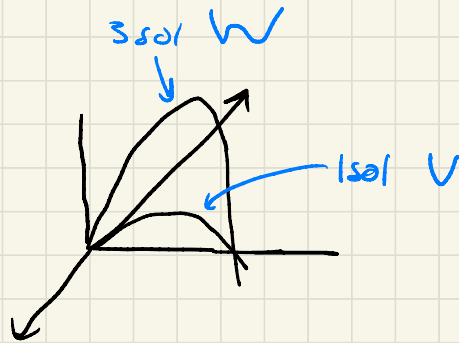


condition

$$\omega = A' \sin \frac{\omega}{\sqrt{2}}$$



for small ω ;

$$\sin \frac{\omega}{\sqrt{2}} \approx \frac{\omega}{\sqrt{2}}$$

$$\text{so } 1 \text{ sol if } |A'| \leq \sqrt{2}$$

$$3 \text{ sol if } |A'| > \sqrt{2}$$

so; A' domain is important.

assume

$$\begin{cases} \varphi_{1 \times dc} = \varphi_{2 \times dc} \\ \varphi_{1 \times dc} = \varphi_{1 \times dc} + \epsilon_1 \\ \varphi_{2 \times dc} = \varphi_{2 \times dc} + \epsilon_2 \end{cases} \quad \begin{cases} \epsilon_+ = \frac{\epsilon_1 + \epsilon_2}{2} \\ \epsilon_- = \frac{\epsilon_1 - \epsilon_2}{2} \end{cases}$$

ϵ is small; but NOT zero

$$A'' = \frac{\sqrt{2}}{\beta} A' = \cos \left(\frac{\varphi_{1 \times dc} + \varphi_{2 \times dc}}{2} \right) + \cos \left(\frac{\varphi_{1 \times dc} - \varphi_{2 \times dc}}{2} \right)$$

$$A'' = \cos [\varphi_{x \times dc} + \epsilon_+] + \cos (\epsilon_-)$$

$$= \cos \varphi_{x \times dc} \cos \epsilon_+ - \sin \varphi_{x \times dc} \sin \epsilon_+ + \cos \epsilon_-$$

examples; assume $\epsilon_{\pm} = \{-.4, .4\}$; $\beta = 10$

case 1: $\varphi_{x \times dc} = \pi$; $\cos \epsilon_{\pm} \rightarrow \{.9, 1\}$

$\sin \epsilon_{\pm} \rightarrow \{-.4, .4\}$

$$A'' = (-1)\{.9-1\} + 0 + \{.9-1\}$$

$$\rightarrow -.1 \leq A'' \leq .1 \quad \leftarrow \text{only 1 well; } \frac{2}{\beta} = .2$$

case 2: $\varphi_{x \times dc} = -2$

$$A'' = (-.4)\{.9-1\} + (-.9)\{-.4, .4\} + \{.9, 1\}$$

$$\rightarrow .14 \leq A'' \leq 1 \quad \leftarrow \text{both 1 well and 2 wells possible}$$

$A'' = \frac{2}{\beta}$
is the
critical
value
where
 $A' = \sqrt{2}$

NOTE

analysis depends
on $\varphi_{x \times dc}$, β ,
and ϵ_{\pm}