

A Naive Bayesian Multi-label Classification Algorithm With Application to Visualize Text Search Results

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Search results visualization has emerged as an important research topic due to its application on search engine amelioration. From the perspective of machine learning, the text search results visualization task fits to the multi-label learning framework that a document is usually related to multiple category labels. In this paper, a Naïve Bayesian (NB) multi-label classification algorithm is proposed by incorporating a two-step feature selection strategy which aims to satisfy the assumption of conditional independency in NB classification theory. The experiments over public data set demonstrate that the proposed method has highly competitive performance with several well-established multi-label classification algorithms. We implement a prototype system named TJ-MLWC based on the proposed algorithm, which acts as an intermediate layer between users and a commercial Internet Search Engine, allowing the search results of a query displaying by one or multiple categories. Testing results indicate that our prototype improves search experience by adding the function of browsing search results by category.

Keywords: Multi-label classification; Naïve Bayesian classification; text search results visualization; Feature selection.

1. Introduction

Nowadays Web documents have been growing rapidly. For example, everyday a large number of documents are uploaded to Web sites. As one of the most prevalent applications in today's network computing environment, Web search engines are widely used for information seeking and knowledge elaboration. However, too many returned results make us submerge in the sea of information. The current search engines (such as Google, MSN, Yahoo, etc.) return sorted search results according to the keywords input by users. In order to find the interesting information, users should browse the title and digest one by one within the search results.

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Focusing on above problems, some researchers begin to explore more advanced information retrieval methods. Generally speaking, there are two ways. One is semantic based information retrieval which uses semantic information to understand the documents and queries. The other is machine learning based method which uses model learned from history data to reorganize Web documents such as classification and clustering. This paper mainly discusses the later, that is, the improvement of information retrieval based on machine learning.

Web search results visualization is a process that layouts search results in a more clear and coherent way according to the content of each result. It aims at improving the search efficiency and accuracy and ameliorating users' browsing experiences. Prevalent technique for this task is text clustering. It regards the visualization task as an unsupervised pattern classification problem. Following the methodology of pattern classification, text features are first extracted from texts to represent the document, and then the document is assigned to a cluster in which documents have high similarity. Generally, the "name" of cluster is given automatically according to the feature words of documents in this cluster. Related researches could be found in literatures.^{2,3,4,5}

The search engines based on clustering technology already exist such as Vivisimo^a and Grokker^b. However, there is a problem that the extracted "name" of each cluster is far from expressing the main contents of its cluster. In this case, it's difficult for users to locate interesting information in a corresponding cluster. This made the process of visualizing search results less significant.

Unlike the traditional pattern classification problems in which each pattern has a unique label, a document may be associated with more than one label (e.g. a document may include the content about economy and computer). Multi-label learning originated from researches on text categorization problems, which each document may belong to several predefined labels. In this case, each document in training set is associated with a set of labels, and the task is to output a label set for each unseen document through analyzing training documents with known label sets.

In this paper, we borrow the idea of granularity computing ⁶ to display search results in a more refined granularity level-category. A Naïve Bayesian Multi-label Classification approach is proposed to handle the web text search results visualization problem. Feature selection strategy is concerned to improve classification performance. A prototype system TJ-MLWC is designed as an application example. In TJ-MLWC, users could look for a document within some interesting classes. In the same time, a document could be found in various corresponding classes.

The rest of this paper is organized as follows. Section 2 reviews the related works of visualizing text search results and multi-label learning. Section 3 proposes the Naïve Bayesian Multi-Label (NBML) approach. Section 4 reports experimental results on public data set. Section 5 presents the prototype system TJ-MLWC.

^aVivisimo Search Engine. http://www.vivisimo.com.

^bGrokker Search Engine. http://www.grokker.com.

Finally, Section 6 summarizes and sets up several issues for future work.

2. Related Works

2.1. Related works on visualizing text search results based on machine learning

Visualizing search results by methods based on machine learning is one obvious solution for dealing with information overload. Clustering is one way that allows users to view categorized results without having to deal with the costs and complexities of building taxonomies (see, for example, the Vivisimo search engine). This advantage makes clustering technique prevalent in the field of visualizing search results. D. Roussinov and H. Chen proposed an approach of summarizing query results by automatic text clustering and implemented a prototype.² G. Mecca et al. used Latent Semantic Indexing on the whole document content and proposed a strategy, called Dynamic Singular Value Decomposition (SVD) Clustering, to discover the optimal number of singular values to be used for clustering purpose. A tool based on this algorithm has been integrated into the Noodles search engine.³ Nicole Lang Beebe et al. proposed a kind of post-retrieval clustering of digital forensic text string search results specifically by using Kohonen self-Organizing Maps, a self-organizing neural network approach.⁴ Zamir and Etzioni made an empirical comparison of standard ranked-list and clustered presentation systems when designing a search engine interface named Grouper, and reported substantial differences in use patterns between the two.⁵ Some researchers have experimented with highly metaphorical visualizations. For example, Cugini et al. presented users with structural overviews of result sets and promoted visualization as the best approach to dealing with broad search tasks. Visualization of this type appears to make it easier for users to locate worthwhile information and to comprehend search results.

Recently, some researches use topic map based on probabilistic graph model theory to improve representation of search results. Newman et al. explored semantic visualizations of Web search results based on topic map. Their topic maps are based on a topic model of the document collection, where the topic model is used to determine the semantic content of each document. The topic model represents documents as a mixture of topics, which is a more flexible representation than k-Means clustering, where a document belongs to just one topic. This richer representation means that one can navigate to related articles via any of the topic facets in a given article (this is not possible for k-Means). Furthermore, since the topic model is based on a generative probabilistic model, it can be flexibly extended to include other meta-data and attributes, such as authors, citation links, and subject headings, and therefore it is also preferred over Nonnegative Matrix Factorization (NMF).

All these researches improved search engine performance to some extent. However, the methodology of clustering suffers from the difficulty of naming the clusters. Users could not comprehend the content of a cluster only from the words automatically given. It is still very difficult for user to find interesting information.

2.2. Related works on multi-label classification approaches

Traditional single-label classification is concerned with learning from a set of examples that are associated with a single label l from a set of disjoint labels L, |L|>1. In multi-label classification, the examples are associated with a set of labels $Y\subseteq L$.¹¹

Some multi-label classification algorithms have been successfully designed for the application of text classification. Majority of traditional machine learning algorithms for single label classification problem have been extended to multi-label cases. Representative research works include the AdaBoost.MH¹² which is the extension of AdaBoost, the extensions of several neural network algorithms, ^{13,14,15} the extension of SVM, 16 the extensions of Naïve Bayesian, 17,18 the extension of Maximum Entropy, ^{19,20} the extension of decision tree, ²¹ the extensions of some lazy-style algorithms^{22,23,24} etc. Recently, several algorithms have also been proposed to improve the performance of learning systems through explore additional information provided by the correlation of class labels^{25,26,27,28,29,30,31} or unlabeled data. 32,33 Naïve Bayesian classification algorithm, as one of the probabilistic generative model, has natural advantage for multi-label learning problem. McCallum¹⁷ proposed a Bayesian approach to multi-label document classification, where a mixture probabilistic model (one mixture component per category) is assumed to generate each document and the EM³⁴ algorithm is used to learn the mixture weights and the word distributions in each mixture component. Min-ling Zhang et al. adapted traditional Naïve Bayesian algorithm to deal with multi-label instances and incorporated feature selection mechanisms into classifier to improve its performance.¹⁸ Other probabilistic generative models are also used for multi-label text classification such as parametric mixture models (PMM1, PMM2).³⁵ Above NB multi-label classification algorithms mainly focused on modeling the relations between words and classes and classification performances are improved to some extent. However, a complex model always accompanies highly computational costs. Our work aims at classifying text search results real-time by using multi-label classifiers with low computational complexity. Consequently, a kind of less complex feature selection strategy is more proper for this task.

3. Naïve Bayesian Multi-label Classification Approach

Naïve Bayesian (NB) algorithm is efficient. For the real-time system, it has a wide application such as Spam filtering system. For the task of multi-label classification, classic NB classifier should be adapted to multi-label data. In addition, there is a factor that may negatively affect its performance. NB classifier has the assumption of class conditional independence, i.e. the effect of a feature value on a given class is independent of the values of other features. In real world applications, however,

this assumption does not usually hold which in turn may deteriorate the learning performance. 18

In this part, the NB classifier adapted for multi-label text classification is designed. The two-step feature selection strategy is proposed to obtain the features as independent as possible.

3.1. Naïve Bayesian Multi-Label (NBML) classifier for text classification

For a random document $d \in D$ associated with label set $Y \subseteq L$, |L| binary NB classifiers $H_l: d \to \{l, \neg l\}$ are learned, one for each different label l in L. That is, the original data set is transformed into |L| data sets D_l that contain all examples of original data set, labeled as l if the labels of the original example contained l and as $\neg l$ otherwise. In this case, the multi-label classification problem is transformed into the combination of several single-label NB classifiers.

For the classification of a new document d, this method outputs a set of labels which is the union of the labels that are output by the |L| classifiers.

$$H(d) = \bigcup_{l \in I_l} \{l : H_l(d) = l\}$$
 (1)

Each single-label NB classifier works according to the classic NB theory which is described as follows.

For a random document d_j , its feature is $(a_1, a_2, ... a_m)$, here a_k is kth feature in document d_j . Document label set is $L = \{l_1, l_2, ..., l_n\}$. The conditional probability of document d_j with relate to each class label $P(l_i|d_j)$ is defined as follows.

$$P(l_i|d_j) = \frac{P(l_i)P(d_j|l_i)}{P(d_i)}$$
(2)

Because $P(l_i)$ does not change the result, it can be ignored. $P(d_j|l_i)$ can be obtained from following formula.

$$P(d_j|l_i) \approx \prod_{k=1}^{m} P(a_k|l_i)$$
(3)

Here, $P(l_i)$ and $P(a_k|l_i)$ can be estimated according to following formulas.

$$\hat{P}(L=l_i) = \frac{N_i}{N} \tag{4}$$

$$\hat{P}(a_k|l_i) = \frac{1 + N_{ki}}{m + \sum_{k=1}^{m} N_{ki}}$$
(5)

Here, N_i is the amount of texts having the label l_i . N_{ki} is the total frequency of word a_k appearing in documents in category l_i . For single-label classifier, the

predicted category of document d_j is the maximum of probability of these categories. In the case of multi-label classification, we use a parameter P_{thres} to represent the average of posterior probability of document d_j in each class as follows.

$$P_{thres} = \frac{1}{n} \sum_{i=1}^{n} P(l_i|d_j) \tag{6}$$

When $P(l_i|d_j) \ge P_{thres}$, we consider that d_j has label l_i . In this strategy, new document d has all labels which satisfy $P(l|d) \ge P_{thres}$. The Eq.(1) could be described as follows.

$$H(d) = \bigcup_{l \in L} \{l : P(l|d) \ge P_{thres}\}$$
(7)

The least amount of labels of a document is "1" when the probability of the document belonging to a class is obviously higher than that of the document belonging to other classes. The maximum amount of labels of a document is "n" when the probabilities of the document belonging to each class are equal.

3.2. Two-step feature selection strategy

Feature selection is a space reduction method which attempts to select the more discriminative features from preprocessed documents in order to improve classification quality and reduce computational complexity. As many words are extracted from documents, we remove stop list words and then perform two-step feature selection. Firstly, discriminative features are selected based on DF (Document Frequency) and χ^2 statistical analysis. Then FCBF (Fast Correlation-Based Filter Solution) algorithm proposed by Yu and Liu³⁷ is conducted to filter relevant and redundant features among classes.

3.2.1. The first step feature selection

The number of words in each class is great. However, most of them occur only one or two times. This kind of words is not representative for a class. It is necessary to cancel these words in a class before further feature selection. We adopt DF to filter this kind of features, which is defined as follows.

In a corpus D, each text belongs to a class set Y. Here, $Y\subseteq L$, $L=\{l_1,l_2,...,l_n\}$ is the class set defined before classification. Relative text frequency is:

$$Text_freq_relative_{ij} = \frac{Text_freq_{ij}}{N_i}$$
 (8)

Here, N_i is the quantity of texts with label l_i in training set. $Text_freq_{ij}$ is the number of texts with label l_i which include word j. Algorithm 1 is designed to filter rare features within a class.

Algorithm 1.

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Begin For l_i \in L, L = \{l_1, l_2...l_i...l_n\}, Term_i' = \emptyset, Term = \emptyset; For word_j \in Term_i, If (Text\_freq\_relative_{ij} < \alpha) remove word_j; Else word_j \in Term_i'. Term = \{Term_1', Term_2'...Term_i'...Term_n'\}. End.
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Here, $Term_i$ includes all the words extracted in the documents with label l_i , $Term'_i$ includes all the words selected in documents with label l_i and Term is word set selected in training set by Algorithm 1.

We construct "feature by class label" matrix (noted as $Matrix_{cf}$) to select discriminative features. In $Matrix_{cf}$, each feature (word) "j" is assigned a numerical score based on its occurrence within the different document labels " l_i ". The choice of the scoring method in this work is the χ^2 test. There are many other tests available as summarized by Sebastiani.³⁸ However, the χ^2 is often cited as one of the best methods for feature selection. The score of word "k" is:

$$\sum_{i} \frac{(O_{ik} - E_{ik})^2}{E_{ik}} \tag{9}$$

Where O_{ik} is the frequency of word k in documents with label l_i . E_{ik} represent the expectation value in the hypothesis of independence of classes and features.

$$E_{ik} = \frac{O_{i+} \times O_{+k}}{O_{++}} \tag{10}$$

Here, O_{i+} is the total word frequency on label l_i and O_{+k} is the accumulation of occurrence of word k in training set.

3.2.2. The second step feature selection

FCBF algorithm proposed a fast feature filter method which could identify relevant features as well as redundancy among relevant features without pair wise correlation analysis.³⁷ In this algorithm, feature dimensionality is reduced dramatically by introducing a novel concept, predominant correlation based on symmetrical uncertainty. Here, FCBF algorithm is conducted on the feature selection results obtained in the first step. The first step of the above algorithm has a linear time complexity in terms of the number of features M. The time complexity of second step algorithm FCBF is O(NMloqM), where, N is the number of instances.³⁷

4. Experiments and Discussions

As reviewed in Section 2, there have been several approaches to solving multi-label problems. In this paper, our algorithm NBML is compared with Adaboost.MH, 21 multi-label K nearest neighbor (ML-kNN) 24 and the multi-label kernel method Rank-SVM, 16 which are all multi-label learning algorithms applicable to various multi-label problems including text classification. We would not compare our method to the NB multi-label classification algorithm proposed respectively by A. McCallum 17 and Min-Ling Zhang 18 because they have high computational complexity which is improper for the application of Web search results visualization.

For the sake of well evaluating our classification algorithm, our experiments are conducted on an public English corpus coming from NTT communication science research group, which contains real Web pages linked from the "yahoo.com" domain, where it consists of 14 top-level categories (i.e. "Arts & Humanities", "Business & Economy", etc.) and each category is classified into a number of second-level subcategories ^c. By focusing on the second-level categories, we selected 11 out of the 14 independent text categorization problems. For each problem, the training set contains 2,000 documents while the test set contains 3,000 documents.

We adopt various evaluation metrics such as Hamming Loss, One-error, Coverage and Average Precision. The definitions of these metrics could be found in Ref.12. Tables 1-4 show the comparisons on various metrics between our NBML and AdaBoost.MH, ML-kNN and Rank-SVM algorithms, where the best result on each corpus is in bold face. The experiment results of AdaBoost.MH, ML-kNN and RANK-SVM are cited. ²⁴ Classification algorithm of NBML is performed on the free platform WEKA. ³⁹ Ten-fold cross-validation is carried out on data set. In the first step of feature selection, we choose $\alpha=0.02$.

Data Set	NBML	ML- kNN	${\bf AdaBoost.MH}$	Rank-SVM
Arts & Humanities	0.0605	0.0612	0.0585	0.0615
Business & Economy	0.0253	0.0269	0.0279	0.0275
Computers & Internet	0.0373	0.0412	0.0396	0.0392
Education	0.0455	0.0387	0.0423	0.0398
Entertainment	0.0544	0.0604	0.0578	0.0630
Health	0.0433	0.0458	0.0397	0.0423
Recreation & sports	0.0610	0.0620	0.0584	0.0605
Reference	0.0314	0.0314	0.0293	0.0300
Science	0.0336	0.0325	0.0344	0.0340
Social & Science	0.0241	0.0218	0.0234	0.0242
Society & Culture	0.0553	0.0537	0.0575	0.0555
Average	0.0429	0.0432	0.0426	0.0434

Table 1. Comparison among different algorithms on Hamming loss

 $^{^{\}rm c}$ Data set available at http://www.kecl.ntt.co.jp/as/members/ueda/yahoo.tar.gz.

Table 1 shows the comparison of Hamming Loss between NBML and other algorithms. We could find that AdaBoost.MH gives the best performance, ML-kNN and NBML follow and Rank-SVM gives the worst. Hamming Loss evaluates how many times an instance-label pair is misclassified, i.e. a label not belonging to the instance is predicted or a label belonging to the instance is not predicted. AdaBoost.MH is designed to minimize Hamming Loss, thus, it could give better prediction on instance-label pair.

Data Set	NBML	ML- kNN	${\bf AdaBoost.MH}$	Rank-SVM
Arts & Humanities	0.5756	0.6330	0.5617	0.6653
Business & Economy	0.1420	0.1213	0.1337	0.1237
Computers & Internet	0.4453	0.4357	0.4613	0.4037
Education	0.5105	0.5207	0.5753	0.4937
Entertainment	0.5209	0.5300	0.4940	0.4933
Health	0.3571	0.4190	0.3470	0.3323
Recreation & sports	0.5517	0.7057	0.5547	0.5627
Reference	0.4776	0.4730	0.4840	0.4323
Science	0.5731	0.5810	0.6170	0.5523
Social & Science	0.3572	0.3270	0.3600	0.3550
Society & Culture	0.4502	0.4357	0.4845	0.4270
Average	0.4510	0.4711	0.4612	0.4401

Table 2. Comparison among different algorithms on One-error

Table 2 shows the comparison of One-error between NBML and other algorithms. We could find that Rank-SVM gives the best performance, NBML gives the second best, AdaBoost.MH follows and ML-kNN gives the worst. One-error evaluates how many times the top-ranked label is not in the set of proper labels of the instance. This indicates that NBML could give good prediction on the top-ranked label of instance.

Table 5. Comparison among different algorithms on coverage				
Data Set	NBML	ML-kNN	AdaBoost.MH	Rank-SVM
Arts & Humanities	5.3471	5.4313	5.1900	9.2723
Business & Economy	2.3210	2.1840	2.4730	3.3637
Computers & Internet	4.4279	4.4117	4.4747	8.7910
Education	3.6840	3.4973	3.9663	8.9560
Entertainment	3.1015	3.1467	3.0877	6.5210
Health	3.0266	3.3043	3.0843	5.5400
Recreation & sports	4.3838	5.1010	4.3380	5.6680
Reference	3.2022	3.5420	3.2643	6.9683
Science	6.4053	6.0470	6.6027	12.4010
Social & Science	3.8422	3.0340	3.4820	8.2177
Society & Culture	5.8794	5.3653	4.9545	6.8837
Average	4.1474	4.0968	4.0834	7.5075

Table 3. Comparison among different algorithms on coverage

Table 3 shows the comparison of Coverage between NBML and other algorithms. We could find that ML-kNN and AdaBoost.MH give the best performance; Results of NBML are very close to the best performance. Rank-SVM gives the worst. Coverage evaluates how far we need, on the average, to go down the list of labels in order to cover all the proper labels of the instance. It is loosely related to precision at the level of perfect recall. This indicates that NBML perform well on recall rate.

Table 4 shows the comparison of Average Precision between NBML and other algorithms. We could find that NBML gives the best performance, AdaBoost.MH and ML-kNN follows and Rank-SVM gives the worst. Average Precision evaluates the average fraction of labels ranked above a particular label $l \in Y$, which actually is in Y. This indicates that NBML could give predictions which have the smallest deviation from the true label set of instance.

Data Set	NBML	ML-kNN	${\bf AdaBoost.MH}$	Rank-SVM
Arts & Humanities	0.5391	0.5097	0.5526	0.4170
Business & Economy	0.8819	0.8798	0.8702	0.8694
Computers & Internet	0.6205	0.6338	0.6235	0.6123
Education	0.5882	0.5993	0.5619	0.5702
Entertainment	0.6503	0.6013	0.6221	0.5637
Health	0.7355	0.6817	0.7257	0.6839
Recreation & sports	0.5535	0.4552	0.5639	0.5315
Reference	0.6309	0.6194	0.6264	0.6176
Science	0.5234	0.5324	0.4940	0.5007
Social & Science	0.7309	0.7481	0.7217	0.6788
Society & Culture	0.6057	0.6128	0.5881	0.5717
Average	0.6418	0.6249	0.6318	0.6015

Table 4. Comparison among different algorithms on Average precision

We summarize above conclusions: Algorithm NBML proposed in this paper has nearly performance comparing to the famous algorithms (i.e. AdaBoost.MH and ML-kNN) in the application of multi-label text classification.

5. Prototype System TJ-MLWC

This section presents an example of visualizing text search results by using multilabel classification methodology, named TJ-MLWC2.0 (The version TJ-MLWC1.0 was designed for Chinese text search visualization.). It calls the API of search engine, performs NB multi-label classification on its search results and provides user the visualized search results by system interface. The classifiers are trained off-line based on part of the multi-label corpus referred in our experiments.

A TJ-MLWC session starts with the user entering her query in the query box. For example, the user inputs "Microsoft" and then the system returns the interface as shown in Fig.1. Here, the labels in left box are the categories pre-defined. In the right, there are all entries returned by search engine. We could choose one or a few

categories, allowing the system to return the entries in specified categories. Each entry in the right, which different from the displaying form of current prevalent search engine, has one or more class labels added by system.

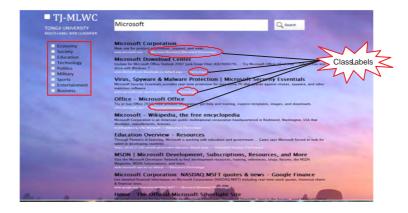


Fig. 1. All search results of "Microsoft"

Fig.2 and Fig.3 show the results of query "Microsoft" by choosing the class label "Technology", "Education" separately. The system returns all the entries involving class label "Technology" in Fig.2 and involving class label "Education" in Fig.3. Fig.4 shows the results of involving class label "Technology" and "Education" in the same time. From the figures, we could find that there are some entries belong to both "Technology" and "Education". For example, "Microsoft - Wikipedia, the free encyclopedia", "Education Overview - Resources" appear in Fig.2 and Fig.3 simultaneously. When we confine the class label as "Technology + Education", the results will be limited to the scope of entries with the two labels as shown in Fig.4.

From the above figures, we could find that a document could appear in more than one class in our system, which is different from the search engine visualization system based on clustering algorithms. Theoretically, if a document concerns the contents in several classes, we could find it in all these classes. However, search engine based on clustering is more likely to assign a document in a certain cluster. Usually, the label for a cluster obtained by clustering algorithm is hard to reflect the content of documents in its cluster properly. In this case, the cluster labels are not very effective for user's locating. In TJ-MLWC, class labels are pre-defined to avoid this problem. Moreover, multiple labels ensure that a document could always be found for users having different interests.

Through testing, we found that there are still some problems to be solved in system TJ-MLWC. Firstly, it mixes the text search results and other kind of search results such as image, video and audio. Further works will focus on constructing a hierarchical classifier which classifies files according to their formation first and then



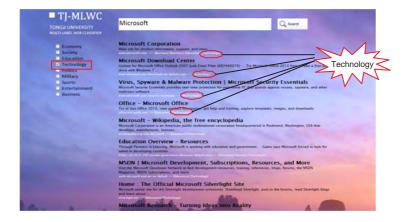


Fig. 2. Search results of "Microsoft" when selecting "Technology" class

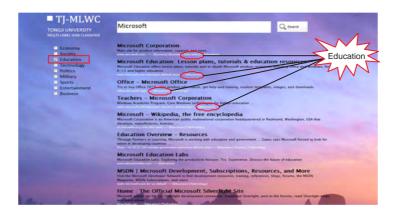


Fig. 3. Search results of "Microsoft" when selecting "Education" class

conducts multi-label classification on each kind of files. Secondly, we pre-defined the taxonomy for search results. However, with gradually rectification of Web contents, documents in new classes will always appear. How can we rectify the taxonomy automatically according to real demand? All of these problems are our future research objectives.

6. Conclusions

This paper presents a new multi-label classification method based on Naïve Bayesian theory. A two-step feature selection strategy based on DF, χ^2 and FCBF algorithm is incorporated into the method to improve classification performance. Experiments on public multi-label corpus show that our method achieves highly competitive



Fig. 4. Search results of "Microsoft" when selecting "Technology" and "Education" class

performance with several famous multi-label classification algorithms. Because our method embedded high efficiency feature selection algorithm, it has low computation costs which allows it to be used for the on-line application, especially for handling high-dimensionality text data. However, our NBML algorithm does not concern the correlation between labels while the dependency among labels exists widely in real applications. Consequently, the improvement of NB multi-label classification itself is our future research issue.

A Web search results visualizing prototype system TJ-MLWC is developed in this paper. Testing results indicate that this system has the function of browsing search results by category. It could also avoid the problem of search result visualization system based on clustering methods. However, with the growing of new contents on Web, the pre-defined taxonomy is hard to extend automatically and the classification ability of model trained off-line will be degraded greatly. Semi-supervised multi-label classification method could make use of the unlabeled online data to improve the performance of classifier. Designing semi-supervised MLNB classifier that can handle online learning problem is an interesting problem to be explored.

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