

1. Multiple Choices Questions

Question 1.1 | Two's Complement

Suppose we use three bits to represent the integers from -4 to 3 using Two's complement notation. What is the bit representation of -1?

- ☐ A: 010
- ☐ B: 100
- ☐ C: 110
- ☐ D: 111

Question 1.2 | Machine Language

Which of the following statements is true about machine language and high-level programming languages?

- ☐ A: Machine language code requires fewer resources to write and is easier to debug.
- ☐ B: High-level programming languages can not be understood by machines directly and require compiling.
- ☐ C: Machine language code is portable across different computers.
- ☐ D: High-level programming language code runs faster as it hides unnecessary details for programmers.

Question 1.3 | CPU

When an algorithm runs by a computer with a 6GHz CPU, its time complexity will be _____ running on a computer with a 4GHz CPU.

- ☐ A: Lower than
- ☐ B: Equal to
- ☐ C: Higher than

D: None of the above: depending on other factors of the computer

Question 1.4 | Algorithms

How can we represent an algorithm?

- ☐ A: Natural Language
- ☐ B: Flow chart
- ☐ C: Pseudocode
- ☐ D: All of the above

Question 1.5 | QuickSort

What is the average-case time complexity of QuickSort when pivot selections are not always the smallest or highest?

- ☐ A: $O(n)$
- ☐ B: $O(\log(n))$
- ☐ C: $O(n \cdot \log(n))$
- ☐ D: $O(n^2)$

Question 1.6 | Search

Which of the following statements is true about searching algorithms?

- ☐ A: Given an unsorted list, binary search will still work with a time complexity of $O(n)$.
- ☐ B: Given a sorted list, binary search always uses fewer comparisons to find the match than linear search.
- ☐ C: Given an unsorted and small list, linear search can run faster than binary search.
- ☐ D: Given a large list, either linear or binary search will be more efficient than hashing.

Question 1.7 | OOP Programming

What is the expected output of the following code?

```
class Animal:
    def sound(self):
        print("Animal Sound")

class Cat(Animal):
    def sound(self):
        print("Meow")

class Dog(Animal):
    def sound(self):
        print("Bark")

kitty = Dog()
kitty.sound()
```

- ☐ A: Animal Sound
- ☐ B: Meow
- ☐ C: Bark
- ☐ D: None

2. Short Answer Questions

Question 2.1 | When to Sort before Search

You are to look for an item in a list of n items, and you will do the lookup (or search) for m times:

- Just-search: just do m linear searches over the list (i.e., each search scans the entire list)
- Sort-then-search: sort the list first, and then do m searches using binary search.

1. Using Big-O notation, write the complexities of the two approaches. Note: in this case, the time complexity is a function of m and n .

2. Describe when one approach is better than the other.

3. In addition to the just-search and sort-then-search, is there any other approach to complete this task? If yes, please specify the approach and explain its time complexity.

Question 2.2 | Complexity Analysis

1. The following is the code for the selection sort.

```
def selection_sort(arr):
    for i in range(len(arr)):
        min_idx = i
        for j in range(i + 1, len(arr)):
            if arr[j] < arr[min_idx]:
                min_idx = j
        arr[i], arr[min_idx] = arr[min_idx], arr[i]

    return arr
```

What is the time complexity of the selection sort (assuming arr has N items)? (in Big-O notation)

2. What is the time complexity of the following code? (in Big-O notation)

```
def int_to_binary(x):
    """Assumes x is a nonnegative int
    Returns a binary string representation of x."""

    digits = '01'
    if x == 0:
        return '0'
```

```
result = ''
while x > 0:
    result = digits[x%2] + result
    x = x//2
return result
```

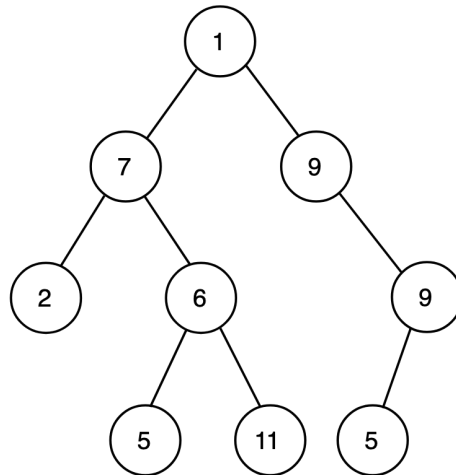
Output = int_to_binary(N)

3. What is the time complexity of the following code? (in Big-O notation)

```
def mystery_function(N):
    sum = []
    i, j = 1, 2
    while i <= N:
        i *= 3
        while j <= N+1:
            sum.append(i+j)
            j *= 2
```

Question 2.3 | Tree Traversal

Here is an example of a binary tree. Write down the different traversals.



Preorder Traversal: _____

Inorder Traversal: _____

Postorder Traversal: _____

3. Programming Questions

**Please write your programming solution as clearly as possible.
Try to add comments to explain each code segment.**

Question 3.1 | Tribonacci Numbers

In the lecture, we learnt how to use recursion to solve Fibonacci numbers defined as

$\text{Fib}(0) = 1$, $\text{Fib}(1) = 1$, and

$$\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$$

for all $n \geq 2$.

Let us define a new sequence called *Tribonacci numbers* as follows. $\text{Tri}(0) = 1$, $\text{Tri}(1) = 1$, $\text{Tri}(2) = 1$ and

$$\text{Tri}(n) = \text{Tri}(n-1) + \text{Tri}(n-2) + \text{Tri}(n-3)$$

for all $n \geq 3$.

Please write a code for computing the n-th Tribonacci number using recursion.

```
def Tribonacci_recur(n):  
    # write your code here
```

Advance version: write it in dynamic programming. And describe the difference of complexity versus recursion.

```
def Tribonacci_dp(n, mem = {}):  
    # write your code here
```

Question 3.2 | Binary Search Returning index

In the lecture, we learnt binary search that returns True or False - whether a given number exists in the list. Now write a function that uses binary search to find the index of the target value in a sorted list. It returns the index of the target value if it is in the list.

Otherwise, it returns -1.

```
In [2]: L = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
In [3]: e = 2
In [4]: bSearch(L, e)
Out[4]: 2
In [5]: e = 9
In [6]: bSearch(L, e)
Out[6]: 9
In [7]: e = 10
In [8]: bSearch(L, e)
Out[8]: -1
```

Below are the arguments for the function input:

- L: the element list to search with;
- e: the target element;
- low=0: index of the first element of L in the given original list, initialized as 0. For example, if the given original list is [0, 1, 2, 3, 4, 5, 6, 7, 8, 9], and the current list L is [5, 6, 7, 8, 9], then, low should be 5(index) since the element 5(value) is the 6th element in the original list.

```
def bSearch(L: list, e: int, low=0):
    # write your code here
```