# Package 'snfa'

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Title	Smooth Non-Parametric Frontier Analys	31S

Version 0.0.1

**Description** Fitting of non-parametric production frontiers for use in efficiency analysis.

Methods are provided for both a smooth analogue of Data Envelopment Analysis (DEA) and a non-parametric analogue of Stochastic Frontier Analysis (SFA). Frontiers are constructed for multiple inputs and a single output using constrained kernel smoothing as in

Racine et al. (2009), which allow for the imposition of monotonicity and concavity constraints on the estimated frontier.

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**Depends** R (>= 3.5.0)

**Imports** abind (>= 1.4.5), ggplot2 (>= 3.1.0), prodlim (>= 2018.4.18), quadprog (>= 1.5.5), Rdpack (>= 0.10.1), rootSolve (>= 1.7)

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2 allocative.efficiency

allocative.efficiency Allocative efficiency estimation

#### **Description**

Fits frontier to data and estimates technical and allocative efficiency

# Usage

```
allocative.efficiency(X, y, X.price, y.price, X.constrained = NA,
H.inv = NA, H.mult = 1, model = "br", method = "u",
scale.constraints = TRUE)
```

# **Arguments**

X	Matrix of inputs
У	Vector of outputs
X.price	Matrix of input prices
y.price	Vector of output prices
X.constrained	Matrix of inputs where constraints apply
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb
H.mult	Scaling factor for rule of thumb smoothing matrix
model	Type of frontier to use; "br" for boundary regression, "sf" for stochastic frontier
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave

scale.constraints

Boolean, whether to scale constraints by their average value, can help with convergence

#### **Details**

This function estimates allocative inefficiency using the methodology in McKenzie (2018). The estimation process is a non-parametric analogue of Schmidt and Lovell (1979). First, the frontier is fit using either a boundary regression or stochastic frontier as in Racine et al. (2009), from which technical efficiency is estimated. Then, gradients and price ratios are computed for each observation and compared to determine the extent of misallocation. Specifically, log-overallocation is computed as

$$\log\left(\frac{w_i^j}{p_i}\right) - \log\left(\phi_i \frac{\partial f(x_i)}{\partial x^j}\right),\,$$

where  $\phi_i$  is the efficiency of observation i,  $\partial f(x_i)/\partial x^j$  is the marginal productivity of input j at observation i,  $w_i^j$  is the cost of input j for observation i, and  $p_i$  is the price of output for observation i.

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#### Value

Returns a list with the following elements

y.fit Estimated value of the frontier at X.fit gradient.fit Estimated gradient of the frontier at X.fit

technical.efficiency

Estimated technical efficiency

log.overallocation

Estimated log-overallocation of each input for each observation

X. eval Matrix of inputs used for fitting

X. constrained Matrix of inputs where constraints applyH. inv Inverse smoothing matrix used in fitting

method Method used to fit frontier

scaling.factor Factor by which constraints are multiplied before quadratic programming

#### References

Aigner D, Lovell CK, Schmidt P (1977). "Formulation and estimation of stochastic frontier production function models." *Journal of econometrics*, **6**(1), 21–37.

McKenzie T (2018). "Semi-Parametric Estimation of Allocative Inefficiency Using Smooth Non-Parametric Frontier Analysis." Working Paper.

Racine JS, Parmeter CF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

Schmidt P, Lovell CK (1979). "Estimating technical and allocative inefficiency relative to stochastic production and cost frontiers." *Journal of econometrics*, **9**(3), 343–366.

4 fit.boundary

fit.boundary

Multivariate smooth boundary fitting with additional constraints

#### **Description**

Fits boundary of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

# Usage

```
fit.boundary(X.eval, y.eval, X.bounded, y.bounded, X.constrained = NA,
   X.fit = NA, y.fit.observed = NA, H.inv = NA, H.mult = 1,
   method = "u", scale.constraints = TRUE)
```

# Arguments

X.eval	Matrix of inputs used for fitting	
y.eval	Vector of outputs used for fitting	
X.bounded	Matrix of inputs where bounding constraints apply	
y.bounded	Vector of outputs where bounding constraints apply	
X.constrained	Matrix of inputs where monotonicity/concavity constraints apply	
X.fit	Matrix of inputs where curve is fit; defaults to X.constrained	
y.fit.observed	Vector of outputs corresponding to observations in X.fit; used for efficiency calculation	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	
H.mult	Scaling factor for rule of thumb smoothing matrix	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constraints		
	Rodenn whether to scale constraints by their average value, can help with con-	

Boolean, whether to scale constraints by their average value, can help with convergence

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#### **Details**

This method fits a smooth boundary of the data (with all data points below the boundary) while imposing specified monotonicity and concavity constraints. The procedure is derived from Racine et al. (2009), which develops kernel smoothing methods with bounding, monotonicity and concavity constraints. Specifically, the smoothing procedure involves finding optimal weights for a Nadaraya-Watson estimator of the form

$$\hat{y} = m(x) = \sum_{i=1}^{N} p_i A(x, x_i) y_i,$$

where x are inputs, y are outputs, p are weights, subscripts index observations, and

$$A(x, x_i) = \frac{K(x, x_i)}{\sum_{h=1}^{N} K(x, x_h)}$$

for a kernel K. This method uses a multivariate normal kernel of the form

$$K(x, x_h) = \exp\left(-\frac{1}{2}(x - x_h)'H^{-1}(x - x_h)\right),$$

where H is a bandwidth matrix. Bandwidth selection is performed via Silverman's (1986) rule-of-thumb, in the function H. inv. select.

Optimal weights  $\hat{p}$  are selected by solving the quadratic programming problem

$$\min_{p} -\mathbf{1}'p + \frac{1}{2}p'p.$$

This method always imposes bounding constraints as specified points, given by

$$m(x_i) - y_i = \sum_{h=1}^{N} p_h A(x_i, x_h) y_h - y_i \ge 0 \quad \forall i.$$

Additionally, monotonicity constraints of the following form can be imposed at specified points:

$$\frac{\partial m(x)}{\partial x^j} = \sum_{h=1}^{N} p_h \frac{\partial A(x, x_h)}{\partial x^j} y_h \ge 0 \quad \forall x, j,$$

where superscripts index inputs. Finally concavity constraints of the following form can also be imposed using Afriat's (1967) conditions:

$$m(x) - m(z) \le \nabla_x m(z) \cdot (x - z) \quad \forall x, z.$$

The gradient of the frontier at a point x is given by

$$\nabla_x m(x) = \sum_{i=1}^N \hat{p}_i \nabla_x A(x, x_i) y_i,$$

where  $\hat{p}_i$  are estimated weights.

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#### Value

Returns a list with the following elements

y.fit Estimated value of the frontier at X.fit
gradient.fit Estimated gradient of the frontier at X.fit
efficiency Estimated efficiencies of y.fit.observed
solution Boolean; TRUE if frontier successfully estimated

X. eval Matrix of inputs used for fitting

X. constrained Matrix of inputs where monotonicity/concavity constraints apply

X.fit Matrix of inputs where curve is fitH.inv Inverse smoothing matrix used in fitting

method Method used to fit frontier

scaling.factor Factor by which constraints are multiplied before quadratic programming

#### References

Racine JS, Parmeter CF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

```
data(univariate)
#Set up data for fitting
X <- as.matrix(univariate$x)</pre>
y <- univariate$y
N.fit <- 100
X.fit <- as.matrix(seq(min(X), max(X), length.out = N.fit))</pre>
#Reflect data for fitting
reflected.data <- reflect.data(X, y)</pre>
X.eval <- reflected.data$X</pre>
y.eval <- reflected.data$y</pre>
#Fit frontiers
frontier.u <- fit.boundary(X.eval, y.eval,</pre>
                             X.bounded = X, y.bounded = y,
                             X.constrained = X.fit,
                             X.fit = X.fit,
                             method = "u")
frontier.m <- fit.boundary(X.eval, y.eval,</pre>
                             X.bounded = X, y.bounded = y,
                             X.constrained = X.fit,
                             X.fit = X.fit,
                             method = "m")
frontier.mc <- fit.boundary(X.eval, y.eval,</pre>
                              X.bounded = X, y.bounded = y,
                              X.constrained = X.fit,
                              X.fit = X.fit,
```

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```
method = "mc")
#Plot frontier
library(ggplot2)
frontier.df <- data.frame(X = rep(X.fit, times = 3),</pre>
                          y = c(frontier.u$y.fit, frontier.m$y.fit, frontier.mc$y.fit),
                          model = rep(c("u", "m", "mc"), each = N.fit))
ggplot(univariate, aes(X, y)) +
  geom_point() +
  geom_line(data = frontier.df, aes(color = model))
#Plot slopes
slope.df <- data.frame(X = rep(X.fit, times = 3),</pre>
                       slope = c(frontier.u$gradient.fit,
                                  frontier.m$gradient.fit,
                                  frontier.mc$gradient.fit),
                       model = rep(c("u", "m", "mc"), each = N.fit))
ggplot(slope.df, aes(X, slope)) +
  geom_line(aes(color = model))
```

fit.mean

Kernel smoothing with additional constraints

# **Description**

Fits conditional mean of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

# Usage

```
fit.mean(X.eval, y.eval, X.constrained = NA, X.fit = NA, H.inv = NA,
   H.mult = 1, method = "u", scale.constraints = TRUE)
```

#### **Arguments**

X.eval	Matrix of inputs used for fitting	
y.eval	Vector of outputs used for fitting	
X.constrained	Matrix of inputs where constraints apply	
X.fit	Matrix of inputs where curve is fit; defaults to X.constrained	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	
H.mult	Scaling factor for rule of thumb smoothing matrix	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constraints		

Boolean, whether to scale constraints by their average value, can help with convergence

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#### **Details**

This method uses kernel smoothing to fit the mean of the data while imposing specified monotonicity and concavity constraints. The procedure is derived from Racine et al. (2009), which develops kernel smoothing methods with bounding, monotonicity and concavity constraints. Specifically, the smoothing procedure involves finding optimal weights for a Nadaraya-Watson estimator of the form

$$\hat{y} = m(x) = \sum_{i=1}^{N} p_i A(x, x_i) y_i,$$

where x are inputs, y are outputs, p are weights, subscripts index observations, and

$$A(x, x_i) = \frac{K(x, x_i)}{\sum_{h=1}^{N} K(x, x_h)}$$

for a kernel K. This method uses a multivariate normal kernel of the form

$$K(x, x_h) = \exp\left(-\frac{1}{2}(x - x_h)'H^{-1}(x - x_h)\right),$$

where H is a bandwidth matrix. Bandwidth selection is performed via Silverman's (1986) rule-of-thumb, in the function H. inv. select.

Optimal weights  $\hat{p}$  are selected by solving the quadratic programming problem

$$\min_{p} -\mathbf{1}'p + \frac{1}{2}p'p.$$

Monotonicity constraints of the following form can be imposed at specified points:

$$\frac{\partial m(x)}{\partial x^j} = \sum_{h=1}^{N} p_h \frac{\partial A(x, x_h)}{\partial x^j} y_h \ge 0 \quad \forall x, j,$$

where superscripts index inputs. Finally concavity constraints of the following form can also be imposed using Afriat's (1967) conditions:

$$m(x) - m(z) \le \nabla_x m(z) \cdot (x - z) \quad \forall x, z.$$

The gradient of the estimated curve at a point x is given by

$$\nabla_x m(x) = \sum_{i=1}^N \hat{p}_i \nabla_x A(x, x_i) y_i,$$

where  $\hat{p}_i$  are estimated weights.

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#### Value

Returns a list with the following elements

y.fit Estimated value of the frontier at X.fit
gradient.fit Estimated gradient of the frontier at X.fit
solution Boolean; TRUE if frontier successfully estimated
X.eval Matrix of inputs used for fitting
X.constrained Matrix of inputs where constraints apply
X.fit Matrix of inputs where curve is fit
H.inv Inverse smoothing matrix used in fitting

method Method used to fit frontier

scaling.factor Factor by which constraints are multiplied before quadratic programming

#### References

Racine JS, Parmeter CF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

```
data(USMacro)
USMacro <- USMacro[complete.cases(USMacro),]</pre>
#Extract data
X <- as.matrix(USMacro[,c("K", "L")])</pre>
y <- USMacro$Y
#Reflect data for fitting
reflected.data <- reflect.data(X, y)</pre>
X.eval <- reflected.data$X</pre>
y.eval <- reflected.data$y</pre>
#Fit frontier
fit.mc <- fit.mean(X.eval, y.eval,</pre>
                    X.constrained = X,
                    X.fit = X,
                    method = "mc")
#Plot input productivities over time
library(ggplot2)
plot.df <- data.frame(Year = rep(USMacro$Year, times = 2),</pre>
                       Elasticity = c(fit.mc\gradient.fit[,1] * X[,1] / y,
                                       fit.mc$gradient.fit[,2] * X[,2] / y),
                       Variable = rep(c("Capital", "Labor"), each = nrow(USMacro)))
ggplot(plot.df, aes(Year, Elasticity)) +
  geom_line() +
  facet_grid(Variable ~ ., scales = "free_y")
```

10 fit.sf

fit.sf

Non-parametric stochastic frontier

#### **Description**

Fits stochastic frontier of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

# Usage

```
fit.sf(X, y, X.constrained = NA, H.inv = NA, H.mult = 1,
  method = "u", scale.constraints = TRUE)
```

# **Arguments**

X Matrix of inputs
 y Vector of outputs
 X. constrained Matrix of inputs where constraints apply
 H. inv Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb
 H. mult Scaling factor for rule of thumb smoothing matrix
 method Constraints to apply; "u" for unconstrained, "m" for monotonically increasing,

and "me" for monotonically increasing and concave

scale.constraints

Boolean, whether to scale constraints by their average value, can help with convergence

# **Details**

This method fits non-parametric stochastic frontier models. The data-generating process is assumed to be of the form

$$ln y_i = ln f(x_i) + v_i - u_i,$$

where  $y_i$  is the *i*th observation of output, f is a continuous function,  $x_i$  is the *i*th observation of input,  $v_i$  is a normally-distributed error term  $(v_i \sim N(0, \sigma_v^2))$ , and  $u_i$  is a normally-distributed error term truncated below at zero  $(u_i \sim N^+(0, \sigma_u))$ . Aigner et al. developed methods to decompose  $\varepsilon_i = v_i - u_i$  into its basic components.

This procedure first fits the mean of the data using fit.mean, producing estimates of output  $\hat{y}$ . Log-proportional errors are calculated as

$$\varepsilon_i = \ln(y_i/\hat{y}_i).$$

Following Aigner et al. (1977), parameters of one- and two-sided error distributions are estimated via maximum likelihood. First,

$$\hat{\sigma}^2 = \frac{1}{N} \sum_{i=1}^{N} \varepsilon_i^2.$$

fit.sf

Then,  $\hat{\lambda}$  is estimated by solving

$$\frac{1}{\hat{\sigma}^2} \sum_{i=1}^{N} \varepsilon_i \hat{y}_i + \frac{\hat{\lambda}}{\hat{\sigma}} \sum_{i=1}^{N} \frac{f_i^*}{1 - F_i^*} y_i = 0,$$

where  $f_i^*$  and  $F_i^*$  are standard normal density and distribution function, respectively, evaluated at  $\varepsilon_i \hat{\lambda} \hat{\sigma}^{-1}$ . Parameters of the one- and two-sided distributions are found by solving the identities

$$\sigma^2 = \sigma_u^2 + \sigma_v^2$$

$$\lambda = \frac{\sigma_u}{\sigma_v}.$$

Mean efficiency over the sample is given by

$$\exp\left(-\frac{\sqrt{2}}{\sqrt{\pi}}\right)\sigma_u,$$

and modal efficiency for each observation is given by

$$-\varepsilon(\sigma_u^2/\sigma^2).$$

#### Value

Returns a list with the following elements

y. fit Estimated value of the frontier at X.fit

gradient.fit Estimated gradient of the frontier at X.fit

mean.efficiency

Average efficiency for X, y as a whole

mode.efficiency

Modal efficiencies for each observation in X, y

X. eval Matrix of inputs used for fitting

X. constrained Matrix of inputs where constraints apply

X. fit Matrix of inputs where curve is fit

H. inv Inverse smoothing matrix used in fitting

method Method used to fit frontier

scaling.factor Factor by which constraints are multiplied before quadratic programming

#### References

Aigner D, Lovell CK, Schmidt P (1977). "Formulation and estimation of stochastic frontier production function models." *Journal of econometrics*, **6**(1), 21–37.

Racine JS, Parmeter CF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

#### **Examples**

```
data(USMacro)
USMacro <- USMacro[complete.cases(USMacro),]</pre>
#Extract data
X <- as.matrix(USMacro[,c("K", "L")])</pre>
y <- USMacro$Y
#Fit frontier
fit.sf <- fit.sf(X, y,</pre>
                  X.constrained = X,
                  method = "mc")
print(fit.sf$mean.efficiency)
# [1] 0.9772484
#Plot efficiency over time
library(ggplot2)
plot.df <- data.frame(Year = USMacro$Year,</pre>
                       Efficiency = fit.sf$mode.efficiency)
ggplot(plot.df, aes(Year, Efficiency)) +
  geom_line()
```

H.inv.select

Bandwidth matrix selection

# **Description**

Computes inverse of bandwidth matrix using rule-of-thumb from Silverman (1986).

# Usage

```
H.inv.select(X, H.mult = 1)
```

# **Arguments**

X Matrix of inputs

H.mult Scaling factor for rule-of-thumb smoothing matrix

#### **Details**

This method performs selection of (inverse) multivariate bandwidth matrices using Silverman's (1986) rule-of-thumb. Specifically, Silverman recommends setting the bandwidth matrix to

$$\begin{split} H_{jj}^{1/2} &= \left(\frac{4}{M+2}\right)^{1/(M+4)} \times N^{-1/(M+4)} \times \operatorname{sd}(x^j) \quad \text{for } j=1,...,M \\ H_{ab} &= 0 \quad \text{for } a \neq b \end{split}$$

where M is the number of inputs, N is the number of observations, and  $\mathrm{sd}(x^j)$  is the sample standard deviation of input j.

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# Value

Returns inverse bandwidth matrix

#### References

Silverman BW (1986). Density estimation for statistics and data analysis, volume 26. CRC press.

# **Examples**

panel.production

Randomly generated panel of production data

# Description

A dataset for illustrating technical and efficiency changes using smooth non-parametric frontiers.

# Usage

```
panel.production
```

### **Format**

A data frame with 200 observations of six variables.

Firm Firm identifier

Year Year of observation

**X.1** Input 1

**X.2** Input 2

**X.3** Input 3

y Output

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#### **Details**

Generated with the following code:

```
set.seed(100)
num.firms <- 20
num.inputs <- 3
num.years <- 10
beta <- runif(num.inputs, 0, 1)</pre>
TFP.trend = 0.25
TFP <- cumsum(rnorm(num.years)) + TFP.trend * (1:num.years)</pre>
sd.measurement <- 0.05
sd.inefficiency <- 0.01
f <- function(X){</pre>
  return(TFP + X
gen.firm.data <- function(i){</pre>
  X = matrix(runif(num.years * num.inputs, 1, 10), ncol = num.inputs)
  y = f(X) +
    rnorm(num.years, sd = sd.measurement) -
    abs(rnorm(num.years, sd = sd.inefficiency))
  firm.df <- data.frame(Firm = i,</pre>
                         Year = 1:num.years,
                         X = exp(X),
                         y = exp(y)
}
panel.production = Reduce(rbind, lapply(1:num.firms, gen.firm.data))
panel.production$Firm = as.factor(panel.production$Firm)
```

reflect.data

Data reflection for kernel smoothing

# Description

This function reflects data below minimum and above maximum for use in reducing endpoint bias in kernel smoothing.

# Usage

```
reflect.data(X, y)
```

### **Arguments**

X Matrix of inputsy Vector of outputs

#### Value

Returns a list with the following elements

```
X.reflected Reflected values of X y.reflected Reflected values of y
```

#### **Examples**

```
technical.efficiency.change
```

Technical and efficiency change estimation

# Description

Estimates technical and efficiency change using SNFA

# Usage

```
technical.efficiency.change(df, input.var.names, output.var.name,
firm.var.name, time.var.name, method = "u")
```

# **Arguments**

```
df Data frame with variables used in estimation input.var.names

Names of input variables; must appear in df output.var.name

Name of output variable; must appear in df firm.var.name

Name of firm variable; must appear in df
```

time.var.name Name of time variable; must appear in df

method Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave

#### Details

This function decomposes change in productivity into efficiency and technical change, as in Fare et al. (1994), using smooth non-parametric frontier analysis. Denoting  $D_s(x_t, y_t)$  as the efficiency of the production plan in year t relative to the production frontier in year s, efficiency change for a given firm in year t is calculated as

$$\frac{D_{t+1}(x_{t+1}, y_{t+1})}{D_t(x_t, y_t)},$$

and technical change is given by

$$\left(\frac{D_t(x_{t+1}, y_{t+1})}{D_{t+1}(x_{t+1}, y_{t+1})} \times \frac{D_t(x_t, y_t)}{D_{t+1}(x_t, y_t)}\right)^{1/2}.$$

#### Value

Returns a data.frame with the following columns

firm.var.name Column of firm name data time.var.name Column of time period data efficiency.change

Average annual efficiency change since the previous period in data technical.change

Average annual technical change since the previous period in data productivity.change

Average annual productivity change since the previous period in data

# References

Fare R, Grosskopf S, Norris M, Zhang Z (1994). "Productivity Growth, Technical Progress, and Efficiency Change in Industrialized Countries." *The American Economic Review*, **84**(1), 66-83.

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```
geom_line(aes(color = Firm))
ggplot(results.df, aes(Year, productivity.change)) +
geom_line(aes(color = Firm))
```

univariate

Randomly generated univariate data

# **Description**

A dataset for illustrating univariate non-parametric boundary regressions and various constraints.

# Usage

univariate

#### **Format**

A data frame with 50 observations of two variables.

- x Input
- y Output

# **Details**

Generated with the following code:

```
set.seed(100)

N <- 50
x <- runif(N, 10, 100)
y <- sapply(x, function(x) 500 * x^0.25 - dnorm(x, mean = 70, sd = 10) * 8000) - abs(rnorm(N, sd = 20))
y <- y - min(y) + 10
df <- data.frame(x, y)</pre>
```

USMacro

US Macroeconomic Data

# Description

A dataset of real output, labor force, capital stock, wages, and interest rates for the U.S. between 1929 and 2014, as available. All nominal values converted to 2010 U.S. dollars using GDP price deflator.

# Usage

USMacro

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# **Format**

A data frame with 89 observations of four variables.

Year Year

Y Real GDP, in billions of dollars

K Capital stock, in billions of dollars

**K.price** Annual cost of \$1 billion of capital, using 10-year treasury

L Labor force, in thousands of people

L.price Annual wage for one thousand people

# Source

https://fred.stlouisfed.org/

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