

# The OS Dip Solver: A Generic Block-Angluar Decomposition Algorithm

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## **Abstract**

In this document we describe how to use the Decomposition in Integer Programming (Dip) package with the Optimization Services (OS) package. The code for this example is contained in the folder `ApplicationTemplates/osDip`.

# 1 Building and Testing the OS-Dip Example

Currently, the Decomposition in Integer Programming (**Dip** package is not a dependency of the Optimization Services (**OS**) package. In order to run the OS Dip solver it is necessary to download both the **OS** and **Dip** projects. Download order is irrelevant. In the discussion that follows we assume that for both **OS** and **Dip** the user has successfully completed a `configure`, `make`, and `make install`. We also assume that the user is working with the trunk version of both **OS** and **Dip**.

The OS Dip solver C++ code is contained in `TemplateApplication/osDip`. The `configure` will create a `Makefile` in the `TemplateApplication/osDip` folder. The `Makefile` must be edited to reflect the location of the **Dip** project. The `Makefile` contains the line

```
DIPPATH = /Users/kmartin/coin/dip-trunk/vpath-debug/
```

This setting assumes that there is a **lib** directory:

```
/Users/kmartin/coin/dip-trunk/vpath-debug/lib
```

with the **Dip** library that results from `make install` and an `include` directory

```
/Users/kmartin/coin/dip-trunk/vpath/include
```

with the **Dip** header files generated by `make install`. The user should adjust

```
/Users/kmartin/coin/dip-trunk/vpath/
```

to a path containing the **Dip** `lib` and `include` directories. After building the executable by executing the `make` command run the `osdip` application using the command:

```
./osdip --param osdip.parm
```

This should produce the following output.

```
FINISH SOLVE
Status= 0 BestLB= 16.00000 BestUB= 16.00000 Nodes= 1
SetupCPU= 0.01 SolveCPU= 0.10 TotalCPU= 0.11 SetupReal= 0.08
SetupReal= 0.12 TotalReal= 0.16
Optimal Solution
-----
Quality = 16.00
0      1.00
1      1.00
12     1.00
13     1.00
14     1.00
15     1.00
17     1.00
```

If you see this output, life is good and things are working. If this doesn't work, I almost certainly did something stupid and forget to fix it. The file `osdip.parm` is a parameter file. The use of the parameter file is explained in Section 4.

## 2 The OS Dip Solver – Code Description

The OS Dip Solver uses **Dip** to implement a Dantzig-Wofe decomposition algorithm for block-angular integer programs.

### 2.1 General Philosophy

### 2.2 The code

The following C++ files are used.

**OSDipMain.cpp**

**OSDipBlockSolver.cpp**

**OSDipBlockCoinSolver.cpp**

**OSDipInterface.cpp**

**OSDipApp.cpp**

## 3 Defining the Problem Instance and Blocks

Here we describe how to use the OSoption stuff and OSInstance.

## 4 The Parameter File

Look at the osdip.parm file. You can see by commenting and uncommenting you can run one of three problems that will also get downloaded.

spl1.osil – a simple plant location problem  
spl2.osil – a second simple plant location problem  
genAssign.osil – a generalize assignment problem

The osol files (the option files) determine behavior. For example, if you use

osolFiles/spl1-b.osol

then the assignment constraints are the block constraints. If you use

osolFiles/spl1.osol

then the setup forcing constraints are the block constraints. This new example also exhibits the problems I filed ticked on.

## 5 Simple Plant/Lockbox Location Example

The problem minimizing the sum of the cost of capital due to float and the cost of operating the lock boxes is the problem.

**Parameters:**

$m$  – number of customers to be assigned a lock box

$n$  – number of potential lock box sites

$c_{ij}$  – annual cost of capital associated with serving customer  $j$  from lock box  $i$

$f_i$  – annual fixed cost of operating a lock box at location  $i$

**Variables:**

$x_{ij}$  – a binary variable which is equal to 1 if customer  $j$  is assigned to lock box  $i$  and 0 if not

$y_i$  – a binary variable which is equal to 1 if the lock box at location  $i$  is opened and 0 if not

The integer linear program for the lock box location problem is

$$\min \sum_{i=1}^n \sum_{j=1}^m c_{ij} x_{ij} + \sum_{i=1}^n f_i y_i \quad (1)$$

$$(LB) \quad \text{s.t.} \quad \sum_{i=1}^n x_{ij} = 1, \quad j = 1, \dots, m \quad (2)$$

$$x_{ij} - y_i \leq 0, \quad i = 1, \dots, n, \quad j = 1, \dots, m \quad (3)$$

$$x_{ij}, y_i \in \{0, 1\}, \quad i = 1, \dots, n, \quad j = 1, \dots, m. \quad (4)$$

The objective (1) is to minimize the sum of the cost of capital plus the fixed cost of operating the lock boxes. The requirement that every customer be assigned a lock box is modeled by constraint (2). Constraints (3) are forcing constraints and play the same role as constraint set (??) in the dynamic lot size model.

**Location Example 1:** A three-by-five example.

|       |   | CUSTOMER |   |   |   |   | FIXED COSTS |
|-------|---|----------|---|---|---|---|-------------|
|       |   | 1        | 2 | 3 | 4 | 5 |             |
| PLANT | 1 | 2        | 3 | 4 | 5 | 7 | 2           |
|       | 2 | 4        | 3 | 1 | 2 | 6 | 3           |
|       | 3 | 5        | 4 | 2 | 1 | 3 | 3           |

**Location Example 2:** A three-by-three example.

$$\min 2x_{11} + x_{12} + x_{13} + x_{21} + 2x_{22} + x_{23} + x_{31} + x_{32} + 2x_{33} + y_1 + y_2 + y_3$$

$$\text{s.t.} \quad \begin{aligned} x_{11} + x_{21} + x_{31} &= 1 \\ x_{12} + x_{22} + x_{32} &= 1 \\ x_{13} + x_{23} + x_{33} &= 1 \end{aligned} \quad Ax \geq b \text{ constraints}$$

$$\begin{aligned} x_{11} &\leq y_1 \leq 1 \\ x_{12} &\leq y_1 \leq 1 \\ x_{13} &\leq y_1 \leq 1 \\ x_{21} &\leq y_2 \leq 1 \\ x_{22} &\leq y_2 \leq 1 \\ x_{23} &\leq y_2 \leq 1 \\ x_{31} &\leq y_3 \leq 1 \\ x_{32} &\leq y_3 \leq 1 \\ x_{33} &\leq y_3 \leq 1 \end{aligned} \quad Bx \geq b \text{ constraints}$$

$$x_{ij}, y_i \geq 0, \quad i = 1, \dots, n, \quad j = 1, \dots, m.$$

## 6 Generalized Assignment Problem Example

A problem that plays a prominent role in vehicle routing is the *generalized assignment problem*. The problem is to assign each of  $n$  tasks to  $m$  servers without exceeding the resource capacity of the servers.

### Parameters:

$n$ — number of required tasks

$m$ — number of servers

$f_{ij}$ — cost of assigning task  $i$  to server  $j$

$b_j$ — units of resource available to server  $j$

$a_{ij}$ — units of server  $j$  resource required to perform task  $i$

### Variables:

$x_{ij}$ — a binary variable which is equal to 1 if task  $i$  is assigned to server  $j$  and 0 if not

The integer linear program for the generalized assignment problem is

$$\min \sum_{i=1}^n \sum_{j=1}^m f_{ij} x_{ij} \quad (5)$$

$$(GAP) \quad \text{s.t.} \quad \sum_{j=1}^m x_{ij} = 1, \quad i = 1, \dots, n \quad (6)$$

$$\sum_{i=1}^n a_{ij} x_{ij} \leq b_j, \quad j = 1, \dots, m \quad (7)$$

$$x_{ij} \in \{0, 1\}, \quad i = 1, \dots, n, \quad j = 1, \dots, m. \quad (8)$$

The objective function (5) is to minimize the total assignment cost. Constraint (6) requires that each task is assigned a server. The requirement that the server capacity not be exceeded is given in (7).

The test problem

$$\begin{aligned} \min \quad & 2 X_{11} + 11 X_{12} + 7 X_{21} + 7 X_{22} + 20 X_{31} + \\ & 2 X_{32} + 5 X_{41} + 5 X_{42} \\ \text{s.t.} \quad & X_{11} + X_{12} = 1 \\ & X_{21} + X_{22} = 1 \\ & X_{31} + X_{32} = 1 \\ & X_{41} + X_{42} = 1 \end{aligned}$$

$$\begin{aligned} 3 X_{11} + 6 X_{21} + 5 X_{31} + 7 X_{41} &\leq 13 \\ 2 X_{12} + 4 X_{22} + 10 X_{32} + 4 X_{42} &\leq 10 \end{aligned}$$

## 7 Implementing A Block Solver

Describe the Factory Code

## 8 Issues to Fix

- Enhance solveRelaxed to allow parallel processing of blocks. See ticket 30.
- Does not work when there are 0 integer variables. See ticket 31.
- Be able to set options in C++ code. See ticket 41.
- Problem with Alps bounds at node 0. See ticket 43
- Figure out how to use BranchEnforceInMaster or BranchEnforceInSubProb so I don't get the large bonds on the variables. See ticket 47.