Mjerenje uspješnosti investicijskih fondova

Priprema podataka

Prilikom proučavanja podataka primjetili smo da vrijednost fonda ErsteAdriaticEquity za 24.1.2016. poprilično odskače od okolnih datuma. Pretragom na stranici Erste grupe ustvrdili smo pogrešku u unosu podataka te smo ručno ispravili vrijednost.

```
source_eval <- function(file) source(file, print.eval = TRUE)
source_eval('uncommon.r')
source('data_extraction.r')
xs <- read_normalize(CSV_DATA)</pre>
```

Priprema i analiza podataka

Podjela prema tipovima fondova

```
investment_funds <- c("ERSTEAdriaticEquity", "OTPMeridian20", "ZBAktiv")
pension_funds <- c("RaiffeisenDMF", "ERSTEPlaviEXPERT", "ERSTEPlaviPROTECT")
all_funds <- c(investment_funds, pension_funds)
market_portfolio <- c("CROBEX")

xs.market_portfolio <- to_data_frame(xs, market_portfolio, xs.market_portfolio)
xs.investment <- to_data_frame(xs, investment_funds, xs.investment)
xs.pension <- to_data_frame(xs, pension_funds, xs.pension)

data_columns <- c(pension_funds, investment_funds, market_portfolio)
xs.funds <- xs[, data_columns]</pre>
```

Povrati

Računanje dnevnih povrata

```
diff_function_log <- function(St, St_minus_one) log(St) - log(St_minus_one)
xs.returns <- to_time_series_diff_df(xs, data_columns, diff_function_log)
#Postavljanje velikih skokova u 0
#xs.returns$ERSTEAdriaticEquity[2211:2212] <- 0
#diff_function_sub <- function(St, St_minus_one) St - St_minus_one
#xs.returns <- to_time_series_diff_df(xs, data_columns, diff_function_sub)</pre>
```

Sažeci

```
xs.summary <- summary(xs.funds)
xs.returns.summary <- summary(xs.returns[data_columns] * 365)
# xs.log_returns.summary <- summary(xs.log_returns[data_columns])</pre>
```

```
df_summary <- function(summary) {</pre>
 return(data.frame(unclass(summary), check.names = FALSE, stringsAsFactors = FALSE))
df_summary(xs.returns.summary)
                         ERSTEPlaviEXPERT ERSTEPlaviPROTECT
##
         RaiffeisenDMF
## 1 Min.
           :-5.79209
                              :-5.73634
                                                 :-2.06945
                       Min.
                                          Min.
## 2 1st Qu.:-0.18757
                       1st Qu.:-0.19025
                                          1st Qu.:-0.05239
## 3 Median : 0.02441
                       Median : 0.02279
                                          Median: 0.04456
## 4 Mean
           : 0.06451
                       Mean
                              : 0.07278
                                          Mean
                                                : 0.06709
## 5 3rd Qu.: 0.31443
                       3rd Qu.: 0.39346
                                          3rd Qu.: 0.20759
## 6 Max.
           : 8.91872
                              : 4.58776
                                                 : 3.22798
                       Max.
                                          Max.
    ERSTEAdriaticEquity
                              OTPMeridian20
                                                        ZBAktiv
## 1 Min.
           :-18.08756 Min.
                               :-23.51025
                                                   :-13.47776
                                           Min.
## 2 1st Qu.: -0.48492
                        1st Qu.: -0.35673
                                            1st Qu.: -0.41271
## 3 Median : 0.00000 Median : 0.00000
                                            Median: 0.00000
## 4 Mean
           : 0.01423
                        Mean : 0.01395
                                            Mean : 0.03645
## 5 3rd Qu.: 0.50246
                        3rd Qu.: 0.63048
                                            3rd Qu.: 0.61738
## 6 Max.
          : 21.67018
                        Max. : 13.60614
                                            Max. : 34.35281
##
                 CROBEX
           :-17.43339
## 1 Min.
## 2 1st Qu.: -0.58382
## 3 Median : 0.00000
## 4 Mean
           : -0.00203
## 5 3rd Qu.: 0.67653
## 6 Max. : 31.25453
```

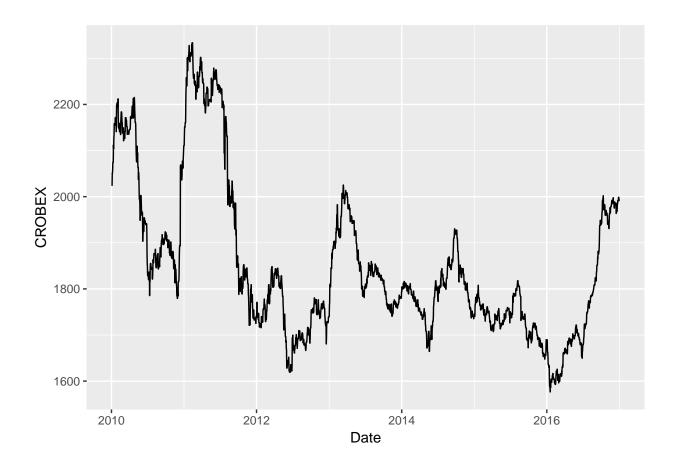
Mjere raspršenosti

```
apply(xs.returns[all_funds] * 365, 2, var, na.rm=T)
## ERSTEAdriaticEquity
                              OTPMeridian20
                                                          ZBAktiv
##
             2.6042430
                                   2.9791195
                                                        2.9481469
##
         RaiffeisenDMF
                           ERSTEPlaviEXPERT
                                               ERSTEPlaviPROTECT
                                  0.5900631
##
             0.4614040
                                                        0.1230300
apply(xs.returns[all_funds] * sqrt(365), 2, sd, na.rm=T)
## ERSTEAdriaticEquity
                              OTPMeridian20
                                                          ZBAktiv
##
            0.08446841
                                 0.09034363
                                                      0.08987277
                           ERSTEPlaviEXPERT
##
         {\tt RaiffeisenDMF}
                                               ERSTEPlaviPROTECT
##
            0.03555447
                                 0.04020710
                                                      0.01835943
```

Grafički prikaz podataka

Prikaz vrijednosti CROBEX-a po danima

```
ggplot(xs, aes(Date, CROBEX)) + geom_line()
```



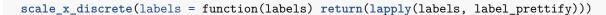
Prikaz vrijednosti investicijskih i mirovinskih fondova po danima

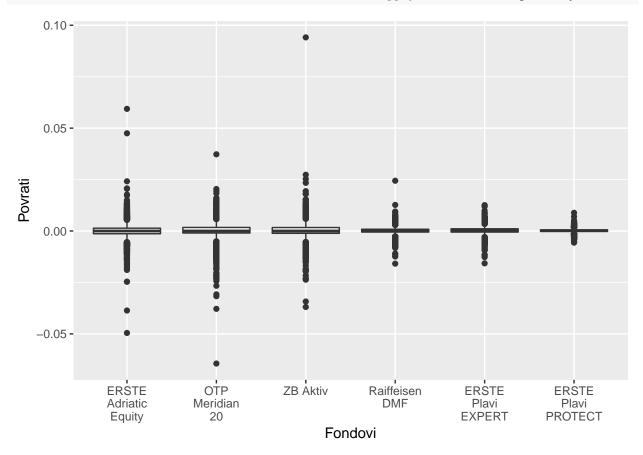


Prikaz boxplotova za sve fondove

ylab("Povrati") +

Iz ovih se grafova vidi kako su investicijski fondovi (prva tri stupca) podložniji većim promjenama vrijednosti od mirovinskih na dnevnoj bazi.

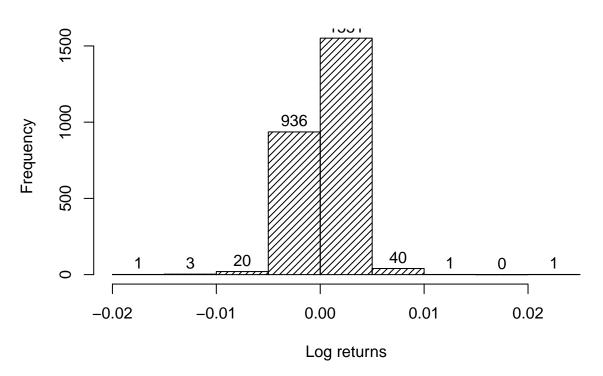




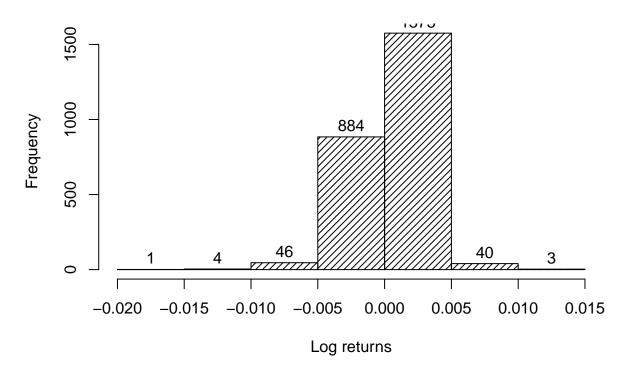
Provjera normalnosti

Sljedećim QQ grafovima želimo ispitati normalnost distribucije burzovnog indeksa. Iz QQ grafa vidimo kako podaci nisu u potpunosti normalni, a iz histograma jasno je i zašto. Teške repove primjećujemo radi sitne granulacije, tj. dnevnog računanja prinosa; u tako kratkom roku zna se dogoditi da pojedina dionica ili naglo naraste ili naglo padne u vrijednosti.

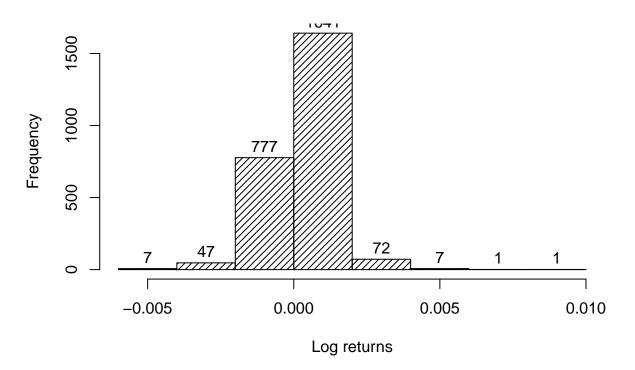
RaiffeisenDMF



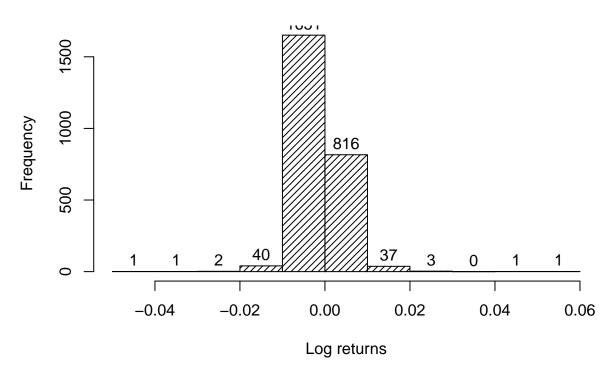
ERSTEPlaviEXPERT



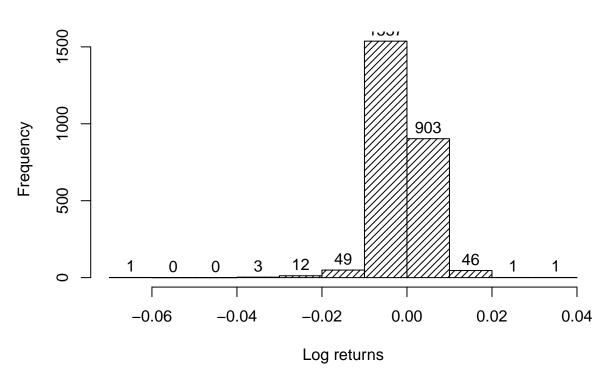
ERSTEPlaviPROTECT



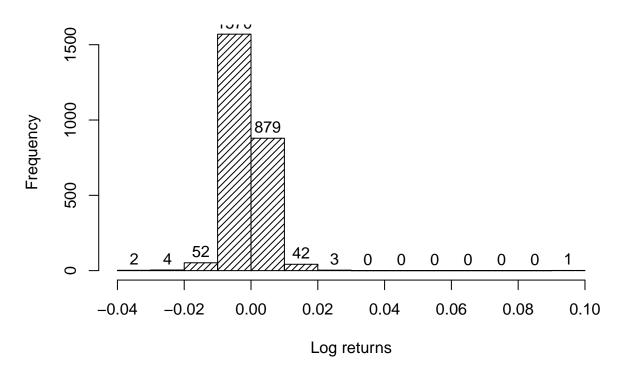
ERSTEAdriaticEquity



OTPMeridian20

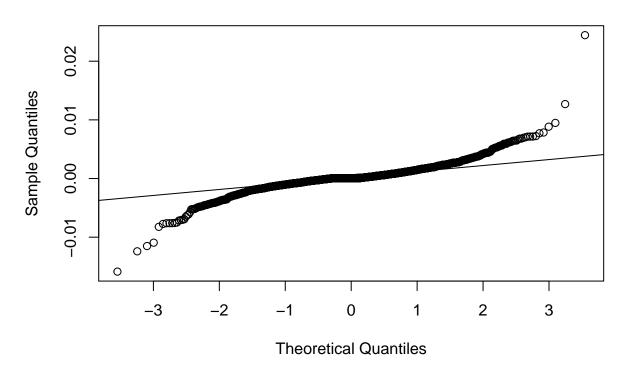


ZBAktiv

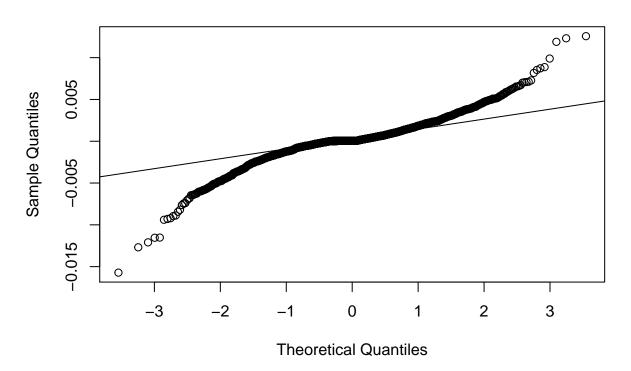


TODO: Kolmogorov-smirnov

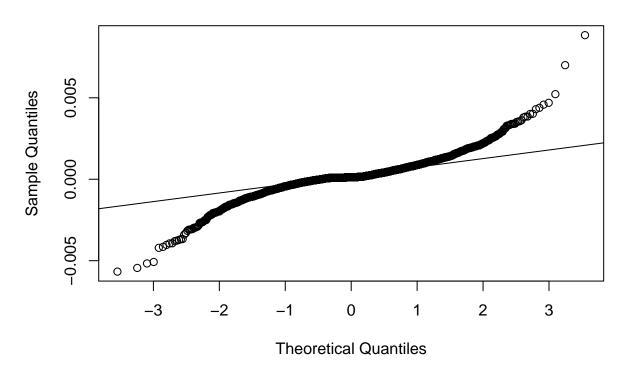
RaiffeisenDMF



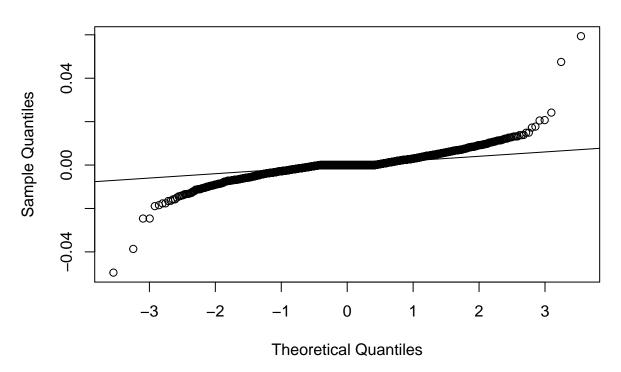
ERSTEPlaviEXPERT



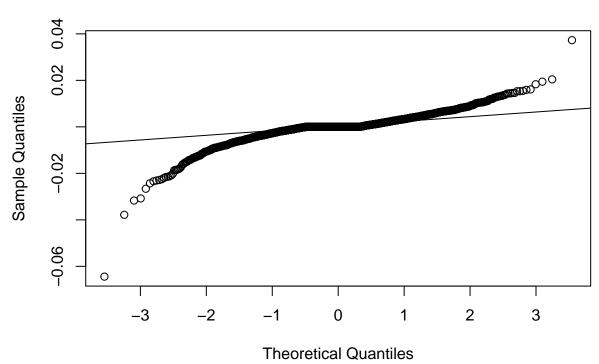
ERSTEPlaviPROTECT



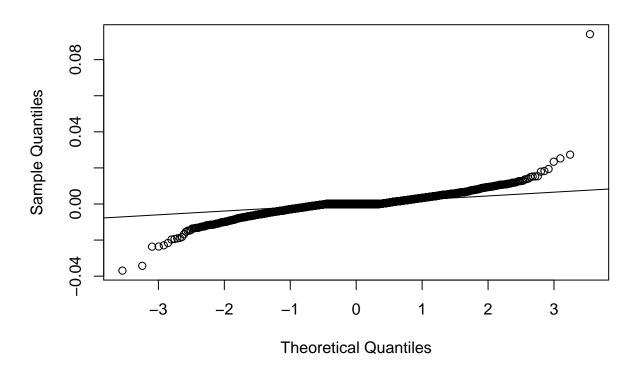
ERSTEAdriaticEquity



OTPMeridian20



ZBAktiv



Testovi fondova

Iako QQ grafovi pokazuju da povrati nisu normalno raspodijeljeni, radimo tu pretpostavku s obzirom na robusnost T-testa. Jasno je da globalni događaji (kriza, teroristički napadi,...) često utječu na cijelo tržište odjednom, pa koristimo T-testove za uparene podatke.

Testovi povrata investicijskih fondova u odnosu na CROBEX

```
## parameter
               2552
                                        2552
## p.value
               0.6331126
                                        0.6682005
## conf.int
                                        Numeric, 2
              Numeric, 2
              -4.454166e-05
                                        -4.377476e-05
## estimate
## null.value 0
## alternative "two.sided"
                                        "two.sided"
## method
              "Paired t-test"
                                        "Paired t-test"
              "index and fund.returns" "index and fund.returns"
## data.name
##
               ZBAktiv
              -0.8207028
## statistic
## parameter
              2552
## p.value
              0.4118922
## conf.int
              Numeric,2
## estimate
              -0.0001054245
## null.value 0
## alternative "two.sided"
## method
               "Paired t-test"
## data.name
               "index and fund.returns"
```

Testovi povrata mirovinskih fondova u odnosu na CROBEX

```
mapply(compare.to.index(xs.returns$CROBEX), xs.returns[pension_funds])
```

```
RaiffeisenDMF
                                        ERSTEPlaviEXPERT
                                        -2.125481
## statistic
               -1.789106
## parameter
               2552
                                        2552
## p.value
               0.07371632
                                        0.03364232
                                        Numeric,2
## conf.int
               Numeric, 2
## estimate
               -0.0001823123
                                        -0.0002049503
## null.value 0
## alternative "two.sided"
                                        "two.sided"
               "Paired t-test"
                                        "Paired t-test"
## method
## data.name
               "index and fund.returns" "index and fund.returns"
##
               ERSTEPlaviPROTECT
## statistic
               -1.711485
               2552
## parameter
## p.value
               0.08711319
## conf.int
               Numeric, 2
## estimate
               -0.0001893649
## null.value 0
## alternative "two.sided"
## method
              "Paired t-test"
## data.name
               "index and fund.returns"
```

Test povrata investicijskih fondova u odnosu na mirovinske fondove

Izračunate su sredine mirovinskih i investicijskih fondova pa je sproveden test njihovih vrijednosti. Dobivamo izrazito malu p-vrijednost, stoga uz relativno veliku sigurnost zaključujemo da možemo odbaciti nul-hipotezu koja tvrdi da su sredine jednake.

```
MeansInvestment = rowMeans(xs.returns[investment_funds]))
t.test(grouped.return.means$MeansPension, grouped.return.means$MeansInvestment, paired = TRUE)

##
## Paired t-test
##
## data: grouped.return.means$MeansPension and grouped.return.means$MeansInvestment
## t = 2.1921, df = 2552, p-value = 0.02846
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.346169e-05 2.417960e-04
## sample estimates:
## mean of the differences
## mean of the differences
## 0.0001276289
```

CAPM model

```
dates <- xs.returns$Date
year <- function(date) format(date, "%Y")</pre>
get_for_year <- function(df, dates, desired_year) df[year(dates) == desired_year, ]</pre>
xs.2010 <- get_for_year(xs.returns, xs.returns$Date, 2010)</pre>
zbaktiv.2010 <- xs.2010$ZBAktiv #xs.2010[c('Date', 'ZBAktiv')]
capm.market.2010 <- xs.2010$CROBEX #xs.2010[c('Date', 'CROBEX')]</pre>
capm.risk_free.2010 <- xs.2010$InterestRate.daily #[c('Date', 'InterestRate.daily')]</pre>
zbaktiv.model <- lm(formula = (zbaktiv.2010 - capm.risk_free.2010) ~ (capm.market.2010 - capm.risk_free
head(zbaktiv.model)
## $coefficients
##
        (Intercept) capm.market.2010
##
       8.227786e-05
                         2.194613e-01
##
## $residuals
##
    3.025737e-03 -4.470165e-04 -1.125709e-03 -4.469784e-03
##
                                                             5.749055e-03
                                             8
               6
                              7
                                                           9
##
   -1.422779e-04 -4.060959e-03 -1.413468e-02
                                               1.628328e-03
                                                              1.153703e-03
              11
                             12
                                            13
                                                          14
   -3.923409e-03
                 1.799371e-03 -1.422779e-04 -1.148207e-04
##
                                                               3.090839e-03
##
                             17
                                            18
                                                          19
   -9.275865e-03 -1.312774e-02 -1.015904e-03 -6.830567e-03 -1.422779e-04
##
##
              21
                             22
                                            23
                                                          24
    1.360527e-03 -3.813505e-03 -3.062942e-03
##
                                               4.800227e-03 -4.606474e-03
##
              26
                             27
                                            28
                                                          29
                                                                         30
    1.163421e-02 -1.422779e-04
                                7.209681e-04
                                                4.670183e-03 -5.655227e-03
##
##
              31
                             32
                                            33
                                                          34
## -1.558577e-02 6.086355e-04 2.601787e-03 -1.422779e-04
                                                              1.641154e-04
##
              36
                             37
                                            38
                                                          39
                                                                         40
```

2.547114e-03 3.003235e-03 7.063579e-03 -3.612323e-03 2.360591e-03

```
42
                              43
            41
  -1.422779e-04 2.683753e-04 3.523494e-03 -9.437075e-04 -3.287487e-03
            46
                    47
                              48
                                          49
   3.689455e-03 6.840831e-04 -1.422779e-04 7.620623e-04 -8.011311e-03
##
##
            51
                        52
                                     53
                                                  54
   3.911053e-03 -5.823963e-04  8.150183e-03  6.414179e-05 -1.422779e-04
##
            56
                       57
                             58
                                                59
##
   -8.340212e-04 3.518260e-03 9.003503e-04 -6.551485e-03
                                                     4.532554e-03
##
            61
                         62
                                     63
                                                  64
   5.709594e-03 -1.422779e-04 -2.551600e-04 -2.693673e-03
                                                      1.644888e-03
            66
                        67
                             68
                                                  69
  -3.936817e-03 -2.757829e-03 -2.199680e-03 -1.422779e-04 -1.311595e-04
            71
                        72
                              73
                                                  74
   3.144101e-03 2.084115e-03 -6.736422e-03 1.892815e-03
                                                     4.760239e-04
            76
                        77
                              78
                                          79
##
   -1.422779e-04
                1.554342e-03 2.222416e-04 -5.274909e-04
                                                      3.821001e-03
                              83
##
            81
                        82
                                                 84
   2.621817e-03
               5.466834e-03 -1.422779e-04 4.284530e-04 -2.880095e-03
                        87
                                    88
                                                 89
##
            86
   2.930759e-03
               9.567567e-03 -6.452707e-04 4.175215e-03 -1.422779e-04
##
           91
                       92
                              93
                                                94
  -1.422779e-04 -9.864963e-04 5.257048e-03 3.830297e-03
                  97
                             98
            96
                                           99
##
  -5.477205e-03 -1.422779e-04 3.265466e-04 -8.945669e-03
                                                     1.245684e-02
           101
                       102
                                   103
                                            104
  -1.753043e-03 -4.178301e-03 -2.520872e-03 -1.422779e-04
                                                     2.327119e-03
           106
                       107
                                   108
                                                109
   4.479376e-03 -2.213307e-03 5.564066e-03 4.111644e-03
                                                     9.326233e-04
          111
                      112
                                   113
                                                114
## -1.422779e-04 -2.355763e-03 -6.856218e-03 2.781178e-03 9.708215e-03
##
           116
                117
                            118
## -3.532648e-03 2.400760e-03 -1.422779e-04 3.436363e-04 -1.081434e-02
          121
                 122
                                   123
                                          124
## -6.628933e-03 -8.098720e-03 -9.129489e-03 2.720435e-02 -1.422779e-04
                                   128
                 127
          126
                                          129
## -3.705188e-03 -9.529607e-03 2.195334e-02 -2.896920e-03 -5.148515e-03
                       132
                                   133
## -5.711107e-03 -1.422779e-04 2.663304e-03 -4.233461e-03 -1.211006e-02
                        137
                                   138
## -6.356160e-03 -3.078393e-03 -4.673230e-03 -1.422779e-04 1.063729e-03
          141
                    142
                                   143
                                                144
## -7.666737e-03 8.450477e-03 1.350024e-02 -1.992360e-03 -6.670915e-03
           146
                       147
                                   148
                                                 149
## -1.422779e-04
               1.633695e-03 4.627718e-04 1.518149e-02 -1.921379e-02
                       152
                                   153
           151
                                                154
  -8.263972e-04 -6.857526e-03 -1.422779e-04 4.507199e-03 5.261117e-03
##
           156
                       157
                                    158
                                                 159
   1.842133e-03
               6.062512e-03 1.037744e-03 3.683170e-04 -1.422779e-04
                       162
                                    163
                                                164
           161
  -3.524443e-03
               2.227869e-03 2.789750e-03 -1.465069e-03 -6.280174e-03
                                                169
##
           166
                       167
                                   168
   6.389691e-03 -1.422779e-04 5.236598e-04 -1.345533e-02 1.088195e-04
                        172
                            173 174
           171
## -1.804282e-04 4.177383e-03 -1.422779e-04 -1.422779e-04 1.946542e-03
```

```
176
                   177
                                178
## -1.433795e-02 5.475015e-03 -3.573459e-03 3.947895e-03 -1.372501e-02
           181
                      182
                                183
                                              184
  -1.422779 \\ e^{-04} \quad 2.827835 \\ e^{-04} \quad 1.012240 \\ e^{-03} \quad 1.256244 \\ e^{-03} \quad 1.602491 \\ e^{-04}
##
            186
                         187
                                       188
   2.919647e-03 -2.147027e-03 -1.422779e-04 4.575906e-03 4.245051e-03
##
           191
                         192
                                      193
                                                    194
##
    4.731801e-03 -1.045075e-02 -1.311676e-02 -8.247260e-03 -1.422779e-04
##
            196
                          197
                                        198
                                                      199
   6.078356e-04 6.072006e-03 -3.854281e-03 1.192621e-02 5.319148e-03
            201
                          202
                                        203
                                                      204
  -3.726342e-05 -1.422779e-04 2.539422e-03 -2.526232e-03 -6.536442e-03
            206
                          207
                                       208
                                                     209
  -1.104574e-03 4.254821e-04 1.025097e-02 -1.422779e-04 -1.705335e-03
                          212
                                       213
                                                     214
            211
   -5.434077e-03 -2.436291e-03 -1.194577e-03 -1.422779e-04
                                                          1.330631e-03
##
            216
                          217
                                       218
                                                     219
   -1.422779e-04 -4.137103e-04 -8.891545e-03 -5.873309e-03 8.942820e-03
            221
                         222
                                       223
                                                     224
##
##
   6.892917e-03 9.606738e-03 -1.422779e-04 -1.660525e-04
                                                          4.668321e-03
##
            226
                         227
                                      228
                                                     229
                1.887936e-03 3.795401e-03 8.813685e-04 -1.422779e-04
    4.298550e-03
                          232
                                       233
                                                     234
            231
##
   -5.437598e-04 -3.940435e-03 -1.326203e-03 -1.502456e-03
                                                          4.632617e-03
##
            236
                          237
                                        238
                                                     239
   3.242167e-03 -1.422779e-04 2.152822e-04 2.483562e-03
                                                          8.607901e-03
            241
                          242
                                        243
                                                      244
   -4.497131e-05 -2.835148e-04 -5.700936e-03 -1.422779e-04
                                                          1.408947e-03
                                      248
            246
                         247
                                                      249
  -7.952797e-03 6.378684e-03 2.539374e-03 1.801488e-03 5.979473e-03
##
            251
                          252
                                        253
                                                      254
## -1.422779e-04 -1.491068e-03 8.590525e-04 -1.488771e-03 -5.489203e-03
            256
                   257
                                258
                                                     259
## -3.639121e-03 3.394330e-03 -1.422779e-04 -7.560073e-04 -1.369226e-03
                                       263
            261
                         262
                                                     264
## -1.585540e-03 -1.103781e-02 4.775733e-03 6.709783e-04 -1.422779e-04
           266
                         267
                                       268
## -1.191407e-03 1.195004e-03 8.979011e-04 -4.279850e-03 1.921430e-03
                                        273
            271
                          272
                                                      274
  -3.803051e-03 -1.422779e-04 1.103877e-03 1.125771e-02 -2.868345e-03
            276
                          277
                                        278
                                                     279
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## -1.422779e-04
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                9.641450e-03 -1.422779e-04 -1.645404e-04 -3.434870e-03
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  -4.409031e-03
                5.384932e-03 -1.997990e-03 -1.453621e-03 -1.422779e-04
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##
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                                                     304
## -1.422779e-04
                 3.007639e-04 -1.689232e-03 2.917322e-03 -7.627164e-03
            306
                          307
                                308
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##
   3.701935e-03 -1.422779e-04 5.693470e-04 4.465995e-03 2.048680e-03
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##
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##
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##
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##
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##
##
   $effects
##
##
        (Intercept) capm.market.2010
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##
##
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                                          -4.121939e-03
                                                             1.651220e-03
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##
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##
##
                        -2.904293e-04
##
       2.453636e-03
                                           2.155908e-05
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##
                                          -3.768629e-03
##
       2.883789e-03
                         6.921115e-03
                                                             2.212440e-03
##
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                         1.277229e-04
                                           3.387209e-03
                                                            -1.144381e-03
##
##
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##
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                         3.518574e-03
                                                            -2.904293e-04
##
##
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                        -8.132671e-03
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                                                            -6.987358e-04
##
##
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                        -8.400969e-05
                                          -2.904293e-04
                                                            -9.948049e-04
##
##
       3.361727e-03
                         8.050524e-04
                                          -6.709185e-03
                                                             4.362279e-03
```

| шш | | | | |
|----------|---------------|---------------|---------------|---------------|
| ## ## | 5.561443e-03 | -2.904293e-04 | -4.053728e-04 | -2.817244e-03 |
| ## ## | 1.465679e-03 | -4.083060e-03 | -2.961252e-03 | -2.347832e-03 |
| ## ## | -2.904293e-04 | -2.791080e-04 | 3.012763e-03 | 1.927909e-03 |
| ## | -6.877315e-03 | 1.764878e-03 | 3.278724e-04 | -2.904293e-04 |
| ## ## | 1.437173e-03 | 5.818563e-05 | -6.657587e-04 | 3.668279e-03 |
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| ## ## | 5.896534e-03 | 8.980793e-04 | 2.201655e-04 | -2.904293e-04 |
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| ## ## | -1.360348e-02 | -3.474665e-05 | -3.330412e-04 | 4.029232e-03 |
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| ## ## | 4.513915e-03 | 4.034846e-03 | 4.579121e-03 | -1.066105e-02 |
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| ## ## | -1.854149e-04 | -2.904293e-04 | 2.440242e-03 | -2.691051e-03 |
| ## ## | -6.707016e-03 | -1.305012e-03 | 2.915525e-04 | 1.010282e-02 |
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##
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      2.945819e-03
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##
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##
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##
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                                                        1.111427e-02
##
##
##
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                                                        -2.904293e-04
##
      4.205789e-04
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##
##
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                                                        -4.983412e-04
##
##
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                                       4.962510e-03
                                                        3.784971e-03
##
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                                                        -1.099594e-02
##
##
##
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                                                        -8.144254e-03
##
##
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##
     -3.103495e-03
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                                       -2.910645e-03
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##
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##
##
##
     -2.399337e-03
##
## $rank
## [1] 2
##
## $fitted.values
                            2
                                           3
##
                                                         4
                                                                       5
   3.026752e-03 8.227786e-05 1.065709e-03 1.662949e-03 8.227786e-05
##
                            7
                                           8
                                                        9
   8.227786e-05 4.000959e-03 -7.192389e-04 2.619371e-03 3.202746e-04
##
##
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```
2.841019e-03 8.227786e-05 8.227786e-05 5.482073e-05 -1.945191e-04
##
                                          18
                                                         19
              16
                            17
                                                            8.227786e-05
##
    1.449630e-03
                  3.694846e-04 -1.540716e-03 8.227786e-05
                            22
                                           23
                                                                        25
##
              21
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##
   -1.420527e-03
                  3.124179e-03
                                2.898016e-03 -1.494100e-04
                                                             7.795969e-04
                                          28
##
              26
                            27
    8.227786e-05
                  8.227786e-05 -7.809681e-04 -7.877117e-05
##
              31
                            32
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                                                         34
##
   -3.279636e-03 -2.780123e-03 8.227786e-05
                                              8.227786e-05
                                                            -2.241154e-04
                            37
##
              36
                                           38
                                                         39
##
    1.284965e-03 -1.489670e-03 -2.291616e-04
                                               5.288101e-04
                                                             8.227786e-05
##
              41
                            42
                                           43
                                                         44
##
   8.227786e-05 -3.283753e-04 -5.675281e-04
                                               2.958397e-03
                                                             9.450918e-04
##
              46
                            47
                                           48
                                                         49
    1.326961e-03 8.227786e-05 8.227786e-05 -8.220623e-04
##
                                                            -1.384856e-03
##
              51
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                                                         54
                                                                        55
    8.532556e-05 -1.659763e-03 -4.385260e-04
                                               8.227786e-05
                                                             8.227786e-05
##
              56
                            57
                                           58
##
                 5.412107e-04 -2.812012e-03
##
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##
              61
                            62
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##
   8.227786e-05
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##
              66
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                                           68
   -2.222362e-05
                  3.108971e-03 8.227786e-05 8.227786e-05
                                                             7.115952e-05
##
##
              71
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##
   -8.384530e-04
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                                                             8.227786e-05
##
              76
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                                          78
                                                                        80
   8.227786e-05 -1.614342e-03
                               9.532162e-04 -4.589593e-04
                                                             3.325609e-04
##
##
              81
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                                          83
                                                         84
    8.330302e-05
                  8.227786e-05
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##
                                                             2.743980e-04
##
              86
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                                                         89
##
    6.729943e-04
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                                8.227786e-05
                                              8.227786e-05
                                                             8.227786e-05
##
              91
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##
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##
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    8.227786e-05
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##
                                         103
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##
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##
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##
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##
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##
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                                                        139
##
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##
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##
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```

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##
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                                                         154
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##
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##
             171
                            172
                                          173
                                                         174
                                                                        175
##
    3.265925e-04
                  8.227786e-05 8.227786e-05
                                               8.227786e-05 -2.006542e-03
##
             176
                            177
                                          178
                                                         179
                                                                        180
##
   -5.413844e-03 -2.295553e-03 -8.780165e-04 -2.018886e-03
                                                              8.227786e-05
##
             181
                           182
                                          183
    8.227786e-05 -3.427835e-04 -1.269295e-05 -5.752286e-04
##
                                                               2.105088e-03
##
             186
                            187
                                           188
                                                          189
                  8.227786e-05
                                8.227786e-05 -4.635906e-03
   -1.397285e-03
                                                               3.480365e-03
##
                            192
                                          193
##
             191
                                                         194
                                1.440999e-03 8.227786e-05
##
    3.302506e-04
                  3.485516e-03
                                                               8.227786e-05
##
             196
                            197
                                           198
                                                         199
##
   -6.678356e-04 -6.858933e-04
                                 1.668370e-04
                                                4.415883e-04 -2.198843e-04
##
             201
                            202
                                           203
                                                         204
    8.227786e-05
                  8.227786e-05 -2.599422e-03
                                                9.950252e-04
##
                                                               1.310107e-03
##
                            207
                                           208
##
    2.945514e-03 -6.965194e-04
                                8.227786e-05
                                               8.227786e-05
                                                              1.645335e-03
##
             211
                            212
                                          213
                                                         214
                                                                        215
    8.731007e-04 -1.447188e-04
                                 8.227786e-05
                                                8.227786e-05
                                                               8.227786e-05
##
##
             216
                            217
                                           218
                                                         219
                                 1.127428e-03 -1.737107e-03 -1.558353e-03
##
    8.227786e-05
                  3.537103e-04
##
             221
                            222
                                           223
                                                         224
##
   -1.142326e-03
                  8.227786e-05
                                 8.227786e-05
                                                1.060525e-04
                                                               8.890869e-04
##
             226
                            227
                                           228
                                                         229
                                                                        230
##
    1.640020e-03
                  2.151176e-04
                                 7.640193e-04
                                                8.227786e-05
                                                               8.227786e-05
                                           233
##
             231
                            232
                                                         234
                                                                        235
    4.837598e-04
                 -1.762631e-03 -2.031749e-03
                                                7.195767e-04
                                                               8.703927e-04
##
                                          238
##
             236
                            237
                                                         239
##
    8.227786e-05
                  8.227786e-05 -2.752822e-04 -3.957727e-04
                                                               2.002390e-03
                                           243
                                                         244
##
             241
                            242
                  1.736451e-03
                                 8.227786e-05
                                                8.227786e-05
##
    1.399113e-03
                                                             -1.468947e-03
##
             246
                            247
                                           248
                                                         249
   -7.590964e-04
                  2.314552e-03
                                 1.445939e-03
                                                7.592170e-04
                                                               8.227786e-05
##
             251
                            252
                                           253
                                                         254
                                                                        255
##
    8.227786e-05
                  1.431068e-03 -9.190525e-04
                                                2.708916e-05
                                                               3.063957e-04
##
             256
                            257
                                           258
                                                         259
   -1.570065e-03
                  8.227786e-05
                                 8.227786e-05
                                                6.960073e-04
                                                               8.047611e-04
             261
                            262
                                           263
                                                          264
                                                                        265
##
   -1.000607e-03 -9.071603e-06
                                 9.779406e-04
                                                8.227786e-05
                                                               8.227786e-05
             266
                            267
                                           268
                                                         269
                                                                        270
##
    1.131407e-03
                 9.780465e-04
                                 2.580277e-04 -8.563032e-04
                                                               7.628920e-04
             271
                            272
                                           273
                                                         274
                                                                        275
##
                  8.227786e-05 -1.163877e-03 -3.753501e-04
##
    8.227786e-05
                                                               1.194790e-03
##
             276
                            277
                                          278
                                                         279
##
   -1.419624e-03
                 8.227786e-05 8.227786e-05 8.227786e-05
                                                              4.774225e-04
##
             281
                            282
                                           283
                                                         284
                                                                        285
```

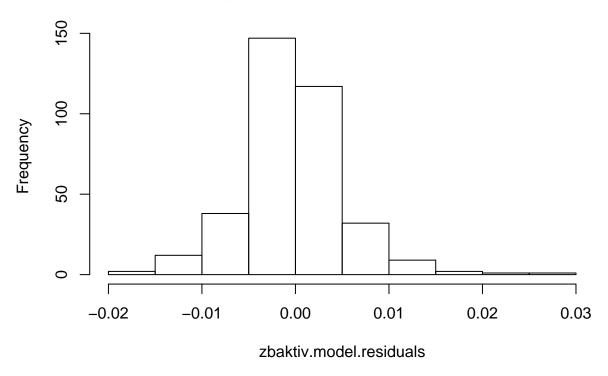
```
-1.941252e-03
                  1.112563e-03 -6.717083e-04
                                                1.708622e-03
##
              286
                             287
                                            288
                                                           289
                                                                          290
    8.227786e-05
                                                                2.762071e-04
##
                  -9.744887e-05
                                 -1.547726e-03 -1.350615e-03
                                            293
                                                                          295
##
             291
                             292
                                                           294
##
   -6.757203e-04
                   8.227786e-05
                                  8.227786e-05
                                                 1.045404e-04
                                                                2.471119e-03
##
             296
                                            298
                                                           299
                             297
                                                                          300
    1.028273e-03
                  -9.193549e-04
                                 -2.688389e-03
                                                 8.227786e-05
##
                                                                8.227786e-05
##
              301
                             302
                                            303
                                                           304
                                                                          305
##
    8.227786e-05
                  -3.607639e-04
                                  1.124411e-03
                                                 6.517138e-04
                                                                2.958735e-04
##
              306
                             307
                                            308
                                                           309
                                                                          310
##
    8.227786e-05
                   8.227786e-05
                                 -6.293470e-04
                                                -1.199546e-03
                                                               -2.309969e-03
##
              311
                                            313
                                                           314
                             312
                                                                          315
##
    1.985414e-03
                   3.900141e-04
                                  8.227786e-05
                                                 8.227786e-05
                                                               -2.150019e-03
##
              316
                             317
                                            318
                                                           319
                                                                          320
##
   -3.605084e-03
                   4.251177e-03
                                  6.314844e-04 -1.102066e-03
                                                                8.227786e-05
##
                             322
                                            323
                                                           324
                                                                          325
    8.227786e-05
                  -1.246260e-03 -1.760110e-03 -6.633952e-04
                                                               -6.136252e-04
##
##
              326
                             327
                                            328
                                                           329
                                                                          330
   -2.271909e-03
                   8.227786e-05
                                  8.227786e-05
                                                -6.159793e-04
                                                                1.055779e-03
##
##
             331
                             332
                                            333
                                                           334
                                                                          335
##
    1.095488e-03
                  -1.252903e-03
                                  3.871590e-03
                                                 8.227786e-05
                                                                8.227786e-05
##
              336
                             337
                                            338
                                                           339
                                                 3.305382e-03
##
    2.864611e-04
                   1.073908e-03
                                  3.641758e-03
                                                                1.342157e-03
##
                             342
                                                           344
                                                                7.388392e-04
                                  4.634838e-05
##
    8.227786e-05
                   8.227786e-05
                                                 1.887449e-02
##
              346
                             347
                                            348
                                                           349
                                                                          350
##
   -3.144979e-03
                   6.907463e-04
                                  8.227786e-05
                                                 8.227786e-05
                                                               -4.755997e-04
##
              351
                             352
                                            353
                                                           354
                                                                          355
##
   -2.257532e-04
                   1.019029e-03
                                  2.369110e-03
                                                 1.210480e-03
                                                                8.227786e-05
##
              356
                             357
                                            358
                                                           359
                                                                          360
##
    8.227786e-05 -1.535022e-03
                                 1.965686e-03
                                                1.132994e-03
                                                               1.288906e-03
##
             361
##
    1.114990e-03
##
## $assign
  [1] 0 1
```

Provjera reziduala

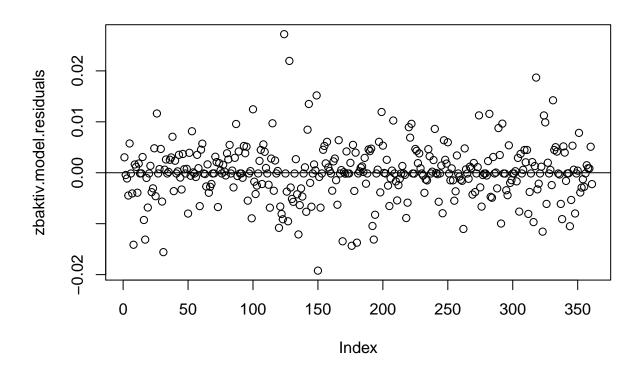
TODO: regresija / vrijednosti i raspodjela reziduala

```
# https://www.r-bloggers.com/r-tutorial-series-simple-linear-regression/
zbaktiv.model.summary <- summary(zbaktiv.model)
zbaktiv.model.residuals <- zbaktiv.model.summary$residuals
hist(zbaktiv.model.residuals)</pre>
```

Histogram of zbaktiv.model.residuals

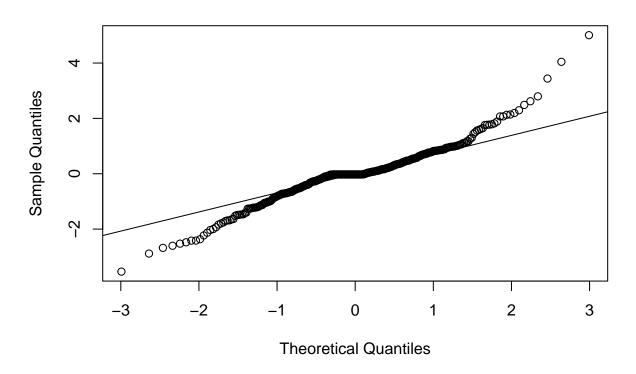


plot(zbaktiv.model.residuals)
abline(0,0)



qqnorm(rstandard(zbaktiv.model))
qqline(rstandard(zbaktiv.model))

Normal Q-Q Plot



```
ks.test(rstandard(zbaktiv.model), 'pnorm')

## Warning in ks.test(rstandard(zbaktiv.model), "pnorm"): ties should not be
## present for the Kolmogorov-Smirnov test

##

## One-sample Kolmogorov-Smirnov test

##

## data: rstandard(zbaktiv.model)

## D = 0.11279, p-value = 0.000205

## alternative hypothesis: two-sided
```

CAPM model 2

```
TODO: tablica modela (alpha / beta) <- VERIFY

require(quantmod)

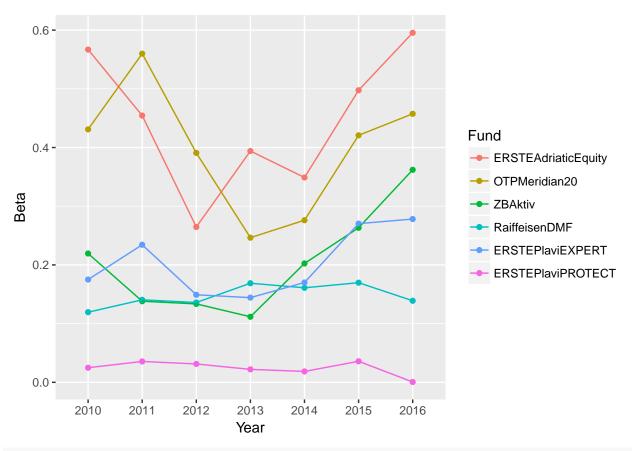
## Loading required package: quantmod

## Loading required package: xts
```

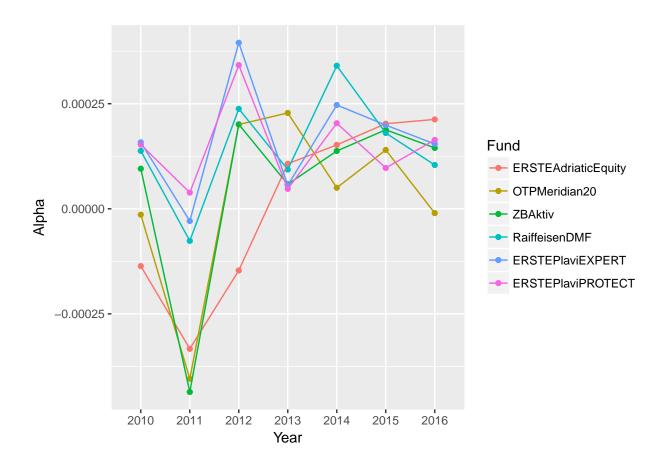
```
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
```

```
##
##
       as.Date, as.Date.numeric
## Loading required package: TTR
## Version 0.4-0 included new data defaults. See ?getSymbols.
require(PerformanceAnalytics)
## Loading required package: PerformanceAnalytics
## Attaching package: 'PerformanceAnalytics'
## The following object is masked from 'package:graphics':
##
##
       legend
library(xts)
get capm for year <- function(df, fund, desired year){</pre>
  xs.year = get_for_year(df, df$Date, desired_year)
  fund.year <- xs.year[c('Date', fund)]</pre>
  fund.ts <- xts(fund.year[, -1], order.by=fund.year$Date)</pre>
  capm.index.year <- xs.year[c('Date', 'CROBEX')]</pre>
  capm.index.ts <- xts(capm.index.year[, -1], order.by=capm.index.year$Date)</pre>
  capm.risk_free.year <- xs.year[c('Date', 'InterestRate.daily')]</pre>
  capm.risk_free.year <- capm.risk_free.year[1, -1]</pre>
  data.frame(fund, as.factor(desired_year),
             CAPM.alpha(fund.ts, capm.index.ts, capm.risk_free.year),
             CAPM.beta(fund.ts, capm.index.ts, capm.risk_free.year))
}
xs.years = seq(from = 2010, by = 1, length = 7)
xs.fund.names = c(investment_funds, pension_funds)
xs.capm <- data.frame(matrix(ncol = 3, nrow = 0))</pre>
for (i in 1:length(xs.fund.names)){
 for (j in 1:length(xs.years)){
    xs.capm <- rbind(xs.capm, get_capm_for_year(xs.returns, xs.fund.names[i], xs.years[j]))</pre>
}
colnames(xs.capm) <- c("Fund", "Year", "Alpha", "Beta")</pre>
xs.capm
##
                     Fund Year
                                        Alpha
                                                       Beta
## 1 ERSTEAdriaticEquity 2010 -1.363158e-04 0.5669352275
## 2 ERSTEAdriaticEquity 2011 -3.331016e-04 0.4543998614
## 3 ERSTEAdriaticEquity 2012 -1.467188e-04 0.2646270122
## 4 ERSTEAdriaticEquity 2013 1.072103e-04 0.3940627807
## 5 ERSTEAdriaticEquity 2014 1.520230e-04 0.3489534496
## 6 ERSTEAdriaticEquity 2015 2.024548e-04 0.4975787045
```

```
ERSTEAdriaticEquity 2016 2.126424e-04 0.5955184335
## 8
            OTPMeridian20 2010 -1.401558e-05 0.4309319208
## 9
            OTPMeridian20 2011 -4.044461e-04 0.5599034422
## 10
            OTPMeridian20 2012 2.005561e-04 0.3908358348
## 11
            OTPMeridian20 2013
                                2.280547e-04 0.2464292424
## 12
            OTPMeridian20 2014
                                5.006249e-05 0.2761167134
## 13
            OTPMeridian20 2015
                                1.400398e-04 0.4208172130
            OTPMeridian20 2016 -1.026420e-05 0.4574313828
## 14
## 15
                  ZBAktiv 2010
                                9.544554e-05 0.2194612955
## 16
                  ZBAktiv 2011 -4.358250e-04 0.1381375343
## 17
                  ZBAktiv 2012 2.009252e-04 0.1336074631
## 18
                  ZBAktiv 2013 5.840394e-05 0.1116804387
## 19
                  ZBAktiv 2014
                                1.375125e-04 0.2024930920
## 20
                  ZBAktiv 2015
                                1.880294e-04 0.2632705419
## 21
                  ZBAktiv 2016
                               1.448745e-04 0.3620458129
## 22
            RaiffeisenDMF 2010
                                1.378239e-04 0.1194627941
## 23
            RaiffeisenDMF 2011 -7.635330e-05 0.1405371249
## 24
            RaiffeisenDMF 2012
                                2.378826e-04 0.1359857205
## 25
            RaiffeisenDMF 2013
                                9.345165e-05 0.1687797266
## 26
            RaiffeisenDMF 2014
                                3.404221e-04 0.1610284601
## 27
            RaiffeisenDMF 2015
                                1.803462e-04 0.1697165854
## 28
            RaiffeisenDMF 2016
                                1.041926e-04 0.1389678904
## 29
         ERSTEPlaviEXPERT 2010
                                1.580814e-04 0.1750763495
## 30
         ERSTEPlaviEXPERT 2011 -2.905792e-05 0.2343404356
         ERSTEPlaviEXPERT 2012
                                3.950473e-04 0.1491048287
## 31
## 32
         ERSTEPlaviEXPERT 2013
                                5.594323e-05 0.1442715157
## 33
         ERSTEPlaviEXPERT 2014
                                2.469191e-04 0.1700392710
## 34
         ERSTEPlaviEXPERT 2015
                                1.991195e-04 0.2703175563
## 35
         ERSTEPlaviEXPERT 2016
                                1.542028e-04 0.2781643675
## 36
        ERSTEPlaviPROTECT 2010
                                1.528344e-04 0.0248670367
## 37
        ERSTEPlaviPROTECT 2011
                                3.855290e-05 0.0355562101
## 38
        ERSTEPlaviPROTECT 2012
                                3.418137e-04 0.0312794690
## 39
        ERSTEPlaviPROTECT 2013
                                4.735975e-05 0.0220619941
## 40
        ERSTEPlaviPROTECT 2014
                                2.035929e-04 0.0185440353
        ERSTEPlaviPROTECT 2015
## 41
                                9.710402e-05 0.0358210528
## 42
        ERSTEPlaviPROTECT 2016
                                1.639057e-04 0.0005997816
ggplot(xs.capm, aes(Year, Beta, color= Fund, group = Fund)) +
geom_point() + geom_line()
```



ggplot(xs.capm, aes(Year, Alpha, color= Fund, group = Fund)) +
geom_point() + geom_line()



PROVJERA NORMALNOSTI REZIDUALA

```
nrows = nrow(xs.capm)
#for(i in 1:361) {
# xs.capm[as.character(i)] <- as.vector(matrix(0,nrow=nrows))</pre>
#}
xs.capm["ks_p_val"] <- as.vector(0)</pre>
get_residuals_norm <- function(df, row) {</pre>
  xs.tmpYear <- get_for_year(xs.returns, xs.returns$Date, df[row,'Year'])</pre>
  fund <- as.character(df[row, 'Fund'])</pre>
  xs.tmpYearFund <- xs.tmpYear[,fund]</pre>
  capm.risk_free.year <- xs.tmpYear$InterestRate.daily #[c('Date', 'InterestRate.daily')]</pre>
  capm.market.year <- xs.tmpYear$CROBEX</pre>
  residuals.tmp <- vector(mode="numeric", length=length(xs.tmpYearFund))</pre>
  for (i in 1:length(xs.tmpYearFund)) {
    residuals.tmp[i] <- ((xs.tmpYearFund[i] - capm.risk_free.year[i]) -</pre>
    (df[row,3] + df[row, 4] * (capm.market.year[i] - capm.risk_free.year[i])))
  scaled.residuals.tmp <- scale(residuals.tmp)</pre>
```

```
x<-ks.test(scaled.residuals.tmp, 'pnorm')

df[row, 'ks_p_val'] <- x$p.value

return(df)
}

for(i in 1:nrows) {
    xs.capm <- get_residuals_norm(xs.capm, i)
}

xs.capm</pre>
```

```
ks_p_val
##
                     Fund Year
                                       Alpha
                                                     Beta
## 1
     ERSTEAdriaticEquity 2010 -1.363158e-04 0.5669352275 7.606159e-08
     ERSTEAdriaticEquity 2011 -3.331016e-04 0.4543998614 8.972995e-10
## 3
     ERSTEAdriaticEquity 2012 -1.467188e-04 0.2646270122 3.976819e-13
## 4
     ERSTEAdriaticEquity 2013
                                1.072103e-04 0.3940627807 3.095202e-11
## 5
     ERSTEAdriaticEquity 2014
                                1.520230e-04 0.3489534496 5.271628e-11
     ERSTEAdriaticEquity 2015
                                2.024548e-04 0.4975787045 2.888248e-09
     ERSTEAdriaticEquity 2016 2.126424e-04 0.5955184335 1.182900e-08
## 7
## 8
            OTPMeridian20 2010 -1.401558e-05 0.4309319208 2.925515e-10
## 9
            OTPMeridian20 2011 -4.044461e-04 0.5599034422 3.870977e-08
## 10
            OTPMeridian20 2012 2.005561e-04 0.3908358348 2.004861e-09
## 11
            OTPMeridian20 2013
                                2.280547e-04 0.2464292424 2.003044e-10
## 12
            OTPMeridian20 2014
                                5.006249e-05 0.2761167134 7.392093e-09
## 13
            OTPMeridian20 2015
                               1.400398e-04 0.4208172130 2.578632e-08
## 14
            OTPMeridian20 2016 -1.026420e-05 0.4574313828 5.335510e-12
## 15
                  ZBAktiv 2010
                                9.544554e-05 0.2194612955 2.049980e-04
## 16
                  ZBAktiv 2011 -4.358250e-04 0.1381375343 2.527614e-05
## 17
                  ZBAktiv 2012 2.009252e-04 0.1336074631 1.354321e-10
                  ZBAktiv 2013 5.840394e-05 0.1116804387 2.323343e-06
## 18
## 19
                  ZBAktiv 2014
                                1.375125e-04 0.2024930920 6.164473e-06
                  ZBAktiv 2015
## 20
                                1.880294e-04 0.2632705419 2.186302e-05
## 21
                  ZBAktiv 2016
                               1.448745e-04 0.3620458129 1.539224e-04
## 22
            RaiffeisenDMF 2010
                               1.378239e-04 0.1194627941 2.717111e-03
## 23
            RaiffeisenDMF 2011 -7.635330e-05 0.1405371249 3.224060e-06
## 24
            RaiffeisenDMF 2012 2.378826e-04 0.1359857205 1.741118e-11
                                9.345165e-05 0.1687797266 2.118944e-04
## 25
            RaiffeisenDMF 2013
## 26
            RaiffeisenDMF 2014
                                3.404221e-04 0.1610284601 2.405696e-04
## 27
            RaiffeisenDMF 2015
                                1.803462e-04 0.1697165854 1.146525e-03
## 28
            RaiffeisenDMF 2016
                                1.041926e-04 0.1389678904 2.727515e-06
## 29
         ERSTEPlaviEXPERT 2010
                                1.580814e-04 0.1750763495 2.160262e-04
         ERSTEPlaviEXPERT 2011 -2.905792e-05 0.2343404356 1.988193e-04
## 30
## 31
         ERSTEPlaviEXPERT 2012
                                3.950473e-04 0.1491048287 7.504533e-05
## 32
         ERSTEPlaviEXPERT 2013
                                5.594323e-05 0.1442715157 3.300715e-04
## 33
         ERSTEPlaviEXPERT 2014
                                2.469191e-04 0.1700392710 2.902686e-03
## 34
         ERSTEPlaviEXPERT 2015
                                1.991195e-04 0.2703175563 3.123242e-03
## 35
                                1.542028e-04 0.2781643675 7.591789e-05
         ERSTEPlaviEXPERT 2016
## 36
        ERSTEPlaviPROTECT 2010
                                1.528344e-04 0.0248670367 1.210117e-05
        ERSTEPlaviPROTECT 2011
## 37
                                3.855290e-05 0.0355562101 4.594969e-05
## 38
        ERSTEPlaviPROTECT 2012
                                3.418137e-04 0.0312794690 1.652921e-05
## 39
        ERSTEPlaviPROTECT 2013 4.735975e-05 0.0220619941 8.751553e-07
```

```
## 40 ERSTEPlaviPROTECT 2014 2.035929e-04 0.0185440353 3.416949e-03
## 41 ERSTEPlaviPROTECT 2015 9.710402e-05 0.0358210528 4.620251e-04
## 42 ERSTEPlaviPROTECT 2016 1.639057e-04 0.0005997816 2.693304e-05
```

ANOVA