November 2, 2023

```
[1]: import numpy as np
     import sys
     import pdb
     from sklearn.neural_network import MLPClassifier
     from sklearn.metrics import classification_report, accuracy_score, f1_score
     import matplotlib.pyplot as plt
     from sklearn.preprocessing import OneHotEncoder
     import random
[2]: def get_data(x_path, y_path):
         Args:
             x_path: path to x file
             y_path: path to y file
         Returns:
             x: np array of [NUM_OF_SAMPLES x n]
             y: np array of [NUM_OF_SAMPLES]
         x = np.load(x_path)
         y = np.load(y_path)
         y = y.astype('float')
         x = x.astype('float')
         #normalize x:
         x = 2*(0.5 - x/255)
         return x, y
[3]: def get_metric(y_true, y_pred):
         Arqs:
             y_true: np array of [NUM_SAMPLES x r] (one hot)
                     or np array of [NUM_SAMPLES]
             y_pred: np array of [NUM_SAMPLES x r] (one hot)
                     or np array of [NUM_SAMPLES]
```

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```
results = classification_report(y_pred, y_true)
print(results)
```

Preparing the X_{train} , y_{train} , X_{test} , y_{test}

```
[5]: class NeuralNetwork:
         def __init__(self, n, n_hidden_nodes, r, M):
             #Number of nodes in the architecture
             self.n = n
             self.n_hidden_nodes = n_hidden_nodes
             self.r = r
             #Mini batch size
             self.M = M
             #Weights and biases
             self.W = dict()
             self.b = dict()
         def initialize_weights_and_biases(self):
             n_nodes = [self.n] + self.n_hidden_nodes + [self.r]
             #Initialize weights
             for i in range(1,len(n_nodes)):
                 self.W[str(i)] = np.random.uniform(low=-0.1, high=0.1,
      \Rightarrowsize=(n_nodes[i], n_nodes[i-1]))
```

```
#Initialize biases
       for i in range(1,len(n_nodes)):
           self.b[str(i)] = np.zeros((n_nodes[i],1))
   Ostaticmethod
   def sigmoid(x, derivative = False):
       if derivative == False:
           return 1 / (1 + np.exp(-x))
       else:
           return NeuralNetwork.sigmoid(x, derivative = False) * (1 -__
→NeuralNetwork.sigmoid(x, derivative = False))
   Ostaticmethod
   def relu(x, derivative = False):
       if derivative == True:
           return np.where(x > 0, 1, np.where(x < 0, 0, np.random.
→random_sample()))
       else:
           return np.where(x <= 0, 0, x)
   @staticmethod
   def softmax(Z):
       return np.exp(Z) / np.sum(np.exp(Z), axis=0)
   def train(self, X_train, y_train, epoch_mode = True, activation="sigmoid", __
⇒EPOCHS = 200, alpha = 0.01, stopping threshold = None,
→adaptive_learning=False, printafter=20):
       self.initialize_weights_and_biases()
       a = dict()
       z = dict()
       del_z = dict()
       del_b = dict()
       del_W = dict()
       if epoch_mode == True:
           for epoch in range(EPOCHS):
               for i in range(0, X_train.shape[0], self.M):
                   y_actual = y_train[i:i+self.M,:].T
                   #Forward
                   a["0"] = X_train[i:i+self.M,:].T
                   for j in range(1,len(self.n_hidden_nodes)+1):
                       z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + 
⇒self.b[str(j)]
```

```
if activation == "relu":
                             a[str(j)] = NeuralNetwork.relu(z[str(j)])
                        else:
                             a[str(j)] = NeuralNetwork.sigmoid(z[str(j)])
                    j += 1
                    z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + self.
\hookrightarrowb[str(j)]
                    a[str(j)] = NeuralNetwork.softmax(z[str(j)])
                    #Backward
                    del_z[str(j)] = a[str(j)] - y_actual
                    del_b[str(j)] = np.sum(del_z[str(j)], axis = 1).
\rightarrowreshape(-1,1)
                    del_W[str(j)] = np.matmul(del_z[str(j)], a[str(j-1)].T)
                    for k in range(j-1,0,-1):
                        if activation == "relu":
                             del_z[str(k)] = np.matmul(self.W[str(k+1)].T,__
\rightarrowdel_z[str(k+1)])*(NeuralNetwork.relu(z[str(k)], derivative=True))
                        else:
                             del_z[str(k)] = np.matmul(self.W[str(k+1)].T,__
→del_z[str(k+1)])*(NeuralNetwork.sigmoid(z[str(k)], derivative=True))
                        del_b[str(k)] = np.sum(del_z[str(k)], axis = 1).
\rightarrowreshape(-1,1)
                        del_W[str(k)] = np.matmul(del_z[str(k)], a[str(k-1)].T)
                    #Update
                    for 1 in range(1,len(self.n_hidden_nodes)+2):
                        if adaptive_learning == False:
                             self.W[str(1)] = self.W[str(1)] - alpha *_{\sqcup}
\rightarrowdel_W[str(1)]
                             self.b[str(1)] = self.b[str(1)] - alpha *_{\sqcup}
\rightarrowdel_b[str(1)]
                        else:
                             self.W[str(1)] = self.W[str(1)] - (alpha/np.
→sqrt(epoch)) * del_W[str(1)]
                             self.b[str(1)] = self.b[str(1)] - (alpha/np.
→sqrt(epoch)) * del_b[str(1)]
                y_pred, softmax_output = NN.predict(X_train,_
→activation=activation)
                softmax_loss = NeuralNetwork.
→compute_softmax_loss(softmax_output, y_train_onehot)
                if epoch%printafter==0:
                    print(f"epoch {epoch}")
```

```
print("accuracy on train data:⊔
→",accuracy_score(y_train_onehot, y_pred))
                    if adaptive_learning:
                        print("learning rate: ",(alpha/np.sqrt(epoch)))
                    print("softmax loss: ",softmax_loss)
                    print("\n")
       else:
           epoch = 1
           window = 5
           loss_avg = 0
           while(True):
               for i in range(0, X_train.shape[0], self.M):
                    y_actual = y_train[i:i+self.M,:].T
                    #Forward
                    a["0"] = X_train[i:i+self.M,:].T
                    for j in range(1,len(self.n_hidden_nodes)+1):
                        z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + 
⇒self.b[str(j)]
                        if activation == "relu":
                            a[str(j)] = NeuralNetwork.relu(z[str(j)])
                        else:
                            a[str(j)] = NeuralNetwork.sigmoid(z[str(j)])
                    i += 1
                    z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + self.
\rightarrowb[str(j)]
                    a[str(j)] = NeuralNetwork.softmax(z[str(j)])
                    #Backward
                    del_z[str(j)] = a[str(j)] - y_actual
                    del_b[str(j)] = np.sum(del_z[str(j)], axis = 1).
\rightarrowreshape(-1,1)
                    del_W[str(j)] = np.matmul(del_z[str(j)], a[str(j-1)].T)
                    for k in range(j-1,0,-1):
                        if activation == "relu":
                            del_z[str(k)] = np.matmul(self.W[str(k+1)].T,__
\rightarrowdel_z[str(k+1)])*(NeuralNetwork.relu(z[str(k)], derivative=True))
                            del_z[str(k)] = np.matmul(self.W[str(k+1)].T,__
→del_z[str(k+1)])*(NeuralNetwork.sigmoid(z[str(k)], derivative=True))
                        del_b[str(k)] = np.sum(del_z[str(k)], axis = 1).
\rightarrowreshape(-1,1)
```

```
del_W[str(k)] = np.matmul(del_z[str(k)], a[str(k-1)].T)
                    #Update
                   for 1 in range(1,len(self.n_hidden_nodes)+2):
                       if adaptive_learning == False:
                            self.W[str(1)] = self.W[str(1)] - alpha *_{\sqcup}
→del_W[str(1)]
                            self.b[str(1)] = self.b[str(1)] - alpha *_{\sqcup}
\rightarrowdel_b[str(1)]
                       else:
                            self.W[str(1)] = self.W[str(1)] - (alpha/np.
→sqrt(epoch)) * del_W[str(l)]
                            self.b[str(1)] = self.b[str(1)] - (alpha/np.
→sqrt(epoch)) * del_b[str(1)]
               y_pred, softmax_output = NN.predict(X_train,_
→activation=activation)
               softmax loss = NeuralNetwork.
→compute_softmax_loss(softmax_output, y_train_onehot)
               if epoch%printafter==0:
                   print(f"epoch {epoch}")
                   print("accuracy on train data:
→",accuracy_score(y_train_onehot, y_pred))
                   if adaptive_learning:
                       print("learning rate: ",(alpha/np.sqrt(epoch)))
                   print("softmax loss: ",softmax_loss)
                   print("\n")
               if epoch <= window:</pre>
                   loss_avg += softmax_loss
                   if epoch == window:
                       loss_avg /= window
               #End the training
               if epoch > window:
                   new loss avg = ((window - 1)*loss avg + softmax loss)/window
                   diff_avg_loss = abs(new_loss_avg - loss_avg)
                   #print("diff avg loss:",diff_avg_loss)
                   if diff_avg_loss < stopping_threshold or epoch > EPOCHS:
                       print("Convergence criteria satisfied!")
                       print(f"epoch {epoch}")
                       print("accuracy on train data:⊔
→",accuracy_score(y_train_onehot, y_pred))
                       if adaptive_learning:
                            print("learning rate: ",(alpha/np.sqrt(epoch)))
                       print("softmax loss: ",softmax_loss)
```

```
print("\n")
                              break
                      epoch += 1
          def predict(self, X_test, activation="sigmoid"):
              y_pred = np.zeros((X_test.shape[0], self.r))
              softmax_output = np.zeros((X_test.shape[0], self.r))
              z = dict()
              a = dict()
              for i in range(X_test.shape[0]):
                  a[str(0)] = X_test[i:i+1,:].T
                  for j in range(1,len(self.n_hidden_nodes)+1):
                      z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + self.
       →b[str(j)]
                      if activation == "relu":
                          a[str(j)] = NeuralNetwork.relu(z[str(j)])
                      else:
                          a[str(j)] = NeuralNetwork.sigmoid(z[str(j)])
                  j += 1
                  z[str(j)] = np.matmul(self.W[str(j)], a[str(j-1)]) + self.b[str(j)]
                  a[str(j)] = NeuralNetwork.softmax(z[str(j)])
                  softmax_output[i] = a[str(j)].flatten()
                  y_pred[i][np.argmax(a[str(j)])] = 1
              return y_pred, softmax_output
          Ostaticmethod
          def compute_softmax_loss(softmax_output, y_pred):
              #Softmax loss
              sm loss = 0
              for i in range(y_pred.shape[0]):
                  sm_loss = -1*np.log2(softmax_output[i][np.argmax(y_pred[i])])
              return sm_loss/(y_pred.shape[0])
[28]: NN = NeuralNetwork(n = 1024, n hidden nodes = [100,50], r = 5, M = 32)
      NN.train(X_train, y_train_onehot, activation="sigmoid", EPOCHS=100, alpha=0.
      \rightarrow001, printafter=10)
      y_pred, softmax_output = NN.predict(X_test, activation="sigmoid")
```

print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred))

get_metric(y_test_onehot, y_pred)

epoch 0

accuracy on train data: 0.2091

softmax loss: 0.00023525478839202835

epoch 10

accuracy on train data: 0.5923

softmax loss: 0.00011264389363753989

epoch 20

accuracy on train data: 0.6572 softmax loss: 5.831073565883006e-05

epoch 30

accuracy on train data: 0.6702 softmax loss: 4.656056662492289e-05

epoch 40

accuracy on train data: 0.6758

softmax loss: 3.9645451044889796e-05

epoch 50

accuracy on train data: 0.6803

softmax loss: 3.4488996828750714e-05

epoch 60

accuracy on train data: 0.6869

softmax loss: 3.0593861550354343e-05

epoch 70

accuracy on train data: 0.6908

softmax loss: 2.8066258449785907e-05

epoch 80

accuracy on train data: 0.6976

softmax loss: 2.7373041902283903e-05

epoch 90

accuracy on train data: 0.7037

softmax loss: 2.8412086233645623e-05

```
accuracy on test data: 0.714
                           recall f1-score
              precision
                                               support
           0
                   0.93
                             0.95
                                        0.94
                                                   224
           1
                   0.75
                             0.76
                                        0.76
                                                   196
                   0.56
                             0.64
                                        0.60
                                                   176
           3
                   0.49
                             0.52
                                        0.51
                                                   177
           4
                   0.80
                             0.66
                                        0.72
                                                   227
                   0.71
                             0.71
                                        0.71
                                                  1000
  micro avg
                   0.71
                             0.70
                                        0.70
                                                  1000
  macro avg
                                        0.72
                   0.72
                             0.71
                                                  1000
weighted avg
samples avg
                   0.71
                             0.71
                                        0.71
                                                  1000
```

```
[34]: print("f1_score: ",f1_score(y_test_onehot, y_pred, average="macro"))
```

f1_score: 0.7029924239467376

Experimenting with single hidden layer

```
[41]: hidden_layers = [[1],[5],[10],[50],[100]]
      number_of_hidden_units = [1,5,10,50,100]
      f1_score_train = []
      f1_score_test = []
      for hidden_layer in hidden_layers:
          print(f"Hidden layer: {hidden_layer}")
          NN = NeuralNetwork(n = 1024, n_hidden_nodes = hidden_layer, r = 5, M = 32)
          NN.train(X_train, y_train_onehot, epoch_mode= False, activation="sigmoid", __
       →alpha = 0.01, stopping_threshold = 1.0e-06, printafter=50)
          y_pred_train, _ = NN.predict(X_train)
          y_pred_test, _ = NN.predict(X_test)
          print("accuracy on train data: ",accuracy_score(y_train_onehot,_
       →y_pred_train))
          print("metrics for train data: ")
          get_metric(y_train_onehot, y_pred_train)
          f1_score_train.append(f1_score(y_train_onehot, y_pred_train,_
       →average="macro"))
          print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
          print("metrics for test data: ")
          get_metric(y_test_onehot, y_pred_test)
          f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
          print("\n")
```

Hidden layer: [1]

epoch 50

accuracy on train data: 0.4706

softmax loss: 0.00014958531153011078

epoch 100

accuracy on train data: 0.2091

softmax loss: 0.00023287816358262217

epoch 150

accuracy on train data: 0.2091 softmax loss: 0.0002328781641601466

epoch 200

accuracy on train data: 0.2091

softmax loss: 0.00023287816494873916

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.2091

softmax loss: 0.00023287816496746151

accuracy on train data: 0.2091

metrics for train data:

		precision	recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.21	0.35	10000
micro	avg	0.21	0.21	0.21	10000
macro	avg	0.20	0.04	0.07	10000
weighted	avg	1.00	0.21	0.35	10000
samples	avg	0.21	0.21	0.21	10000

accuracy on test data: 0.187

metrics for test data:

precision		recall	f1-score	support
0	0.00	0.00	0.00	0
1	0.00	0.00	0.00	0

	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.19	0.32	1000
micro	avg	0.19	0.19	0.19	1000
macro	avg	0.20	0.04	0.06	1000
weighted	avg	1.00	0.19	0.32	1000
samples	avg	0.19	0.19	0.19	1000

Hidden layer: [5]

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

epoch 50

accuracy on train data: 0.6775

softmax loss: 5.1494534443521053e-05

epoch 100

accuracy on train data: 0.6858 softmax loss: 3.220427274554847e-05

epoch 150

accuracy on train data: 0.6952

softmax loss: 2.7774495226855474e-05

epoch 200

accuracy on train data: 0.6982 softmax loss: 2.603425353508207e-05

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.6977

softmax loss: 2.6049241749681784e-05

accuracy on train data: 0.6977

metrics for train data:

		precision	recall	f1-score	support
	0	0.95	0.86	0.90	2176
	1	0.64	0.77	0.70	1652
	2	0.73	0.56	0.63	2544
	3	0.41	0.56	0.47	1447
	4	0.77	0.73	0.75	2181
micro	avg	0.70	0.70	0.70	10000
macro	avg	0.70	0.70	0.69	10000
weighted	avg	0.72	0.70	0.70	10000
samples	avg	0.70	0.70	0.70	10000

accuracy on test data: 0.689

metrics for test data:

		precision	recall	f1-score	support
	0	0.94	0.87	0.91	246
	1	0.63	0.76	0.69	163
	2	0.72	0.58	0.64	248
	3	0.41	0.49	0.45	158
	4	0.69	0.70	0.69	185
micro	avg	0.69	0.69	0.69	1000
macro	avg	0.68	0.68	0.68	1000
weighted	avg	0.71	0.69	0.69	1000
samples	avg	0.69	0.69	0.69	1000

Hidden layer: [10]

epoch 50

accuracy on train data: 0.6885

softmax loss: 2.3303944233466556e-05

epoch 100

accuracy on train data: 0.7189

softmax loss: 2.3564423526932722e-05

epoch 150

accuracy on train data: 0.7241 softmax loss: 2.151708934034692e-05

epoch 200

accuracy on train data: 0.7438

softmax loss: 1.7535741967859166e-05

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.7436

softmax loss: 1.7259669594328303e-05

accuracy on train data: 0.7436

metrics for train data:

		precision	recall	f1-score	support
	0	0.93	0.95	0.94	1930
	1 2	0.75 0.67	0.81 0.66	0.78 0.66	1852 2000
	3 4	0.51 0.85	0.59 0.72	0.55 0.78	1752 2466
	4	0.65	0.72	0.76	2400
micro	avg	0.74	0.74	0.74	10000
macro	avg	0.74	0.74	0.74	10000
weighted	avg	0.75	0.74	0.75	10000
samples	avg	0.74	0.74	0.74	10000

accuracy on test data: 0.724

metrics for test data:

		precision	recall	f1-score	support
	0	0.89	0.96	0.92	212
	1	0.73	0.76	0.75	191
	2	0.65	0.64	0.65	204
	3	0.51	0.55	0.53	175
	4	0.80	0.69	0.74	218
micro	avg	0.72	0.72	0.72	1000
macro	avg	0.72	0.72	0.72	1000
weighted	avg	0.73	0.72	0.72	1000
samples	avg	0.72	0.72	0.72	1000

Hidden layer: [50]

epoch 50

accuracy on train data: 0.7392

softmax loss: 2.6987471937410535e-05

epoch 100

accuracy on train data: 0.7839

softmax loss: 1.7227472892700306e-05

epoch 150

accuracy on train data: 0.7706

softmax loss: 1.6560629492585795e-05

epoch 200

accuracy on train data: 0.7877 softmax loss: 8.237749203355322e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.788

softmax loss: 7.399416514018198e-06

accuracy on train data: 0.788

metrics for train data:

		precision	recall	f1-score	support
	0 1 2 3	0.94 0.79 0.64 0.65	0.98 0.88 0.72 0.62	0.96 0.84 0.68 0.64	1878 1783 1734 2106
	4	0.91	0.76	0.83	2499
micro	avg	0.79	0.79	0.79	10000
macro	avg	0.79	0.79	0.79	10000
weighted	avg	0.79	0.79	0.79	10000
samples	avg	0.79	0.79	0.79	10000

accuracy on test data: 0.735

metrics for test data:

	precision	recall	f1-score	support
0	0.93	1.00	0.96	215
1	0.76	0.82	0.79	183
2	0.55	0.65	0.60	168
3	0.63	0.52	0.57	229
4	0.76	0.70	0.73	205

micro	avg	0.73	0.73	0.73	1000
macro	avg	0.73	0.74	0.73	1000
weighted	avg	0.73	0.73	0.73	1000
samples	avg	0.73	0.73	0.73	1000

Hidden layer: [100]

epoch 50

accuracy on train data: 0.733

softmax loss: 4.538836493085465e-05

epoch 100

accuracy on train data: 0.7818

softmax loss: 1.8238639023683118e-05

epoch 150

accuracy on train data: 0.8035 softmax loss: 9.2365944713612e-06

epoch 200

accuracy on train data: 0.8139 softmax loss: 9.666839084236848e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.8133 softmax loss: 9.72563184360032e-06

accuracy on train data: 0.8133

		precision	recall	f1-score	support
	0	0.98	0.96	0.97	2010
	1	0.82	0.92	0.87	1766
	2	0.74	0.77	0.75	1883
	3	0.64	0.67	0.65	1914
	4	0.88	0.76	0.82	2427
micro	avg	0.81	0.81	0.81	10000
macro	avg	0.81	0.82	0.81	10000
weighted	avg	0.82	0.81	0.81	10000
samples	avg	0.81	0.81	0.81	10000

```
accuracy on test data: 0.77
metrics for test data:
              precision
                           recall f1-score
                                               support
           0
                   0.97
                             0.97
                                        0.97
                                                   228
           1
                   0.74
                             0.84
                                        0.79
                                                   174
           2
                   0.65
                             0.68
                                        0.67
                                                   191
           3
                   0.63
                             0.59
                                        0.61
                                                   197
           4
                   0.82
                             0.73
                                        0.78
                                                   210
  micro avg
                   0.77
                             0.77
                                        0.77
                                                  1000
                   0.76
                             0.77
                                        0.76
                                                  1000
  macro avg
                                        0.77
                                                  1000
weighted avg
                   0.77
                             0.77
 samples avg
                   0.77
                             0.77
                                        0.77
                                                  1000
```



Experimenting with hidden layers

```
[44]: hidden layers = [[512], [512,256], [512,256,128], [512,256,128,64]]
      network_depth = [1,2,3,4]
      f1 score train = []
      f1_score_test = []
      for hidden_layer in hidden_layers:
          print(f"Hidden layer: {hidden_layer}")
          NN = NeuralNetwork(n = 1024, n_hidden_nodes = hidden_layer , r = 5, M = 32)
          NN.train(X_train, y_train_onehot, epoch_mode= False, activation="sigmoid", __
       →alpha = 0.01, stopping_threshold = 1.0e-06, printafter=50)
          y_pred_train, _ = NN.predict(X_train)
          y_pred_test, _ = NN.predict(X_test)
          print("accuracy on train data: ",accuracy_score(y_train_onehot,__
       →y_pred_train))
          print("metrics for train data: ")
          get_metric(y_train_onehot, y_pred_train)
          f1_score_train.append(f1_score(y_train_onehot, y_pred_train,_
       →average="macro"))
          print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
          print("metrics for test data: ")
          get_metric(y_test_onehot, y_pred_test)
          f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
          print("\n")
```

Hidden layer: [512]

epoch 50

accuracy on train data: 0.7327

softmax loss: 3.9801766116042114e-05

epoch 100

accuracy on train data: 0.7921 softmax loss: 5.780218764128989e-06

epoch 150

accuracy on train data: 0.8118

softmax loss: 3.7589816123345803e-06

epoch 200

accuracy on train data: 0.8299

softmax loss: 1.2992431023633802e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.831

softmax loss: 1.239104246690159e-06

accuracy on train data: 0.831

metrics for train data:

		precision	recall	f1-score	support
	0	0.97	0.99	0.98	1933
	1	0.87	0.92	0.89	1863
	2	0.70	0.82	0.75	1669
	3	0.75	0.66	0.70	2286
	4	0.87	0.81	0.84	2249
micro	avg	0.83	0.83	0.83	10000
macro	avg	0.83	0.84	0.83	10000
${\tt weighted}$	avg	0.83	0.83	0.83	10000
samples	avg	0.83	0.83	0.83	10000

accuracy on test data: 0.782

metrics for test data:

support	f1-score	recall	precision	
223	0.98	0.99	0.97	0
181	0.84	0.88	0.81	1

	2	0.58	0.72	0.64	162
	3	0.73	0.56	0.64	241
	4	0.80	0.77	0.78	193
micro	avg	0.78	0.78	0.78	1000
macro	avg	0.78	0.79	0.78	1000
weighted	avg	0.78	0.78	0.78	1000
samples	avg	0.78	0.78	0.78	1000

Hidden layer: [512, 256]

epoch 50

accuracy on train data: 0.7299

softmax loss: 2.5517614437811225e-05

epoch 100

accuracy on train data: 0.7836 softmax loss: 6.656917643055116e-06

epoch 150

accuracy on train data: 0.8126 softmax loss: 5.07376437203254e-06

epoch 200

accuracy on train data: 0.8213 softmax loss: 6.25927649641769e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.8206 softmax loss: 6.134507568326737e-06

accuracy on train data: 0.8206

	precision	recall	f1-score	support
0	0.97	0.99	0.98	1943
1	0.91	0.90	0.90	1997
2	0.71	0.83	0.76	1661
3	0.58	0.68	0.63	1733
4	0.93	0.73	0.82	2666

micro	avg	0.82	0.82	0.82	10000
macro	avg	0.82	0.82	0.82	10000
weighted	avg	0.84	0.82	0.82	10000
samples	avg	0.82	0.82	0.82	10000

accuracy on test data: 0.78

metrics for test data:

		precision	recall	f1-score	support
	0	0.98	0.99	0.98	226
	1	0.88	0.84	0.86	206
	2	0.59	0.76	0.66	154
	3	0.57	0.57	0.57	186
	4	0.85	0.70	0.77	228
micro	avg	0.78	0.78	0.78	1000
macro	avg	0.77	0.77	0.77	1000
weighted	avg	0.79	0.78	0.78	1000
samples	avg	0.78	0.78	0.78	1000

Hidden layer: [512, 256, 128]

epoch 50

accuracy on train data: 0.7228 softmax loss: 3.62084087252217e-05

epoch 100

accuracy on train data: 0.7799 softmax loss: 1.917585498575037e-05

epoch 150

accuracy on train data: 0.8019 softmax loss: 1.001024824261873e-05

epoch 200

accuracy on train data: 0.8182 softmax loss: 5.357968292509009e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.8138 softmax loss: 6.170754618629236e-06

accuracy on train data: 0.8138

metrics for train data:

		precision	recall	f1-score	support
	0	0.99	0.98 0.94	0.99	1996 1853
	2	0.68	0.80	0.74	1651
	3	0.58	0.64	0.61	1809
	4	0.94	0.73	0.82	2691
micro	avg	0.81	0.81	0.81	10000
macro	avg	0.81	0.82	0.81	10000
weighted	avg	0.83	0.81	0.82	10000
samples	avg	0.81	0.81	0.81	10000

accuracy on test data: 0.778

metrics for test data:

		precision	recall	f1-score	support
	0	1.00	0.99	0.99	230
	1	0.82	0.89	0.85	182
	2	0.58	0.72	0.65	160
	3	0.60	0.56	0.58	201
	4	0.86	0.70	0.77	227
micro	avg	0.78	0.78	0.78	1000
macro	avg	0.77	0.77	0.77	1000
weighted	avg	0.79	0.78	0.78	1000
samples	avg	0.78	0.78	0.78	1000

Hidden layer: [512, 256, 128, 64] Convergence criteria satisfied!

epoch 25

accuracy on train data: 0.2091 softmax loss: 0.0002359463199165115

accuracy on train data: 0.2091

	precision	recall	f1-score	support
0	0.00	0.00	0.00	0
1	0.00	0.00	0.00	0
2	0.00	0.00	0.00	0
3	0.00	0.00	0.00	0

	4	1.00	0.21	0.35	10000
		2 24	0.04	0.04	
micro	avg	0.21	0.21	0.21	10000
macro	avg	0.20	0.04	0.07	10000
weighted	avg	1.00	0.21	0.35	10000
samples	avg	0.21	0.21	0.21	10000

accuracy on test data: 0.187

metrics for test data:

	precision		recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.19	0.32	1000
micro	avg	0.19	0.19	0.19	1000
macro	avg	0.20	0.04	0.06	1000
weighted	avg	1.00	0.19	0.32	1000
samples	avg	0.19	0.19	0.19	1000

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

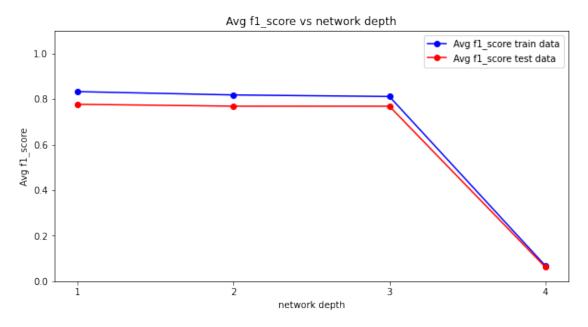
_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

```
plt.legend()
plt.show()
```



Adaptive learning

```
[46]: hidden_layers = [[512], [512,256], [512,256,128], [512,256,128,64]]
      network_depth = [1,2,3,4]
      f1_score_train = []
      f1_score_test = []
      for hidden_layer in hidden_layers:
          print(f"Hidden layer: {hidden layer}")
          NN = NeuralNetwork(n = 1024, n_hidden_nodes = hidden_layer, r = 5, M = 32)
          NN.train(X_train, y_train_onehot, epoch_mode= False, activation="sigmoid", __
       →adaptive_learning = True, alpha = 0.01, stopping_threshold = 5.0e-06, □
       →printafter=50)
          y_pred_train, _ = NN.predict(X_train)
          y_pred_test, _ = NN.predict(X_test)
          print("accuracy on train data: ",accuracy_score(y_train_onehot,_
       →y_pred_train))
          print("metrics for train data: ")
          get_metric(y_train_onehot, y_pred_train)
          f1_score_train.append(f1_score(y_train_onehot, y_pred_train,__
       →average="macro"))
          print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
          print("metrics for test data: ")
```

get_metric(y_test_onehot, y_pred_test)
f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
print("\n")

Hidden layer: [512]

epoch 50

accuracy on train data: 0.701 learning rate: 0.001414213562373095 softmax loss: 2.4384530256167004e-05

epoch 100

accuracy on train data: 0.7294

learning rate: 0.001

softmax loss: 2.2590405138106635e-05

epoch 150

accuracy on train data: 0.7535

learning rate: 0.0008164965809277261
softmax loss: 2.4823077935786723e-05

epoch 200

accuracy on train data: 0.7701

learning rate: 0.0007071067811865475
softmax loss: 2.5202653816610038e-05

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.7705

learning rate: 0.0007053456158585983
softmax loss: 2.518159706339217e-05

accuracy on train data: 0.7705

	precision	recall	f1-score	${ t support}$
0	0.97	0.94	0.95	2031
1	0.81	0.83	0.82	1937
2	0.65	0.70	0.68	1809
3	0.57	0.62	0.59	1849
4	0.85	0.75	0.80	2374

micro	avg	0.77	0.77	0.77	10000
macro	avg	0.77	0.77	0.77	10000
weighted	avg	0.78	0.77	0.77	10000
samples	avg	0.77	0.77	0.77	10000

accuracy on test data: 0.769

metrics for test data:

		precision	recall	f1-score	support
	•	0.07	0.00	0.00	000
	0	0.97	0.96	0.96	232
	1	0.80	0.81	0.81	194
	2	0.61	0.69	0.65	176
	3	0.63	0.59	0.61	199
	4	0.80	0.75	0.77	199
micro	avg	0.77	0.77	0.77	1000
macro	avg	0.76	0.76	0.76	1000
weighted	avg	0.77	0.77	0.77	1000
samples	avg	0.77	0.77	0.77	1000

Hidden layer: [512, 256]

epoch 50

accuracy on train data: 0.6913 learning rate: 0.001414213562373095 softmax loss: 2.829604797009096e-05

epoch 100

accuracy on train data: 0.7283

learning rate: 0.001

softmax loss: 2.5478154341155774e-05

epoch 150

accuracy on train data: 0.7609

learning rate: 0.0008164965809277261
softmax loss: 3.3394030775105174e-05

epoch 200

accuracy on train data: 0.7788

learning rate: 0.0007071067811865475
softmax loss: 2.511949838152347e-05

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.779

learning rate: 0.0007053456158585983
softmax loss: 2.4884937458219116e-05

accuracy on train data: 0.779

metrics for train data:

		precision	recall	f1-score	support
	0 1 2 3 4	0.98 0.84 0.66 0.56 0.85	0.96 0.86 0.72 0.61 0.74	0.97 0.85 0.69 0.58 0.79	1996 1951 1801 1850 2402
micro	•	0.78	0.78	0.78	10000
macro weighted samples	avg	0.78 0.79 0.78	0.78 0.78 0.78	0.78 0.78 0.78	10000 10000 10000

accuracy on test data: 0.78

metrics for test data:

		precision	recall	f1-score	support
	0 1 2 3	0.97 0.83 0.63 0.62	0.98 0.83 0.71 0.60	0.98 0.83 0.67 0.61	228 199 177 193
	4	0.80	0.74	0.77	203
micro macro	•	0.78 0.77	0.78 0.77	0.78 0.77	1000 1000
weighted samples	_	0.78 0.78	0.78 0.78	0.78 0.78	1000 1000

Hidden layer: [512, 256, 128]

epoch 50

accuracy on train data: 0.6908 learning rate: 0.001414213562373095 softmax loss: 2.5470862546841987e-05

epoch 100

accuracy on train data: 0.734

learning rate: 0.001

softmax loss: 3.018135410329875e-05

epoch 150

accuracy on train data: 0.7671

learning rate: 0.0008164965809277261 softmax loss: 3.57361083756996e-05

epoch 200

accuracy on train data: 0.7839

learning rate: 0.0007071067811865475
softmax loss: 1.8145684474911947e-05

 ${\tt Convergence\ criteria\ satisfied!}$

epoch 201

accuracy on train data: 0.7838

learning rate: 0.0007053456158585983 softmax loss: 1.784769632453523e-05

accuracy on train data: 0.7838

metrics for train data:

		precision	recall	f1-score	support
	0 1 2 3 4	0.98 0.85 0.70 0.54 0.85	0.97 0.87 0.72 0.62 0.73	0.98 0.86 0.71 0.58 0.79	1991 1923 1914 1762 2410
micro macro weighted samples	avg avg	0.78 0.78 0.79 0.78	0.78 0.78 0.78 0.78	0.78 0.78 0.79 0.78	10000 10000 10000 10000

accuracy on test data: 0.783

metrics for test data:

	precision	recall	f1-score	support
0	0.99	0.99	0.99	229
1	0.83	0.85	0.84	194
2	0.68	0.71	0.70	192
3	0.57	0.60	0.58	176
4	0.80	0.72	0.76	209
micro avg	0.78	0.78	0.78	1000

macro avg	0.77	0.77	0.77	1000
weighted avg	0.79	0.78	0.78	1000
samples avg	0.78	0.78	0.78	1000

Hidden layer: [512, 256, 128, 64] Convergence criteria satisfied!

epoch 6

accuracy on train data: 0.2091 learning rate: 0.004082482904638631 softmax loss: 0.000232068269599483

accuracy on train data: 0.2091

metrics for train data:

		precision	recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.21	0.35	10000
micro	avg	0.21	0.21	0.21	10000
macro	avg	0.20	0.04	0.07	10000
weighted	avg	1.00	0.21	0.35	10000
samples	avg	0.21	0.21	0.21	10000

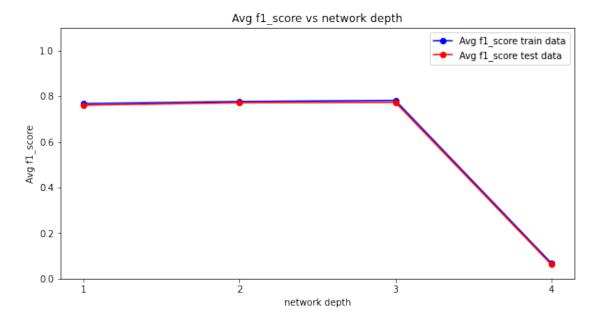
accuracy on test data: 0.187

metrics for test data:

		precision	recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.19	0.32	1000
micro	avg	0.19	0.19	0.19	1000
macro	avg	0.20	0.04	0.06	1000
weighted	avg	1.00	0.19	0.32	1000
samples	avg	0.19	0.19	0.19	1000

/home/tkarthikeyan/.local/lib/python3.8/site-

```
packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall
and F-score are ill-defined and being set to 0.0 in labels with no true samples.
Use `zero_division` parameter to control this behavior.
   _warn_prf(average, modifier, msg_start, len(result))
/home/tkarthikeyan/.local/lib/python3.8/site-
packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall
and F-score are ill-defined and being set to 0.0 in labels with no true samples.
Use `zero_division` parameter to control this behavior.
   _warn_prf(average, modifier, msg_start, len(result))
```



Relu activation function

```
[48]: hidden layers = [[512], [512,256], [512,256,128], [512,256,128,64]]
      network_depth = [1,2,3,4]
      f1_score_train = []
      f1_score_test = []
      for hidden_layer in hidden_layers:
          print(f"Hidden layer: {hidden_layer}")
          NN = NeuralNetwork(n = 1024, n_hidden_nodes = hidden_layer , r = 5, M = 32)
          NN.train(X_train, y_train_onehot, epoch_mode= False, activation="relu", u
       →adaptive_learning = True, alpha = 0.01, stopping_threshold = 5.0e-06, __
       ⇒printafter=50)
          y_pred_train, _ = NN.predict(X_train, activation="relu")
          y_pred_test, _ = NN.predict(X_test, activation="relu")
          print("accuracy on train data: ",accuracy_score(y_train_onehot,_
       →y_pred_train))
          print("metrics for train data: ")
          get_metric(y_train_onehot, y_pred_train)
          f1_score_train.append(f1_score(y_train_onehot, y_pred_train,_
       →average="macro"))
          print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
          print("metrics for test data: ")
          get_metric(y_test_onehot, y_pred_test)
          f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
          print("\n")
     Hidden layer: [512]
     Convergence criteria satisfied!
     accuracy on train data: 0.2091
     learning rate: 0.004082482904638631
     softmax loss: 0.00023208783009197323
     accuracy on train data: 0.2091
     metrics for train data:
                   precision
                              recall f1-score
                                                   support
                0
                        0.00
                                  0.00
                                            0.00
                                                         0
                1
                        0.00
                                  0.00
                                            0.00
                                                         0
                2
                        0.00
                                  0.00
                                            0.00
                                                         0
                3
                        0.00
                                  0.00
                                            0.00
                                                         0
                        1.00
                                  0.21
                                            0.35
                                                      10000
                                  0.21
                                            0.21
        micro avg
                        0.21
                                                      10000
        macro avg
                        0.20
                                  0.04
                                            0.07
                                                      10000
```

weighted avg	1.00	0.21	0.35	10000
samples avg	0.21	0.21	0.21	10000

accuracy on test data: 0.187

metrics for test data:

		precision	recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.19	0.32	1000
micro	avg	0.19	0.19	0.19	1000
macro	avg	0.20	0.04	0.06	1000
weighted	avg	1.00	0.19	0.32	1000
samples	avg	0.19	0.19	0.19	1000

Hidden layer: [512, 256]

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

Convergence criteria satisfied!

epoch 6

accuracy on train data: 0.2091 learning rate: 0.004082482904638631 softmax loss: 0.00023044619233218206

accuracy on train data: 0.2091

	precision	recall	f1-score	support
0	0.00	0.00	0.00	0
1	0.00	0.00	0.00	0
2	0.00	0.00	0.00	0
3	0.00	0.00	0.00	0
4	1.00	0.21	0.35	10000

micro	avg	0.21	0.21	0.21	10000
macro	avg	0.20	0.04	0.07	10000
weighted	avg	1.00	0.21	0.35	10000
samples	avg	0.21	0.21	0.21	10000

accuracy on test data: 0.187

metrics for test data:

		precision	recall	f1-score	support
	0	0.00	0.00	0.00	0
	1	0.00	0.00	0.00	0
	2	0.00	0.00	0.00	0
	3	0.00	0.00	0.00	0
	4	1.00	0.19	0.32	1000
micro	avg	0.19	0.19	0.19	1000
macro	avg	0.20	0.04	0.06	1000
weighted	avg	1.00	0.19	0.32	1000
samples	avg	0.19	0.19	0.19	1000

Hidden layer: [512, 256, 128]

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

epoch 50

accuracy on train data: 0.7289 learning rate: 0.001414213562373095 softmax loss: 3.145936113878991e-05

epoch 100

accuracy on train data: 0.7583

learning rate: 0.001

softmax loss: 3.272657747861718e-05

epoch 150

accuracy on train data: 0.7812

learning rate: 0.0008164965809277261
softmax loss: 1.1503443467968143e-05

epoch 200

accuracy on train data: 0.7962

learning rate: 0.0007071067811865475
softmax loss: 1.7943773712320744e-06

 ${\tt Convergence\ criteria\ satisfied!}$

epoch 201

accuracy on train data: 0.8045

learning rate: 0.0007053456158585983
softmax loss: 2.1482919875104044e-06

accuracy on train data: 0.8045

metrics for train data:

		precision	recall	f1-score	support
		precision	recarr	II SCOLE	Support
	0	0.98	0.99	0.99	1966
	1	0.87	0.93	0.90	1845
	2	0.66	0.80	0.72	1624
	3	0.59	0.61	0.60	1932
	4	0.91	0.72	0.80	2633
micro	avg	0.80	0.80	0.80	10000
macro	avg	0.80	0.81	0.80	10000
weighted	avg	0.82	0.80	0.81	10000
samples	avg	0.80	0.80	0.80	10000

accuracy on test data: 0.762

metrics for test data:

		precision	recall	f1-score	support
	0	0.98	0.99	0.98	226
	1	0.80	0.88	0.84	179
	2	0.57	0.70	0.63	164
	3	0.57	0.54	0.55	199
	4	0.85	0.69	0.76	232
micro	avg	0.76	0.76	0.76	1000
macro	avg	0.75	0.76	0.75	1000
weighted	avg	0.77	0.76	0.76	1000
samples	avg	0.76	0.76	0.76	1000

Hidden layer: [512, 256, 128, 64]

epoch 50

accuracy on train data: 0.7216 learning rate: 0.001414213562373095 softmax loss: 1.9969842319606146e-05

epoch 100

accuracy on train data: 0.7709

learning rate: 0.001

softmax loss: 1.154033885296016e-05

epoch 150

accuracy on train data: 0.8061

learning rate: 0.0008164965809277261
softmax loss: 9.192962043513032e-07

epoch 200

accuracy on train data: 0.8028

learning rate: 0.0007071067811865475
softmax loss: 4.717764805687347e-06

Convergence criteria satisfied!

epoch 201

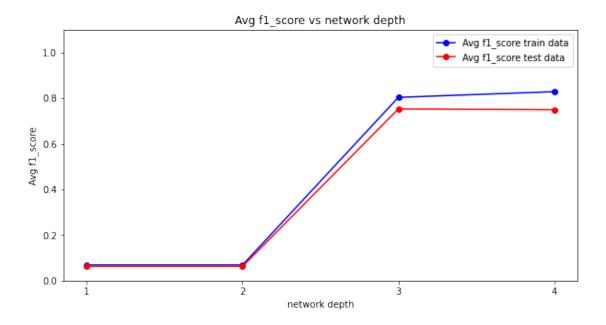
accuracy on train data: 0.832

learning rate: 0.0007053456158585983 softmax loss: 9.181468735261794e-07

accuracy on train data: 0.832

		precision	recall	f1-score	support
		•			
	^	0.00	0.00	0.00	1000
	0	0.99	0.98	0.98	1988
	1	0.93	0.91	0.92	2034
	2	0.79	0.80	0.80	1932
	3	0.57	0.71	0.63	1602
	4	0.88	0.76	0.81	2444
micro	avg	0.83	0.83	0.83	10000
macro	avg	0.83	0.83	0.83	10000
weighted	avg	0.85	0.83	0.84	10000
samples	avg	0.83	0.83	0.83	10000

accuracy on test data: 0.761 metrics for test data: precision recall f1-score support 0 0.97 0.98 0.97 225 1 0.81 0.83 0.86 210 2 0.62 0.68 0.65 182 3 0.52 0.56 0.54 174 4 0.80 0.71 0.75 209 0.76 0.76 0.76 1000 micro avg 0.75 0.75 0.75 1000 macro avg 0.77 0.76 0.76 1000 weighted avg samples avg 0.76 0.76 0.76 1000



Relu activation function (with learning rate = 0.001)

```
[6]: hidden layers = [[512], [512,256], [512,256,128], [512,256,128,64]]
     network_depth = [1,2,3,4]
     f1_score_train = []
     f1_score_test = []
     for hidden_layer in hidden_layers:
        print(f"Hidden layer: {hidden_layer}")
        NN = NeuralNetwork(n = 1024, n_hidden_nodes = hidden_layer , r = 5, M = 32)
        NN.train(X_train, y_train_onehot, epoch_mode= False, activation="relu", u
      →adaptive_learning = True, alpha = 0.001, stopping_threshold = 5.0e-06,
      ⇒printafter=50)
        y_pred_train, _ = NN.predict(X_train, activation="relu")
        y_pred_test, _ = NN.predict(X_test, activation="relu")
        print("accuracy on train data: ",accuracy_score(y_train_onehot,_
      →y_pred_train))
        print("metrics for train data: ")
        get_metric(y_train_onehot, y_pred_train)
        f1_score_train.append(f1_score(y_train_onehot, y_pred_train,_
      →average="macro"))
        print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
        print("metrics for test data: ")
        get metric(y test onehot, y pred test)
        f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
```

print("\n")

Hidden layer: [512]

epoch 50

accuracy on train data: 0.6984

learning rate: 0.0001414213562373095
softmax loss: 3.2206525277455114e-05

epoch 100

accuracy on train data: 0.7177

learning rate: 0.0001

softmax loss: 2.8674372883269804e-05

epoch 150

accuracy on train data: 0.7355

learning rate: 8.164965809277261e-05
softmax loss: 2.6139527954960384e-05

epoch 200

accuracy on train data: 0.7488

learning rate: 7.071067811865475e-05 softmax loss: 2.3554841256167726e-05

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.7493

learning rate: 7.053456158585983e-05 softmax loss: 2.3523313554780805e-05

accuracy on train data: 0.7493

metrics for train data:

	precisio		recall	f1-score	support
	0	0.95	0.91	0.93	2050
	1	0.78	0.77	0.78	1990
	2	0.64	0.66	0.65	1904
	3	0.54	0.62	0.58	1748
	4	0.84	0.76	0.80	2308
micro a	vg	0.75	0.75	0.75	10000
macro a	vg	0.75	0.74	0.75	10000
weighted a	vg	0.76	0.75	0.75	10000

samples avg 0.75 0.75 0.75 10000

accuracy on test data: 0.734

metrics for test data:

	precision recall f1-		f1-score	support	
	0	0.94	0.95	0.95	228
	1	0.77	0.76	0.76	200
	2	0.60	0.63	0.61	189
	3	0.57	0.56	0.56	189
	4	0.75	0.73	0.74	194
micro	avg	0.73	0.73	0.73	1000
macro	avg	0.73	0.72	0.73	1000
weighted	avg	0.74	0.73	0.73	1000
samples	avg	0.73	0.73	0.73	1000

Hidden layer: [512, 256]

epoch 50

accuracy on train data: 0.7485

learning rate: 0.0001414213562373095
softmax loss: 2.3803159130456424e-05

epoch 100

accuracy on train data: 0.7995

learning rate: 0.0001

softmax loss: 1.7794089613993414e-05

epoch 150

accuracy on train data: 0.8238

learning rate: 8.164965809277261e-05
softmax loss: 1.1009632399852487e-05

epoch 200

accuracy on train data: 0.842

learning rate: 7.071067811865475e-05 softmax loss: 8.309603697956972e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.8419

learning rate: 7.053456158585983e-05

softmax loss: 8.155999959208848e-06

accuracy on train data: 0.8419

metrics for train data:

	precision	recall	f1-score	support
0	0.98	0.98	0.98	1956
1	0.88	0.91	0.90	1910
2	0.77	0.81	0.78	1857
3	0.69	0.71	0.70	1963
4	0.89	0.80	0.84	2314
micro avg	0.84	0.84	0.84	10000
macro avg	0.84	0.84	0.84	10000
weighted avg	0.84	0.84	0.84	10000
samples avg	0.84	0.84	0.84	10000

accuracy on test data: 0.803

metrics for test data:

precision		recall	f1-score	support	
	0	0.97	1.00	0.98	224
	1	0.85	0.86	0.86	196
	2	0.69	0.75	0.72	182
	3	0.64	0.62	0.63	191
	4	0.83	0.75	0.79	207
micro	avg	0.80	0.80	0.80	1000
macro	avg	0.80	0.80	0.80	1000
weighted	avg	0.80	0.80	0.80	1000
samples	avg	0.80	0.80	0.80	1000

Hidden layer: [512, 256, 128]

epoch 50

accuracy on train data: 0.7774

learning rate: 0.0001414213562373095
softmax loss: 2.9403732478028548e-05

epoch 100

accuracy on train data: 0.8168

learning rate: 0.0001

softmax loss: 1.2094483311416297e-05

epoch 150

accuracy on train data: 0.847

learning rate: 8.164965809277261e-05 softmax loss: 8.964043796841776e-06

epoch 200

accuracy on train data: 0.8617

learning rate: 7.071067811865475e-05 softmax loss: 5.319551939104827e-06

 ${\tt Convergence\ criteria\ satisfied!}$

epoch 201

accuracy on train data: 0.8618

learning rate: 7.053456158585983e-05 softmax loss: 5.11851412273001e-06

accuracy on train data: 0.8618

metrics for train data:

	precision		recall	f1-score	support
	0 1 2	0.97 0.88 0.82	0.99 0.93 0.83	0.98 0.91 0.82	1922 1872 1927
	3	0.71	0.76	0.74	1893
	4	0.92	0.81	0.86	2386
micro macro	•	0.86 0.86	0.86 0.86	0.86 0.86	10000 10000
weighted	avg	0.86	0.86	0.86	10000
samples	avg	0.86	0.86	0.86	10000

accuracy on test data: 0.816

metrics for test data:

		precision	recall	f1-score	support	
	0	0.97	0.99	0.98	224	
	1	0.83	0.89	0.86	186	
	2	0.70	0.76	0.73	182	
	3	0.72	0.64	0.67	211	
	4	0.83	0.79	0.81	197	
micro	avg	0.82	0.82	0.82	1000	
macro	avg	0.81	0.81	0.81	1000	
weighted	avg	0.81	0.82	0.81	1000	
samples	avg	0.82	0.82	0.82	1000	

Hidden layer: [512, 256, 128, 64]

epoch 50

accuracy on train data: 0.7796

learning rate: 0.0001414213562373095
softmax loss: 2.1823853735152896e-05

epoch 100

accuracy on train data: 0.8303

learning rate: 0.0001

softmax loss: 9.080570686102212e-06

epoch 150

accuracy on train data: 0.8567

learning rate: 8.164965809277261e-05
softmax loss: 5.53839396842743e-06

epoch 200

accuracy on train data: 0.8847

learning rate: 7.071067811865475e-05 softmax loss: 5.457597634399534e-06

Convergence criteria satisfied!

epoch 201

accuracy on train data: 0.8908

learning rate: 7.053456158585983e-05 softmax loss: 3.781473057701032e-06

accuracy on train data: 0.8908

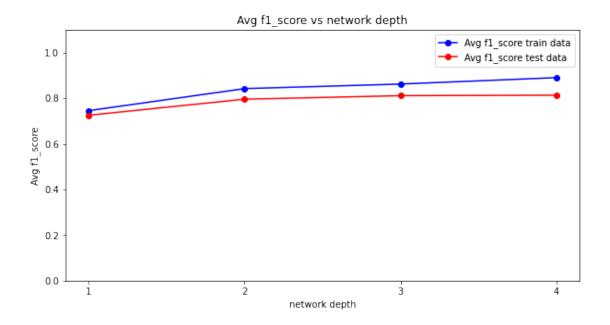
metrics for train data:

		precision	recall	f1-score	support
		_			
	0	0.99	0.98	0.99	1990
	1	0.93	0.95	0.94	1941
	2	0.85	0.87	0.86	1903
	3	0.74	0.81	0.78	1832
	4	0.94	0.84	0.89	2334
micro	avg	0.89	0.89	0.89	10000
macro	avg	0.89	0.89	0.89	10000
weighted	avg	0.89	0.89	0.89	10000

samples avg 0.89 0.89 0.89 10000

accuracy on test data: 0.82 metrics for test data:

	precision		precision recall		f1-score	support
	0	4 00	0.00	0.00	000	
	0	1.00	0.98	0.99	232	
	1	0.87	0.91	0.89	191	
	2	0.71	0.80	0.76	177	
	3	0.67	0.63	0.65	201	
	4	0.81	0.76	0.78	199	
micro	avg	0.82	0.82	0.82	1000	
macro	avg	0.81	0.82	0.81	1000	
weighted	avg	0.82	0.82	0.82	1000	
samples	avg	0.82	0.82	0.82	1000	



Neural Networks using scikit learn

```
[19]: hidden layers = [[512], [512,256], [512,256,128], [512,256,128,64]]
      network_depth = [1,2,3,4]
      f1 score train = []
      f1_score_test = []
      for hidden_layer in hidden_layers:
          print(f"Hidden layer: {hidden_layer}")
          clf = MLPClassifier(activation="relu", solver="sgd", alpha = 0,
       →batch_size=32, hidden_layer_sizes=np.array(hidden_layer),
       →learning_rate="invscaling", tol=5e-6, n_iter_no_change=5, verbose=True,
       →learning_rate_init=0.01).fit(X_train, y_train_onehot)
          y_pred_train = clf.predict(X_train)
          y_pred_test = clf.predict(X_test)
          print("accuracy on train data: ",accuracy_score(y_train_onehot,_
       →y_pred_train))
          print("metrics for train data: ")
          get_metric(y_train_onehot, y_pred_train)
          f1_score_train.append(f1_score(y_train_onehot, y_pred_train,_
       →average="macro"))
          print("accuracy on test data: ",accuracy_score(y_test_onehot, y_pred_test))
          print("metrics for test data: ")
          get_metric(y_test_onehot, y_pred_test)
          f1_score_test.append(f1_score(y_test_onehot, y_pred_test, average="macro"))
```

print("\n")

```
Hidden layer: [512]
Iteration 1, loss = 1.82100347
Iteration 2, loss = 1.71391782
Iteration 3, loss = 1.52315981
Iteration 4, loss = 1.51474497
Iteration 5, loss = 1.51029548
Iteration 6, loss = 1.50750493
Iteration 7, loss = 1.50565037
Iteration 8, loss = 1.50367111
Iteration 9, loss = 1.50203666
Iteration 10, loss = 1.50045418
Iteration 11, loss = 1.49933494
Iteration 12, loss = 1.49815999
Iteration 13, loss = 1.49698195
Iteration 14, loss = 1.49620743
Iteration 15, loss = 1.49550628
Iteration 16, loss = 1.49454919
Iteration 17, loss = 1.49363666
Iteration 18, loss = 1.49279152
Iteration 19, loss = 1.49200207
Iteration 20, loss = 1.49143824
Iteration 21, loss = 1.49060290
Iteration 22, loss = 1.48995872
Iteration 23, loss = 1.48938653
Iteration 24, loss = 1.48872835
Iteration 25, loss = 1.48810307
Iteration 26, loss = 1.48745704
Iteration 27, loss = 1.48675391
Iteration 28, loss = 1.48601222
Iteration 29, loss = 1.48555051
Iteration 30, loss = 1.48489258
Iteration 31, loss = 1.48442929
Iteration 32, loss = 1.48394169
Iteration 33, loss = 1.48350804
Iteration 34, loss = 1.48292553
Iteration 35, loss = 1.48245257
Iteration 36, loss = 1.48207413
Iteration 37, loss = 1.48157765
Iteration 38, loss = 1.48119172
Iteration 39, loss = 1.48078643
Iteration 40, loss = 1.48028934
Iteration 41, loss = 1.47994385
Iteration 42, loss = 1.47956204
Iteration 43, loss = 1.47913680
Iteration 44, loss = 1.47881800
```

```
Iteration 45, loss = 1.47835719
Iteration 46, loss = 1.47806096
Iteration 47, loss = 1.47762217
Iteration 48, loss = 1.47733798
Iteration 49, loss = 1.47684794
Iteration 50, loss = 1.47658435
Iteration 51, loss = 1.47617737
Iteration 52, loss = 1.47584291
Iteration 53, loss = 1.47550371
Iteration 54, loss = 1.47513914
Iteration 55, loss = 1.47476276
Iteration 56, loss = 1.47438837
Iteration 57, loss = 1.47401940
Iteration 58, loss = 1.47368000
Iteration 59, loss = 1.47319879
Iteration 60, loss = 1.47285898
Iteration 61, loss = 1.47256885
Iteration 62, loss = 1.47207112
Iteration 63, loss = 1.47172472
Iteration 64, loss = 1.47138364
Iteration 65, loss = 1.47103137
Iteration 66, loss = 1.47073728
Iteration 67, loss = 1.47036312
Iteration 68, loss = 1.47003571
Iteration 69, loss = 1.46979185
Iteration 70, loss = 1.46951244
Iteration 71, loss = 1.46925222
Iteration 72, loss = 1.46899571
Iteration 73, loss = 1.46865432
Iteration 74, loss = 1.46840627
Iteration 75, loss = 1.46819481
Iteration 76, loss = 1.46778235
Iteration 77, loss = 1.46766729
Iteration 78, loss = 1.46732930
Iteration 79, loss = 1.46709043
Iteration 80, loss = 1.46691234
Iteration 81, loss = 1.46659407
Iteration 82, loss = 1.46647751
Iteration 83, loss = 1.46619232
Iteration 84, loss = 1.46591034
Iteration 85, loss = 1.46570945
Iteration 86, loss = 1.46540203
Iteration 87, loss = 1.46522251
Iteration 88, loss = 1.46499896
Iteration 89, loss = 1.46479823
Iteration 90, loss = 1.46448519
Iteration 91, loss = 1.46429983
Iteration 92, loss = 1.46408573
```

```
Iteration 93, loss = 1.46382916
Iteration 94, loss = 1.46363847
Iteration 95, loss = 1.46335830
Iteration 96, loss = 1.46317960
Iteration 97, loss = 1.46292187
Iteration 98, loss = 1.46274574
Iteration 99, loss = 1.46254516
Iteration 100, loss = 1.46228647
Iteration 101, loss = 1.46209452
Iteration 102, loss = 1.46192999
Iteration 103, loss = 1.46172054
Iteration 104, loss = 1.46138636
Iteration 105, loss = 1.46131177
Iteration 106, loss = 1.46108355
Iteration 107, loss = 1.46087098
Iteration 108, loss = 1.46064470
Iteration 109, loss = 1.46041485
Iteration 110, loss = 1.46027431
Iteration 111, loss = 1.46008784
Iteration 112, loss = 1.45988650
Iteration 113, loss = 1.45972962
Iteration 114, loss = 1.45952104
Iteration 115, loss = 1.45931163
Iteration 116, loss = 1.45909816
Iteration 117, loss = 1.45895664
Iteration 118, loss = 1.45877721
Iteration 119, loss = 1.45861600
Iteration 120, loss = 1.45835821
Iteration 121, loss = 1.45818034
Iteration 122, loss = 1.45801117
Iteration 123, loss = 1.45784181
Iteration 124, loss = 1.45764247
Iteration 125, loss = 1.45748175
Iteration 126, loss = 1.45728778
Iteration 127, loss = 1.45711550
Iteration 128, loss = 1.45688891
Iteration 129, loss = 1.45679229
Iteration 130, loss = 1.45655648
Iteration 131, loss = 1.45639470
Iteration 132, loss = 1.45618799
Iteration 133, loss = 1.45606132
Iteration 134, loss = 1.45590004
Iteration 135, loss = 1.45568361
Iteration 136, loss = 1.45551304
Iteration 137, loss = 1.45533163
Iteration 138, loss = 1.45524969
Iteration 139, loss = 1.45502739
Iteration 140, loss = 1.45485948
```

```
Iteration 141, loss = 1.45471283
Iteration 142, loss = 1.45452669
Iteration 143, loss = 1.45431788
Iteration 144, loss = 1.45420511
Iteration 145, loss = 1.45401596
Iteration 146, loss = 1.45389316
Iteration 147, loss = 1.45370787
Iteration 148, loss = 1.45356289
Iteration 149, loss = 1.45343819
Iteration 150, loss = 1.45324188
Iteration 151, loss = 1.45308210
Iteration 152, loss = 1.45292444
Iteration 153, loss = 1.45276024
Iteration 154, loss = 1.45260947
Iteration 155, loss = 1.45243541
Iteration 156, loss = 1.45227674
Iteration 157, loss = 1.45219223
Iteration 158, loss = 1.45195802
Iteration 159, loss = 1.45185917
Iteration 160, loss = 1.45166933
Iteration 161, loss = 1.45155882
Iteration 162, loss = 1.45138742
Iteration 163, loss = 1.45124925
Iteration 164, loss = 1.45108788
Iteration 165, loss = 1.45094660
Iteration 166, loss = 1.45077949
Iteration 167, loss = 1.45066910
Iteration 168, loss = 1.45050262
Iteration 169, loss = 1.45032493
Iteration 170, loss = 1.45023156
Iteration 171, loss = 1.45006452
Iteration 172, loss = 1.44994194
Iteration 173, loss = 1.44978832
Iteration 174, loss = 1.44964848
Iteration 175, loss = 1.44951194
Iteration 176, loss = 1.44936269
Iteration 177, loss = 1.44922681
Iteration 178, loss = 1.44907058
Iteration 179, loss = 1.44894591
Iteration 180, loss = 1.44877779
Iteration 181, loss = 1.44865781
Iteration 182, loss = 1.44852393
Iteration 183, loss = 1.44839336
Iteration 184, loss = 1.44824172
Iteration 185, loss = 1.44808943
Iteration 186, loss = 1.44795043
Iteration 187, loss = 1.44782687
Iteration 188, loss = 1.44768827
```

Iteration 189, loss = 1.44756264
Iteration 190, loss = 1.44745318
Iteration 191, loss = 1.44731446
Iteration 192, loss = 1.44718501
Iteration 193, loss = 1.44703131
Iteration 194, loss = 1.44688879
Iteration 195, loss = 1.44674095
Iteration 196, loss = 1.44659639
Iteration 197, loss = 1.44651981
Iteration 198, loss = 1.44630971
Iteration 199, loss = 1.44626250
Iteration 200, loss = 1.44608502

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/neural_network/_multilayer_perceptron.py:691:

ConvergenceWarning: Stochastic Optimizer: Maximum iterations (200) reached and the optimization hasn't converged yet.

warnings.warn(

accuracy on train data: 0.3589

metrics for train data:

	precision		recall	f1-score	support
	0 1 2	0.88 0.21 0.03	0.87 0.75 0.58	0.88 0.33 0.07	1990 557 117
	3 4	0.00	0.00	0.00	0 1890
micro a macro a weighted a samples a	vg vg	0.36 0.36 0.68 0.36	0.79 0.59 0.79 0.36	0.49 0.39 0.71 0.36	4554 4554 4554 4554

accuracy on test data: 0.363

metrics for test data:

	precision		precision recall f1-		support
	0	0.88	0.89	0.89	226
	1	0.20	0.71	0.31	56
	2	0.05	0.60	0.08	15
	3	0.00	0.00	0.00	0
	4	0.60	0.69	0.65	163
micro	avg	0.36	0.79	0.50	460
macro	avg	0.35	0.58	0.39	460
weighted	avg	0.67	0.79	0.71	460
samples	avg	0.36	0.36	0.36	460

Hidden layer: [512, 256] /home/tkarthikeyan/.local/lib/python3.8/sitepackages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior. _warn_prf(average, modifier, msg_start, len(result)) /home/tkarthikeyan/.local/lib/python3.8/sitepackages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior. _warn_prf(average, modifier, msg_start, len(result)) /home/tkarthikeyan/.local/lib/python3.8/sitepackages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in labels with no true samples. Use `zero_division` parameter to control this behavior. _warn_prf(average, modifier, msg_start, len(result)) /home/tkarthikeyan/.local/lib/python3.8/sitepackages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior. _warn_prf(average, modifier, msg_start, len(result)) Iteration 1, loss = 1.75599291Iteration 2, loss = 1.50284355Iteration 3, loss = 1.39129507Iteration 4, loss = 1.38382212Iteration 5, loss = 1.37945388Iteration 6, loss = 1.37674041Iteration 7, loss = 1.37485859Iteration 8, loss = 1.37307523Iteration 9, loss = 1.37166307Iteration 10, loss = 1.37024469Iteration 11, loss = 1.36924451Iteration 12, loss = 1.36834121Iteration 13, loss = 1.36742281Iteration 14, loss = 1.36596267Iteration 15, loss = 1.36591150Iteration 16, loss = 1.36515085Iteration 17, loss = 1.36496215Iteration 18, loss = 1.36400063Iteration 19, loss = 1.36335653Iteration 20, loss = 1.36291710Iteration 21, loss = 1.36243440Iteration 22, loss = 1.36167984Iteration 23, loss = 1.36167079

Iteration 24, loss = 1.36108227

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Iteration 26, loss = 1.35995516
Iteration 27, loss = 1.35961524
Iteration 28, loss = 1.35919002
Iteration 29, loss = 1.35920701
Iteration 30, loss = 1.35863334
Iteration 31, loss = 1.35818692
Iteration 32, loss = 1.35783203
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Iteration 34, loss = 1.35744524
Iteration 35, loss = 1.35693297
Iteration 36, loss = 1.35671225
Iteration 37, loss = 1.35632659
Iteration 38, loss = 1.35607923
Iteration 39, loss = 1.35565661
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Iteration 47, loss = 1.35384404
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Iteration 49, loss = 1.35333122
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Iteration 55, loss = 1.35190118
Iteration 56, loss = 1.35157876
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Iteration 59, loss = 1.35098145
Iteration 60, loss = 1.35093349
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Iteration 62, loss = 1.35031236
Iteration 63, loss = 1.35013024
Iteration 64, loss = 1.35012739
Iteration 65, loss = 1.35003691
Iteration 66, loss = 1.34982555
Iteration 67, loss = 1.34947631
Iteration 68, loss = 1.34929738
Iteration 69, loss = 1.34929669
Iteration 70, loss = 1.34913114
Iteration 71, loss = 1.34883042
Iteration 72, loss = 1.34868134
```

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Iteration 73, loss = 1.34864712
Iteration 74, loss = 1.34836011
Iteration 75, loss = 1.34807917
Iteration 76, loss = 1.34797559
Iteration 77, loss = 1.34787465
Iteration 78, loss = 1.34777258
Iteration 79, loss = 1.34758600
Iteration 80, loss = 1.34750898
Iteration 81, loss = 1.34723970
Iteration 82, loss = 1.34714625
Iteration 83, loss = 1.34700567
Iteration 84, loss = 1.34683882
Iteration 85, loss = 1.34662978
Iteration 86, loss = 1.34655793
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Iteration 90, loss = 1.34599202
Iteration 91, loss = 1.34590211
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Iteration 93, loss = 1.34562009
Iteration 94, loss = 1.34530316
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Iteration 98, loss = 1.34492088
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Iteration 112, loss = 1.34330118
Iteration 113, loss = 1.34307329
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Iteration 116, loss = 1.34288639
Iteration 117, loss = 1.34263167
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Iteration 119, loss = 1.34240821
Iteration 120, loss = 1.34237846
```

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Iteration 121, loss = 1.34209611
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Iteration 123, loss = 1.34199165
Iteration 124, loss = 1.34185707
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Iteration 132, loss = 1.34104560
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Iteration 145, loss = 1.33978189
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Iteration 149, loss = 1.33943153
Iteration 150, loss = 1.33934654
Iteration 151, loss = 1.33923359
Iteration 152, loss = 1.33923656
Iteration 153, loss = 1.33907638
Iteration 154, loss = 1.33897517
Iteration 155, loss = 1.33882380
Iteration 156, loss = 1.33879743
Iteration 157, loss = 1.33873184
Iteration 158, loss = 1.33852695
Iteration 159, loss = 1.33854091
Iteration 160, loss = 1.33844815
Iteration 161, loss = 1.33841766
Iteration 162, loss = 1.33822323
Iteration 163, loss = 1.33813612
Iteration 164, loss = 1.33808318
Iteration 165, loss = 1.33807003
Iteration 166, loss = 1.33790580
Iteration 167, loss = 1.33785206
Iteration 168, loss = 1.33775579
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Iteration 169, loss = 1.33763462
Iteration 170, loss = 1.33757735
Iteration 171, loss = 1.33748661
Iteration 172, loss = 1.33754250
Iteration 173, loss = 1.33731174
Iteration 174, loss = 1.33731091
Iteration 175, loss = 1.33705106
Iteration 176, loss = 1.33725832
Iteration 177, loss = 1.33692821
Iteration 178, loss = 1.33708370
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Iteration 185, loss = 1.33644886
Iteration 186, loss = 1.33631704
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Iteration 188, loss = 1.33621864
Iteration 189, loss = 1.33608505
Iteration 190, loss = 1.33600338
Iteration 191, loss = 1.33588587
Iteration 192, loss = 1.33582098
Iteration 193, loss = 1.33584034
Iteration 194, loss = 1.33574212
Iteration 195, loss = 1.33565059
Iteration 196, loss = 1.33556211
Iteration 197, loss = 1.33560856
Iteration 198, loss = 1.33546104
Iteration 199, loss = 1.33536024
Iteration 200, loss = 1.33527121
```

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/neural_network/_multilayer_perceptron.py:691:

ConvergenceWarning: Stochastic Optimizer: Maximum iterations (200) reached and the optimization hasn't converged yet.

warnings.warn(

accuracy on train data: 0.5267

metrics for train data:

	precision recall		f1-score	support
0	0.89	0.88	0.89	2008
1	0.64	0.70	0.67	1806
2	0.35	0.59	0.44	1168
3	0.06	0.56	0.11	227
4	0.68	0.73	0.70	1967

micro	avg	0.53	0.73	0.61	7176
macro	avg	0.53	0.69	0.56	7176
weighted	avg	0.66	0.73	0.68	7176
samples	avg	0.53	0.53	0.53	7176

accuracy on test data: 0.521

metrics for test data:

		precision	recall	f1-score	support
	0	0.90	0.90	0.90	229
	1	0.62	0.69	0.65	178
	2	0.34	0.61	0.44	112
	3	0.06	0.50	0.11	22
	4	0.61	0.70	0.65	164
micro	avg	0.52	0.74	0.61	705
macro	avg	0.51	0.68	0.55	705
weighted	avg	0.65	0.74	0.68	705
samples	avg	0.52	0.52	0.52	705

Hidden layer: [512, 256, 128]

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

Iteration 1, loss = 1.76380936

Iteration 2, loss = 1.38822441

Iteration 3, loss = 1.37395561

Iteration 4, loss = 1.36949873

Iteration 5, loss = 1.36609622

Iteration 6, loss = 1.36384879

Iteration 7, loss = 1.36170042

Iteration 8, loss = 1.36104174

Iteration 9, loss = 1.35993561

Iteration 10, loss = 1.35869727

Iteration 11, loss = 1.35788140

Iteration 12, loss = 1.35715549

Iteration 13, loss = 1.35655835

Iteration 14, loss = 1.35555626

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Iteration 16, loss = 1.35481342
Iteration 17, loss = 1.35427231
Iteration 18, loss = 1.35355794
Iteration 19, loss = 1.35328877
Iteration 20, loss = 1.35279381
Iteration 21, loss = 1.35206872
Iteration 22, loss = 1.35187235
Iteration 23, loss = 1.35125906
Iteration 24, loss = 1.35109893
Iteration 25, loss = 1.35066431
Iteration 26, loss = 1.35031724
Iteration 27, loss = 1.34988212
Iteration 28, loss = 1.34967275
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Iteration 39, loss = 1.34637387
Iteration 40, loss = 1.34622964
Iteration 41, loss = 1.34576911
Iteration 42, loss = 1.34561575
Iteration 43, loss = 1.34543691
Iteration 44, loss = 1.34494329
Iteration 45, loss = 1.34484796
Iteration 46, loss = 1.34442891
Iteration 47, loss = 1.34450047
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Iteration 55, loss = 1.34286864
Iteration 56, loss = 1.34254717
Iteration 57, loss = 1.34214021
Iteration 58, loss = 1.34238252
Iteration 59, loss = 1.34202606
Iteration 60, loss = 1.34194018
Iteration 61, loss = 1.34165714
Iteration 62, loss = 1.34165045
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Iteration 63, loss = 1.34128502
Iteration 64, loss = 1.34113178
Iteration 65, loss = 1.34106945
Iteration 66, loss = 1.34079202
Iteration 67, loss = 1.34061909
Iteration 68, loss = 1.34038140
Iteration 69, loss = 1.34046859
Iteration 70, loss = 1.34008239
Iteration 71, loss = 1.33991804
Iteration 72, loss = 1.33994966
Iteration 73, loss = 1.33973863
Iteration 74, loss = 1.33955967
Iteration 75, loss = 1.33927927
Iteration 76, loss = 1.33915318
Iteration 77, loss = 1.33905393
Iteration 78, loss = 1.33881603
Iteration 79, loss = 1.33875910
Iteration 80, loss = 1.33869055
Iteration 81, loss = 1.33849121
Iteration 82, loss = 1.33841044
Iteration 83, loss = 1.33829843
Iteration 84, loss = 1.33780279
Iteration 85, loss = 1.33802149
Iteration 86, loss = 1.33781639
Iteration 87, loss = 1.33781684
Iteration 88, loss = 1.33736824
Iteration 89, loss = 1.33746816
Iteration 90, loss = 1.33722624
Iteration 91, loss = 1.33701026
Iteration 92, loss = 1.33701021
Iteration 93, loss = 1.33679836
Iteration 94, loss = 1.33670708
Iteration 95, loss = 1.33646210
Iteration 96, loss = 1.33652772
Iteration 97, loss = 1.33630714
Iteration 98, loss = 1.33620470
Iteration 99, loss = 1.33623657
Iteration 100, loss = 1.33598109
Iteration 101, loss = 1.33585048
Iteration 102, loss = 1.33569540
Iteration 103, loss = 1.33551924
Iteration 104, loss = 1.33556123
Iteration 105, loss = 1.33533158
Iteration 106, loss = 1.33514170
Iteration 107, loss = 1.33500388
Iteration 108, loss = 1.33476624
Iteration 109, loss = 1.33489067
Iteration 110, loss = 1.33468848
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Iteration 111, loss = 1.33461397
Iteration 112, loss = 1.33423274
Iteration 113, loss = 1.33441666
Iteration 114, loss = 1.33423589
Iteration 115, loss = 1.33388573
Iteration 116, loss = 1.33426413
Iteration 117, loss = 1.33396289
Iteration 118, loss = 1.33379433
Iteration 119, loss = 1.33395570
Iteration 120, loss = 1.33367703
Iteration 121, loss = 1.33348642
Iteration 122, loss = 1.33339904
Iteration 123, loss = 1.33335125
Iteration 124, loss = 1.33330120
Iteration 125, loss = 1.33314045
Iteration 126, loss = 1.33295453
Iteration 127, loss = 1.33279385
Iteration 128, loss = 1.33279488
Iteration 129, loss = 1.33266766
Iteration 130, loss = 1.33263197
Iteration 131, loss = 1.33244764
Iteration 132, loss = 1.33238185
Iteration 133, loss = 1.33233309
Iteration 134, loss = 1.33211635
Iteration 135, loss = 1.33206129
Iteration 136, loss = 1.33191412
Iteration 137, loss = 1.33193500
Iteration 138, loss = 1.33174531
Iteration 139, loss = 1.33164275
Iteration 140, loss = 1.33157977
Iteration 141, loss = 1.33158093
Iteration 142, loss = 1.33150074
Iteration 143, loss = 1.33117412
Iteration 144, loss = 1.33116357
Iteration 145, loss = 1.33111280
Iteration 146, loss = 1.33101557
Iteration 147, loss = 1.33097566
Iteration 148, loss = 1.33084151
Iteration 149, loss = 1.33060484
Iteration 150, loss = 1.33070459
Iteration 151, loss = 1.33060298
Iteration 152, loss = 1.33041688
Iteration 153, loss = 1.33034815
Iteration 154, loss = 1.33019880
Iteration 155, loss = 1.33029594
Iteration 156, loss = 1.33010516
Iteration 157, loss = 1.32992872
Iteration 158, loss = 1.32984731
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Iteration 159, loss = 1.32972096
Iteration 160, loss = 1.32968075
Iteration 161, loss = 1.32959529
Iteration 162, loss = 1.32949004
Iteration 163, loss = 1.32923991
Iteration 164, loss = 1.32951352
Iteration 165, loss = 1.32934075
Iteration 166, loss = 1.32920078
Iteration 167, loss = 1.32911943
Iteration 168, loss = 1.32898543
Iteration 169, loss = 1.32894605
Iteration 170, loss = 1.32869095
Iteration 171, loss = 1.32877422
Iteration 172, loss = 1.32867062
Iteration 173, loss = 1.32861083
Iteration 174, loss = 1.32855360
Iteration 175, loss = 1.32839278
Iteration 176, loss = 1.32834345
Iteration 177, loss = 1.32824340
Iteration 178, loss = 1.32808126
Iteration 179, loss = 1.32813627
Iteration 180, loss = 1.32815307
Iteration 181, loss = 1.32796064
Iteration 182, loss = 1.32788895
Iteration 183, loss = 1.32779912
Iteration 184, loss = 1.32772729
Iteration 185, loss = 1.32754699
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Iteration 190, loss = 1.32732263
Iteration 191, loss = 1.32716804
Iteration 192, loss = 1.32695542
Iteration 193, loss = 1.32709863
Iteration 194, loss = 1.32680616
Iteration 195, loss = 1.32680788
Iteration 196, loss = 1.32691740
Iteration 197, loss = 1.32686565
Iteration 198, loss = 1.32667633
Iteration 199, loss = 1.32653160
Iteration 200, loss = 1.32654795
/home/tkarthikeyan/.local/lib/python3.8/site-
packages/sklearn/neural_network/_multilayer_perceptron.py:691:
ConvergenceWarning: Stochastic Optimizer: Maximum iterations (200) reached and
the optimization hasn't converged yet.
  warnings.warn(
```

accuracy on train data: 0.5642

metrics for train data:

		precision	recall	f1-score	support
	0	0.89	0.88	0.88	1985
	1	0.67	0.70	0.68	1889
	2	0.42	0.59	0.49	1384
	3	0.14	0.54	0.23	531
	4	0.71	0.71	0.71	2067
micro	avg	0.56	0.72	0.63	7856
macro	avg	0.56	0.68	0.60	7856
weighted	avg	0.65	0.72	0.68	7856
samples	avg	0.56	0.56	0.56	7856

accuracy on test data: 0.562

metrics for test data:

		precision	recall	f1-score	support
	0	0.90	0.91	0.90	225
	1	0.64	0.68	0.66	184
	2	0.40	0.61	0.48	130
	3	0.18	0.54	0.27	63
	4	0.63	0.68	0.66	173
micro	avg	0.56	0.73	0.63	775
macro	avg	0.55	0.69	0.59	775
weighted	avg	0.63	0.73	0.67	775
samples	avg	0.56	0.56	0.56	775

Hidden layer: [512, 256, 128, 64]

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

Iteration 1, loss = 1.81368436

Iteration 2, loss = 1.44544842

Iteration 3, loss = 1.38917601

Iteration 4, loss = 1.38138721

Iteration 5, loss = 1.37689060Iteration 6, loss = 1.37331294Iteration 7, loss = 1.37047256Iteration 8, loss = 1.36867094Iteration 9, loss = 1.36701830Iteration 10, loss = 1.36629762Iteration 11, loss = 1.36428958Iteration 12, loss = 1.36411254Iteration 13, loss = 1.36277406Iteration 14, loss = 1.36201276Iteration 15, loss = 1.36122268 Iteration 16, loss = 1.36026491Iteration 17, loss = 1.35992904Iteration 18, loss = 1.35911954Iteration 19, loss = 1.35855620Iteration 20, loss = 1.35809020Iteration 21, loss = 1.35724215Iteration 22, loss = 1.35677803Iteration 23, loss = 1.35652282Iteration 24, loss = 1.35581300Iteration 25, loss = 1.35539375Iteration 26, loss = 1.35481140Iteration 27, loss = 1.35403886Iteration 28, loss = 1.35396309Iteration 29, loss = 1.35331822Iteration 30, loss = 1.35319095Iteration 31, loss = 1.35287776Iteration 32, loss = 1.35243008Iteration 33, loss = 1.35148415Iteration 34, loss = 1.35169121Iteration 35, loss = 1.35138144Iteration 36, loss = 1.35108106Iteration 37, loss = 1.35077123Iteration 38, loss = 1.35049022Iteration 39, loss = 1.35019795Iteration 40, loss = 1.34961928 Iteration 41, loss = 1.34928929Iteration 42, loss = 1.34920142Iteration 43, loss = 1.34881146Iteration 44, loss = 1.34820406Iteration 45, loss = 1.34864597Iteration 46, loss = 1.34793955Iteration 47, loss = 1.34757309Iteration 48, loss = 1.34729816Iteration 49, loss = 1.34697372Iteration 50, loss = 1.34694880Iteration 51, loss = 1.34656289Iteration 52, loss = 1.34625051

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Iteration 53, loss = 1.34602164
Iteration 54, loss = 1.34617614
Iteration 55, loss = 1.34566605
Iteration 56, loss = 1.34559899
Iteration 57, loss = 1.34530104
Iteration 58, loss = 1.34506928
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Iteration 62, loss = 1.34423867
Iteration 63, loss = 1.34389345
Iteration 64, loss = 1.34411251
Iteration 65, loss = 1.34349359
Iteration 66, loss = 1.34326719
Iteration 67, loss = 1.34327519
Iteration 68, loss = 1.34291595
Iteration 69, loss = 1.34269664
Iteration 70, loss = 1.34257381
Iteration 71, loss = 1.34238822
Iteration 72, loss = 1.34225701
Iteration 73, loss = 1.34217715
Iteration 74, loss = 1.34199308
Iteration 75, loss = 1.34156418
Iteration 76, loss = 1.34145023
Iteration 77, loss = 1.34130128
Iteration 78, loss = 1.34107888
Iteration 79, loss = 1.34097266
Iteration 80, loss = 1.34051020
Iteration 81, loss = 1.34031797
Iteration 82, loss = 1.34050280
Iteration 83, loss = 1.34022977
Iteration 84, loss = 1.34014982
Iteration 85, loss = 1.33990893
Iteration 86, loss = 1.33985747
Iteration 87, loss = 1.33962806
Iteration 88, loss = 1.33948541
Iteration 89, loss = 1.33930273
Iteration 90, loss = 1.33923741
Iteration 91, loss = 1.33903170
Iteration 92, loss = 1.33890641
Iteration 93, loss = 1.33867310
Iteration 94, loss = 1.33863891
Iteration 95, loss = 1.33824019
Iteration 96, loss = 1.33817394
Iteration 97, loss = 1.33787108
Iteration 98, loss = 1.33795980
Iteration 99, loss = 1.33778427
Iteration 100, loss = 1.33762673
```

```
Iteration 101, loss = 1.33748697
Iteration 102, loss = 1.33726676
Iteration 103, loss = 1.33727729
Iteration 104, loss = 1.33722797
Iteration 105, loss = 1.33697452
Iteration 106, loss = 1.33682430
Iteration 107, loss = 1.33675692
Iteration 108, loss = 1.33645577
Iteration 109, loss = 1.33642302
Iteration 110, loss = 1.33632492
Iteration 111, loss = 1.33604307
Iteration 112, loss = 1.33606265
Iteration 113, loss = 1.33586589
Iteration 114, loss = 1.33588622
Iteration 115, loss = 1.33560642
Iteration 116, loss = 1.33555894
Iteration 117, loss = 1.33544376
Iteration 118, loss = 1.33528809
Iteration 119, loss = 1.33515806
Iteration 120, loss = 1.33508599
Iteration 121, loss = 1.33489823
Iteration 122, loss = 1.33480901
Iteration 123, loss = 1.33486307
Iteration 124, loss = 1.33455791
Iteration 125, loss = 1.33450993
Iteration 126, loss = 1.33431833
Iteration 127, loss = 1.33432848
Iteration 128, loss = 1.33407660
Iteration 129, loss = 1.33384337
Iteration 130, loss = 1.33399172
Iteration 131, loss = 1.33385179
Iteration 132, loss = 1.33338531
Iteration 133, loss = 1.33348674
Iteration 134, loss = 1.33337484
Iteration 135, loss = 1.33334390
Iteration 136, loss = 1.33319013
Iteration 137, loss = 1.33311663
Iteration 138, loss = 1.33289270
Iteration 139, loss = 1.33284942
Iteration 140, loss = 1.33269074
Iteration 141, loss = 1.33260482
Iteration 142, loss = 1.33249308
Iteration 143, loss = 1.33238653
Iteration 144, loss = 1.33241869
Iteration 145, loss = 1.33235419
Iteration 146, loss = 1.33195410
Iteration 147, loss = 1.33200446
Iteration 148, loss = 1.33184600
```

```
Iteration 149, loss = 1.33173865
Iteration 150, loss = 1.33163852
Iteration 151, loss = 1.33162311
Iteration 152, loss = 1.33157170
Iteration 153, loss = 1.33124986
Iteration 154, loss = 1.33114563
Iteration 155, loss = 1.33117362
Iteration 156, loss = 1.33111677
Iteration 157, loss = 1.33091936
Iteration 158, loss = 1.33059599
Iteration 159, loss = 1.33069087
Iteration 160, loss = 1.33072471
Iteration 161, loss = 1.33060597
Iteration 162, loss = 1.33048843
Iteration 163, loss = 1.33034758
Iteration 164, loss = 1.33026873
Iteration 165, loss = 1.32985650
Iteration 166, loss = 1.33006810
Iteration 167, loss = 1.33002381
Iteration 168, loss = 1.33001853
Iteration 169, loss = 1.32981868
Iteration 170, loss = 1.32967690
Iteration 171, loss = 1.32967191
Iteration 172, loss = 1.32964922
Iteration 173, loss = 1.32915260
Iteration 174, loss = 1.32933370
Iteration 175, loss = 1.32919457
Iteration 176, loss = 1.32925131
Iteration 177, loss = 1.32907655
Iteration 178, loss = 1.32889414
Iteration 179, loss = 1.32900540
Iteration 180, loss = 1.32868908
Iteration 181, loss = 1.32884859
Iteration 182, loss = 1.32870995
Iteration 183, loss = 1.32838215
Iteration 184, loss = 1.32848429
Iteration 185, loss = 1.32849773
Iteration 186, loss = 1.32830025
Iteration 187, loss = 1.32789618
Iteration 188, loss = 1.32815089
Iteration 189, loss = 1.32800030
Iteration 190, loss = 1.32774316
Iteration 191, loss = 1.32808793
Iteration 192, loss = 1.32764538
Iteration 193, loss = 1.32781256
Iteration 194, loss = 1.32763628
Iteration 195, loss = 1.32751946
Iteration 196, loss = 1.32739331
```

Iteration 197, loss = 1.32729238
Iteration 198, loss = 1.32733673
Iteration 199, loss = 1.32719312
Iteration 200, loss = 1.32718437

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/neural_network/_multilayer_perceptron.py:691:

ConvergenceWarning: Stochastic Optimizer: Maximum iterations (200) reached and the optimization hasn't converged yet.

warnings.warn(

accuracy on train data: 0.5846

metrics for train data:

		precision	recall	f1-score	support
	0 1	0.89 0.68	0.88 0.69	0.88 0.69	1997 1958
	2	0.46	0.58	0.51	1568
	3 4	0.18 0.71	0.53 0.71	0.27 0.71	688 2064
micro	avg	0.58	0.71	0.64	8275
macro	avg	0.58	0.68	0.61	8275
weighted	avg	0.66	0.71	0.67	8275
samples	avg	0.58	0.58	0.58	8275

accuracy on test data: 0.581

metrics for test data:

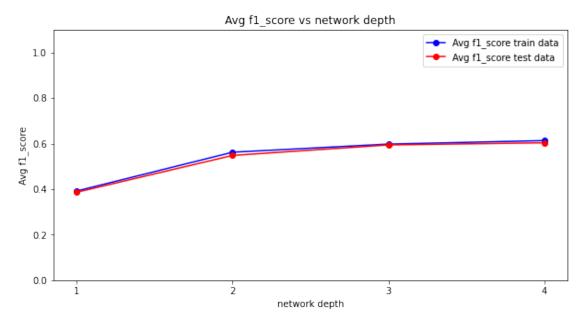
		precision	recall	f1-score	support
	0	0.90	0.90	0.90	228
	1	0.66	0.68	0.67	194
	2	0.44	0.59	0.51	149
	3	0.20	0.45	0.28	85
	4	0.64	0.69	0.66	172
micro	avg	0.58	0.70	0.64	828
macro	avg	0.57	0.66	0.60	828
weighted	avg	0.64	0.70	0.66	828
samples	avg	0.58	0.58	0.58	828

/home/tkarthikeyan/.local/lib/python3.8/site-

packages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall and F-score are ill-defined and being set to 0.0 in samples with no true labels. Use `zero_division` parameter to control this behavior.

_warn_prf(average, modifier, msg_start, len(result))

/home/tkarthikeyan/.local/lib/python3.8/sitepackages/sklearn/metrics/_classification.py:1469: UndefinedMetricWarning: Recall
and F-score are ill-defined and being set to 0.0 in samples with no true labels.
Use `zero_division` parameter to control this behavior.
_warn_prf(average, modifier, msg_start, len(result))



[]: