 1001	1	М
4	10 <u>11</u> 1100	3	Н
5	10 <u>11</u> 1001	3	Н

C. How many sets are there? 2 bits \rightarrow 4 sets How big is each cache line? 4 bits \rightarrow 16 bytes

In summary...

- Read the write-up textbook!
- Also read the write-up lecture slides!
- Midterm covers CS:APP Ch. 1-3, 6
- Ask questions on Piazza! For the midterm, make them public and specific if from the practice server!
- G~O~O~D~~L~U~C~K