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Monadic Concurrency in OCaml

Part II in Computer Science

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Proforma

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Original Aims of the Project

To write an OCaml framework for lightweight threading. This framework should be defined from basic semantics and have these semantics represented in a theorem prover setting for verification. The verification should include proofs of basic monadic laws. This theorem prover representation should be extracted to OCaml where the extracted code should be as faithful to the representation as possible. The extracted code should be able to run OCaml code concurrently.

Work Completed

All that has been completed appears in this dissertation.

Special Difficulties

Learning how to incorporate encapsulated postscript into a L^AT_EX document on both CUS and Thor.

¹This word count was computed by `detex diss.tex | tr -cd '0-9A-Za-z \n' | wc -w`

Declaration

I, Tamás Kispéter of Churchill College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose.

Signed [signature]

Date April 18, 2014

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Acknowledgements

Chapter 1

Introduction

The goal of this project is to build a concurrency framework for OCaml. This framework will be designed with correctness in mind: developing the well defined semantics, modelled in a proof assistant and finally extracted to actual code. This project aims to be a verifiable reference implementation.

1.1 Motivation

Verification of core libraries is becoming increasingly important as we discover more and more subtle bugs that even extensive unit testing could not find. As Dijkstra said, testing shows the presence, not the absence of bugs. On the other hand verification can show the absence of bugs, at least with respect to the formal model of the system.

Motivation of the project is to investigate the lack of certified implementation of a concurrency framework. Verified concurrent systems have been researched for languages like C[25], C++ and Java[21], but not yet for OCaml.

1.2 Overview of concurrency

Concurrency is the concept of more than one thread of execution making progress in the same time period. A particular form of concurrency is parallelism, when threads physically run simultaneously.

Concurrent computation has become common in many applications in computer science with the rise of faster systems often with multiple cores. This can be exploited on multiple levels ranging from hardware supported instruction and thread level parallelism to software based heavy and lightweight models.

This project aims to model lightweight, cooperative concurrency. No threads are exposed to the underlying operating system or hardware. This means that blocking operations on the process level will still block all internal threads. The threads expose the points of possible interleaving and the scheduling is done in software.

The issue of concurrency occurs in most general programming languages. However, functional languages are often both less developed in this area and also fit well with concurrency without races for mutable data structures. Functional languages that have both actual industrial applications and large set of features are of particular interest. These languages include OCaml and Haskell. This project focuses on OCaml.

1.3 Current implementations of a concurrency framework in OCaml

There are two very successful monadic concurrency frameworks, LWT[2] and Async[28]. They both provide the primitives and syntax extensions for concurrent development in OCaml, however neither is supported by a clear semantic description. This is because their main focus was ease of use and speed.

LWT, the lightweight cooperative threading library[30] was designed as an open source framework entirely written in OCaml in a monadic style. It was successfully used in several large projects including the Unison file synchroniser and the Ocsigen Web server. This library includes many primitives to provide a feature rich framework, including primitives for thread creation, composition and cancel, thread local storage and support for various synchronisation techniques.

1.3. CURRENT IMPLEMENTATIONS OF A CONCURRENCY FRAMEWORK IN OCAML3

```
1 open Lwt
2
3 let main () =
4   let heads =
5     Lwt_unix.sleep 1.0 >>
6     return (print_endline "Heads");
7   in
8   let tails =
9     Lwt_unix.sleep 2.0 >>
10    return (print_endline "Tails");
11  in
12  let () = heads <&> tails in
13  return (print_endline "Finished")
14
15 let _ = Lwt_main.run (main ())
```

Listing 1.1: LWT example

In this example we can see some of the syntax of Lwt where we define **heads**, a function that sleeps for 1 second and then prints “Head” and **tails** which does the same with 2 seconds and “Tails”. These are then both waited on, until they are both finished and followed by the text “Finished”. In Lwt semantics mostly follow the principle of a continuation monads, that is we build a sequence of continuations that the scheduler can pick between.

An other implementation, Async is an open source concurrency library for OCaml developed by Jane Street. Unlike LWT the basic semantics are designed with the promise monads in mind.

```
1 open Jane.Std
2 open Async.Std
3
4 let heads = (after (sec 1.0) >>| fun () -> (print_endline "Heads"
5   ));;
6 let tails = (after (sec 2.0) >>| fun () -> (print_endline "Tails"))
7   ;;
8 let head_and_tails = (Deferred.both
9   heads
10  tails);;
11 let () = upon (head_and_tails) (fun _ -> ());;
12
13 let () = never_returns (Scheduler.go ());;
```

Listing 1.2: Async example

In this snippet we define `heads` and `tails` as Deferred values of the respective code sequences. A Deferred value is the promise of that value evaluating. It can be used in place of a value of the same type and binding on it returns a deferred value that is when is fulfilled applies the bound function.

There are a number of other experimental implementations for concurrency in OCaml, including JoCaml[22] that implements join calculus over Ocaml, Functory[15] that focuses on distributed computation, Ocamlnet that exploits multiple cores and OCamlMPI[17] which provides bindings for the standard MPI message passing framework.

1.4 Semantics of concurrency

There have been a lot of work on how exactly to formulate the semantics of concurrent and distributed systems. Some of the most common models for lightweight concurrency[11] are captured[12] and delimited[16] continuations[26], trampolined style[13], continuation monads[9], promise monads[20] and event based programming(used in the OCamlNet[27] project). This work focuses on the continuation monad style.

A monad[14] in functional programming is a construct to structure computations that are in some sense "sequenced" together. This sequencing can be for example string concatenation, simple operation sequencing (the well known ;) or conditional execution. Two operations, commonly called bind and return form a monad when they obey a set of axioms called monadic laws.

Most monads support further operations and a concurrency monad is one such monad. Beside the two necessary operations (return and bind) it has to support at least one that deals with concurrent execution. This operation can come in many forms and under many names, for example fork, join or choose. Each of these may have slightly differing signatures and semantics depending on the style.

1.5 Semantics to logic

These semantics can be modelled in logic, in particular logics used by proof assistants. A model like this can be used for formal verification of properties about said semantics [6, 8, 7, 18]. Most often used proof assistants include Coq [4], HOL and Isabelle. There has been much effort to make the modelling as easy as possible with tools like Ott[23] which enables semanticists to describe their

language in a simple, ascii-art like style and export these models to destination languages, including the above mentioned proof assistants and L^AT_EX.

1.6 Logic to runnable code

While a number of proof assistants have utilities for direct computation, in most cases semantics is described as a set of logical relations. This representation is more amenable to proofs than to actual execution. Much research has gone into extraction of these representations as certified programs in functional programming languages like OCaml [19] and Haskell. The extracted code then can be run and the certification is a proof that the code is faithful to the representation in the proof assistant.

Chapter 2

Preparation

During the preparation phase of this project many decisions had to be made, including the concurrency model, large scale semantics and the tool chain used in the process.

2.1 Design of concurrent semantics

Concurrency may be modelled in many ways. A popular way of modelling concurrency is with a process calculus. A process calculus is an algebra of processes or threads where. A thread is a unit of control, sometimes also a unit of resources. This algebra often comes with a number of operations like

- $P|Q$ for parallel composition where P and Q are processes
- $a.P$ for sequential composition where a is an atomic action and P is a process executed sequentially
- $!P$ for replication where P is a process and $!P \equiv P|!P$
- $x\langle y \rangle \cdot P$ and $x(v) \cdot Q$ for sending and receiving messages through channel x respectively

This project aimed to have simple but powerful operational semantics. Simplicity is required in both the design and the interface. There is a short and limited timespan for implementation and an even shorter period for the user to understand the system. On the other hand, the model should have comparable formal properties to full, well known process calculi.

I focused on providing primitives for operations on processes including parallel and sequential composition and recursion. Formal treatment of communication channels have been left out to limit the scope of the project.

2.2 Choice of implementation style

A number of implementation styles of lightweight concurrency were surveyed for OCaml by Christophe Deleuze[11]. These fall in two broad categories: direct and indirect styles. Direct styles like captured and delimited continuations involve keeping an explicit queue of continuations that can be executed at any given time and a scheduler that picks the next element from the queue. Indirect styles include the trampolined style and two monadic styles: continuations and promises.

Simplicity and similarity to current implementations like Lwt and Async were the two factors in the decision between these styles. Both direct styles and the promise monad style keep concurrency state data that is external to the language and has to be maintained at runtime explicitly. This would make implementation slightly more complicated. Lwt and Async both provide monadic style interfaces therefore I chose the continuation monad style.

2.3 Design of monadic semantics

Category theory has been a general tool used to model functional programming languages and programs. Monads are a concept originating from this connection.

A monad on a category C is a triple (T, η, μ) where T is an endofunctor on C , that is, it maps the category to itself. The last two, η and μ are natural transformations such that $\eta : 1_C \rightarrow T$, that is between the identity functor and T , and $\mu : T^2 \rightarrow T$. The first transformation, η describes a lift operation: essentially we can wrap the object in C and preserving its properties. The second transformation, μ is about an operation called join. This operation unwraps a layer of wrapping if there are two. To call a triple like this a monad it has to satisfy two conditions, called coherence conditions.

1.

$$\mu \circ T\mu = \mu \circ \mu T$$

Or as commutative diagram:

$$\begin{array}{ccc} T^3 & \xrightarrow{T\mu} & T^2 \\ \mu T \downarrow & & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array}$$

This roughly demands that unwrapping from three layers to one is associative.

2.

$$\mu \circ T\eta = \mu \circ \eta T = 1_T$$

Or as commutative diagram:

$$\begin{array}{ccc} T & \xrightarrow{\eta T} & T^2 \\ T\eta \downarrow & \searrow & \downarrow \mu \\ T^2 & \xrightarrow{\mu} & T \end{array}$$

This roughly translates to wrapping and then subsequently unwrapping behaves as an identity.

This description entails three operations (lift, join and map) and their behaviour (associativity and identity), however this is a formulation rarely used in practice. There is an equivalent pair of operations (ret and bind) with similar behaviour constraints that is used in most monadic programming constructs.

Most implementations go along the following lines: there is a parametric type **con** α where α is the type parameter. Note **con** is an arbitrary name, marker for a particular monad. The I/O monad would have IO as the marker.

The ret takes a value of the language and gives its monadic counterpart. With types this can be represented as **ret** : $\forall \alpha. \alpha \rightarrow \mathbf{con} \alpha$.

The bind (often written as $\gg=$) takes a monadic value (that is one in the parametric type **con** α) and a function that can map the inner value to a new monadic value (that is, it has type $\alpha \rightarrow \mathbf{con} \beta$). Bind then returns a **con** β . With types this means: $\gg= : \forall \alpha \beta. \mathbf{con} \alpha \rightarrow (\alpha \rightarrow \mathbf{con} \beta) \rightarrow \mathbf{con} \beta$.

To call this system a monad, we need to satisfy three axioms:

1. ret is essentially a left neutral element:

$$(\mathbf{ret} \ x) \gg= f \quad \equiv \quad f \ x$$

2. ret is essentially a right neutral element:

$$m \gg= \mathbf{ret} \quad \equiv \quad m$$

3. bind is associative:

$$(m \gg= f) \gg= g \quad \equiv \quad m \gg= (\lambda x. (f \ x \gg= g))$$

We will return to the exact nature of \equiv used in this project in the evaluation section and the exact form this will take.

2.4 Tools

The project uses a chain of three tools:

1. Ott, a tool for transforming informal, readable semantics to both \LaTeX and formal proof assistant code.
2. Coq, a proof assistant supported by Ott.
3. OCaml, the target language.

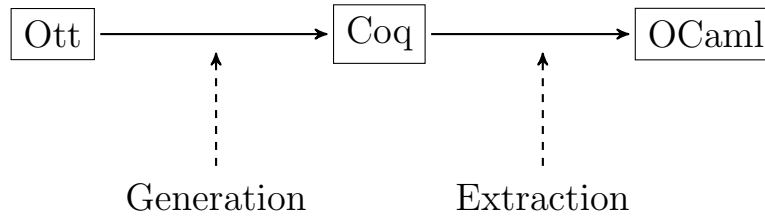


Figure 2.1: Toolchain outline

In the preparation phase I got acquainted with all three of these systems, as I have not used them before for any serious work.

2.4.1 Ott

To avoid duplication of the semantics in several formats I have to chosen to use a supporting tool called Ott. It enables the use of a simple ASCII-art like description of grammars, typing and reduction relations. Ott can export to various destination formats including most proof assistants and \LaTeX . This is the primary form of the semantics that all further forms are derived from in the project.

For someone familiar to formal semantics Ott has an easy to use and intuitive syntax.

Metavariables used in productions are defined with their destination language equivalents and potentially (in the case of Coq) their equality operation

```

1 metavar termvar, x ::= {{ com term variable }}
2 {{ isa string }} {{ coq nat }} {{ hol string }} {{ coq-equality }}
3 {{ ocaml int }} {{ lex alphanum }} {{ tex \mathit{[[termvar]]} }}

```

Listing 2.1: Ott metavariable definition

Term expression grammars and other grammars can be defined in the well known Backus-Naur form with some extensions.

```

1 grammar
2 t :: 't_' ::=                                {{ com term      }}
3 | x                :: :: Var                  {{ com variable }}
4 | \ x . t          :: :: Lam (+ bind x in t +) {{ com lambda   }}
5 | t t'             :: :: App                  {{ com app      }}
6 | ( t )           :: S:: Paren                 {{ icho [[t]]   }}
7 | { t / x } t'     :: M:: Tsub
8                      {{ icho (tsubst_t [[t]] [[x]] [[t']) }}

```

Listing 2.2: Ott grammar example

In this example the non-terminal t for terms is defined with 5 productions: variables, lambda abstractions, applications, parentheses grouping and variable substitution. Each of these rules have a name, for example `Var` and `Lam`. Each of these names are prefixed by the unique prefix `t_` to have non-ambiguous names. The right hand side of each line describes the translation to target languages, for example `com` will generate the given description for the \LaTeX target.

There are meta flags `S` and `M` to describe syntactical sugar and meta productions that are not generated as data structure elements in target languages, but instead have their own instructions: for example the substitution term will be rewritten as an application of the `tsubst_t` relation defined elsewhere.

In many languages one might want to define a value subgrammar, which can be used both in the reduction relation definition and in proving properties of the semantics. Ott has support for general subgrammar relation check.

```

1 v :: 'v_' ::=                                {{ com value    }}
2 | \ x . t          :: :: Lam                  {{ com lambda   }}
3
4 subrules
5 v <:: t

```

Listing 2.3: Ott value subgrammar example

Here v is a subgrammar of t . The statement $v <:: t$ is exported as a target language subroutine that checks whether this holds and during translation it checks for obvious bugs.

Another common feature of semantics is substitution of values for variables, for example in function application. This is so frequent that Ott provides both single and multiple variable substitutions for the target languages as subroutines in the translated code.

```

1 substitutions
2 single t x :: tsubst

```

Listing 2.4: Ott substitution example

The statement `single t x :: tsubsts` defines a single substitution function called `tsubsts_t` over terms defined by the grammar for `t` and for variables represented by the metavariable `x`. This is the relation mentioned in the grammar for the target language version for $\{ t / x \} t'$.

Finally paramount to most semantics are relations like the reduction relation.

```

1  defs
2  Jop  ::  ' '  ::=
3
4  defn
5  t1 --> t2  ::  ::reduce:: ' '  {{ com  [[t1]]  reduces to  [[t2]] }} by
6
7
8  -----  ::  ax_app
9  (\x.t12) v2 -->  {v2/x}t12
10
11  t1 --> t1 '
12  -----  ::  ctx_app_fun
13  t1 t --> t1 ' t
14
15  t1 --> t1 '
16  -----  ::  ctx_app_arg
17  v t1 --> v t1 '

```

Listing 2.5: Ott reduction relation example

In this example I define a set of mutually recursive relations named `Jop` with one relation in it the `-->` or `reduce` relation. Each element of this relation takes the form `t1 --> t2`, where `t1` and `t2` are both terms of the grammar defined above. There are three statements for function application: the actual substitution, reduction of the first term and reduction of the second term.

```

1  t1 --> t1 '
2  -----  ::  ctx_app_fun
3  t1 t --> t1 ' t

```

Listing 2.6: Ott single reduction

The premise(s) appear line-by-line above the ascii-art line, while and the result below the line. Next to the line is the name of the statement which is then prefixed by the name of the relation to avoid ambiguity.

2.4.2 Coq

There are a number of proof assistants available as destinations for Ott, out of which Coq and Isabelle provide good extraction facilities to OCaml. They are at a glance rather similar. The choice between the two came down to advice from supervisors as I did not have experience with either systems. This project was developed with the Coq proof assistant.

Coq is formal proof assistant with a mathematical higher-level language called *Gallina*, based around the Calculus of Inductive Constructions, that can be used to define functions and predicates, state, formally prove and machine check mathematical theorems and extract certified programs to high level languages like Haskell and OCaml.

Objects in Coq can be divided into two sorts, *Prop* (propositions) and *Type*. A proposition like $\forall A, B. A \wedge B \rightarrow B \vee B$ translates as

```
1 forall A B : Prop, A ∧ B → B ∨ B
```

Listing 2.7: Coq Prop logic example

Predicates like equality and other sets can be used as well

```
1 forall x y : Z, x * y = 0 → x = 0 ∨ y = 0
```

Listing 2.8: Coq Prop predicate example

New predicates can be defined inductively

```
1 Inductive even : N → Prop :=
2   | even_0 : even 0
3   | even_S n : odd n → even (n + 1)
4 with odd : N → Prop :=
5   | odd_S n : even n → odd (n + 1).
```

Listing 2.9: Coq Prop new predicate example

Data structures can also be defined both inductively and coinductively

```
1 Inductive seq : nat → Set :=
2   | niln : seq 0
3   | consn : forall n : nat, nat → seq n → seq (S n).
```

Listing 2.10: Coq inductive data structure example

```
1 CoInductive stream (A:Type) : Type :=
2   | Cons : A → stream → stream.
```

Listing 2.11: Coq coinductive data structure example

Functions over these data structures are defined as fixpoints and cofixpoints respectively.

```

1 Fixpoint length (n : nat) (s : seq n) {struct s} : nat :=
2   match s with
3   | niln  $\Rightarrow$  0
4   | consn i _ s'  $\Rightarrow$  S (length i s')
5   end.

```

Listing 2.12: Coq fixpoint example

Finally theorems can be proven with these propositions and structures.

```

1 Theorem length_corr : forall (n : nat) (s : seq n), length n s = n.
2 Proof.
3   intros n s.
4
5   (* reasoning by induction over s. Then, we have two new goals
6     corresponding on the case analysis about s (either it is
7     niln or some consn *)
8   induction s.
9
10  (* We are in the case where s is void. We can reduce the
11    term: length 0 niln *)
12  simpl.
13
14  (* We obtain the goal 0 = 0. *)
15  trivial.
16
17  (* now, we treat the case s = consn n e s with induction
18    hypothesis IHs *)
19  simpl.
20
21  (* The induction hypothesis has type length n s = n.
22    So we can use it to perform some rewriting in the goal: *)
23  rewrite IHs.
24
25  (* Now the goal is the trivial equality: S n = S n *)
26  trivial.
27
28  (* Now all sub cases are closed, we perform the ultimate
29    step: typing the term built using tactics and save it as
30    a witness of the theorem. *)
31  Qed.

```

Listing 2.13: Coq theorem example

Each Lemma, Theorem, Example have a name and a statement. The statement is a proposition. This is followed by the proof in which a sequence of steps modify

the assumed hypotheses and the goal proposition until it has been proven. These steps are called tactics which can be simple application of previous theorems and axioms or as complex as a SAT solver. Coq comes with a language Ltac to allow users to build their own tactics.

Coq also provides built in facilities for the certified extraction of code to OCaml, Haskell and Scheme. These can be invoked with the keywords `Extraction` and `Recursive Extraction`.

```

1 type nat =
2 | O
3 | S of nat
4
5 type seq =
6 | Niln
7 | Consn of nat * nat * seq

```

Listing 2.14: Coq to OCaml extraction of seq

```

1 (** val length : nat -> seq -> nat **)
2
3 let rec length n = function
4 | Niln -> O
5 | Consn (i, n0, s') -> S (length i s')

```

Listing 2.15: Coq to OCaml extraction of length

Out of the box, Coq does not provide facilities for the extraction of so called logical inductive systems. These are essentially inductively defined propositions.

```

1 Inductive add : nat -> nat -> nat -> Prop :=
2 | addO : forall n , add n O n
3 | addS : forall n m p, add n m p -> add n (S m) (S p) .

```

Listing 2.16: Coq logical inductive example

However with the help of a plugin developed by David Delahaye, Catherine Dubois, Jean-Frédéric Étienne and Pierre-Nicolas Tollitte [10, 29] by marking different modalities of the inductively generated proposition we can generate code with an input-output convention.


```

1 (** val add12 : nat → nat → nat **)
2
3 let rec add12 p1 p2 =
4   match (p1, p2) with
5   | (n, O) → n
6   | (n, S m) →
7     (match add12 n m with
8      | p → S p
9      | _ → assert false (* *))
10  | _ → assert false (* *)

```

Listing 2.17: Coq to OCaml extraction of a logical inductive relation

Most descriptions of reduction relations and indeed the output of Ott is of this kind, therefore this plugin helps with the extraction of a reduction relation directly.

2.4.3 OCaml

OCaml is a high level programming language. It combines functional, object-oriented and imperative paradigms and used in large scale industrial and academic projects where speed and correctness are of utmost importance. OCaml uses one of the most powerful type and inference systems available to make efficient and correct software engineering possible.

OCaml, like many other functional languages support a wide range of features, from simple functions, to mutually recursive functions with pattern matching.

```

1 let square x = x * x

```

Listing 2.18: OCaml simple function example: square

```

1 let rec fact x =
2   if x <= 1 then 1 else x * fact (x - 1)

```

Listing 2.19: OCaml recursive function example: factorial

```

1 let rec sort = function
2   | [] → []
3   | x :: l → insert x (sort l)
4 and insert elem = function
5   | [] → [elem]
6   | x :: l → if elem < x then elem :: x :: l
7               else x :: insert elem l

```

Listing 2.20: OCaml complex function example: insertion sort

Furthermore, it was designed as a versatile, general purpose programming language. OCaml features include objects, modules, support for imperative style and higher order functions.

```

1 let add_polynom p1 p2 =
2   let n1 = Array.length p1
3   and n2 = Array.length p2 in
4   let result = Array.create (max n1 n2) 0 in
5   for i = 0 to n1 - 1 do result.(i) <- p1.(i) done;
6   for i = 0 to n2 - 1 do result.(i) <- result.(i) + p2.(i) done;

```

Listing 2.21: OCaml imperative function example

```

1 let rec sigma f = function
2   | [] -> 0
3   | x :: l -> f x + sigma f l

```

Listing 2.22: OCaml higher order functions example

```

1 type expression =
2   | Num of int
3   | Var of string
4   | Let of string * expression * expression
5   | Binop of string * expression * expression

```

Listing 2.23: OCaml data structure example

```

1 let rec eval env = function
2   | Num i -> i
3   | Var x -> List.assoc x env
4   | Let (x, e1, in_e2) ->
5     let val_x = eval env e1 in
6     eval ((x, val_x) :: env) in_e2
7   | Binop (op, e1, e2) ->
8     let v1 = eval env e1 in
9     let v2 = eval env e2 in
10    eval_op op v1 v2
11 and eval_op op v1 v2 =
12   match op with
13   | "+" -> v1 + v2
14   | "-" -> v1 - v2
15   | "*" -> v1 * v2
16   | "/" -> v1 / v2
17   | _ -> failwith ("Unknown operator: " ^ op)

```

Listing 2.24: OCaml evaluation function example

Chapter 3

Implementation

3.1 The semantics

3.1.1 Expressions

Arrow types

Sum types

Product types

Fixpoint combinator

Monadic primitives

The concurrency monad consists of a parametric type $\alpha \mathbf{con}$, where α is a type parameter describing the type of computation or value enclosed and three key operations

- `ret`, also known as `return`. It has type $\alpha \rightarrow \alpha \mathbf{con}$ and simply evaluates its parameter and boxes up the result in the parametric type
- `>>=`, also known as `bind`, sequences two operations. The second argument is the continuation for the first parameter. More formally it has a type $\alpha \mathbf{con} \rightarrow (\alpha \rightarrow \beta \mathbf{con}) \rightarrow \beta \mathbf{con}$, that is it takes a boxed up computation and a function that takes the value of the computation and returns a new box. `Bind` then evaluates the expression within the box of the first argument and passes it to the second argument.

Fork

The third operation is fork, which is the way to spawn new threads (two in this particular case). The approach taken in this work is to have fork take two arguments and evaluate the two paths concurrently. The concurrency is achieved by reducing either side of the fork step by step based on some scheduler. When either path reduced to a value it returns a boxed up pair of results. This result is value and a boxed up computation (that is, the partially reduced other path).

Therefore the signature of fork is slightly more complicated

$$\text{fork} : \alpha \text{ con} \rightarrow \beta \text{ con} \rightarrow ((\alpha * \beta \text{ con}) + (\alpha \text{ con} * \beta)) \text{ con}$$

Computation placeholders

3.1.2 Transition system

Labelled transitions

Select operator

3.1.3 Type system

3.2 Proof assistant system

3.2.1 Outline of the proof assistant code

3.2.2 Modification

3.2.3 Extractable version

3.3 OCaml system

3.3.1 Outline of the OCaml code

3.3.2 Hand modifications and justifications

3.3.3 Sugar

Chapter 4

Evaluation

4.1 Theoretical evaluation

Properties to evaluate: monadic laws, fork commutativity and associativity (liveness ?), type preservation and progress ?.

4.1.1 Methods

Weak bisimilarity

Intro to weak bisimilarity.

What form does a general weak bisimilarity proof take.

How does it appear here.

4.1.2 Properties

Monadic laws

Fork commutativity

Outline of fork commutativity

Fork associativity

Liveness?

Type preservation?

Progress?

4.2 Practical evaluation

Evaluation of speed and memory requirements absolutely and relative to implementations in LWT and Async.

4.2.1 Methods

4.2.2 Examples

Kahn process network

Eratosthene Sieve

Concurrent sort

Chapter 5

Conclusion

I hope that this rough guide to writing a dissertation is \LaTeX has been helpful and saved you time.

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Appendix A

Ott source

A.1 diss.tex

```
% The master copy of this demo dissertation is held on my filespace
% on the cl file serve (/homes/mr/teaching/demodissert/)

% Last updated by MR on 2 August 2001

\documentclass[12pt,twoside,notitlepage]{report}

\usepackage{a4}
\usepackage{verbatim}
\usepackage{etoolbox}

\newtoggle{colourtoggle}
\newtoggle{wordcount}

\togglefalse{wordcount}

\toggletrue{colourtoggle}

\usepackage{url}
\input{epsf} % to allow postscript inclusions
% On thor and CUS read top of file:
% /opt/TeX/lib/texmf/tex/dvips/epsf.sty
% On CL machines read:
% /usr/lib/tex/macros/dvips/epsf.tex

\raggedbottom % try to avoid widows and orphans
\sloppy
\clubpenalty1000%
\widowpenalty1000%

\addtolength{\oddsidemargin}{6mm} % adjust margins
\addtolength{\evensidemargin}{-8mm}

\renewcommand{\baselinestretch}{1.1} % adjust line spacing to make
% more readable
```

```

% Listings set up
\usepackage{listings, lstlangcoq, lstlangott, lstlanglwt, bold-extra}
\usepackage{usenames,dvipsnames,svgnames,table}{xcolor}

\iftoggle{colourtoggle}{
\definecolor{mygreen}{rgb}{0,0.6,0}
\definecolor{myblue}{rgb}{0,0,1}
\definecolor{myemerald}{rgb}{0.0,0.66,0.42}
\definecolor{mygray}{rgb}{0.5,0.5,0.5}
\definecolor{mymauve}{rgb}{0.58,0,0.82}
\definecolor{myseagreen}{rgb}{0.95,0.999,0.95}
}{
\definecolor{mygreen}{rgb}{0.35,0.35,0.35}
\definecolor{myblue}{RGB}{5,5,5}
\definecolor{mygray}{rgb}{0.5,0.5,0.5}
\definecolor{myemerald}{RGB}{111,111,111}
\definecolor{mymauve}{rgb}{0.25,0.25,0.25}
\definecolor{myseagreen}{rgb}{0.98,0.98,0.98}
}

\lstset{ %
  backgroundcolor=\color{myseagreen},    % choose the background color; you must add \usepackage{color} or \usepackage{xcolor}
  basicstyle=\footnotesize,              % the size of the fonts that are used for the code
  breakatwhitespace=false,               % sets if automatic breaks should only happen at whitespace
  breaklines=true,                       % sets automatic line breaking
  captionpos=b,                          % sets the caption-position to bottom
  commentstyle=\color{mygreen},           % comment style
  deletekeywords={...},                  % if you want to delete keywords from the given language
  escapeinside={\%*}{(*)},               % if you want to add LaTeX within your code
  extendedchars=true,                    % lets you use non-ASCII characters; for 8-bits encodings only, does not work with UTF-8
  frame=shadowbox,                       % adds a frame around the code
  frameround=tttt,
  keepspaces=true,                       % keeps spaces in text, useful for keeping indentation of code (possibly needs columns=flexible)
  keywordstyle=\color{myblue},            % keyword style
  language=[Objective]Caml,              % the language of the code
  morekeywords={*,...},                  % if you want to add more keywords to the set
  numbers=left,                           % where to put the line-numbers; possible values are (none, left, right)
  numbersep=5pt,                         % how far the line-numbers are from the code
  numberstyle=\tiny\color{myemerald},     % the style that is used for the line-numbers
  rulecolor=\color{myemerald},            % if not set, the frame-color may be changed on line-breaks within not-black text (e.g.
  showspaces=false,                      % show spaces everywhere adding particular underscores; it overrides 'showstringspaces'
  showstringspaces=false,                 % underline spaces within strings only
  showtabs=false,                        % show tabs within strings adding particular underscores
  stepnumber=1,                          % the step between two line-numbers. If it's 1, each line will be numbered
  stringstyle=\color{mymauve},           % string literal style
  tabsize=2,                             % sets default tabsize to 2 spaces
  title=\lstname                         % show the filename of files included with \lstinputlisting; also try caption instead of title
}

% Tikz set up
\usepackage{tikz}
\usepackage{tikz-cd}
\usetikzlibrary{arrows, shapes}

\begin{document}

```

```
\bibliographystyle{plain}
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Title
```

```
\pagestyle{empty}
```

```
\hfill{\LARGE \bf Tam\'as Kisp\'eter}
```

```
\vspace*{60mm}
\begin{center}
\Huge
{\bf Monadic Concurrency in OCaml} \\\
\vspace*{5mm}
Part II in Computer Science \\\
\vspace*{5mm}
Churchill College \\\
\vspace*{5mm}
\today % today's date
\end{center}
```

```
\cleardoublepage
```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% Proforma, table of contents and list of figures
```

```
\setcounter{page}{1}
\pagenumbering{roman}
\pagestyle{plain}
```

```
\chapter*[Proforma]
```

```
{\large
\begin{tabular}{ll}
Name: & & \bf Tam\'as Kisp\'eter & \\\
College: & & \bf Churchill College & \\\
Project Title: & & \bf Monadic Concurrency in OCaml & \\\
Examination: & & \bf Part II in Computer Science, July 2014 & \\\
Word Count: & & \bf 1587\footnotemark[1] & \\\
(well less than the 12000 limit) & & & \\\
Project Originator: & & Tam\'as Kisp\'eter & \\\
Supervisor: & & Jeremy Yallop & \\\
\end{tabular}
}
\footnotetext[1]{This word count was computed
by {\tt detex diss.tex | tr -cd '0-9A-Za-z $\tt\backslash$' | wc -w}
}
\stepcounter{footnote}
```

```
\section*[Original Aims of the Project]
```

To write an OCaml framework for lightweight threading. This framework should be defined from basic semantics and have the

```
\section*[Work Completed]
```

All that has been completed appears in this dissertation.

`\section*{Special Difficulties}`

Learning how to incorporate encapsulated postscript into a `\LaTeX\` document on both CUS and Thor.

`\newpage`

`\section*{Declaration}`

I, Tam\’as Kisp\’eter of Churchill College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose.

`\bigskip`

`\leftline{Signed [signature]}`

`\medskip`

`\leftline{Date \today}`

`\cleardoublepage`

`\tableofcontents`

`\listoffigures`

`\lstlistoflistings`

`\newpage`

`\section*{Acknowledgements}`

%%%

% now for the chapters

`\cleardoublepage` % just to make sure before the page numbering
 % is changed

`\setcounter{page}{1}`

`\pagenumbering{arabic}`

`\pagestyle{headings}`

% Proforma + Intro + prep = 3100

% Implementation = 4700

% Evaluation + conclusion = 2200

% Appendicies = \infty

`\chapter{Introduction}`

The goal of this project is to build a concurrency framework for OCaml. This framework will be designed with correctness in mind.

`\section{Motivation}`

Verification of core libraries is becoming increasingly important as we discover more and more subtle bugs that even extensive testing can miss.

Motivation of the project is to investigate the lack of certified implementation of a concurrency framework. Verified concurrency is a new paradigm.

`\section{Overview of concurrency}`

Concurrency is the concept of more than one thread of execution making progress in the same time period. A particular form of concurrency is parallelism.

Concurrent computation has become common in many applications in computer science with the rise of faster systems often . . .

This project aims to model lightweight, cooperative concurrency. No threads are exposed to the underlying operating system . . .

The issue of concurrency occurs in most general programming languages. However, functional languages are often both less . . .

\section{Current implementations of a concurrency framework in OCaml}

There are two very successful monadic concurrency frameworks, LWT\cite{LWT} and Async\cite{Async}. They both provide the . . .

LWT, the lightweight cooperative threading library\cite{vouillon2008lwt} was designed as an open source framework entire . . .

```
\begin{minipage}{\linewidth}
\begin{lstlisting}[alsolanguage={Lwt}, caption={LWT example}]
open Lwt

let main () =
  let heads =
    Lwt_unix.sleep 1.0 >>
    return (print_endline "Heads");
  in
  let tails =
    Lwt_unix.sleep 2.0 >>
    return (print_endline "Tails");
  in
  lwt () = heads <&& tails in
  return (print_endline "Finished")

let _ = Lwt_main.run (main ())
\end{lstlisting}
\end{minipage}
```

In this example we can see some of the syntax of Lwt where we define \code{heads}, a function that sleeps for 1 second and . . .

An other implementation, Async is an open source concurrency library for OCaml developed by Jane Street. Unlike LWT the . . .

```
\begin{lstlisting}[caption={Async example}]
open Jane.Std
open Async.Std

let heads = (after (sec 1.0) >>| fun () -> (print_endline "Heads"));;
let tails = (after (sec 2.0) >>| fun () -> (print_endline "Tails"));;
let head_and_tails = (Deferred.both
  heads
  tails);;

let () = upon (head_and_tails) (fun _ -> ());;

let () = never_returns (Scheduler.go ());;
\end{lstlisting}
```

In this snippet we define \code{heads} and \code{tails} as Deferred values of the respective code sequences. A Deferred . . .

There are a number of other experimental implementations for concurrency in OCaml, including JoCaml\cite{jocaml} that im . . .

\section{Semantics of concurrency}

There have been a lot of work on how exactly to formulate the semantics of concurrent and distributed systems. Some of the most

A monad\cite{hoareetal2001tackling} in functional programming is a construct to structure computations that are in some sense

Most monads support further operations and a concurrency monad is one such monad. Beside the two necessary operations (return

\section{Semantics to logic}

These semantics can be modelled in logic, in particular logics used by proof assistants. A model like this can be used for formal

\section{Logic to runnable code}

While a number of proof assistants have utilities for direct computation, in most cases semantics is described as a set of logic

\chapter{Preparation}

During the preparation phase of this project many decisions had to be made, including the concurrency model, large scale seman

\section{Design of concurrent semantics}

%Brief overview of techniques for concurrency

Concurrency may be modelled in many ways. A popular way of modelling concurrency is with a process calculus. A process calculu

\begin{itemize}

\item{ $P \mid Q$ for parallel composition where P and Q are processes}

\item{ $a.P$ for sequential composition where a is an atomic action and P is a process executed sequentially}

\item{ $!P$ for replication where P is a process and $!P \equiv P \mid !P$ }

\item{ $x \triangleleft y \triangleleft \cdot P$ and $x(v) \cdot Q$ for sending and receiving messages through channel x respectively}

\end{itemize}

%Process calculus ?

%Choices for concurrency semantics

This project aimed to have simple but powerful operational semantics. Simplicity is required in both the design and the interf

I focused on providing primitives for operations on processes including parallel and sequential composition and recursion. For

\section{Choice of implementation style}

%Why I chose continuation monads vs. World

A number of implementation styles of lightweight concurrency were surveyed for OCaml by Christophe Deleuze\cite{deleuzelight}.

Simplicity and similarity to current implementations like Lwt and Async were the two factors in the decision between these sty

\section{Design of monadic semantics}

Category theory has been a general tool used to model functional programming languages and programs. Monads are a concept orig

A monad on a category C is a triple (T, η, μ) where T is an endofunctor on C , that is, it maps the category

\begin{enumerate}

\item{

\[$\mu \circ T \mu = \mu \circ \mu \circ T$ \]

Or as commutative diagram:

```
\begin{center}
\begin{tikzcd}
T^3 \arrow{r}{T\mu} \arrow{d}[swap]{\mu T}
& T^2 \arrow{d}{\mu} \\
T^2 \arrow{r}[swap]{\mu} & T
\end{tikzcd}
\end{center}
```

This roughly demands that unwrapping from three layers to one is associative.

```
}
\item{
\[\mu \circ T\eta = \mu \circ \eta T = 1_T \]
```

Or as commutative diagram:

```
\begin{center}
\begin{tikzcd}
T \arrow{r}{\eta T} \arrow{d}[swap]{T \eta} \arrow[equal]{rd}
& T^2 \arrow{d}{\mu} \\
T^2 \arrow{r}[swap]{\mu} & T
\end{tikzcd}
\end{center}
```

This roughly translates to wrapping and then subsequently unwrapping behaves as an identity.

```
}
\end{enumerate}
```

This description entails three operations (lift, join and map) and their behaviour (associativity and identity), however

Most implementations go along the following lines: there is a parametric type $\text{con} \, \alpha$ where α

The `\lstineline|ret|` takes a value of the language and gives its monadic counterpart. With types this can be represented

The `\lstineline|bind|` (often written as $\text{gg} =$) takes a monadic value (that is one in the parametric type $\text{con} \, \alpha$)

To call this system a monad, we need to satisfy three axioms:

```
\begin{enumerate}
\item{\lstineline|ret| is essentially a left neutral element:
\[(\text{ret} \, \lambda x. \text{gg} \, \lambda f. f \, \text{ret} \, x) \equiv f \, x\]}
\item{\lstineline|ret| is essentially a right neutral element:
\[\text{gg} \, m \, \lambda f. f \, \text{ret} \, m \equiv m\]}
\item{\lstineline|bind| is associative:
\[(\text{gg} \, m \, \lambda f. \text{gg} \, (f \, m) \, \lambda g. g) \equiv \text{gg} \, m \, \lambda g. g\]}
\end{enumerate}
```

We will return to the exact nature of \equiv used in this project in the evaluation section and the exact form this

`\section{Tools}`

The project uses a chain of three tools: `\begin{enumerate}`

```
\item{
Ott, a tool for transforming informal, readable semantics to both LaTeX and formal proof assistant code.}
\item{Coq, a proof assistant supported by Ott. }
\item{OCaml, the target language. }
\end{enumerate}
```

```

\begin{figure}[h!]
\centering
\begin{tikzpicture}[node distance=1.8cm, auto, >=stealth',pil/.style={
    ->,
    thick,
    shorten <=2pt,
    shorten >=2pt,}, pildashed/.style={
    ->,
    thick,
    dashed,
    shorten <=2pt,
    shorten >=2pt,}, scale=1.2, every node/.style={scale=1.2}, ]
\node[draw, rectangle] (o) {Ott};
\node[right of=o] (otch) {};
\node[below of={otch}] (otc) {Generation}
    edge[pildashed] (otch);
\node[draw, rectangle, right of={otch}] (c) {Coq}
    edge[pil, <-] (o);
\node[right of=c] (ceoh) {};
\node[below of={ceoh}] (ceo) {Extraction}
    edge[pildashed] (ceoh);
\node[draw, rectangle, right of={ceoh}] (oc) {OCaml}
    edge[pil, <-] (c);

\end{tikzpicture}
\caption{Toolchain outline}
\end{figure}

```

In the preparation phase I got acquainted with all three of these systems, as I have not used them before for any serious work.

\subsection{Ott}

% Why Ott (because it is awesome)

To avoid duplication of the semantics in several formats I have chosen to use a supporting tool called Ott. It enables the

For someone familiar to formal semantics Ott has an easy to use and intuitive syntax.

Metavariables used in productions are defined with their destination language equivalents and potentially (in the case of Coq)

```

\begin{lstlisting}[language={Ott}, caption={Ott metavariable definition}]
metavar termvar, x ::= {{ com term variable }}
{{ isa string }} {{ coq nat }} {{ hol string }} {{ coq-equality }}
{{ ocaml int }} {{ lex alphanum }} {{ tex \mathit{[[termvar]] }}
\end{lstlisting}

```

Term expression grammars and other grammars can be defined in the well known Backus-Naur form with some extensions.

```

\begin{lstlisting}[language={Ott}, caption={Ott grammar example}]
grammar
t :: 't_' ::=
  | x          :: :: Var          {{ com variable }}
  | \ x . t    :: :: Lam (+ bind x in t +) {{ com lambda }}
  | t t'       :: :: App          {{ com app }}
  | ( t )      :: S:: Paren        {{ icho [[t]] }}
  | { t / x } t' :: M:: Tsub
                        {{ icho (tsubst_t [[t]] [[x]] [[t']) }}
\end{lstlisting}

```

In this example the non-terminal t for terms is defined with 5 productions: variables, lambda abstractions, applications, parens,

There are meta flags S and M to describe syntactical sugar and meta productions that are not generated as data structure elements.

In many languages one might want to define a value subgrammar, which can be used both in the reduction relation definition.

```
\begin{lstlisting}[language={Ott}, caption={Ott value subgrammar example}]
v :: 'v_' ::=                                {{ com value   }}
  | \ x . t      :: :: Lam                    {{ com lambda  }}
\end{lstlisting}
```

subrules

```
v <:: t
```

```
\end{lstlisting}
```

Here v is a subgrammar of t . The statement $v \text{ \$<::\$ } t$ is exported as a target language subroutine that checks whether this

Another common feature of semantics is substitution of values for variables, for example in function application. This is

```
\begin{lstlisting}[language={Ott}, caption={Ott substitution example}]
substitutions
  single t x :: tsubst
\end{lstlisting}
```

The statement `\stinline[language={Ott}]|single t x :: tsubst|` defines a single substitution function called `tsubst`.

Finally paramount to most semantics are relations like the reduction relation.

```
\begin{lstlisting}[language={Ott}, caption={Ott reduction relation example}]
```

```
defs
```

```
Jop :: '' ::=
```

```
defn
```

```
t1 --> t2 :: ::reduce::'' {{ com [[t1]] reduces to [[t2]]}} by
```

```
----- :: ax_app
```

```
(\x.t12) v2 --> {v2/x}t12
```

```
t1 --> t1'
```

```
----- :: ctx_app_fun
```

```
t1 t --> t1' t
```

```
t1 --> t1'
```

```
----- :: ctx_app_arg
```

```
v t1 --> v t1'
```

```
\end{lstlisting}
```

In this example I define a set of mutually recursive relations named `Jop` with one relation in it the `-->` or reduce relation.

```
\begin{lstlisting}[language={Ott}, caption={Ott single reduction}]
```

```
t1 --> t1'
```

```
----- :: ctx_app_fun
```

```
t1 t --> t1' t
```

```
\end{lstlisting}
```

The premise(s) appear line-by-line above the ascii-art line, while and the result below the line. Next to the line is the

```
\subsection{Coq}
```

% Brief overview of proof assistants, reason for the choice of Coq

There are a number of proof assistants available as destinations for Ott, out of which Coq and Isabelle provide good ext

Coq is formal proof assistant with a mathematical higher-level language called `\textit{Gallina}`, based around the Calcul

% Short guide to reading Coq

Objects in Coq can divided into two sorts, `\textit{Prop}` (propositions) and `\textit{Type}`. A proposition like `\forall`

```
\begin{lstlisting}[language={Coq},caption={Coq Prop logic example}]
forall A B : Prop, A /\ B -> B \/ B
\end{lstlisting}
```

Predicates like equality and other sets can be used as well

```
\begin{lstlisting}[language={Coq},caption={Coq Prop predicate example}]
forall x y : Z, x * y = 0 -> x = 0 \/ y = 0
\end{lstlisting}
```

New predicates can be defined inductively

```
\begin{lstlisting}[language={Coq},caption={Coq Prop new predicate example}]
Inductive even : N -> Prop :=
| even_0 : even 0
| even_S n : odd n -> even (n + 1)
with odd : N -> Prop :=
| odd_S n : even n -> odd (n + 1).
\end{lstlisting}
```

Data structures can also be defined both inductively and coinductively

```
\begin{lstlisting}[language={Coq},caption={Coq inductive data structure example}]
Inductive seq : nat -> Set :=
| niln : seq 0
| consn : forall n : nat, nat -> seq n -> seq (S n).
\end{lstlisting}
```

```
\begin{lstlisting}[language={Coq},caption={Coq coinductive data structure example}]
CoInductive stream (A:Type) : Type :=
| Cons : A -> stream -> stream.
\end{lstlisting}
```

Functions over these data structures are defined as fixpoints and cofixpoints respectively.

```
\begin{lstlisting}[language={Coq},caption={Coq fixpoint example}]
Fixpoint length (n : nat) (s : seq n) {struct s} : nat :=
  match s with
  | niln => 0
  | consn i _ s' => S (length i s')
  end.
\end{lstlisting}
```

Finally theorems can be proven with these propositions and structures.

```
\begin{minipage}{\linewidth}
\begin{lstlisting}[language={Coq},caption={Coq theorem example}]
Theorem length_corr : forall (n : nat) (s : seq n), length n s = n.
Proof.
  intros n s.

  (* reasoning by induction over s. Then, we have two new goals
     corresponding on the case analysis about s (either it is
     niln or some consn *)
  induction s.

  (* We are in the case where s is void. We can reduce the
     term: length 0 niln *)
  simpl.
```

```

(* We obtain the goal  $0 = 0$ . *)
trivial.

(* now, we treat the case  $s = \text{consn } n \ e \ s$  with induction
   hypothesis IHs *)
simpl.

(* The induction hypothesis has type  $\text{length } n \ s = n$ .
   So we can use it to perform some rewriting in the goal: *)
rewrite IHs.

(* Now the goal is the trivial equality:  $S \ n = S \ n$  *)
trivial.

(* Now all sub cases are closed, we perform the ultimate
   step: typing the term built using tactics and save it as
   a witness of the theorem. *)
Qed.

```

`\end{lstlisting}`

`\end{minipage}`

Each Lemma, Theorem, Example have a name and a statement. The statement is a proposition. This is followed by the proof.

% Methods of extraction

Coq also provides built in facilities for the certified extraction of code to OCaml, Haskell and Scheme. These can be in-

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={Coq to OCaml extraction of seq}]
type nat =
| 0
| S of nat

```

```

type seq =
| Niln
| Consn of nat * nat * seq
\end{lstlisting}
\end{minipage}

```

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={Coq to OCaml extraction of length}]
(** val length : nat -> seq -> nat **)

```

```

let rec length n = function
| Niln -> 0
| Consn (i, n0, s') -> S (length i s')
\end{lstlisting}
\end{minipage}

```

% Extraction plugin

Out of the box, Coq does not provide facilities for the extraction of so called logical inductive systems. These are ess-

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[language={Coq},caption={Coq logical inductive example}]
Inductive add : nat -> nat -> nat -> Prop :=
| add0 : forall n , add n 0 n

```

```
| addS : forall n m p, add n m p -> add n (S m) (S p).
\end{lstlisting}
\end{minipage}
```

However with the help of a plugin developed by David Delahaye, Catherine Dubois, Jean-Frédéric Etienne and Pierre-Nicola

```
\begin{minipage}{\linewidth}
\begin{lstlisting}[language={Coq},caption={Coq to OCaml extraction of a logical inductive relation}]
(** val add12 : nat -> nat -> nat **)

let rec add12 p1 p2 =
  match (p1, p2) with
  | (n, 0) -> n
  | (n, S m) ->
    (match add12 n m with
     | p -> S p
     | _ -> assert false (* *))
  | _ -> assert false (* *)
\end{lstlisting}
\end{minipage}
```

Most descriptions of reduction relations and indeed the output of Ott is of this kind, therefore this plugin helps with the ex

```
\subsection{OCaml}
% Brief overview of OCaml
OCaml is a high level programming language. It combines functional, object-oriented and imperative paradigms and used in large

OCaml, like many other functional languages support a wide range of features, from simple functions, to mutually recursive fun
\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml simple function example: square}]
let square x = x * x
\end{lstlisting}
\end{minipage}
```

```
\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml recursive function example: factorial}]
let rec fact x =
  if x <= 1 then 1 else x * fact (x - 1)
\end{lstlisting}
\end{minipage}
```

```
\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml complex function example: insertion sort}]
let rec sort = function
| [] -> []
| x :: l -> insert x (sort l)
and insert elem = function
| [] -> [elem]
| x :: l -> if elem < x then elem :: x :: l
           else x :: insert elem l
\end{lstlisting}
\end{minipage}
```

Furthermore, it was designed as a versatile, general purpose programming language. OCaml features include objects, modules, su


```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml imperative function example}]
let add_polynom p1 p2 =
  let n1 = Array.length p1
  and n2 = Array.length p2 in
  let result = Array.create (max n1 n2) 0 in
  for i = 0 to n1 - 1 do result.(i) <- p1.(i) done;
  for i = 0 to n2 - 1 do result.(i) <- result.(i) + p2.(i) done;
\end{lstlisting}
\end{minipage}

```

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml higher order functions example}]
let rec sigma f = function
| [] -> 0
| x :: l -> f x + sigma f l
\end{lstlisting}
\end{minipage}

```

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml data structure example}]
type expression =
| Num of int
| Var of string
| Let of string * expression * expression
| Binop of string * expression * expression
\end{lstlisting}
\end{minipage}

```

```

\begin{minipage}{\linewidth}
\begin{lstlisting}[caption={OCaml evaluation function example}]
let rec eval env = function
| Num i -> i
| Var x -> List.assoc x env
| Let (x, e1, in_e2) ->
  let val_x = eval env e1 in
  eval ((x, val_x) :: env) in_e2
| Binop (op, e1, e2) ->
  let v1 = eval env e1 in
  let v2 = eval env e2 in
  eval_op op v1 v2
and eval_op op v1 v2 =
  match op with
  | "+" -> v1 + v2
  | "-" -> v1 - v2
  | "*" -> v1 * v2
  | "/" -> v1 / v2
  | _ -> failwith ("Unknown operator: " ^ op)
\end{lstlisting}
\end{minipage}

```

```
% Short guide to reading OCaml
```

```

\cleardoublepage
\chapter{Implementation}
\section{The semantics}
\subsection{Expressions}
\subsubsection{Arrow types}

```

```

\subsection{Sum types}
\subsubsection{Product types}
\subsubsection{Fixpoint combinator}
\subsubsection{Monadic primitives}
The concurrency monad consists of a parametric type  $\alpha$ ,  $\text{con}$ , where  $\alpha$  is a type parameter describing
\begin{itemize}
\item{ret, also known as return. It has type  $\alpha \rightarrow \text{con}$  and simply evaluates its parameter}
\item{ $\gg$ , also known as bind, sequences two operations. The second argument is the continuation for the first parameter.}
\end{itemize}

\subsection{Fork}
The third operation is fork, which is the way to spawn new threads (two in this particular case). The approach taken in this work
Therefore the signature of fork is slightly more complicated

$$[\text{fork}] : \alpha \rightarrow \beta \rightarrow ((\alpha * \beta) \rightarrow \text{con})$$

\subsubsection{Computation placeholders}
\subsection{Transition system}
\subsubsection{Labelled transitions}
\subsubsection{Select operator}
\subsection{Type system}
\section{Proof assistant system}
\subsection{Outline of the proof assistant code}
\subsection{Modification}
\subsection{Extractable version}
\section{OCaml system}
\subsection{Outline of the OCaml code}
\subsection{Hand modifications and justifications}
\subsection{Sugar}

\cleardoublepage
\chapter{Evaluation}

\section{Theoretical evaluation}
Properties to evaluate: monadic laws, fork commutativity and associativity (liveness?), type preservation and progress?.

\subsection{Methods}
\subsubsection{Weak bisimilarity}
Intro to weak bisimilarity.

What form does a general weak bisimilarity proof take.

How does it appear here.
\subsection{Properties}
\subsubsection{Monadic laws}
\subsubsection{Fork commutativity}
Outline of fork commutativity
\subsubsection{Fork associativity}
\subsubsection{Liveness?}
\subsubsection{Type preservation?}
\subsubsection{Progress?}
%Theoretical evaluation
% - Monadic laws
% - Fork commutativity
% - Fork associativity (limited?)

```

```

% - Liveness ?
% - Type preservation ?
% - Progress

% Practical evaluation
\section{Practical evaluation}
Evaluation of speed and memory requirements absolutely and relative to implementations in LWT and Async.
\subsection{Methods}
\subsection{Examples}
\subsubsection{Kahn process network}
\subsubsection{Eratosthene Sieve}
\subsubsection{Concurrent sort}
%

\cleardoublepage
\chapter{Conclusion}

I hope that this rough guide to writing a dissertation is \LaTeX\ has
been helpful and saved you time.


\cleardoublepage

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% the bibliography

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%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
% the appendices
\appendix

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\section{proposal.tex}
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\section{propbody.tex}
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A.2 proposal.tex

A.3 propbody.tex

Appendix B

Makefile

B.1 Makefile

B.2 refs.bib

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}  
  
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  author = "Francesco Zappa Nardelli"  
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@MISC{Claessen99functionalpearls, author = {Koen Claessen}, title = {Functional Pearls: A Poor Man's Concurrency Monad},  
  
@article{deleuzelight,  
  title={Light Weight Concurrency in OCaml: Continuations, Monads, Promises, Events},  
  author={Deleuze, Christophe}  
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  title={Lwt: a cooperative thread library},
  author={Vouillon, J{\`e}r{\`o}me},
  booktitle={Proceedings of the 2008 ACM SIGPLAN workshop on ML},
  pages={3--12},
  year={2008},
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}

@MISC{OCamlLightWeb,
  title = {Ott, a tool for writing definitions of programming languages and calculi},
  howpublished = {\url{http://www.cl.cam.ac.uk/~so294/ocaml/}},
  year={2008}}

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  title={A sound semantics for OCaml light},
  author={Owens, Scott},
  booktitle={Programming Languages and Systems},
  pages={1--15},
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}

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  title={A mechanized bisimulation for the nu-calculus},
  author={Benton, Nick and Koutavas, Vasileios},
  journal={Higher-Order and Symbolic Computation (to appear, 2013)},
  year={2008}
}

@article{blazy2009mechanized,
  title={Mechanized semantics for the Clight subset of the C language},
  author={Blazy, Sandrine and Leroy, Xavier},
  journal={Journal of Automated Reasoning},
  volume={43},
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  pages={263--288},
  year={2009},
  publisher={Springer}
}

@incollection{blazy2006formal,
  title={Formal verification of a C compiler front-end},
  author={Blazy, Sandrine and Dargaye, Zaynah and Leroy, Xavier},
  booktitle={FM 2006: Formal Methods},
  pages={460--475},
  year={2006},
  publisher={Springer}
}

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  title={Formal verification of a realistic compiler},
  author={Leroy, Xavier},
  journal={Communications of the ACM},
  volume={52},
  number={7},

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    pages={107--115},
    year={2009},
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@incollection{letouzey2008extraction,
  title={Extraction in coq: An overview},
  author={Letouzey, Pierre},
  booktitle={Logic and Theory of Algorithms},
  pages={359--369},
  year={2008},
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  title={Program extraction from normalization proofs},
  author={Berger, Ulrich},
  booktitle={Typed Lambda Calculi and Applications},
  pages={91--106},
  year={1993},
  publisher={Springer}
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  title={A new extraction for Coq},
  author={Letouzey, Pierre},
  booktitle={Types for proofs and programs},
  pages={200--219},
  year={2003},
  publisher={Springer}
}

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  title={Extracting purely functional contents from logical inductive types},
  author={Delahaye, David and Dubois, Catherine and {\textbackslash}E{tienne, Jean-Fr{\textbackslash}e{d}{\textbackslash}e{ric}},
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  publisher={Springer}
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  title={JoCaml: A language for concurrent distributed and mobile programming},
  author={Fournet, C{\textbackslash}e{dric and Le Fessant, Fabrice and Maranget, Luc and Schmitt, Alan},
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  pages={129--158},
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  title={Shift to control},
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    year={2004}
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  title={Applications of continuations},
  author={Friedman, Daniel P},
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  year={1988}
}

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  title={Delimited control in OCaml, abstractly and concretely: System description},
  author={Kiselyov, Oleg},
  booktitle={Functional and Logic Programming},
  pages={304--320},
  year={2010},
  publisher={Springer}
}

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  title={Trapolined style},
  author={Ganz, Steven E and Friedman, Daniel P and Wand, Mitchell},
  booktitle={ACM SIGPLAN Notices},
  volume={34},
  number={9},
  pages={18--27},
  year={1999},
  organization={ACM}
}

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  title={Tackling the awkward squad: monadic input/output, concurrency, exceptions, and foreign-language calls in Haskell},
  author={Hoareetal, CAR},
  journal={Engineering theories of software construction},
  volume={180},
  pages={47},
  year={2001},
  publisher={IOS Press}
}

@book{liskov1988promises,
  title={Promises: linguistic support for efficient asynchronous procedure calls in distributed systems},
  author={Liskov, Barbara and Shriram, Liuba},
  volume={23},
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  author = {Gerd Stolpmann}
}

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    title={Relaxed-memory concurrency and verified compilation},
    author={{\`S}ev{\v{c}}ik, Jaroslav and Vafeiadis, Viktor and Zappa Nardelli, Francesco and Jagannathan, Suresh and Sew},
    booktitle={ACM SIGPLAN Notices},
    volume={46},
    number={1},
    pages={43--54},
    year={2011},
    organization={ACM}
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  title={A Machine-Checked, Type-Safe Model of Java Concurrency: Language, Virtual Machine, Memory Model, and Verified C},
  author={Lochbihler, Andreas},
  year={2012},
  publisher={KIT Scientific Publishing}
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  howpublished = {\url{https://www.lri.fr/~filliatr/functory/About.html}},
  urldate = {2014-03-20},
  author={Kalyanasundaram, Jean-Christophe Filli{\`a}tre K},
  year={2010}
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  author={Leroy, Xavier}
}

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  author = {Mandel, Louis and Maranget, Luc},
  year = {2007},
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  author={Delahaye, David and Dubois, Catherine and {\`E}tienne, Jean-Fr{\`e}d{\`e}ric},
  booktitle={Theorem Proving in Higher Order Logics},
  pages={70--85},
  year={2007},
  publisher={Springer}
}

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  booktitle={Certified Programs and Proofs},
  pages={76--91},
  year={2012},
  publisher={Springer}
}

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Appendix C

Project Proposal

C.1 Introduction of work to be undertaken

With the rise of ubiquitous multiple core systems it is necessary for a working programmer to use concurrency to the greatest extent. However concurrent code has never been easy to write as human reasoning is often poorly equipped with the tools necessary to think about such systems. That is why it is essential for a programming language to provide safe and sound primitives to tackle this problem.

My project aims to do this in the OCaml[3] language by developing a lightweight cooperating threading framework that holds correctness as a core value. The functional nature allows the use of one of the most recent trends in languages popular in academia, monads, to be used for a correct implementation.

There have been two very successful frameworks, LWT[2] and Async[28] that both provided the primitives for concurrent development in OCaml however neither is supported by a clear semantic description as their main focus was ease of use and speed.

C.2 Description of starting point

My personal starting points are the courses ML under Windows (IA), Semantics of Programming Languages (IB), Logic and Proof (IB) and Concepts in Programming Languages (IB). Furthermore I have done extracurricular reading into semantics and typing and attended the Denotational Semantics (II) course in the past year.

The preparatory research period has to include familiarising myself with OCaml and the chosen specification and proof assistant tools.

C.3 Substance and structure

The project will consist of first creating a formal specification for a simple monad that has three main operations `bind`, `return` and `choose`. The behaviour of these operations will be specified in a current semantics tool like `Lem`[1] or `Ott`[23].

As large amount of research has gone into both monadic concurrency and implementations in OCaml, the project will draw inspiration from Claessen[9], Deleuze[11] and Vouillon[30].

Some atomic, blocking operations will also be specified including reading and writing to a console prompt or file to better illustrate the concurrency properties and make testing and evaluation possible.

This theory driven executable specification will be paired by a hand implementation and will be thoroughly checked against each other to ensure that both adhere to the desired semantics.

Both of these implementations will be then compared against the two current frameworks for simplicity and speed on various test cases.

If time allows, an extension will also be carried out on the theorem prover version of the specification to formally verify that the implementation is correct.

C.4 Criteria

For the project to be deemed a success the following items must be successfully completed.

1. A specification for a monadic concurrency framework must be designed in the format of a semantics tool.
2. This specification needs to be exported to a proof assistant and has a runnable OCaml version
3. Test cases must be written that can thoroughly check a concurrency framework
4. A hand implementation needs to be designed, implemented and tested against the specification
5. The implementations must be compared to the frameworks LWT and Async based on speed
6. The dissertation must be planned and written

In case the extension will also become viable then its success criterion is that there is a clear formal verification accompanying the automated theorem prover version of the specification.

C.5 Timetable

The project will be split into two week packages

C.5.1 Week 1 and 2

Preparatory reading and research into tools that can be used for writing the specification and in the extension, the proofs. The tools of choice at the time of proposal are Ott for the specification step and Coq[4] as the proof assistant. Potentially a meeting arranged in the Computer Lab by an expert in using these tools.

Deliverable: Small example specifications to try out the tool chain, including SKI combinator calculus.

C.5.2 Week 3 and 4

Investigating the two current libraries and their design decisions and planning the necessary parts of specification. Identifying the test cases that are thorough and common in concurrent code.

Deliverable: A document describing the major design decisions of the two libraries, the difference in design of the specification and a set of test cases much like the ones used in OCaml Light [24, 5], but with a concurrency focus.

C.5.3 Week 5 and 6

Writing the specification and exporting to automated theorem provers and OCaml.

Deliverable: The specification document in the format of the semantics tool and exported in the formats of the proof assistant and OCaml.

C.5.4 Week 7 and 8

Hand implement a version that adheres to the specification and test it against the runnable semantics.

C.5.5 Week 9 and 10

Evaluating the implementations of the concurrency framework against LWT and Async. Writing up the halfway report.

Deliverable: Evaluation data and charts, the halfway report.

C.5.6 Week 11 and 12

If unexpected complexity occurs these two weeks can be used to compensate, otherwise starting on the verification proof in the proof assistant.

C.5.7 Week 13 and 14

If necessary adding more primitives (I/O, network) to test with, improving performance and finishing the verification proof. If time allows writing guide for future use of the framework.

C.5.8 Week 15 and 16

Combining all previously delivered documents as a starting point for the dissertation and doing any necessary further evaluation and extension. Creating the first, rough draft of the dissertation.

C.5.9 Week 17 and 18

Getting to the final structure but not necessarily final wording of the dissertation, acquiring all necessary graphs and charts, incorporating ongoing feedback from the supervisor.

C.5.10 Week 19 and 20

Finalising the dissertation and incorporating all feedback and polishing.

C.6 Resource Declaration

The project will need the following resources:

- MCS computer access that is provided for all projects
- The OCaml core libraries and compiler

- The LWT and Async libraries
- The Lem tool
- The Ott tool
- The use of my personal laptop, to work more efficiently

As my personal laptop is included a suitable back-up plan is necessary which will consist of the following:

- A backup to my personal Dropbox account
- A Git repository on Github
- Frequent backups (potentially remotely) to the MCS partition

My supervisor and on request my overseers will receive access to both the Dropbox account and Github repository to allow full transparency.