## Mjerenje uspješnosti investicijskih fondova

#### Učitavanje podataka i pomoćnih biblioteka

Prilikom proučavanja podataka primjetili smo da vrijednost fonda ErsteAdriaticEquity za 24.1.2016. poprilično odskače od okolnih datuma. Pretragom na stranici Erste grupe ustvrdili smo pogrešku u unosu podataka te smo ručno ispravili vrijednost.

```
library(reshape2)
library(dplyr)
library(magrittr)
library(ggplot2)
library(stringr)
library(xts)
require(quantmod)
require(PerformanceAnalytics)
source('data_extraction.r')
xs <- read_normalize('./investicijski_fondovi_data.csv')</pre>
```

### Priprema i analiza podataka

### Podjela prema tipovima fondova

```
investment_funds <- c("ERSTEAdriaticEquity", "OTPMeridian20", "ZBAktiv")
pension_funds <- c("RaiffeisenDMF", "ERSTEPlaviEXPERT", "ERSTEPlaviPROTECT")
market_portfolio <- c("CROBEX")

all_funds <- c(investment_funds, pension_funds)
data_columns <- c(pension_funds, investment_funds, market_portfolio)</pre>
```

#### Povrati

```
Računanje dnevnih povrata prema formuli: R(t) = \log(S(t)/S(t-1))

diff_function_log <- function(St, St_minus_one) log(St) - log(St_minus_one)

xs.returns <- to_time_series_diff_df(xs, data_columns, diff_function_log)
```

#### Sažeci

Prikaz mjera centralne tendencije

```
xs.returns.summary <- summary(xs.returns[data_columns] * 365)
data.frame(unclass(xs.returns.summary), check.names = FALSE, stringsAsFactors = FALSE)</pre>
```

```
## RaiffeisenDMF ERSTEPlaviEXPERT ERSTEPlaviPROTECT
## 1 Min. :-5.79209 Min. :-5.73634 Min. :-2.06945
## 2 1st Qu.:-0.18757 1st Qu.:-0.19025 1st Qu.:-0.05239
## 3 Median : 0.02441 Median : 0.02279 Median : 0.04456
## 4 Mean : 0.06451 Mean : 0.07278 Mean : 0.06709
```

```
## 5 3rd Qu.: 0.31443
                      3rd Qu.: 0.39346
                                        3rd Qu.: 0.20759
## 6 Max. : 8.91872
                      Max. : 4.58776
                                        Max. : 3.22798
                            OTPMeridian20
                                                     ZBAktiv
    ERSTEAdriaticEquity
         :-18.08756 Min.
                                                :-13.47776
## 1 Min.
                            :-23.51025
                                         Min.
## 2 1st Qu.: -0.48492
                       1st Qu.: -0.35673
                                         1st Qu.: -0.41271
## 3 Median : 0.00000
                      Median: 0.00000
                                        Median: 0.00000
## 4 Mean : 0.01423
                       Mean : 0.01395
                                         Mean : 0.03645
## 5 3rd Qu.: 0.50246
                       3rd Qu.: 0.63048
                                         3rd Qu.: 0.61738
## 6 Max.
         : 21.67018
                       Max. : 13.60614
                                         Max. : 34.35281
##
                CROBEX
## 1 Min.
          :-17.43339
## 2 1st Qu.: -0.58382
## 3 Median : 0.00000
## 4 Mean
         : -0.00203
## 5 3rd Qu.: 0.67653
## 6 Max.
         : 31.25453
```

### Mjere raspršenosti

Prikaz vrijednosti standardne devijacije i varijance za svaki fond

```
variances <- apply(xs.returns[all_funds] * 365, 2, var, na.rm = T)
std.devs <- apply(xs.returns[all_funds] * sqrt(365), 2, sd, na.rm = T)
data.frame(std.devs, variances)</pre>
```

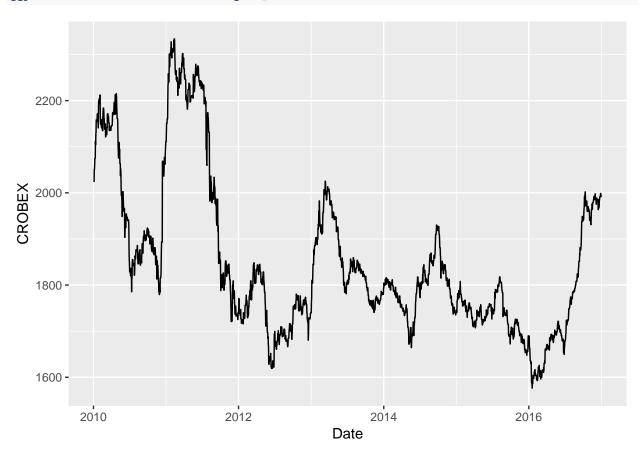
```
## ERSTEAdriaticEquity 0.08446841 2.6042430  
## OTPMeridian20 0.09034363 2.9791195  
## ZBAktiv 0.08987277 2.9481469  
## RaiffeisenDMF 0.03555447 0.4614040  
## ERSTEPlaviEXPERT 0.04020710 0.5900631  
## ERSTEPlaviPROTECT 0.01835943 0.1230300
```

### Grafički prikaz podataka

### Prikaz vrijednosti CROBEX-a po danima

Kretanje vrijednosti burzovnog indeksa od početka 2010. godine do kraja 2016. godine.

ggplot(xs, aes(Date, CROBEX)) + geom\_line()



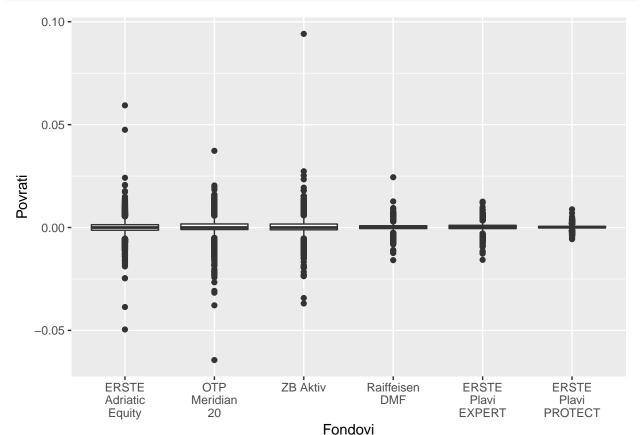
### Prikaz vrijednosti investicijskih i mirovinskih fondova po danima

Iz grafa se vidi kako investicijski fondovi imaju veću tendenciju rasta.



### Prikaz boxplotova za sve fondove

Iz ovog se grafa ne može zaključiti mnogo, ali vidi kako su investicijski fondovi (prva tri stupca) na dnevnoj bazi podložniji većim promjenama vrijednosti od mirovinskih, jer ima više stršećih vrijednosti.

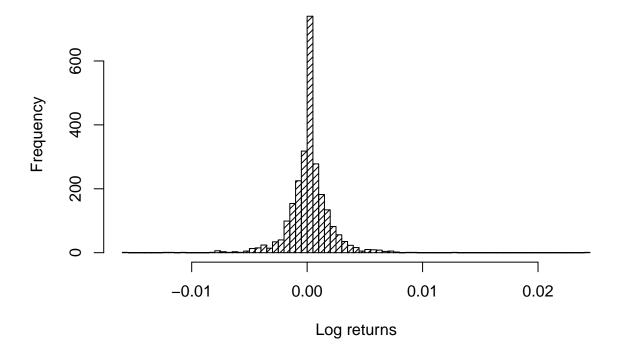


### Provjera normalnosti dnevnih povrata fondova

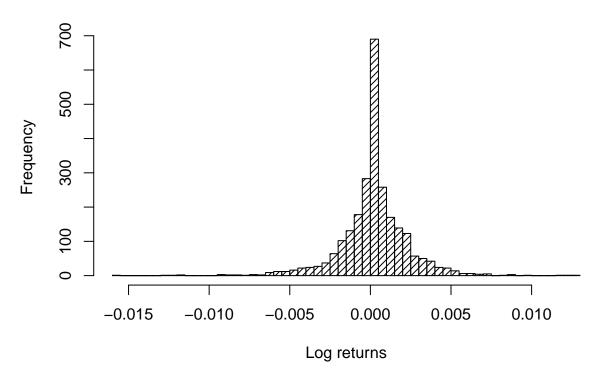
#### Histogramima

Iscrtavamo histograme povrata za svaki fond. Vidimo da imaju prilično teške repove, što ukazuje kako nisu baš normalno distribuirani.

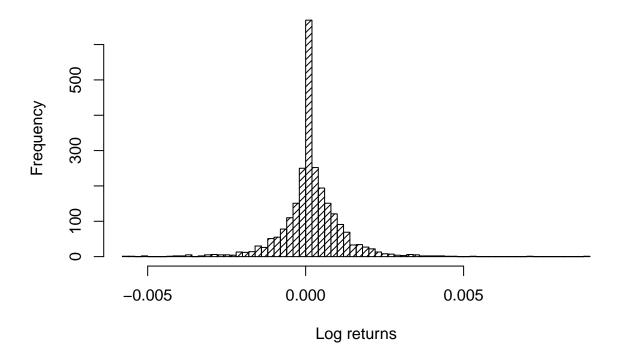
### RaiffeisenDMF



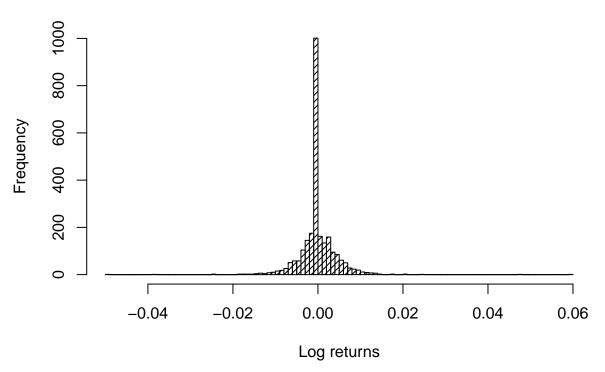
## **ERSTEPlaviEXPERT**

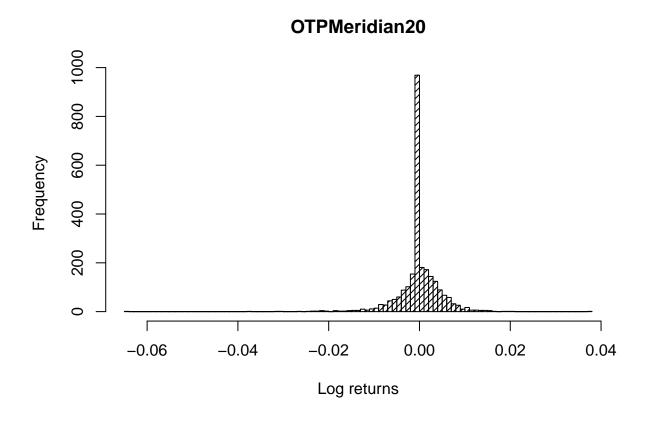


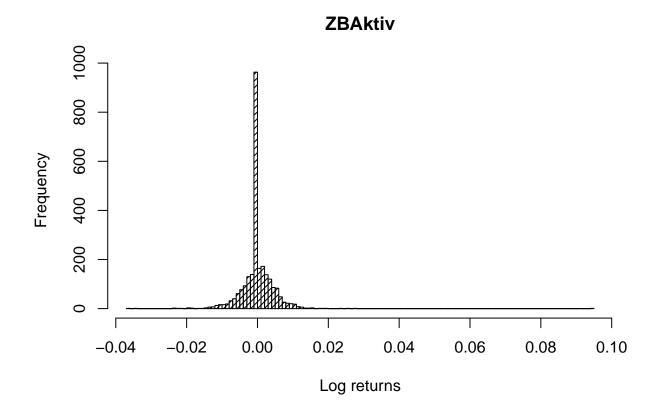
## **ERSTEPlaviPROTECT**



## **ERSTEAdriaticEquity**



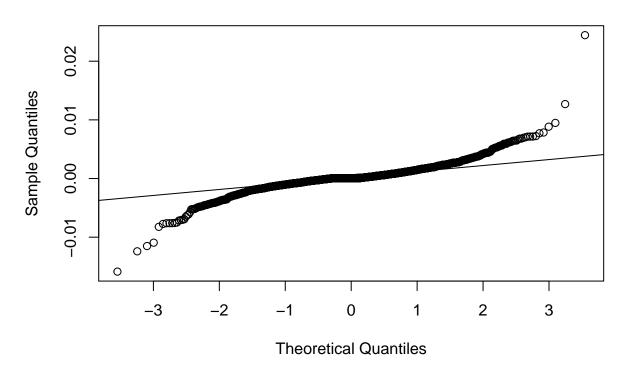




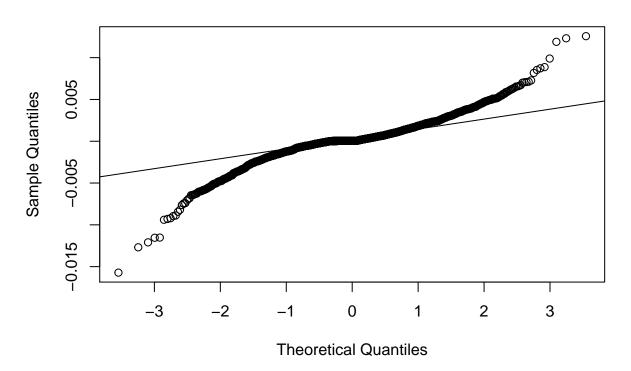
### $\mathbf{Q}\mathbf{Q}$ grafovima

Sljedećim QQ grafovima želimo ispitati normalnost distribucije povrata svih fondova. Teške repove primjećujemo radi sitne granulacije, tj. dnevnog računanja prinosa; u tako kratkom roku zna se dogoditi da pojedina dionica ili naglo naraste ili naglo padne u vrijednosti.

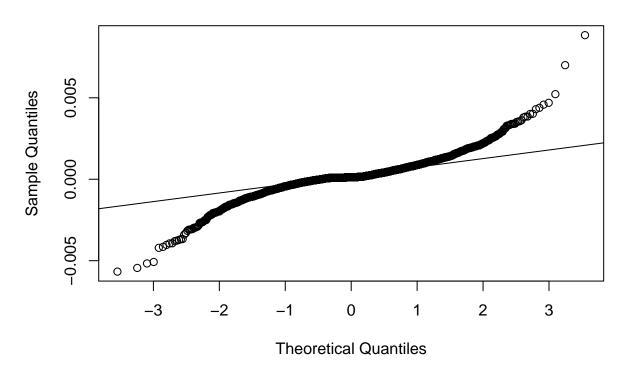
## RaiffeisenDMF



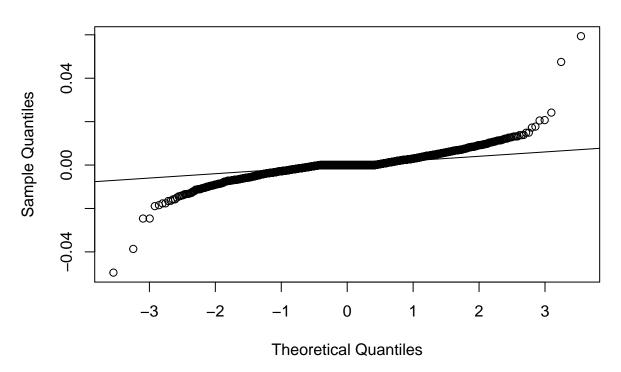
## **ERSTEPlaviEXPERT**



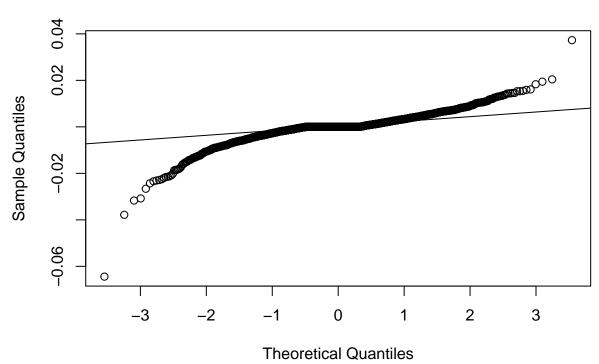
## **ERSTEPlaviPROTECT**



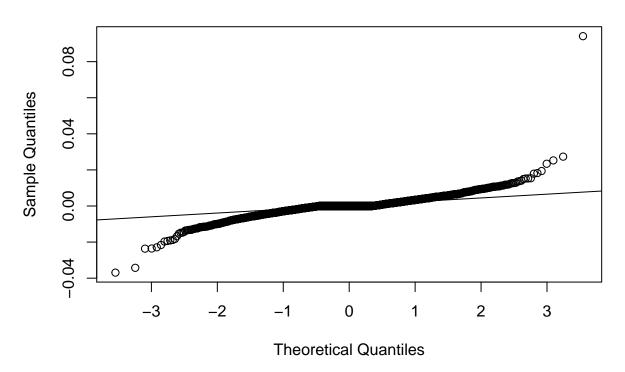
# **ERSTEAdriaticEquity**



## OTPMeridian20



## **ZBAktiv**



#### Testovi fondova

Iako QQ grafovi pokazuju da povrati nisu normalno raspodijeljeni, radimo tu pretpostavku s obzirom na robusnost T-testa. Jasno je da globalni događaji (kriza, teroristički napadi,...) često utječu na cijelo tržište odjednom, pa koristimo T-testove za uparene podatke.

#### Testovi povrata investicijskih fondova u odnosu na CROBEX

Za H0 hipotezu uzimamo kako su sredine investicijskih fondova i CROBEX indeksa jednake. Iz sljedećih testova vidimo da ne možemo opovrgnuti tu hipozetu.

```
OTPMeridian20
##
               ERSTEAdriaticEquity
## statistic
               -0.4774079
                                         -0.4286687
## parameter
               2552
                                         2552
## p.value
               0.6331126
                                         0.6682005
## conf.int
                                         Numeric, 2
               Numeric, 2
               -4.454166e-05
                                         -4.377476e-05
## estimate
## null.value 0
## alternative "two.sided"
                                         "two.sided"
               "Paired t-test"
                                         "Paired t-test"
## method
               "index and fund.returns" "index and fund.returns"
## data.name
##
               ZBAktiv
## statistic
              -0.8207028
## parameter
               2552
               0.4118922
## p.value
## conf.int
               Numeric, 2
## estimate
               -0.0001054245
## null.value 0
## alternative "two.sided"
## method
               "Paired t-test"
## data.name
               "index and fund.returns"
```

#### Testovi povrata mirovinskih fondova u odnosu na CROBEX

Za H0 hipotezu uzimamo kako su sredine mirovinskih fondova i CROBEX indeksa jednake. Iz sljedećih testova zaključujemo da možemo odbaciti H0 hipotezu uz nivo značajnosti 10%.k

```
mapply(compare.to.index(xs.returns$CROBEX), xs.returns[pension_funds])
```

```
##
               RaiffeisenDMF
                                         ERSTEPlaviEXPERT
## statistic
               -1.789106
                                         -2.125481
## parameter
               2552
                                         2552
## p.value
               0.07371632
                                         0.03364232
## conf.int
               Numeric, 2
                                         Numeric, 2
               -0.0001823123
                                         -0.0002049503
## estimate
## null.value 0
## alternative "two.sided"
                                         "two.sided"
## method
               "Paired t-test"
                                         "Paired t-test"
```

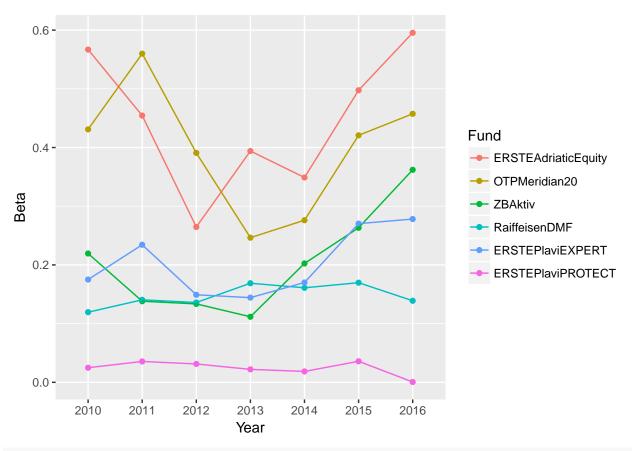
```
"index and fund.returns" "index and fund.returns"
## data.name
              ERSTEPlaviPROTECT
##
              -1.711485
## statistic
## parameter
              2552
## p.value
              0.08711319
## conf.int
              Numeric, 2
## estimate
              -0.0001893649
## null.value 0
## alternative "two.sided"
## method
              "Paired t-test"
## data.name
               "index and fund.returns"
```

#### Test povrata investicijskih fondova u odnosu na mirovinske fondove

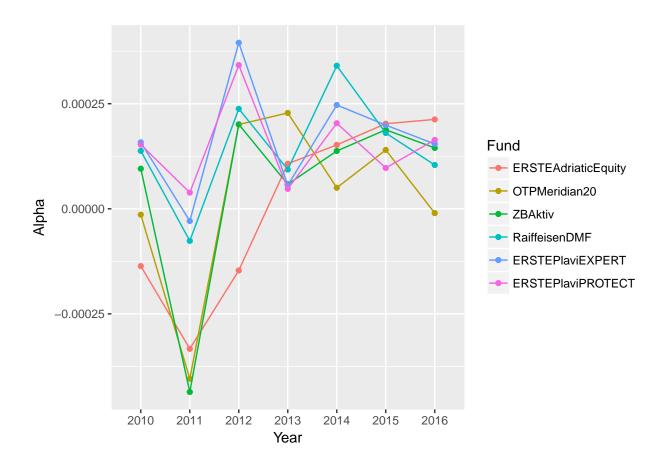
Izračunate su sredine mirovinskih i investicijskih fondova pa je sproveden test njihovih vrijednosti. Dobivamo izrazito malu p-vrijednost, stoga uz relativno veliku sigurnost zaključujemo da možemo odbaciti nul-hipotezu koja tvrdi da su sredine jednake.

#### CAPM model

```
year <- function(date) format(date, "%Y")</pre>
get_for_year <- function(df, dates, desired_year) df[year(dates) == desired_year, ]</pre>
get_capm_for_year <- function(df, fund, desired_year){</pre>
  xs.year = get_for_year(df, df$Date, desired_year)
  fund.year <- xs.year[c('Date', fund)]</pre>
  fund.ts <- xts(fund.year[, -1], order.by=fund.year$Date)</pre>
  capm.index.year <- xs.year[c('Date', 'CROBEX')]</pre>
  capm.index.ts <- xts(capm.index.year[, -1], order.by=capm.index.year$Date)</pre>
  capm.risk_free.year <- xs.year[c('Date', 'InterestRate.daily')]</pre>
  capm.risk_free.year <- capm.risk_free.year[1, -1]</pre>
  data.frame(fund, as.factor(desired_year),
              CAPM.alpha(fund.ts, capm.index.ts, capm.risk_free.year),
              CAPM.beta(fund.ts, capm.index.ts, capm.risk_free.year))
}
xs.years = seq(from = 2010, by = 1, length = 7)
xs.fund.names = c(investment_funds, pension_funds)
xs.capm <- data.frame(matrix(ncol = 3, nrow = 0))</pre>
for (i in 1:length(xs.fund.names)){
  for (j in 1:length(xs.years)){
    xs.capm <- rbind(xs.capm, get_capm_for_year(xs.returns, xs.fund.names[i], xs.years[j]))</pre>
}
colnames(xs.capm) <- c("Fund", "Year", "Alpha", "Beta")</pre>
ggplot(xs.capm, aes(Year, Beta, color= Fund, group = Fund)) +
  geom_point() + geom_line()
```



ggplot(xs.capm, aes(Year, Alpha, color= Fund, group = Fund)) +
geom\_point() + geom\_line()



### Provjera reziduala

```
nrows = nrow(xs.capm)
get_residuals_norm <- function(df, row) {</pre>
  xs.tmpYear <- get_for_year(xs.returns, xs.returns$Date, df[row,'Year'])</pre>
  fund <- as.character(df[row, 'Fund'])</pre>
  xs.tmpYearFund <- xs.tmpYear[,fund]</pre>
  capm.risk_free.year <- xs.tmpYear$InterestRate.daily</pre>
  capm.market.year <- xs.tmpYear$CROBEX</pre>
  residuals.tmp <- vector(mode="numeric", length=length(xs.tmpYearFund))</pre>
  for (i in 1:length(xs.tmpYearFund)) {
    residuals.tmp[i] <- ((xs.tmpYearFund[i] - capm.risk_free.year[i]) -</pre>
       (df[row,3] + df[row, 4] * (capm.market.year[i] - capm.risk_free.year[i])))
  }
  scaled.residuals.tmp <- scale(residuals.tmp)</pre>
  x <- ks.test(scaled.residuals.tmp, 'pnorm')</pre>
  df[row, 'KS.p'] <- x$p.value</pre>
  return(df)
```

```
for(i in 1:nrows) {
   xs.capm <- suppressWarnings( get_residuals_norm(xs.capm, i) )
}</pre>
```

### R kvadrat test prilagodbe modela

```
alpha_beta_r <- function(vals, alpha, beta, index, risk.free) {</pre>
  model <- alpha + beta * (index - risk.free) + risk.free
 SSE = (vals - model)^2 %>% sum
  SST = (vals - mean(vals))^2 %>% sum
  return(1 - SSE / SST)
}
rsquared.from_returns <- function(desired_year, fund, alpha, beta) {
  xs.curr <- xs.returns[year(xs.returns$Date) == desired_year, ]</pre>
  fund.actual.vals <- xs.curr[, as.character(fund)]</pre>
  return(alpha_beta_r(fund.actual.vals,
                       alpha, beta,
                       xs.curr$CROBEX,
                       xs.curr$InterestRate.daily))
}
xs.capm$R.squared <- mapply(rsquared.from_returns,</pre>
                             xs.capm$Year,
                             xs.capm$Fund,
                             xs.capm$Alpha,
                             xs.capm$Beta)
xs.capm
```

```
##
                     Fund Year
                                       Alpha
                                                     Beta
                                                                  KS.p
     ERSTEAdriaticEquity 2010 -1.363158e-04 0.5669352275 7.606159e-08
     ERSTEAdriaticEquity 2011 -3.331016e-04 0.4543998614 8.972995e-10
     ERSTEAdriaticEquity 2012 -1.467188e-04 0.2646270122 3.976819e-13
     ERSTEAdriaticEquity 2013 1.072103e-04 0.3940627807 3.095202e-11
     ERSTEAdriaticEquity 2014 1.520230e-04 0.3489534496 5.271628e-11
## 6
     ERSTEAdriaticEquity 2015
                               2.024548e-04 0.4975787045 2.888248e-09
## 7
     ERSTEAdriaticEquity 2016 2.126424e-04 0.5955184335 1.182900e-08
## 8
            OTPMeridian20 2010 -1.401558e-05 0.4309319208 2.925515e-10
## 9
            OTPMeridian20 2011 -4.044461e-04 0.5599034422 3.870977e-08
## 10
            OTPMeridian20 2012 2.005561e-04 0.3908358348 2.004861e-09
## 11
            OTPMeridian20 2013 2.280547e-04 0.2464292424 2.003044e-10
## 12
            OTPMeridian20 2014 5.006249e-05 0.2761167134 7.392093e-09
## 13
           OTPMeridian20 2015 1.400398e-04 0.4208172130 2.578632e-08
## 14
            OTPMeridian20 2016 -1.026420e-05 0.4574313828 5.335510e-12
## 15
                  ZBAktiv 2010 9.544554e-05 0.2194612955 2.049980e-04
## 16
                  ZBAktiv 2011 -4.358250e-04 0.1381375343 2.527614e-05
                  ZBAktiv 2012 2.009252e-04 0.1336074631 1.354321e-10
## 17
```

```
## 18
                  ZBAktiv 2013 5.840394e-05 0.1116804387 2.323343e-06
## 19
                  ZBAktiv 2014
                                1.375125e-04 0.2024930920 6.164473e-06
## 20
                  ZBAktiv 2015
                               1.880294e-04 0.2632705419 2.186302e-05
                  ZBAktiv 2016 1.448745e-04 0.3620458129 1.539224e-04
## 21
## 22
            RaiffeisenDMF 2010
                                1.378239e-04 0.1194627941 2.717111e-03
## 23
            RaiffeisenDMF 2011 -7.635330e-05 0.1405371249 3.224060e-06
            RaiffeisenDMF 2012 2.378826e-04 0.1359857205 1.741118e-11
## 24
            RaiffeisenDMF 2013
                                9.345165e-05 0.1687797266 2.118944e-04
## 25
## 26
            RaiffeisenDMF 2014
                                3.404221e-04 0.1610284601 2.405696e-04
## 27
            RaiffeisenDMF 2015
                                1.803462e-04 0.1697165854 1.146525e-03
## 28
            RaiffeisenDMF 2016
                                1.041926e-04 0.1389678904 2.727515e-06
         ERSTEPlaviEXPERT 2010
## 29
                                1.580814e-04 0.1750763495 2.160262e-04
##
  30
         ERSTEPlaviEXPERT 2011 -2.905792e-05 0.2343404356 1.988193e-04
## 31
         ERSTEPlaviEXPERT 2012
                                3.950473e-04 0.1491048287 7.504533e-05
## 32
         ERSTEPlaviEXPERT 2013
                                5.594323e-05 0.1442715157 3.300715e-04
## 33
         ERSTEPlaviEXPERT 2014
                                2.469191e-04 0.1700392710 2.902686e-03
##
  34
         ERSTEPlaviEXPERT 2015
                                1.991195e-04 0.2703175563 3.123242e-03
## 35
         ERSTEPlaviEXPERT 2016
                                1.542028e-04 0.2781643675 7.591789e-05
## 36
        ERSTEPlaviPROTECT 2010
                                1.528344e-04 0.0248670367 1.210117e-05
        ERSTEPlaviPROTECT 2011
## 37
                                3.855290e-05 0.0355562101 4.594969e-05
## 38
        ERSTEPlaviPROTECT 2012
                                3.418137e-04 0.0312794690 1.652921e-05
## 39
        ERSTEPlaviPROTECT 2013
                                4.735975e-05 0.0220619941 8.751553e-07
## 40
        ERSTEPlaviPROTECT 2014
                                2.035929e-04 0.0185440353 3.416949e-03
        ERSTEPlaviPROTECT 2015
                                9.710402e-05 0.0358210528 4.620251e-04
##
  41
        ERSTEPlaviPROTECT 2016 1.639057e-04 0.0005997816 2.693304e-05
##
  42
         R.squared
## 1
      6.639383e-01
      3.595653e-01
  2
## 3
     9.948311e-02
## 4
      2.788338e-01
## 5
      2.204703e-01
## 6
      3.111983e-01
## 7
      3.610346e-01
## 8
     3.027301e-01
## 9
     4.105272e-01
## 10 2.900392e-01
## 11 1.049314e-01
## 12 1.008854e-01
## 13 1.860068e-01
## 14 2.315158e-01
## 15 9.085646e-02
## 16 3.700341e-02
## 17 1.484719e-02
## 18 2.126078e-02
## 19 5.614227e-02
## 20 6.677313e-02
## 21 1.805736e-01
## 22 3.803706e-01
## 23 3.017203e-01
## 24 1.256158e-01
## 25 1.440430e-01
## 26 1.489808e-01
## 27 1.418445e-01
## 28 1.094703e-01
```

```
## 29 3.765089e-01

## 30 3.700067e-01

## 31 1.752146e-01

## 32 1.982458e-01

## 33 2.481500e-01

## 34 2.457412e-01

## 35 3.209855e-01

## 36 4.085443e-02

## 37 6.580049e-02

## 38 1.991347e-02

## 39 1.191934e-02

## 40 1.559203e-02

## 41 2.075516e-02

## 42 1.035892e-05
```

### **ANOVA**

```
num.items <- xs.returns %>% dim %>% first
anova.subset <- all_funds</pre>
anova.returns <- xs.returns %>%
  subset.data.frame(select=anova.subset) %>%
anova.factors.funds <- anova.subset %>%
 rep(rep(num.items, length(.))) %>%
  as.factor
anova(lm(anova.returns ~ anova.factors.funds))
## Analysis of Variance Table
## Response: anova.returns
                                        Mean Sq F value Pr(>F)
                          Df
                               Sum Sq
## anova.factors.funds
                           5 0.000069 1.3891e-05
                                                  1.144 0.3345
## Residuals
                      15312 0.185924 1.2142e-05
```

### 2-factor ANOVA