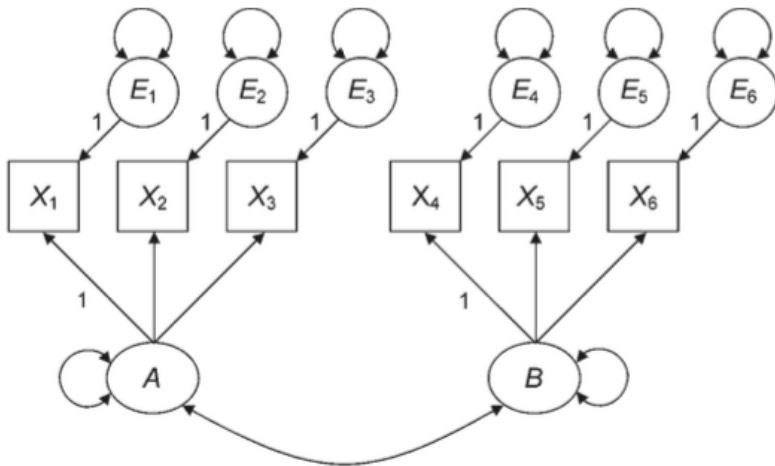


Confirmatory Factor Analysis (CFA)

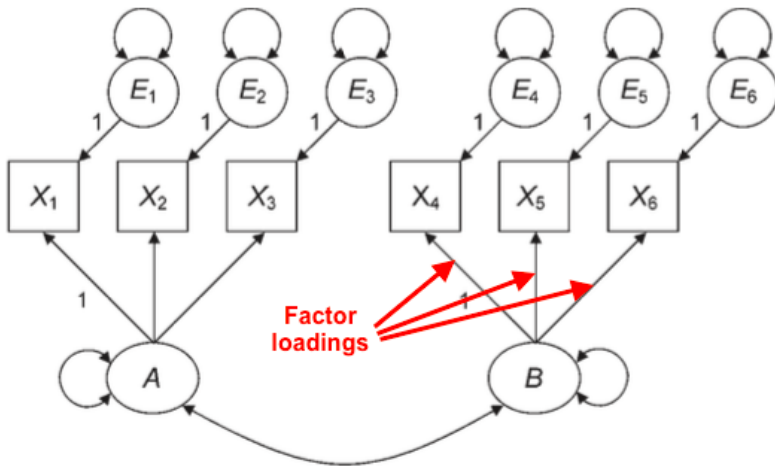
Todd K. Hartman
Lecturer in Quantitative Methods
Sheffield Methods Institute

5 May 2021

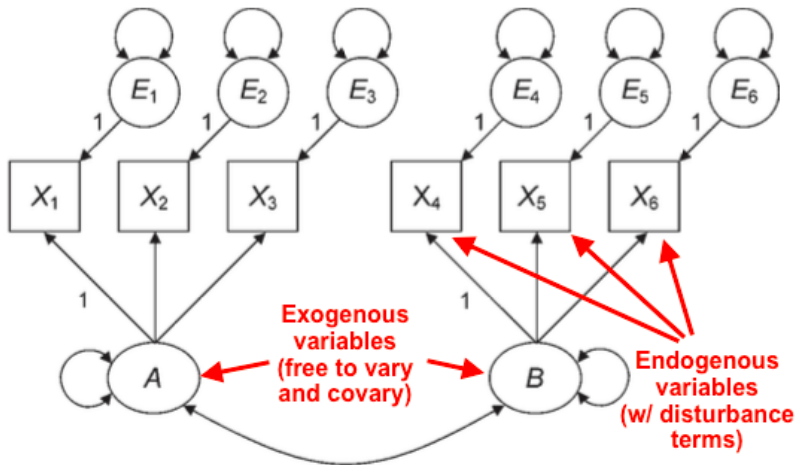
Confirmatory Factor Analysis



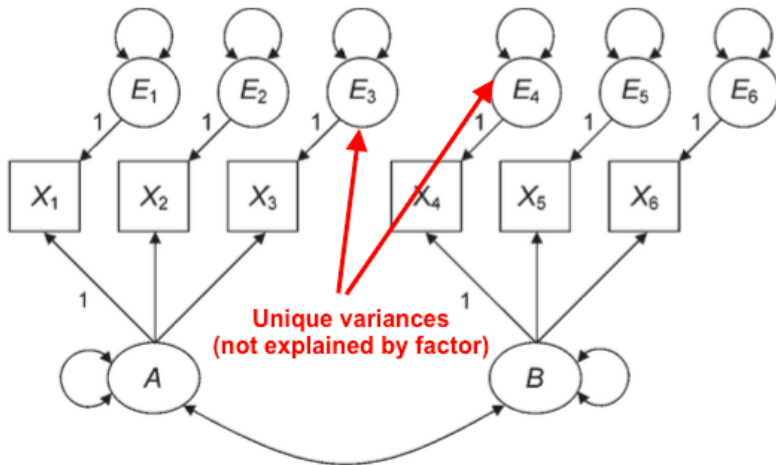
Confirmatory Factor Analysis



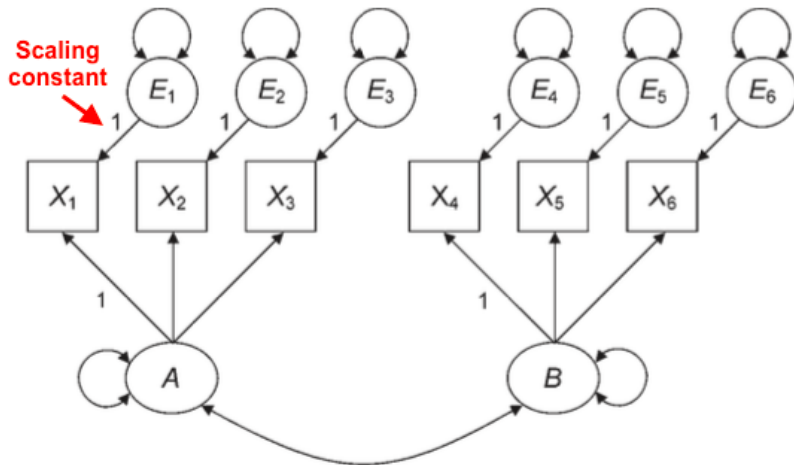
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- Discriminant validity: estimated correlations between factors not excessively high
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