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# **Computation time**

**Total** None

# **Experimental condition**

Type of tomography	StandardQst
Nrep	100
N	[100, 1000, 10000]
RNG seed	777

# True object

**Type** State

Dim	2
Vec	[0.70710678 0.40824829 0.40824829 0.40824829]

# **Tester objects**

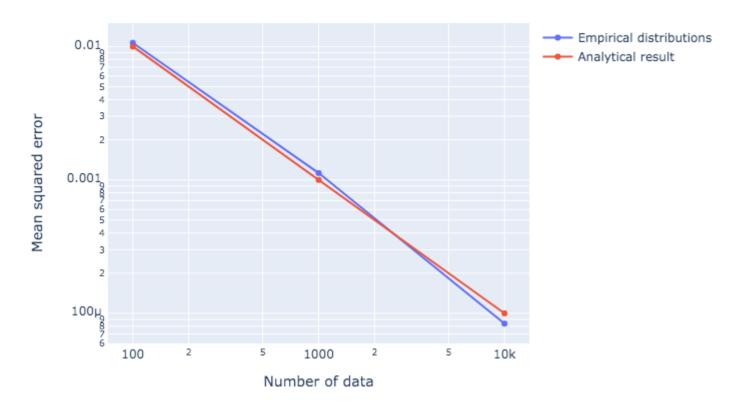
0	Туре	Povm
	Dim	2
	Number of outcomes	2
	Vecs	[0.70710678 0.70710678 0. 0. ] [ 0.70710678 -0.70710678 0. 0. ]
1	Туре	Povm
	Dim	2
	Number of outcomes	2
	Vecs	[0.70710678 0. 0.70710678 0. ] [ 0.70710678 00.70710678 0. ]
2	Туре	Povm
	Dim	2
	Number of outcomes	2
	Vecs	[0.70710678 0. 0. 0.70710678] [ 0.70710678 0. 00.70710678]

# Cases

	Name	Parameterization	Tomography	Estimator
0	LinearEstimator(True)	True	StandardQst	LinearEstimator
1	LinearEstimator(False)	False	StandardQst	LinearEstimator
2	ProjectedLinearEstimator(True)	True	StandardQst	ProjectedLinearEstimator
3	ProjectedLinearEstimator(False)	False	StandardQst	ProjectedLinearEstimator

# **MSE** of empirical distributions

# Mean squared error



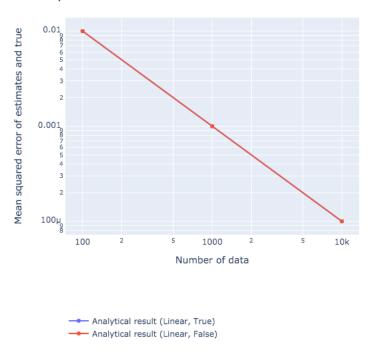
# **Consistency test**

	Type of tomography	Parametorization	Estimator	Result
0	StandardQst	True	LinearEstimator	9.244464e-33
1	StandardQst	False	LinearEstimator	5.854827e-32
2	StandardQst	True	ProjectedLinearEstimator	2.095412e-31
3	StandardQst	False	ProjectedLinearEstimator	3.050673e-31

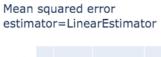
# **MSE** of estimators

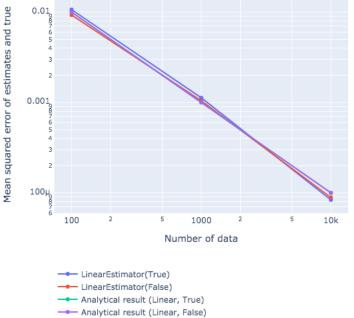
# **Comparison of analytical results**

#### Mean squared error Analytical result

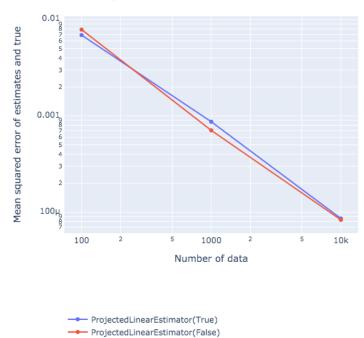


# **Comparison of parametrization**



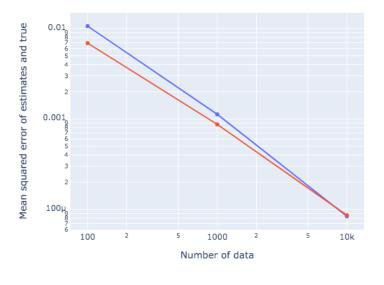


# Mean squared error estimator=ProjectedLinearEstimator

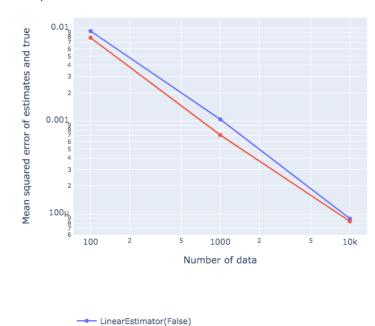


# **Comparison of estimators**





# Mean squared error parametrization=False



ProjectedLinearEstimator(False)

LinearEstimator(True)ProjectedLinearEstimator(True)

# **Physicality violation test**

# Test of equality constraint violation

**Case 0: LinearEstimator(True)** 

# N=100, Nrep=100 0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2

Min: 0.99999999999998 Max: 0.99999999999998

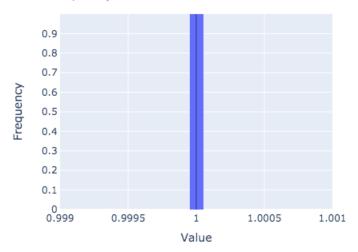
1 Value

|Max-Min|: 0.0

1.0005

1.001

N=1000, Nrep=100



Min: 0.99999999999998 Max: 0.99999999999998 |Max-Min|: 0.0

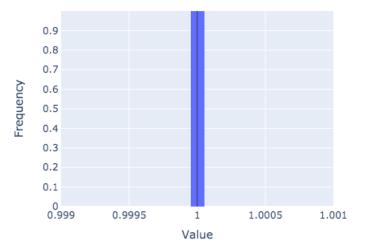
**Case 1: LinearEstimator(False)** 

0.9995



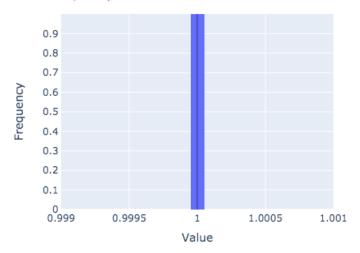
0.1

0



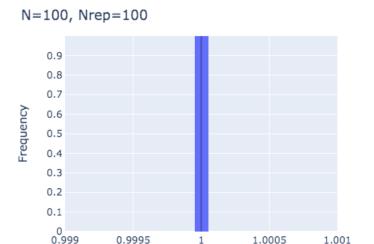
Min: 0.9999999999998 Max: 1.0000000000000002 |Max-Min|: 4.440892098500626e-16

N=1000, Nrep=100



Min: 0.99999999999998 Max: 1.00000000000000002 |Max-Min|: 4.440892098500626e-16

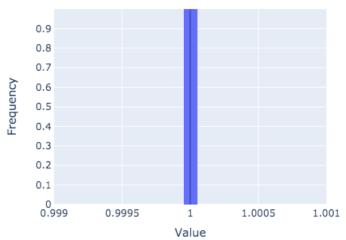
Case 2: ProjectedLinearEstimator(True)



Min: 0.99999999999998 Max: 0.99999999999998 |Max-Min|: 0.0

Value

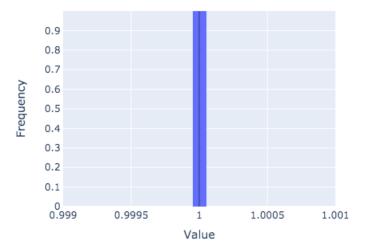
N=1000, Nrep=100



Min: 0.99999999999998 Max: 0.99999999999998 |Max-Min|: 0.0

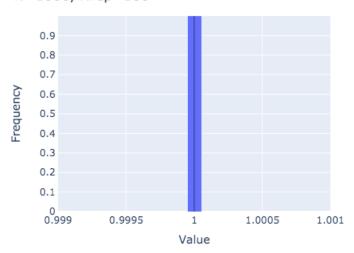
Case 3: ProjectedLinearEstimator(False)





Min: 0.999999999999998 Max: 0.99999999999998 |Max-Min|: 0.0

N=1000, Nrep=100



Min: 0.999999999999998 Max: 0.99999999999998 |Max-Min|: 0.0

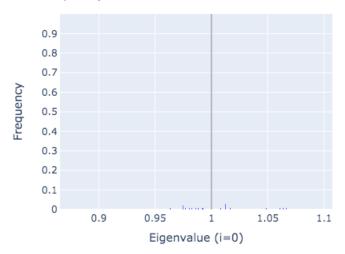
# Test of inequality constraint violation

## **Eigenvalue**

## **Case 0: LinearEstimator(True)**

N=100

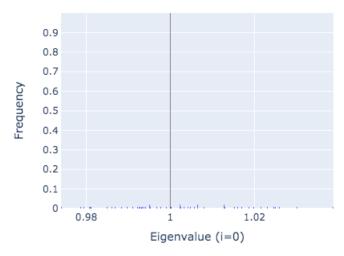
## N=100, Nrep=100



Min: 0.8656501059756443 Max: 1.1073713855624088 |Max-Min|: 0.24172127958676448

N=1000

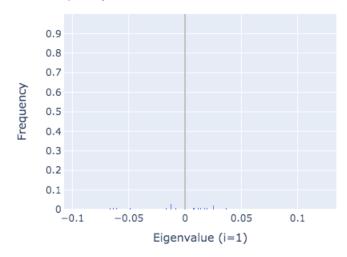
## N=1000, Nrep=100



Min: 0.974055903876326 Max: 1.038734628551015 |Max-Min|: 0.06467872467468905

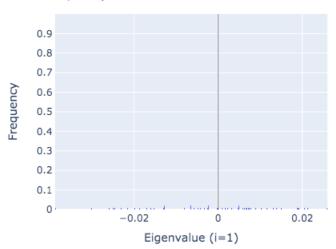
N=10000

N=100, Nrep=100



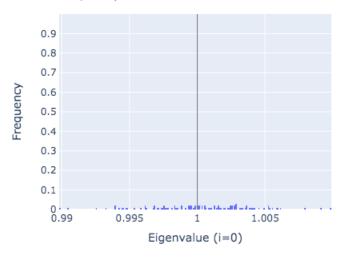
Min: -0.10737138556240879 Max: 0.13434989402435554 |Max-Min|: 0.24172127958676431

## N=1000, Nrep=100



Min: -0.03873462855101516 Max: 0.025944096123674317 |Max-Min|: 0.06467872467468948

## N=10000, Nrep=100

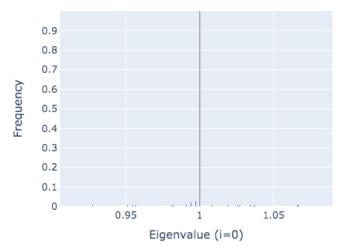


Min: 0.9898449346476905 Max: 1.0098202428307452 |Max-Min|: 0.019975308183054707

## **Case 1: LinearEstimator(False)**

#### N=100

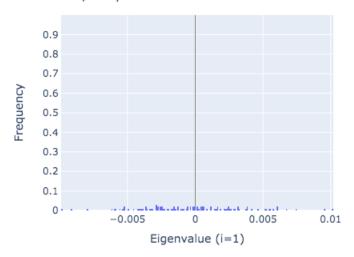
# N=100, Nrep=100



Min: 0.9054626986542657 Max: 1.08974570791147 |Max-Min|: 0.18428300925720442

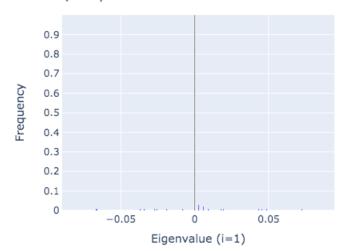
#### N=1000

## N=10000, Nrep=100



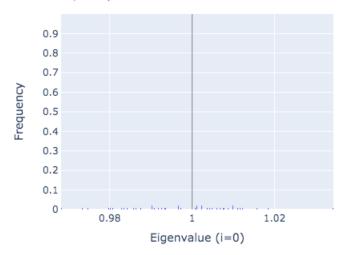
Min: -0.009820242830745339 Max: 0.010155065352309402 |Max-Min|: 0.019975308183054742

## N=100, Nrep=100



Min: -0.08974570791146932 Max: 0.09453730134573403 |Max-Min|: 0.18428300925720337

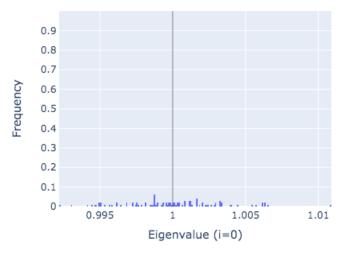
## N=1000, Nrep=100



Min: 0.9682873049742009 Max: 1.0342967340345623 |Max-Min|: 0.06600942906036145

N=10000

# N=10000, Nrep=100

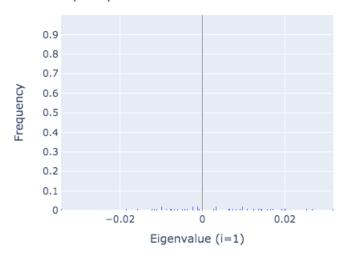


Min: 0.9922677015608485 Max: 1.0108647570541545 |Max-Min|: 0.018597055493305925

Case 2: ProjectedLinearEstimator(True)

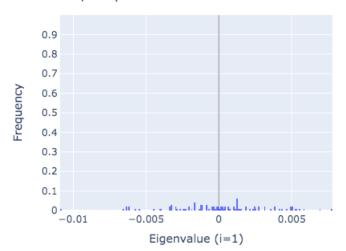
N=100

## N=1000, Nrep=100



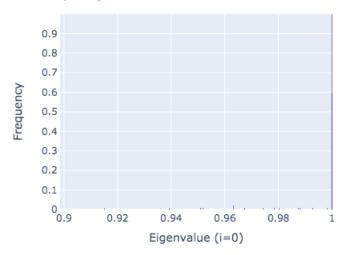
Min: -0.03429673403456271 Max: 0.03171269502579911 |Max-Min|: 0.06600942906036182

## N=10000, Nrep=100



Min: -0.010864757054154343 Max: 0.00773229843915209 |Max-Min|: 0.01859705549330643

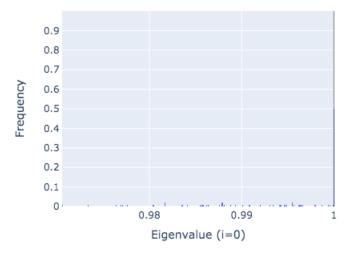
## N=100, Nrep=100



Min: 0.8986226285598955 Max: 1.000000000009304 |Max-Min|: 0.10137737144103487

N=1000

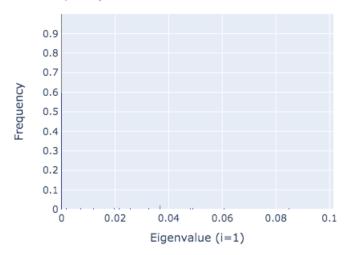
## N=1000, Nrep=100



Min: 0.9705943051079131 Max: 1.000000000126343 |Max-Min|: 0.029405694904721225

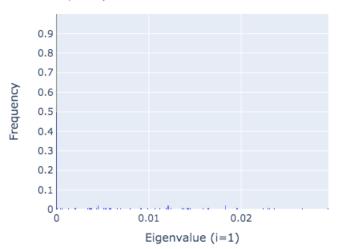
N=10000

## N=100, Nrep=100



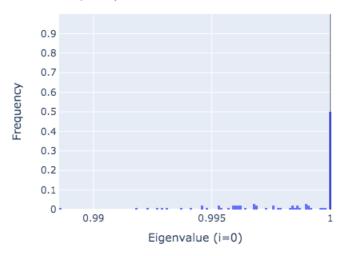
Min: -9.306224459265484e-13 Max: 0.10137737144010481 |Max-Min|: 0.10137737144103542

## N=1000, Nrep=100



Min: -1.2634835348919929e-11 Max: 0.02940569489208648 |Max-Min|: 0.029405694904721315

## N=10000, Nrep=100

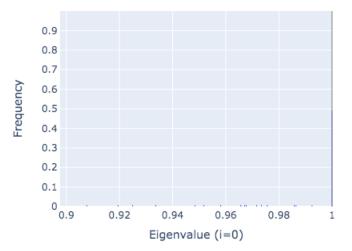


Min: 0.9885819276231976 Max: 1.0000000001516711 |Max-Min|: 0.011418072528473489

# Case 3: ProjectedLinearEstimator(False)

#### N=100

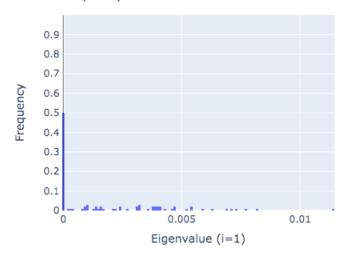
N=100, Nrep=100



Min: 0.8977436360270267 Max: 1.0000000000014884 |Max-Min|: 0.1022563639744617

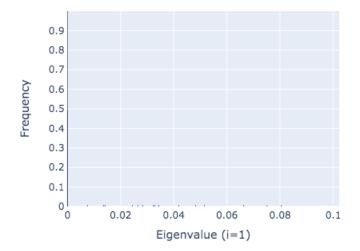
N=1000

## N=10000, Nrep=100



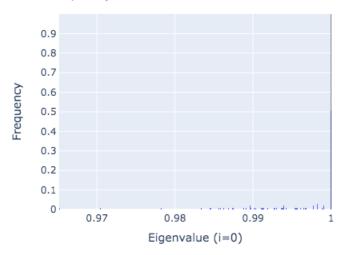
Min: -1.51670780996407e-10 Max: 0.011418072376801695 |Max-Min|: 0.011418072528472477

## N=100, Nrep=100



Min: -1.4889802201828985e-12 Max: 0.10225636397297323 |Max-Min|: 0.10225636397446221

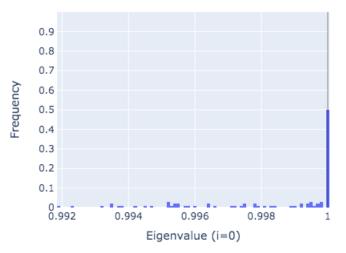
## N=1000, Nrep=100



Min: 0.9651892088172294 Max: 1.000000000121578 |Max-Min|: 0.03481079119492847

#### N=10000

# N=10000, Nrep=100



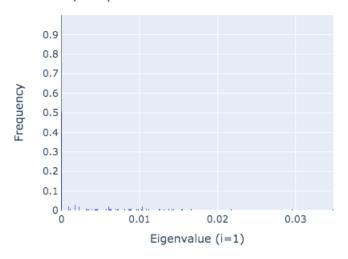
Min: 0.9919080605153767 Max: 1.000000000279459 |Max-Min|: 0.008091939512569146

# Sum of unphysical eigenvalues

# **Case 0: LinearEstimator(True)**

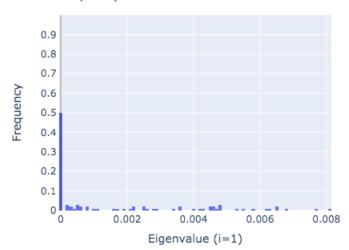
N=100

## N=1000, Nrep=100



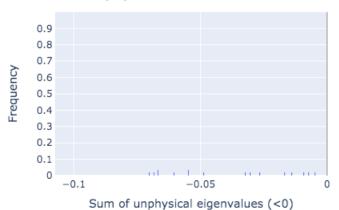
Min: -1.2158255693186201e-11 Max: 0.0348107911827703 |Max-Min|: 0.03481079119492855

## N=10000, Nrep=100



Min: -2.7945709912996674e-11 Max: 0.008091939484622813 |Max-Min|: 0.008091939512568523

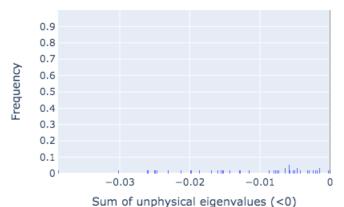
N=100, Nrep=56 Number of unphysical estimates=56



Min: -0.10737138556240879 Max: -0.0013980454688671121 |Max-Min|: 0.10597334009354167

N=1000

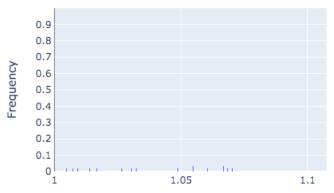
N=1000, Nrep=56 Number of unphysical estimates=56



Min: -0.03873462855101516 Max: -1.2999831004603704e-05 |Max-Min|: 0.03872162872001055

N=10000

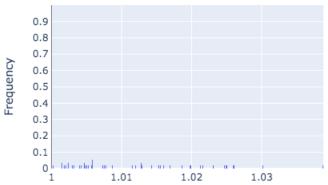
N=100, Nrep=56 Number of unphysical estimates=56



Sum of unphysical eigenvalues (>1)

Min: 1.0013980454688673 Max: 1.1073713855624088 |Max-Min|: 0.10597334009354142

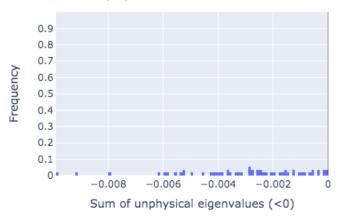
N=1000, Nrep=56 Number of unphysical estimates=56



Sum of unphysical eigenvalues (>1)

Min: 1.0000129998310041 Max: 1.038734628551015 |Max-Min|: 0.03872162872001095

# N=10000, Nrep=55 Number of unphysical estimates=55

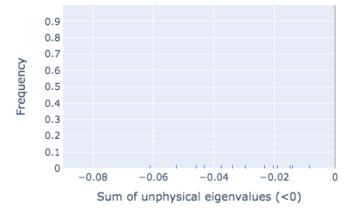


Min: -0.009820242830745339 Max: -1.367981286283877e-05 |Max-Min|: 0.0098065630178825

## **Case 1: LinearEstimator(False)**

#### N=100

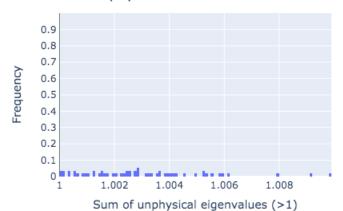
N=100, Nrep=48 Number of unphysical estimates=48



Min: -0.08974570791146932 Max: -0.002095608425328001 |Max-Min|: 0.08765009948614133

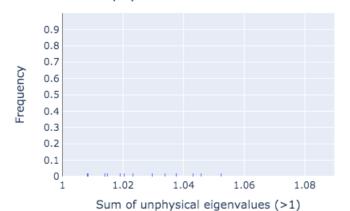
N=1000

N=10000, Nrep=55 Number of unphysical estimates=55



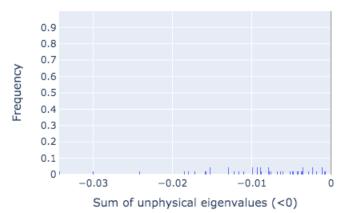
Min: 1.000013679812863 Max: 1.0098202428307452 |Max-Min|: 0.009806563017882297

N=100, Nrep=48 Number of unphysical estimates=48



Min: 1.0020956084253272 Max: 1.08974570791147 |Max-Min|: 0.08765009948614289

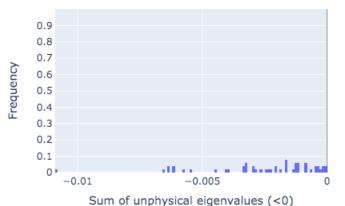
## N=1000, Nrep=46 Number of unphysical estimates=46



Min: -0.03429673403456271 Max: -0.0007654141411925565 |Max-Min|: 0.03353131989337015

N=10000

N=10000, Nrep=50 Number of unphysical estimates=50

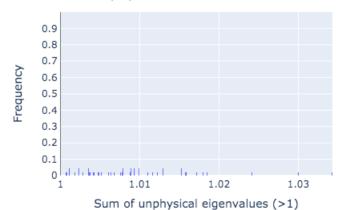


Min: -0.010864757054154343 Max: -4.852764506780333e-05 |Max-Min|: 0.01081622940908654

Case 2: ProjectedLinearEstimator(True)

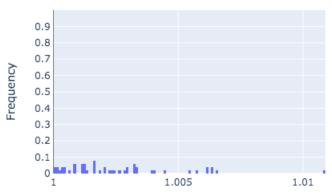
N=100

N=1000, Nrep=46 Number of unphysical estimates=46



Min: 1.0007654141411926 Max: 1.0342967340345623 |Max-Min|: 0.03353131989336977

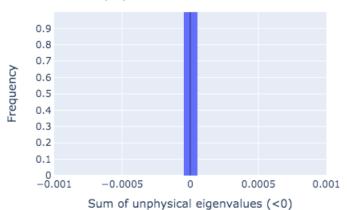
N=10000, Nrep=50 Number of unphysical estimates=50



Sum of unphysical eigenvalues (>1)

Min: 1.0000485276450675 Max: 1.0108647570541545 |Max-Min|: 0.010816229409086997

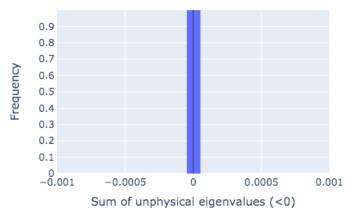
# N=100, Nrep=16 Number of unphysical estimates=16



Min: -9.306224459265484e-13 Max: -1.0114343792145144e-13 |Max-Min|: 8.29479008005097e-13

N=1000

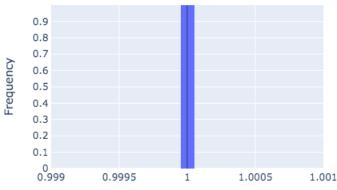
N=1000, Nrep=32 Number of unphysical estimates=32



Min: -1.2634835348919929e-11 Max: -1.0549739363132764e-13 |Max-Min|: 1.2529337955288602e-11

N=10000

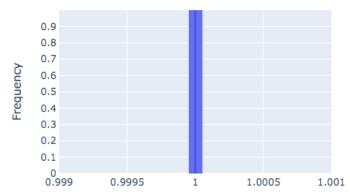
N=100, Nrep=16 Number of unphysical estimates=16



Sum of unphysical eigenvalues (>1)

Min: 1.000000000001013 Max: 1.000000000009304 |Max-Min|: 8.291145547900669e-13

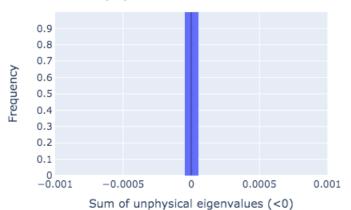
N=1000, Nrep=32 Number of unphysical estimates=32



Sum of unphysical eigenvalues (>1)

Min: 1.000000000001048 Max: 1.000000000126343 |Max-Min|: 1.2529532966709667e-11

## N=10000, Nrep=50 Number of unphysical estimates=50



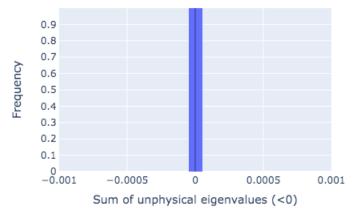
Min: -1.51670780996407e-10 Max: -1.0141518784760772e-13 Max-MinI: 1.515693658085594e-10

|Max-Min|: 1.515693658085594e-10

# Case 3: ProjectedLinearEstimator(False)

#### N=100

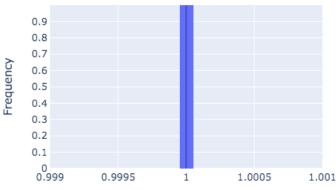
N=100, Nrep=17 Number of unphysical estimates=17



Min: -1.4889802201828985e-12 Max: -1.0116813698156475e-13 |Max-Min|: 1.3878120832013337e-12

N=1000

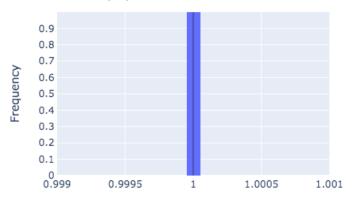
N=10000, Nrep=50 Number of unphysical estimates=50



Sum of unphysical eigenvalues (>1)

Min: 1.000000000001013 Max: 1.0000000001516711 |Max-Min|: 1.5156986776787562e-10

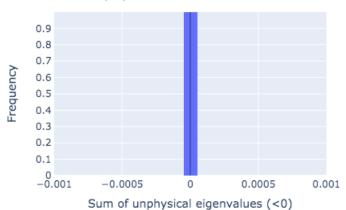
N=100, Nrep=17 Number of unphysical estimates=17



Sum of unphysical eigenvalues (>1)

Min: 1.000000000001013 Max: 1.000000000014884 |Max-Min|: 1.3871126469666706e-12

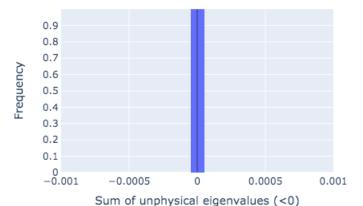
## N=1000, Nrep=30 Number of unphysical estimates=30



Min: -1.2158255693186201e-11 Max: -1.0561238991422653e-13 |Max-Min|: 1.2052643303271975e-11

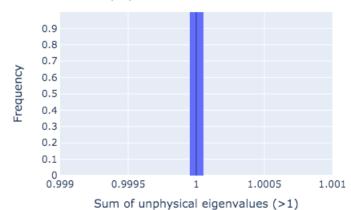
N=10000

N=10000, Nrep=50 Number of unphysical estimates=50



Min: -2.7945709912996674e-11 Max: -1.150714736951101e-13 |Max-Min|: 2.7830638439301564e-11

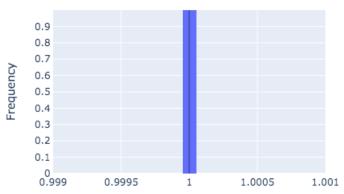
N=1000, Nrep=30 Number of unphysical estimates=30



Min: 1.000000000001057 Max: 1.000000000121578

|Max-Min|: 1.205213706612085e-11

N=10000, Nrep=50 Number of unphysical estimates=50



Sum of unphysical eigenvalues (>1)

Min: 1.000000000001146 Max: 1.0000000000279459 |Max-Min|: 2.783129282590835e-11