# CSED321 Assignment 1 - Fun with Objective CAML

Homework #1 (Due Wednesday, February 27th)

Welcome to CSED321 Programming Languages! In this assignment, you will familiarize yourself with functional programming in OCaml by implementing functions of various types. Each function can be implemented with no more than a few lines of code, but requires a bit of thinking. This assignment should not be painstaking programming; rather it will be great fun!

In order to assist the teaching staff in grading your assignment, you should *strictly* follow the submission instruction. Please make sure that you have an account on the programming server 141.223.163.223, port 2022 (use your Hemos ID to login to the server).

#### 1 Submission instruction

let rec fib \_ = raise Not\_implemented
let rec gcd \_ = raise Not\_implemented
let rec max \_ = raise Not\_implemented

Download the zip file hw1.zip from the course webpage or by running the command receive on the server 141.223.163.223, and unzip it:

```
$ receive hw1
start download...
download finished...
$ unzip hw1.zip
Archive: hw1.zip
    creating: hw1/
inflating: hw1/.depend
inflating: hw1/hw1.mli
inflating: hw1/hw1.ml
inflating: hw1/Makefile

You will write code in hw1.ml and never touch other files. The stub file hw1.ml looks like:
exception Not_implemented

type 'a tree = Leaf of 'a | Node of 'a tree * 'a * 'a tree

let rec sum _ = raise Not_implemented

let rec fac _ = raise Not_implemented
```

. . .

1. Fill the function body with your own code only if you have a correct implementation of the function. This is absolutely crucial; if you leave code that does not compile, you will receive no credit. If you cannot implement a function, just leave it intact! Make sure that your program compiles by running make:

```
$ cd hw1
$ ls
hw1.ml hw1.mli Makefile
$ make
ocamlc -c hw1.mli -o hw1.cmi
ocamlc -c hw1.ml -o hw1.cmo
ocamlc -o hw1 hw1.cmo
```

2. To run your program on the OCaml interpreter, use the OCaml command #use. Here is a sample session:

3. When you have the file hw1.ml ready for submission, just run the handin command in the same directory, and your file will be submitted automatically. The handin command also runs simple test cases (different from test input for grading) and shows the results (either passed or failed). For example:

```
$ handin hw1.ml
start submission...
start building...
find target file
foo ---
sum: passed
fac: passed
fib: passed
gcd: passed
max: passed
...
```

Notice that you must submit your assignment before the deadline; any attempt to submit after the deadline will not be considered.

# 2 Functions to be implemented

For this assignment, do not use any library functions provided by OCaml.

#### 2.1 Functions on integers

#### 2.1.1 sum for adding integers 1 to n (inclusive) [4 points]

```
(Type) sum : int -> int (Description) sum n returns \sum_{i=1}^{n} i. (Invariant) n > 0. (Example) # sum 10 ;; - : int = 55
```

# 2.1.2 fac for factorials [4 points]

```
(Type) fac: int -> int (Description) fac n returns \Pi_{i=1}^n i. (Invariant) n > 0. (Hint) Change the code for sum.
```

# 2.1.3 fib for Fibonacci numbers [3 points]

```
(Type) fib: int -> int  (\text{Description})  fib n returns fib (n-1) + fib (n-2) when n \geq 2. fib n returns 1 if n=0 or n=1.  (\text{Invariant}) \ n \geq 0.
```

#### 2.1.4 gcd for finding the greatest common divisor [4 points]

```
(Type) gcd: int -> int -> int
```

(Description) gcd m n returns the greatest common divisor of m and n, using Euclid's algorithm.

```
(Invariant) m \ge 0, n \ge 0, m + n > 0.
```

(Example) The result below is specific to the sample solution. Your code may be differ in behavior.

### 2.1.5 max for finding the largest integer in a list of integers [4 points]

(Type) max: int list -> int

(Description) max l returns the largest integer in the list l. If an empty list is given, return 0.

(Example) max [5; 3; 6; 7; 4] returns 7.

#### 2.2 Functions on binary trees

#### 2.2.1 sum\_tree for computing the sum of integers stored in a binary tree [4 points]

(Type) sum\_tree : int tree -> int

(Description) sum\_tree t returns the sum of integers stored in the tree t.

(Example) sum\_tree (Node (Node (Leaf 1, 3, Leaf 2), 7, Leaf 4)) returns 17.

### 2.2.2 depth for computing the depth of tree [4 points]

(Type) depth : 'a tree -> int

(Description) depth t returns the length of the longest path from the root to leaf.

(Example) depth (Node (Node (Leaf 1, 3, Leaf 2), 7, Leaf 4)) returns 2.

### 2.2.3 bin\_search for searching an element in a binary search tree [4 points]

(Type) bin\_search : int tree -> int -> bool

(Description) bin\_search t x returns true if the number x is found in the binary search tree t; otherwise it returns false.

(Invariant) t is a binary search tree: all numbers in a left subtree are smaller than the number of the root, and all numbers in a right subtree are greater than the number of the root. We further assume that all numbers are distinct.

(Example) bin\_search (Node (Node (Leaf 1, 2, Leaf 3), 4, Leaf 7)) 2 returns true. bin\_search (Node (Node (Leaf 1, 2, Leaf 3), 4, Leaf 7)) 5 returns false.

#### 2.2.4 preorder for a preorder traversal of binary trees [4 points]

(Type) preorder: 'a tree -> 'a list

(Description) preorder t returns a list of elements produced by a preorder traversal of the tree t.

(Example) preorder (Node (Node (Leaf 1, 3, Leaf 2), 7, Leaf 4)) returns [7; 3; 1; 2; 4].

## 2.3 Functions on lists of integers

#### 2.3.1 list\_add for adding each pair of integers from two lists [4 points]

(Type) list add: int list -> int list -> int list

(Description) list\_add [a; b; c; ...] [x; y; z; ...] returns [a+x; b+y; c+z; ...]. If one list is longer than the other, the remaining list of elements is appended to the result.

(Example) list\_add [1; 2] [3; 4; 5] returns [4; 6; 5].

### 2.3.2 insert for inserting an element into a sorted list [4 points]

```
(Type) insert: int -> int list -> int list
```

(Description) insert m l inserts m into a sorted list l. The resultant list is also sorted.

(Invariant) The list l is sorted in ascending order.

```
(Example) insert 3 [1; 2; 4; 5] returns [1; 2; 3; 4; 5].
```

### 2.3.3 insort for insertion sort [4 points]

```
(Type) insort: int list -> int list
```

(Description) insort l returns a sorted list of elements in l.

(Example) insort [3; 7; 5; 1; 2] returns [1; 2; 3; 5; 7].

(Hint) Use insert above.

#### 2.4 Higher-order functions

### 2.4.1 compose for functional composition [4 points]

```
(Type) compose: ('a -> 'b) -> ('b -> 'c) -> ('a -> 'c)
```

(Description) compose f g returns  $g \circ f$ . That is, (compose f g) x is equal to g (f x).

### 2.4.2 curry for currying [4 points]

```
(Type) curry: ('a * 'b -> 'c) -> ('a -> 'b -> 'c)
```

(Description) We have a choice of how to write functions of two or more arguments. Functions are in *curried form* if they take arguments one at a time. *Uncurried* functions take arguments as a pair. curry f transforms an uncurried function f into a curried version.

(Example)

```
let multiply x y = x * y (* curried function *)
let multiplyUC (x, y) = x * y (* uncurried function *)
```

If we apply curry to multiplyUC, we get multiply.

#### 2.4.3 uncurry for uncurrying [4 points]

```
(Type) uncurry: ('a -> 'b -> 'c) -> ('a * 'b -> 'c)
```

(Description) See the above exercise. uncurry f transforms an curried function f into a uncurried version.

(Example) If we apply uncurry to multiply, we get multiplyUC.

### 2.4.4 multifun for applying a function n-times [4 points]

```
(Type) multifun : ('a -> 'a) -> int -> ('a -> 'a) 

(Description) (multifun f n) x returns the result of \underbrace{f(f(\cdots f(x)\cdots))}_{n-times} (Example) (multifun (fn x => x + 1) 3) 1 returns 4. 

(multifun (fn x => x * x) 3) 2 returns 256. 

(Invariant) n \geq 1.
```

#### 2.5 Functions on 'a list

#### 2.5.1 Itake for taking the list of the first i element of l [4 points]

```
(Type) ltake: 'a list -> int -> 'a list
```

(Description) ltake l n returns the list of the first n elements of l. If n is larger than the length of 1, then return 1.

```
(Example) ltake [3; 7; 5; 1; 2] 3 returns [3; 7; 5].

ltake [3; 7; 5; 1; 2] 7 returns [3; 7; 5; 1; 2].

ltake ["s"; "t"; "r"; "i"; "k"; "e"; "r"; "z"] 5 returns

["s"; "t"; "r"; "i"; "k"].
```

#### 2.5.2 lall for examining a list [4 points]

```
(Type) lall : ('a -> bool) -> 'a list -> bool
```

(Description) lall f l returns true if for every element x of l, f x evaluates to true; otherwise it returns false. In other words, lall f l tests if all elements in l satisfy the predicate f.

```
(Example) lall (fun x => x > 0) [1; 2; 3] evaluates to true. lall (fun x => x > 0) [-1; -2; 3] evaluates to false.
```

#### 2.5.3 lmap for converting a list into another list [5 points]

```
(Type) lmap : ('a -> 'b) -> 'a list -> 'b list
```

(Description) lmap f l applies f to each element of l from left to right, returning the list of results.

```
(Example) lmap (fun x \Rightarrow x + 1) [1; 2; 3] returns [2; 3; 4].
```

#### 2.5.4 lrev for reversing a list [5 points]

```
(Type) lrev: 'a list -> 'a list
(Description) lrev l reverses l.
(Example) lrev [1; 2; 3; 4] returns [4; 3; 2; 1].
```

#### 2.5.5 lzip for pairing corresponding members of two lists [5 points]

```
(Type) lzip: 'a list -> b' list -> ('a * 'b) list
```

(Description) lzip  $[x_1; \dots; x_n]$   $[y_1; \dots; y_n] \Rightarrow [(x_1, y_1); \dots; (x_n, y_n)]$ . If two lists differ in length, ignore surplus elements.

(Example) lzip ["Rooney"; "Park"; "Scholes"; "C.Ronaldo"] [8; 13; 18; 7; 10; 12] returns [("Rooney", 8); ("Park", 13); ("Scholes", 18); ("C.Ronaldo", 7)].

#### 2.5.6 split for splitting a list into two lists [7 points]

```
(Type) split: 'a list -> 'a list * 'a list
```

(Description) split l returns a pair of two lists. The first list consists of elements in odd positions and the second consists of elements in even positions in a given list respectively. For an empty list, split returns ([],[]). For a singleton list [x], split returns ([x],[]).

(Example) split [1; 3; 5; 7; 9; 11] returns ([1; 5; 9], [3; 7; 11]).

### 2.5.7 cartprod for the Cartesian product of two sets [7 points]

```
(Type) cartprod: 'a list -> 'b list -> ('a * 'b) list
```

(Description) cartprod S T returns the set of all pairs (x,y) with  $x \in S$  and  $y \in T$ . The order of elements is important:

```
cartprod [x_1; \dots; x_n] [y_1; \dots; y_n] \Rightarrow [(x_1, y_1); \dots; (x_1, y_n); (x_2, y_1); \dots; (x_n, y_n)].
```

(Example) cartprod [1; 2] [3; 4; 5]  $\Rightarrow$  [(1, 3); (1, 4); (1, 5); (2, 3); (2, 4); (2, 5)].