

ICDS Spring 2025

Computer Architecture

How a program being executed

Recap: Data in the memory

- Objects (programs/data) are stored in the memory (e.g., in RAM cells)
- Memory cells have unique addresses
- Create a variable → associated it with an address that stores the object
 - immutable → the memory cell of the data is locked; modification is not allowed
 - mutable → the memory cell is unlocked; you may change the values in the cell

```
In [1]: a = 1
In [2]: id(a)
Out[2]: 4311873888
In [3]: a = 2
In [4]: id(a)
Out[4]: 4311873920
```

a is immutable; change its value
virtually associates it with another cell.

- `id()`: the built-in function to show the memory address of the variable.

```
In [6]: a = [1, 2, 3, [4, 5, 6]]
In [7]: b = a[:]
In [8]: b[3][0] = "Four"
In [9]: a
Out[9]: [1, 2, 3, ['Four', 5, 6]]
In [10]: id(a[3])
Out[10]: 140511199555392
In [11]: id(b[3])
Out[11]: 140511199555392
```

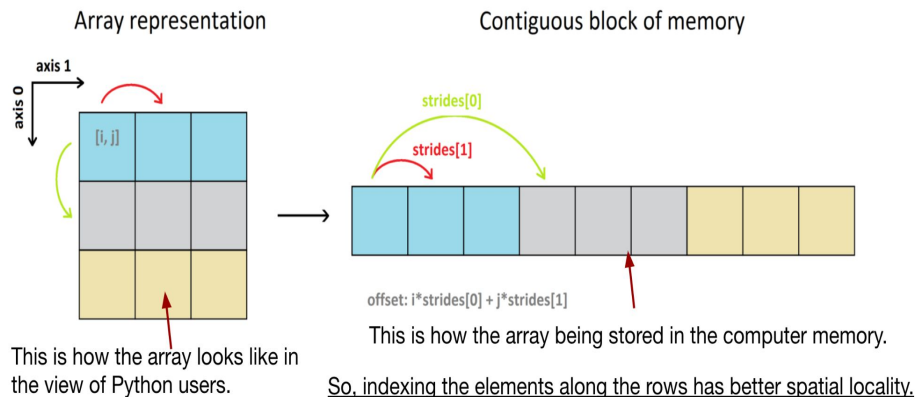
A variable (e.g. list) is a container of addresses

- `a[3]` is the address of the list `[4, 5, 6]`.

Shallow copy a only makes a copy the elements in a which are addresses, so, `b[3]` and `a[3]` refer to the same list. → change elements in `b[3]` will change elements in `a[3]`.

Recap: Locality

- Computers “guess” what data will be used in the next step and load them into cache.
- They do it by following two principles of locality. (temporal/spatial locality)



```
26 import numpy as np
27
28 ##Create an numpy array
29 a = np.array([5, 4, 3, 2, 1])
30
31 # do something with the 3rd element;
32 # Which element(s) will be loaded into
33 cache together with a[2]?
34 print(a[2])
```

Q: Which elements are **most likely** to be loaded into cache together with `a[2]`?

Exercise: Locality

Q: Which elements are **most likely** to be loaded into cache together with `a[2]`?

- A. `a[0]`
- B. `a[1]`
- C. `1`
- D. `2`



← Scan to answer!

```
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28 ##Create an numpy array
29 a = np.array([5, 4, 3, 2, 1])
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```

Agenda

- Computer architecture
- Cycle of program execution
 - Vole: a simple computer
 - Machine language
 - Running codes in high/low-level programming languages
- Appendix

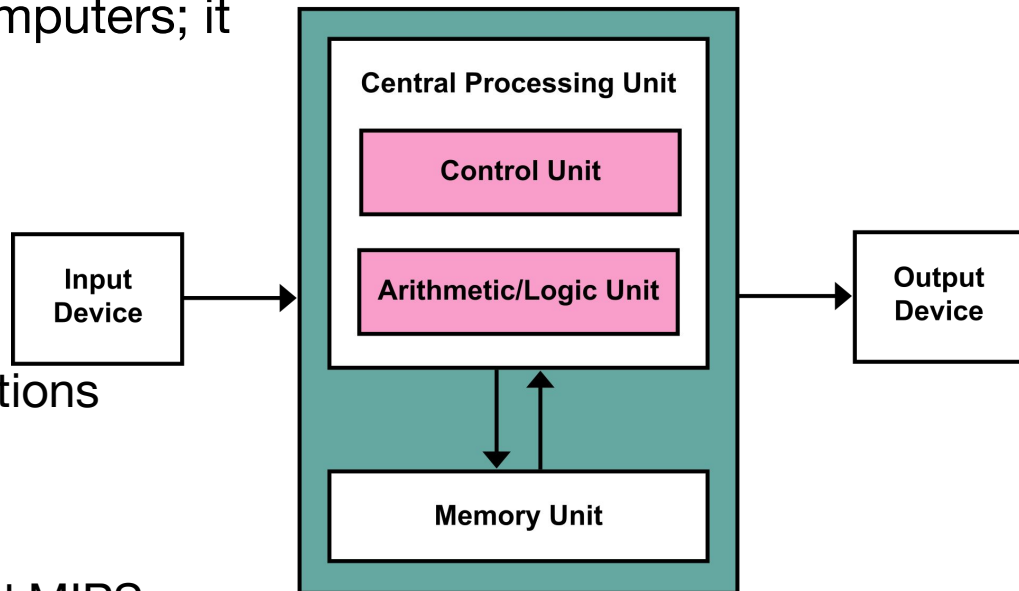
Computer architecture

It is a blueprint for building a computer, it tells

- what circuit blocks (primitive components) the machine needs, and
- how these components can work together
 - e.g., how to coordinate the CPU and the memory

von Neumann architecture

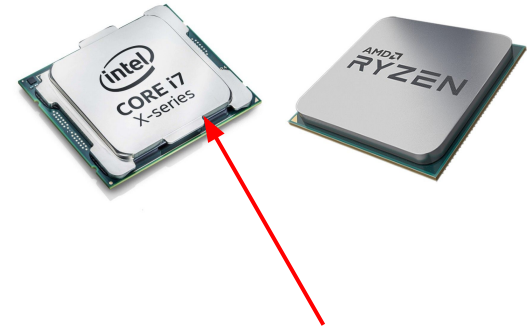
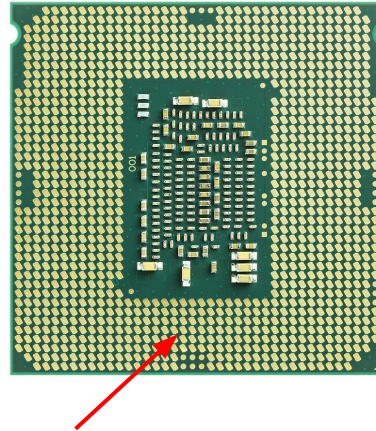
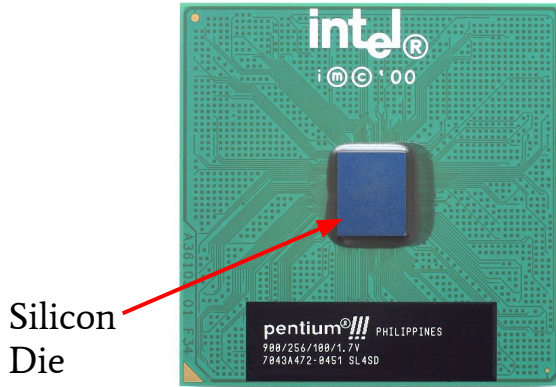
- The mainstream of modern computers; it has,
- A central processor unit
 - Control unit
 - ALU
 - Registers (memory in CPU)
- Memory stores data and instructions
- Input and output devices



Modern processors, such as x86 and MIPS, are examples of the von Neumann architecture.

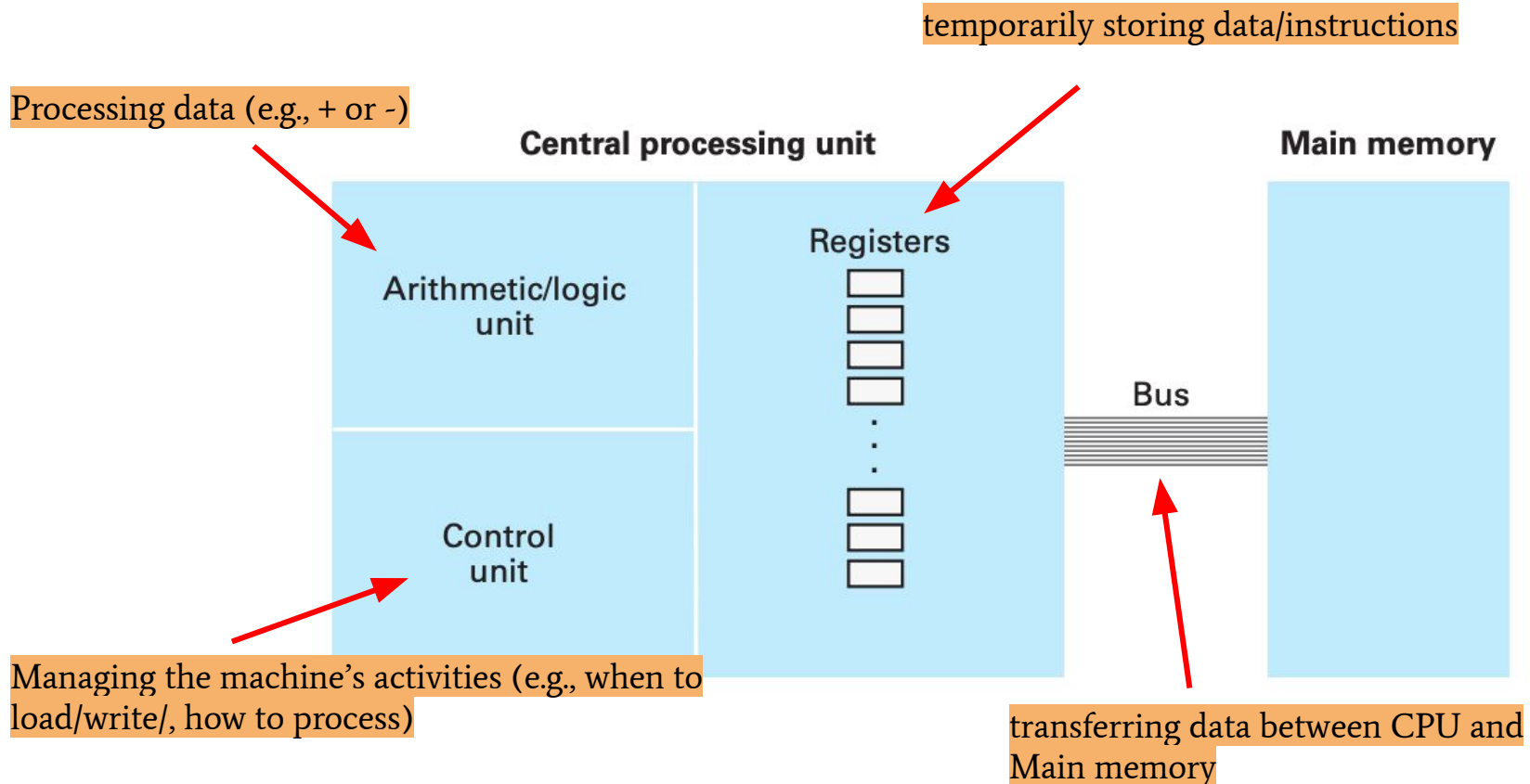
The schematic is from from [Wikipedia](https://en.wikipedia.org/wiki/Von_Neumann_architecture).

Modern CPU



[How a cpu made.](#)

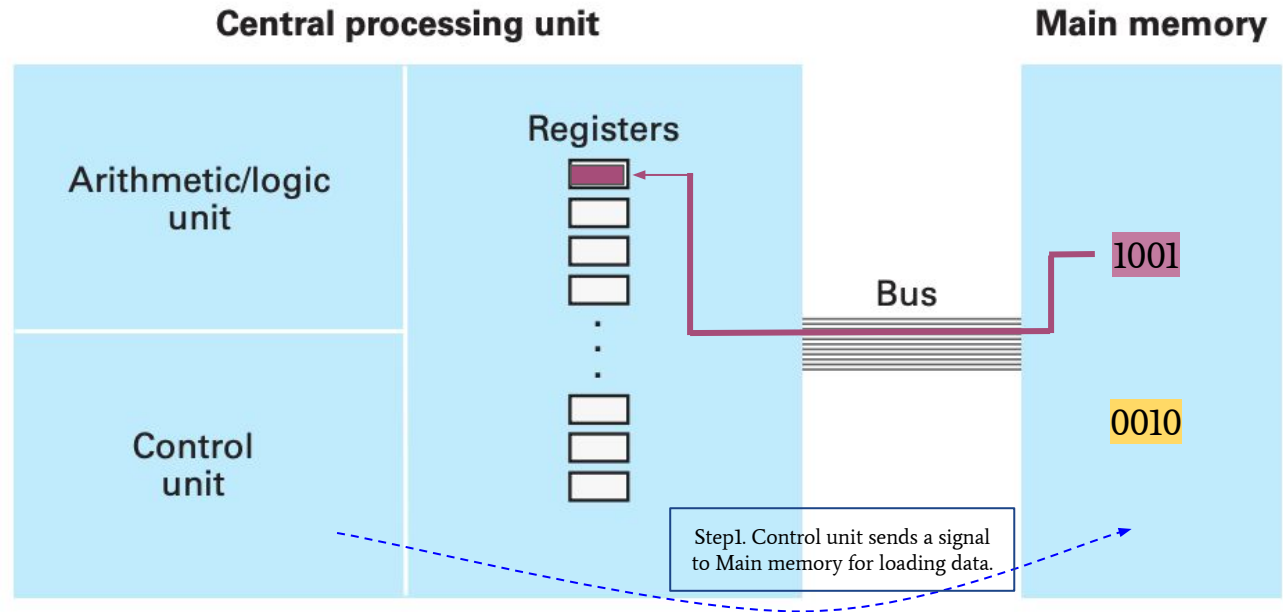
The heart of a computer



How a CPU adds two numbers

To add two values (e.g., 9_{10} , and 2_{10}) stored in Main memory.

Step 1. Load 1001 from Main memory into a register

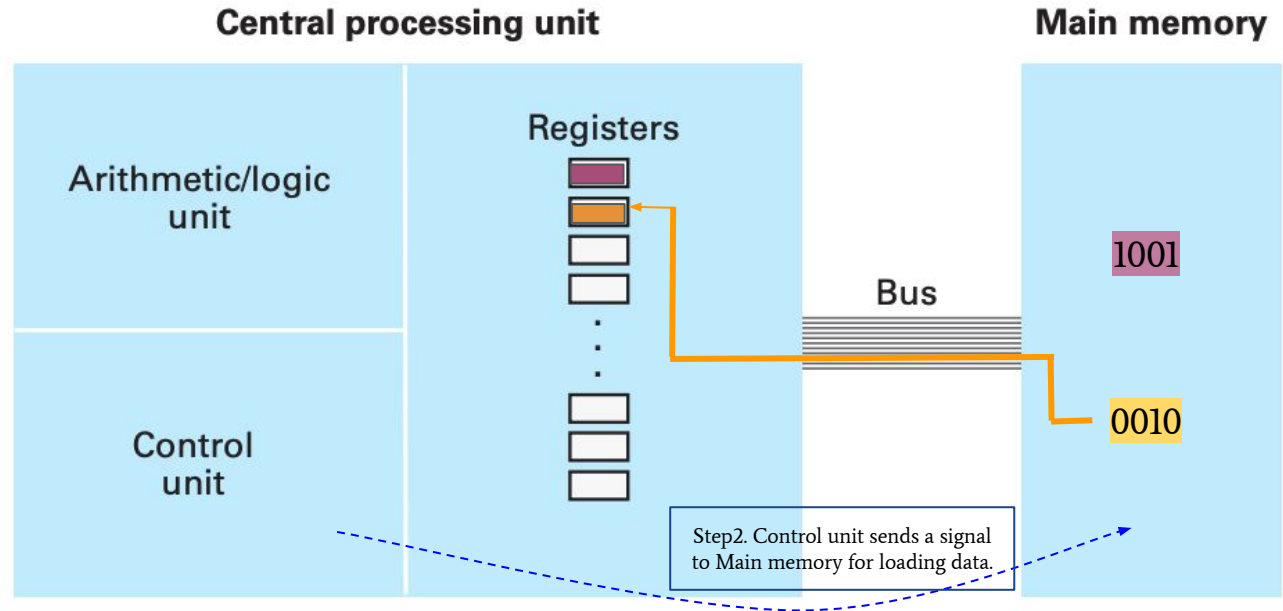


How CPU add two numbers

To add two values (e.g., 9_{10} , and 2_{10}) stored in Main memory.

Step 1. Load 1001 from
Main memory into a
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Step 2. Load 0010 from
Main memory into another
register



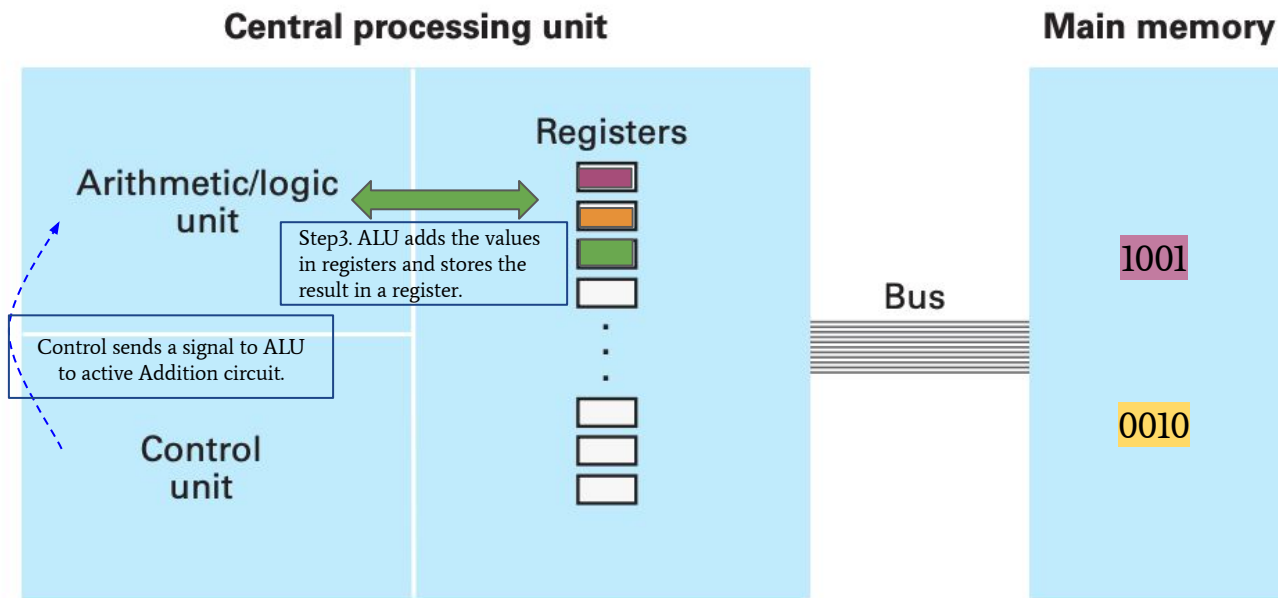
How CPU add two numbers

To add two binary values (e.g., 9_{10} , and 2_{10}) stored in Main memory.

Step 1. Load two values from Main memory into two registers

Step 2. Load 0010 from Main memory into another register

Step 3. ALU **operates on the registers**; the result is temporary stored in a register.



How CPU add two numbers

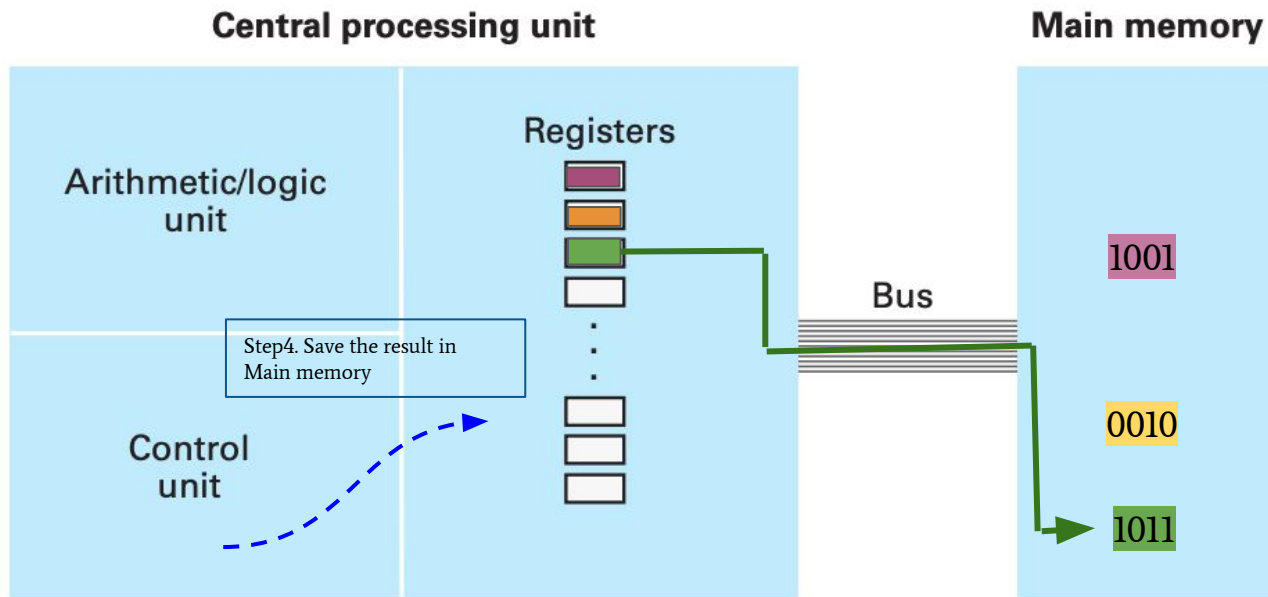
To add two binary values (e.g., 1001, 0010) stored in Main memory.

Step 1. Load two values from Main memory into two registers

Step 2. Load 0010 from Main memory into a register

Step 3. ALU operates on the registers; the result is temporary stored in a register

Step 4. **Store the result** in Main memory



How CPU add two numbers

To add two binary values (e.g., 1001, 0010) stored in Main memory.

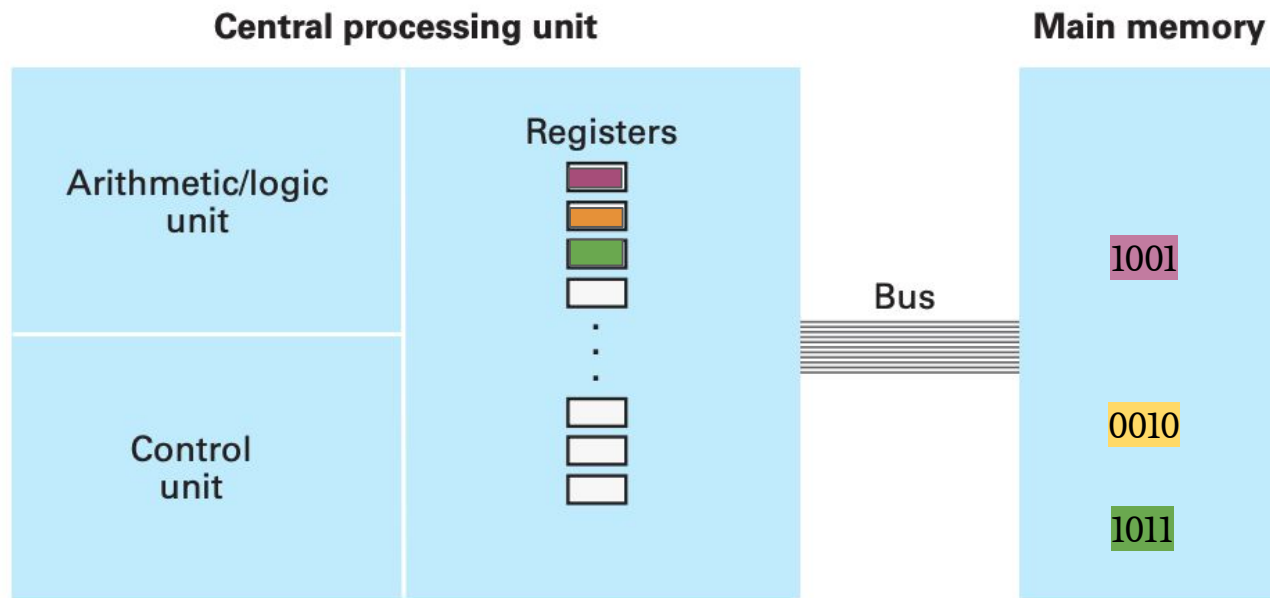
Step 1. Load two values from Main memory into two registers

Step 2. Active the addition circuitry in ALU

Step 3. ALU operates on the registers; the result is temporary stored in a register

Step 4. Store the result in Main memory

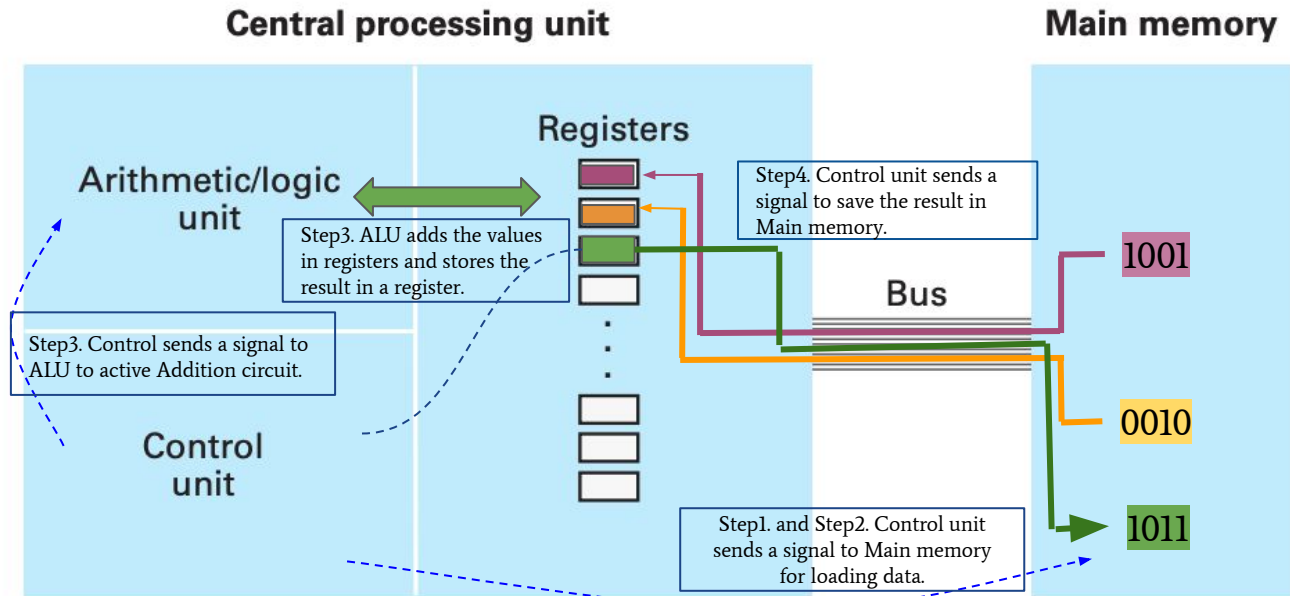
Step 5. **Stop**



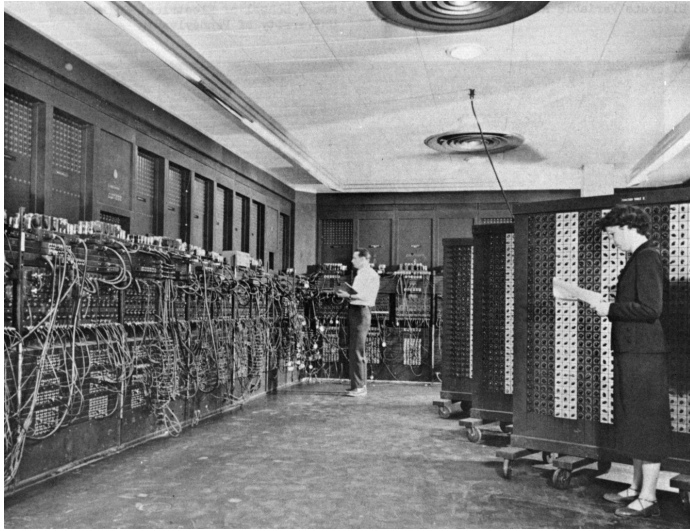
How CPU add two numbers (overview)

Adding two binary values (e.g., 1001, 0010) stored in Main memory.

1. **Load 1001** from Main memory into a register
2. **Load 0010** from Main memory into a register
3. **ALU operates on the registers**; the result is temporary stored in a register
4. **Store the result** in Main memory
5. **Stop**



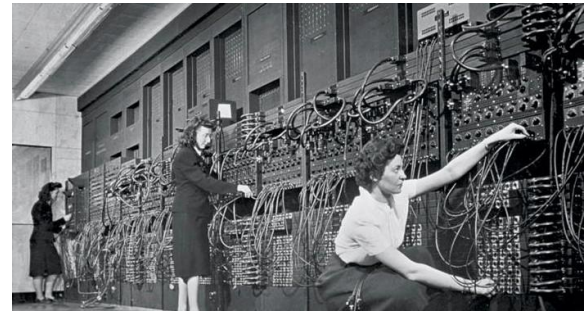
Fixed-program computers (like electricity calculators)



The figure is ENIAC, the first electronic general-purpose computer. People had to change the connection among circuit blocks to reprogram it.

In the early days, human played the role of control unit.

- To program was to reconnect the circuit blocks for different tasks.
- Reprogramming took days



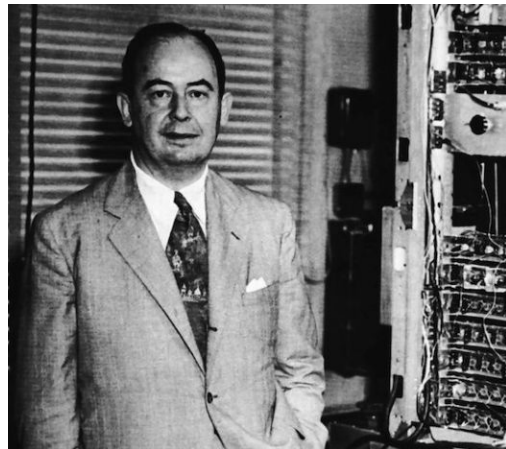
Stored-program computers

Instructions can be stored in main memory, like data!

- They can be represented as binary strings, so, having the same storage format as data

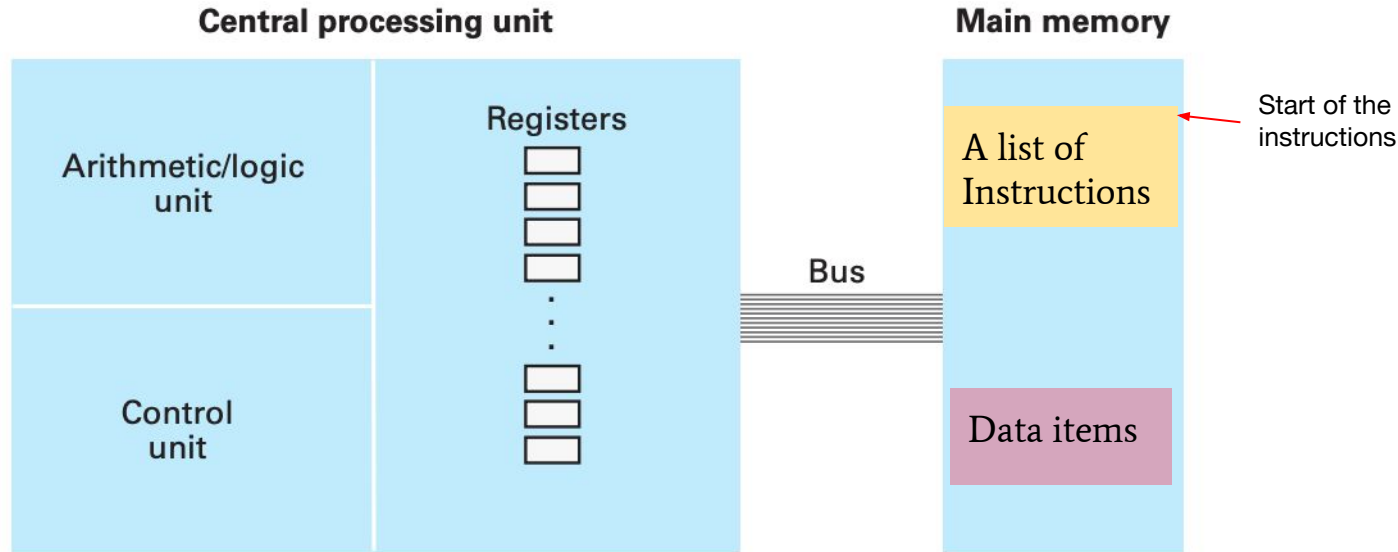
Almost all modern computers are stored-program computers.

- They store data and instructions together in main memory.
- The stored-program concept was introduced by von Neumann



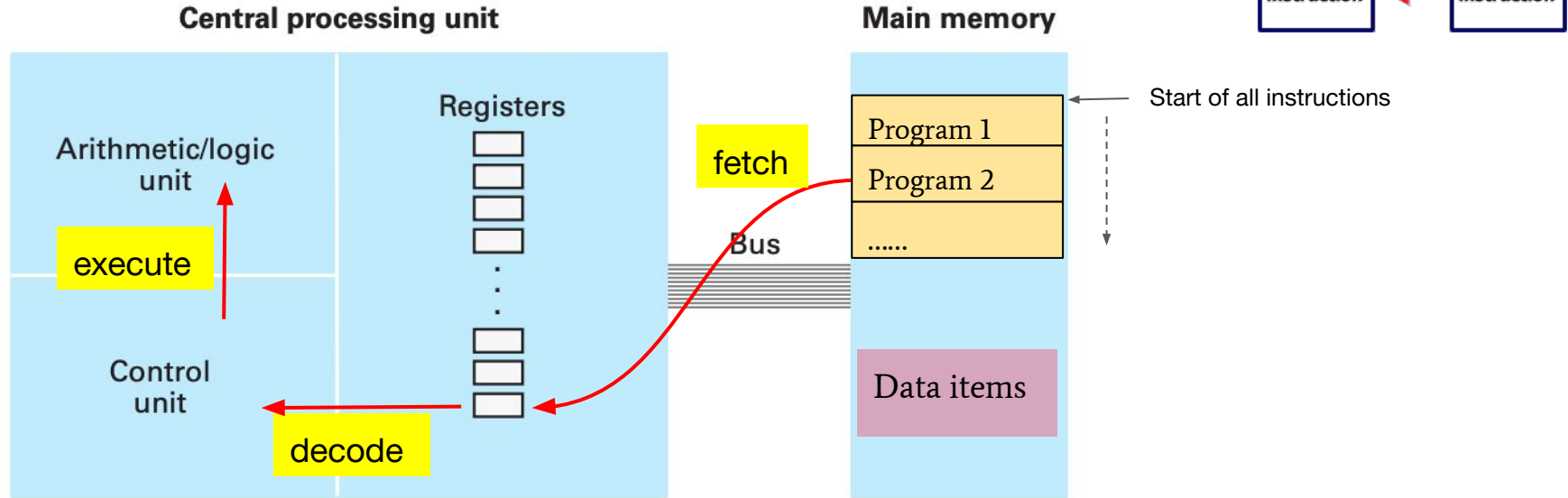
John von Neumann,
1903-1957

Stored-program computers



- Instructions and data are both stored in the main memory.
- Instructions are listed in a list (like an address book)
- CPU loads one instruction at a time from the list and run it \Rightarrow it repeats this action until all instructions are done

The cycle of execution



By default, the CPU will fetch instructions from the start of the list, following a top-down order. Of course, this is not enough.

- How can we control the order of execution?
- We often use two special registers to solve it.

Vole: a simplified computer

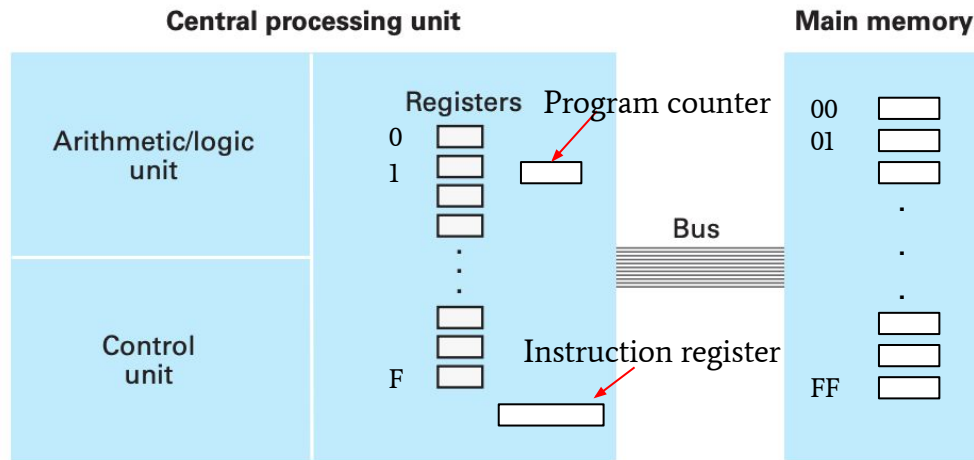
Now, let's look at a very simple computer, namely, Vole.

Vole's Architecture

- 16 8-bit general-purpose registers
- 256 main memory 8-bit cells
- one instruction register (16-bit)
- one program counter (8-bit)

Other specifications:

- The registers are labeled with 0 through F (hexadecimal, i.e., 0-15 in decimal)
- The address of the memory cell are from 00 to FF (i.e., 0-255 in decimal)
- a machine instruction of Vole has 16 bits

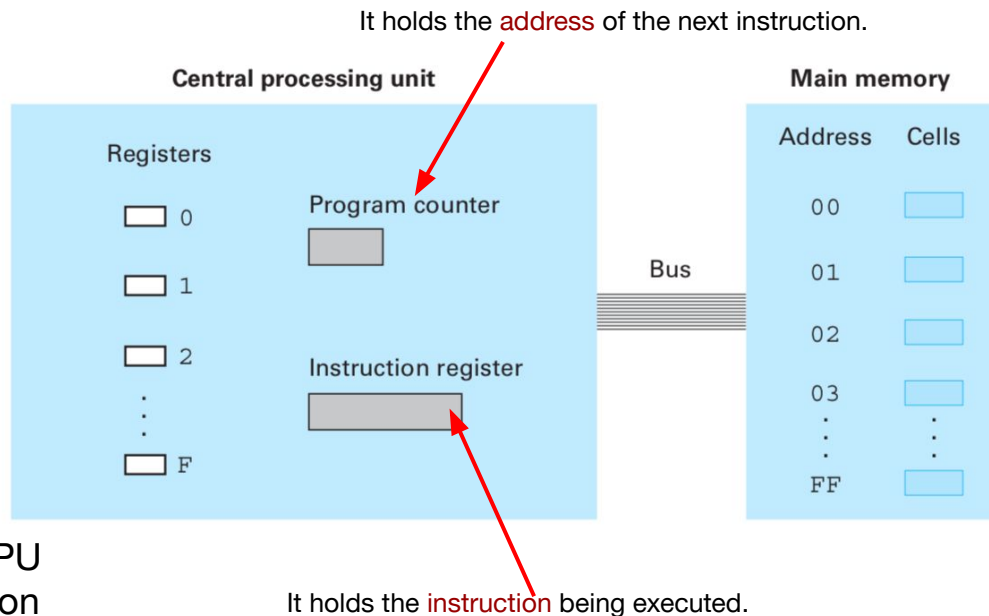


Two special-purpose registers in the CPU

- Program counter (**PC**): holding the **address** of the next instruction
- Instruction register (**IR**): holding the **instruction** being executed

During the fetch step, CPU loads the instruction from the address in PC, then, increments the address (recall the address is a binary) so that it becomes the address of the next instruction.

The instruction is loaded into the IR where the CPU decodes the instruction (associating the instruction to some concrete operations on circuits).



Machine language

In stored-program computers, instructions are represented in **binary strings**.

- Machine language is a set of binary patterns that represent instructions

Instructions

Machine instructions should follow some **pre-defined format** so that CPUs can “understand” them.

- A machine instruction contains **two** parts: op-code and operand
 - The op-code: the operation to take. (e.g., load/store)
 - The operand: the information needed by the op-code. (e.g., where to load/store)

Op-code	Operand		
0011	0101	1010	0111

An example of a 16-bit instruction.

- Different designs of processors may have different instruction formats.
 - Machine language of a PC is different to that of an Apple M1. (PC uses x86; M1 uses ARM64)

Two philosophies of machine languages

- RISC (**reduced** instructions set computer)
 - CPUs are designed to execute a minimal set of instructions, e.g., it may have $A + B$ but no $A \times B$.
 - Running fast and less expensive
 - Apple silicon M1 is RISC
- CISC (**complex** instructions set computer)
 - CPUs can execute many complex, redundant instructions
 - e.g., it has $A + B$ and $A \times B$.
 - Convenient for programming
 - x86 is CISC

By the way, if you would like to have a taste of a compact programming language, you may have a look at [this](#).
(Don't be astonished by its name, it reproduces the pain for programming with RISC machine languages).

The instruction repertoire

Machine's instructions can be categorized into 3 groups:

- Data transfer
 - Instructions for copying/moving data from one location to another
 - e.g., load, store, I/O instructions
- Arithmetic/Logic
 - Instructions for activities of ALU.
 - e.g., +, -, Boolean operations (AND, OR, XOR)
- Control
 - Instructions for directing the execution of the program
 - e.g., halt, jump

Machine language of Vole

We set, from left to right,

- The 1st hexadecimal digits (4 bits) represents the op-code
- The next 3 hexadecimal digits (12 bits) are operands

The format of a Vole's instruction

Op-code	Operand		
0011	0101	1010	0111



Representing binaries with **hexadecimals**

Op-code	Operand		
0x3	0x5	0xA	0x7

We often use hexadecimal notations which is more concise than binaries.

Note: The “0x” prefix indicates the number is hexadecimal.

Machine language of Vole

Op-code	Operand	Description	Example
1	RXY	LOAD the register R with the bit pattern found in the memory cell whose address is XY	14A3 would cause the contents of the memory cell located at address A3 to be placed in register 4.
2	RXY	LOAD the register R with the bit pattern XY	20A3 would cause the value A3 to be placed in register 0.
3	RXY	STORE the bit pattern found in register R in the memory cell whose address is XY	35B1 would cause the contents of register 5 to be placed in the memory cell whose address is B1
4	0RS	MOVE the bit pattern found in Register R to Register S	40A4 would cause the contents of register A to be copied into register 4.
5	RST	ADD the bit patterns in registers S and T as though they were two's complement representations and leave the result in register R.	5726 would cause the binary values in register 2 and 6 to be added and the sum placed in register 7.
6	RST	ADD the bit patterns in registers S and T as though they were two's floating-point notations and leave the result in register R.	634E would cause the values in register 4 and E to be added as floating-point values and the result to be placed in register 3.

R, S, and T:
3 different registers

X, and Y:
Hexadecimal digits

3	5	B	1
STORE	register 5	Memory address B1	

To save contents in register 5 to B1 of the main memory

Machine language of Vole (continued)

Op-code	Operand	Description	Example
7	RST	OR the bit patterns in register S and T and place the result in register R.	7CB4 would cause the result of ORing the contents of registers B and 4 to be placed in register C.
8	RST	AND the bit patterns in register S and T and place the result in register R.	8045 would cause the result of ANDing the contents of registers 4 and 5 to be placed in register 0.
9	RST	XOR the bit patterns in register S and T and place the result in register R.	95F3 would cause the result of XORing the contents of registers F and 3 to be placed in register 5.
A	R0X	ROTATE the bit pattern in register R one bit to the right X times. Each time place the bit that started at the low-order end at the high-order end.	A403 would cause the contents of register 4 to be rotated 3 bits to the right in a circular fashion.
B	RXY	JUMP to the instruction located in the memory cell at address XY if the bit pattern in register R is equal to the bit pattern in register 0. Otherwise, continue with the normal sequence of execution. (The jump is implemented by copying XY into the program counter during the execute phase.)	B43C would first compare the contents of register 4 with the contents of register 0. If the two were equal, the pattern 3C would be placed in the program counter so that the next instruction executed would be the one located at the memory address 3C. Otherwise, nothing would be done and program execution would continue in its normal sequence.
C	000	HALT execution.	C000 would cause program execution to stop.

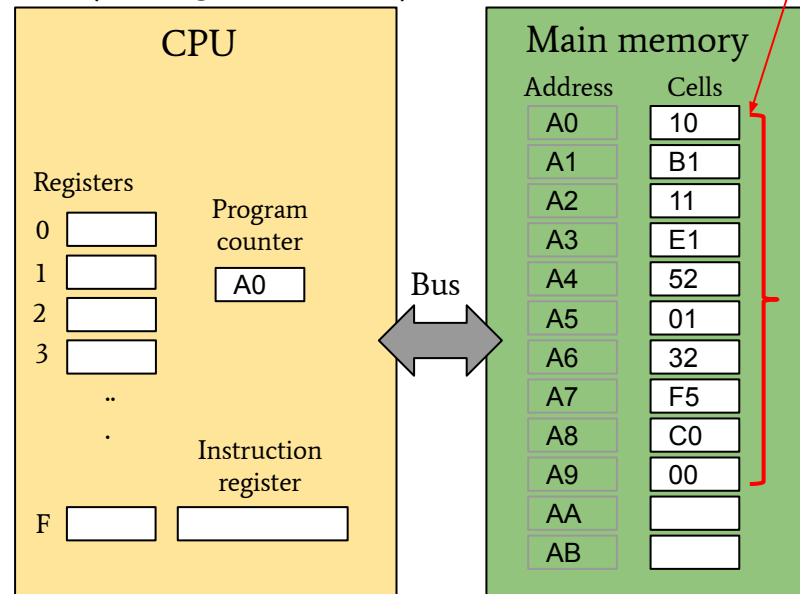
R, S, and T:
3 different registers

X, and Y:
Hexadecimal digits

Example: adding two values

The program is stored in main memory and ready for execution. (adding two values)

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
32F5	Store the contents of register 2 at address F5
C000	Halt

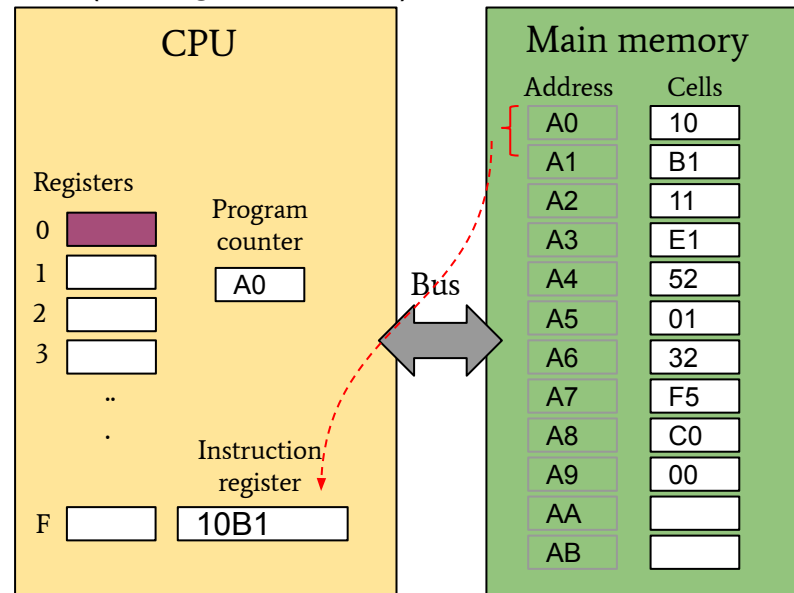


The first instruction is loaded from A0, because Program counter is **set to be A0** at the **beginning**.

Example of execution

The program is stored in main memory and ready for execution. (adding two values)

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10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
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C000	Halt

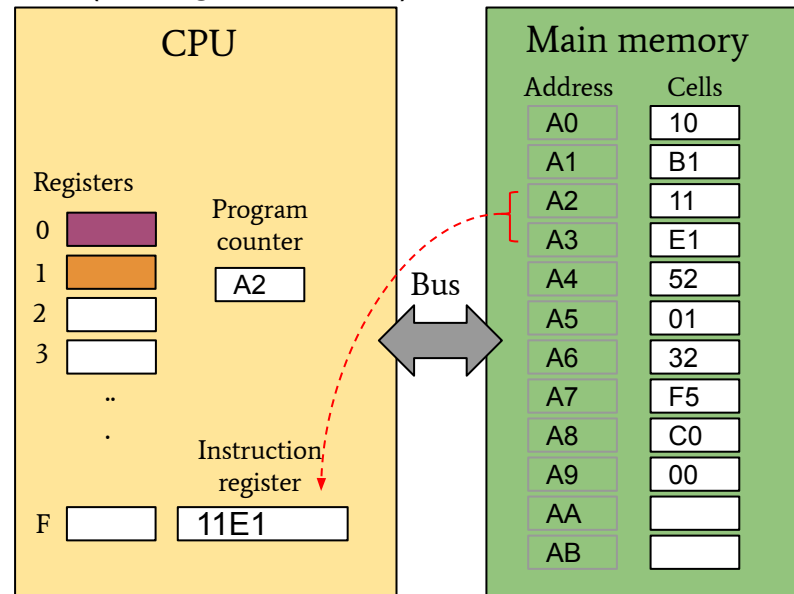


Loading from A0: Since each instruction in Vole has 2 bytes long, the CPU fetches two memory cells from the main memory and **increments the PC by 2** (2 is the default value of this machine) so that the next fetch will start from A2.

Example of execution

The program is stored in main memory and ready for execution. (adding two values)

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
32F5	Store the contents of register 2 at address F5
C000	Halt

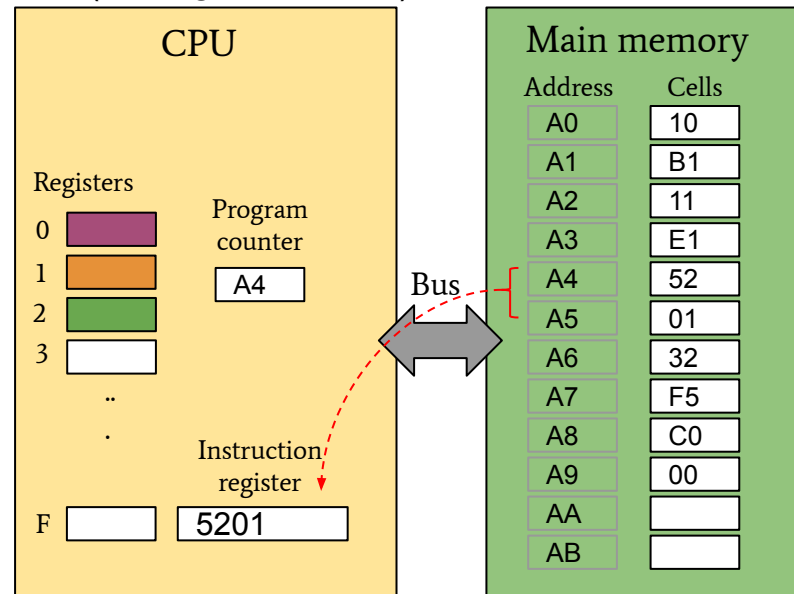


Loading from A2, incrementing PC by two to A4

Example of execution

The program is stored in main memory and ready for execution. (adding two values)

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
32F5	Store the contents of register 2 at address F5
C000	Halt

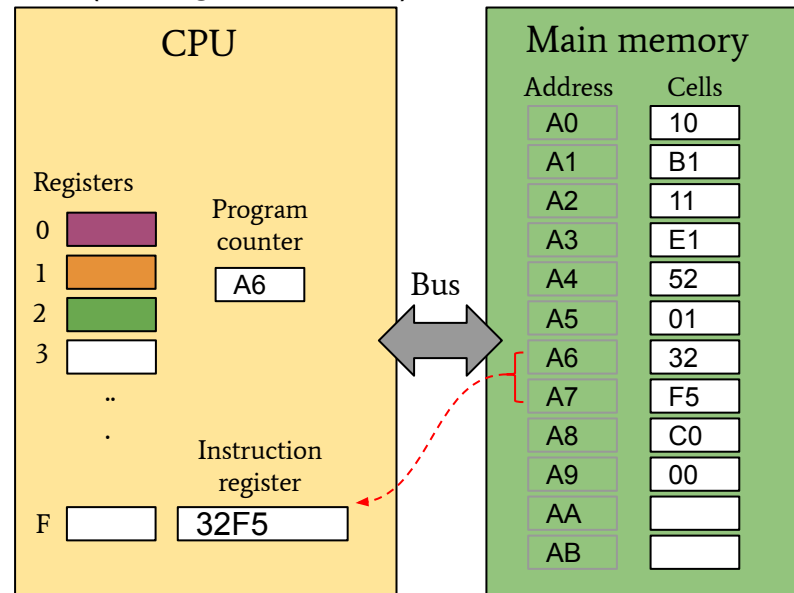


Loading from A4, incrementing PC by two to A6.

Example of execution

The program is stored in main memory and ready for execution. (adding two values)

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
32F5	Store the contents of register 2 at address F5
C000	Halt

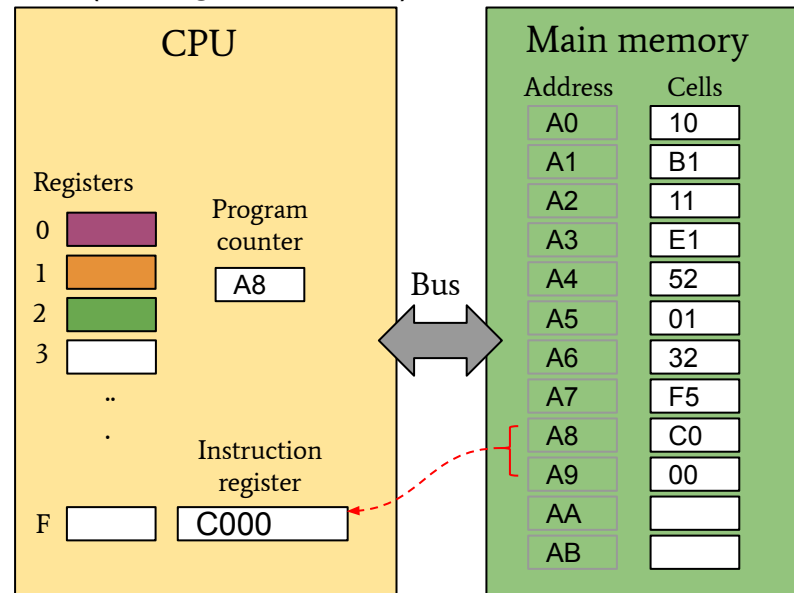


Loading from A6, incrementing PC by two to A8

Example of execution

The program is stored in main memory and ready for execution. (adding two values)

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
5201	Add contents of register 0 and 1; leave the result in register 2
32F5	Store the contents of register 2 at address F5
C000	Halt



Loading from A8, incrementing PC by two to AA; the program ends.

Example: run if/else in Vole

Now, let's see the execution of some Python script in Vole.

1. The if/else statements (i.e., branch)

Assume the value of m is stored at **B1**, and the value of n is stored at **E1**.

```
m = 3
n = 3

if m==n:
    m = m+n
else:
    m = n
```

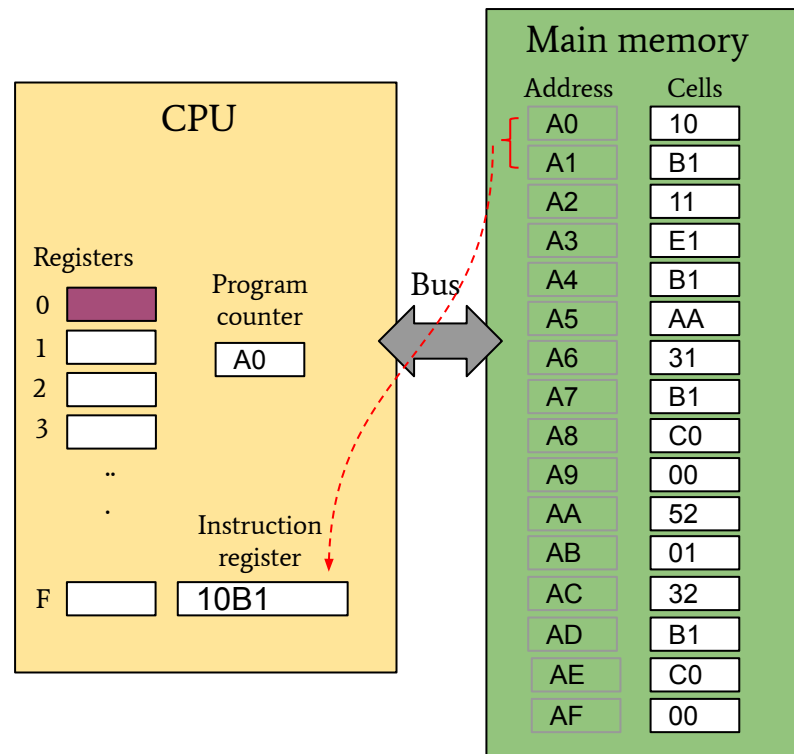
We carry out the if/else by using JUMP.

B	R	X	Y
JUMP	Register R	Memory address XY	

Put **XY** into the **PC** if the value in **Register R** is equal to **Register 0**.

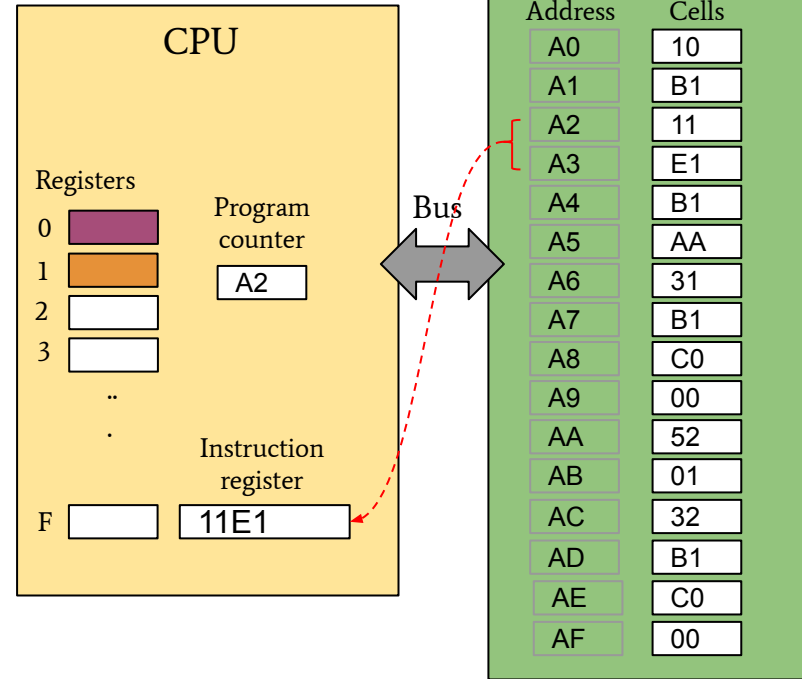
The if/else statement

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
B1AA	If Reg.1 is equal to Reg. 0, jump to AA
31B1	Store the contents of Reg.1 at address B1
C000	Halt
5201	Add contents of register 0 and 1; leave the result in register 2
32B1	Store the contents of Reg. 2 at address B1
C000	Halt



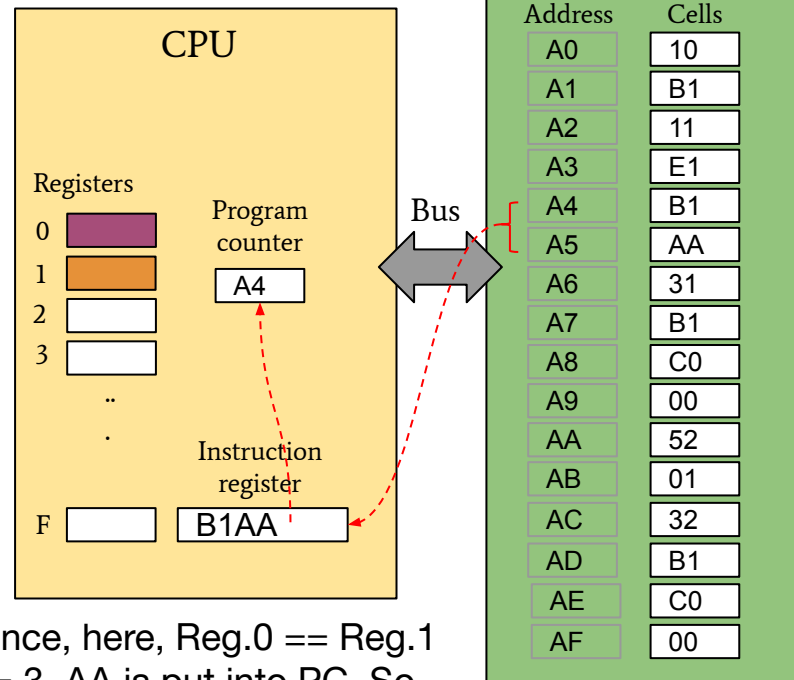
The if/else statement

Encoded instructions	Translation
10B1	Load register 0 from address B1
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B1AA	If Reg.1 is equal to Reg. 0, jump to AA
31B1	Store the contents of Reg.1 at address B1
C000	Halt
5201	Add contents of register 0 and 1; leave the result in register 2
32B1	Store the contents of Reg. 2 at address B1
C000	Halt



The if/else statement

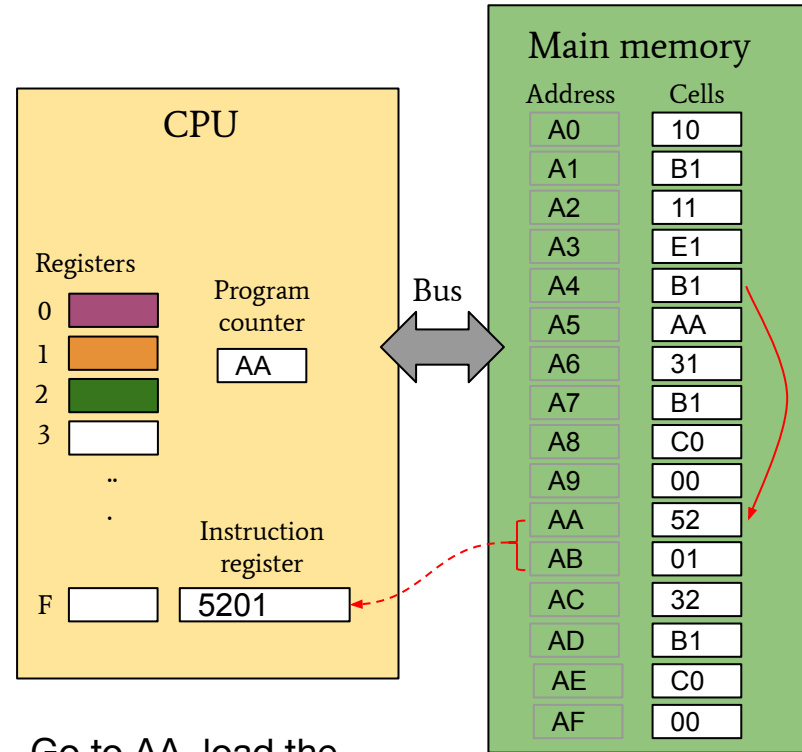
Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
B1AA	If Reg.1 is equal to Reg. 0, jump to AA
31B1	Store the contents of Reg.1 at address B1
C000	Halt
5201	Add contents of register 0 and 1; leave the result in register 2
32B1	Store the contents of Reg. 2 at address B1
C000	Halt



Since, here, Reg.0 == Reg.1 == 3, AA is put into PC. So, next instruction is from AA.

The if/else statement

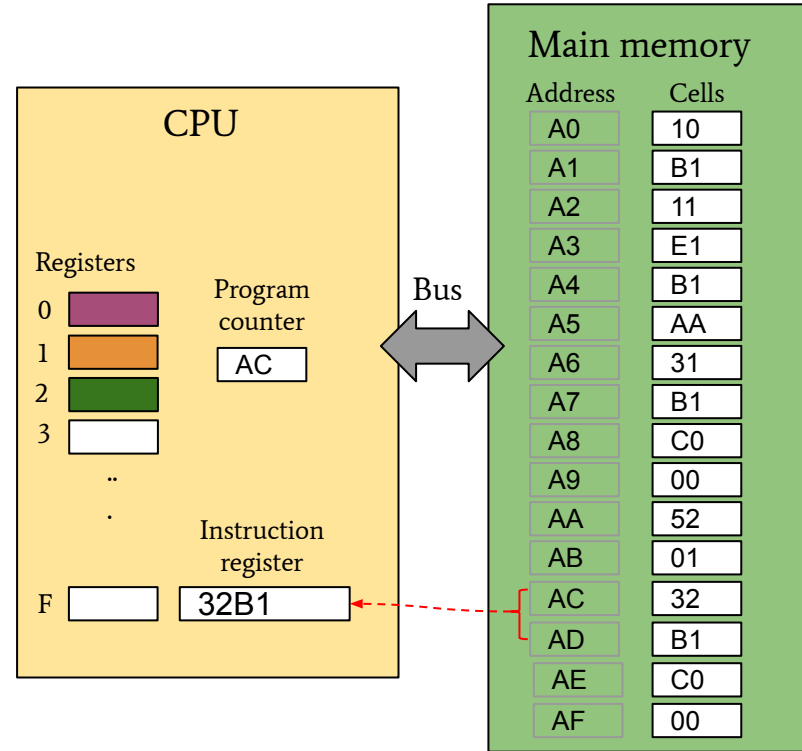
Encoded instructions	Translation
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B1AA	If Reg.1 is equal to Reg. 0, jump to AA
31B1	Store the contents of Reg.1 at address B1
C000	Halt
5201	Add contents of Reg. 0 and Reg. 1; leave the result in Reg. 2
32B1	Store the contents of Reg. 2 at address B1
C000	Halt



Go to AA, load the instruction into IR

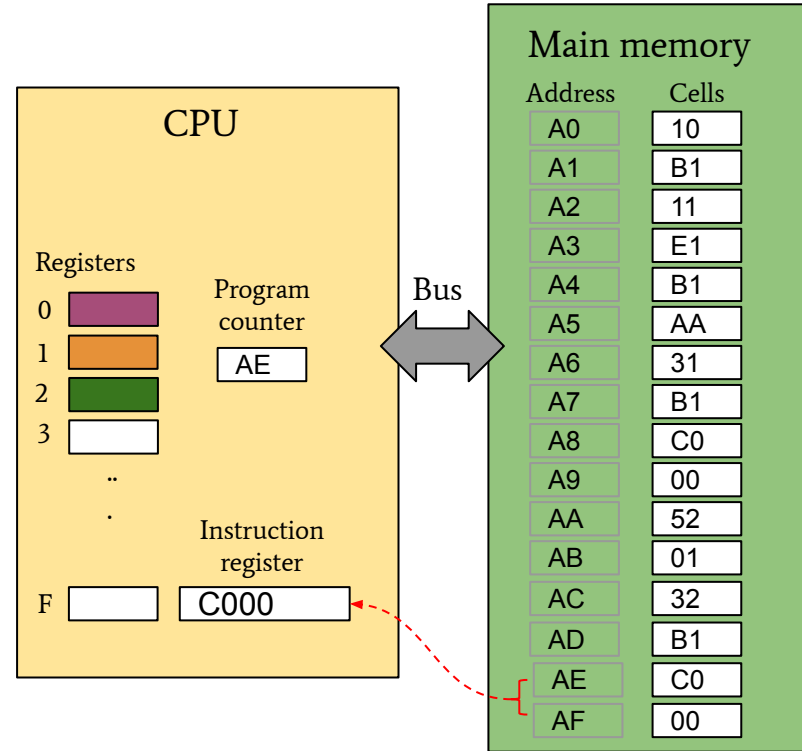
The if/else statement

Encoded instructions	Translation
10B1	Load register 0 from address B1
11E1	Load register 1 from address E1
B1A8	If Reg.1 is equal to Reg. 0, jump to AA
31B1	Store the contents of Reg.1 at address B1
C000	Halt
5201	Add contents of register 0 and 1; leave the result in register 2
32B1	Store the contents of Reg. 2 at address B1
C000	Halt

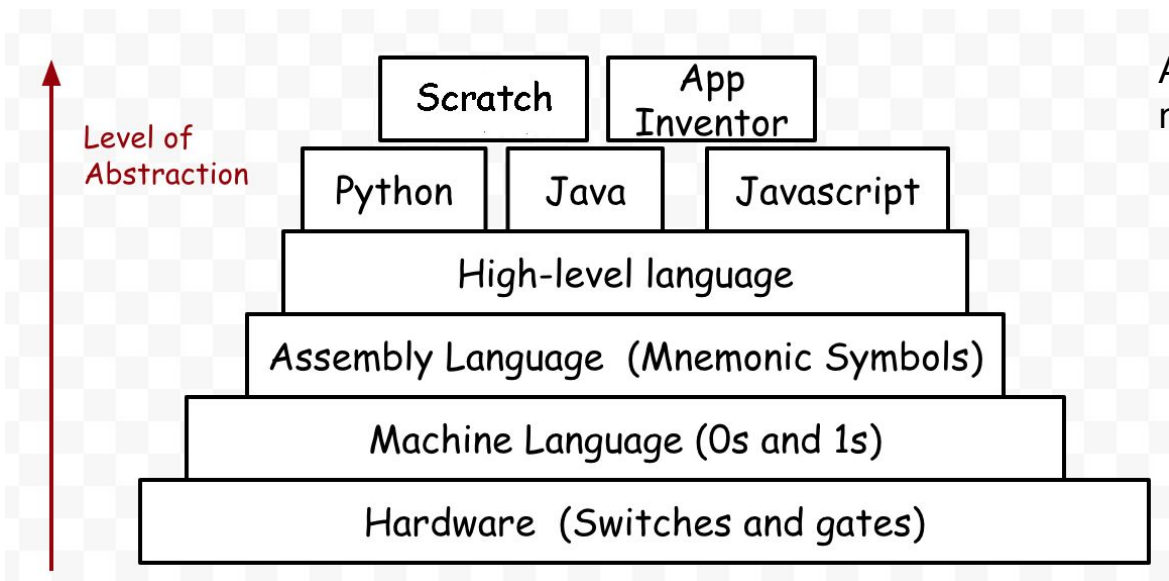


The if/else statement

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C000	Halt



Levels of languages



Abstraction: a powerful tool for managing complexity.

- representing complex systems, processes, or data in a simplified or more manageable form, while hiding unnecessary details or complexities

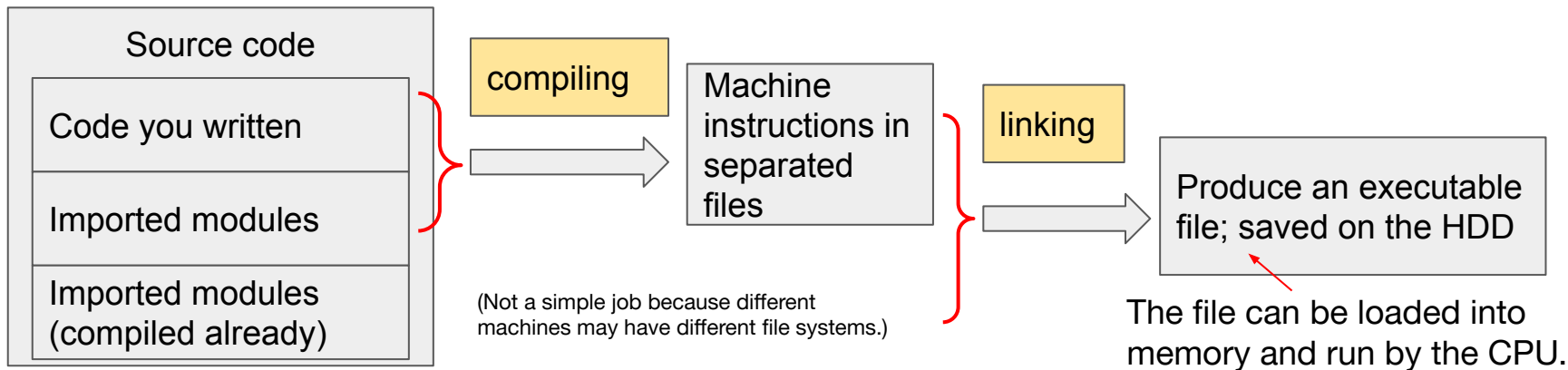
Running codes in high-level languages

- CPUs only “understand” machine languages.
- Programs in high-level languages must be translated into machine languages
⇒ compiling and linking are needed

Compiling and Linking

Translating the source code to a runnable file

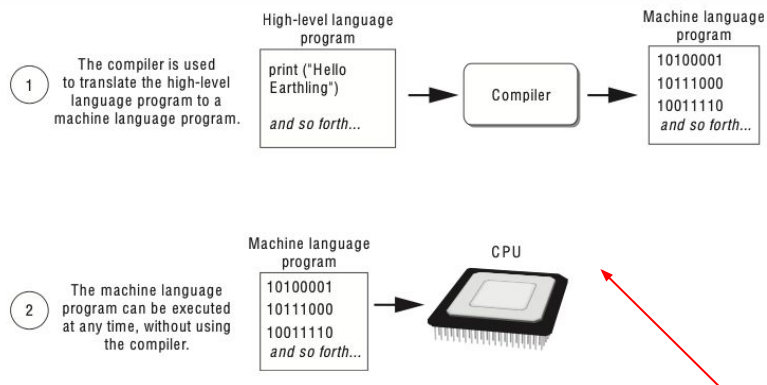
- Compilation: produce the machine language instructions according to the source code
- Linking: merge all the files that are needed to execute your code. For example, the modules/packages you imported in your source code.



Two types of the translation

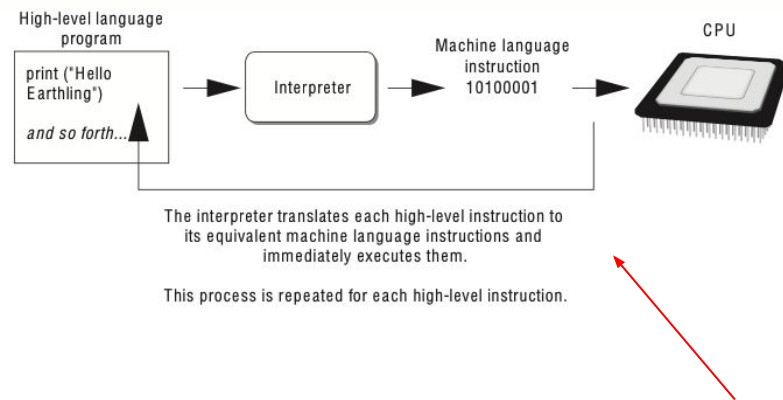
- using a compiler: C, C++, Java, etc.
- using an interpreter: Python, Javascript, Matlab
- But both need compiling and linking

Figure 1-18 Compiling a high-level program and executing it



Translating the all instructions into machine language in one time.

Figure 1-19 Executing a high-level program with an interpreter

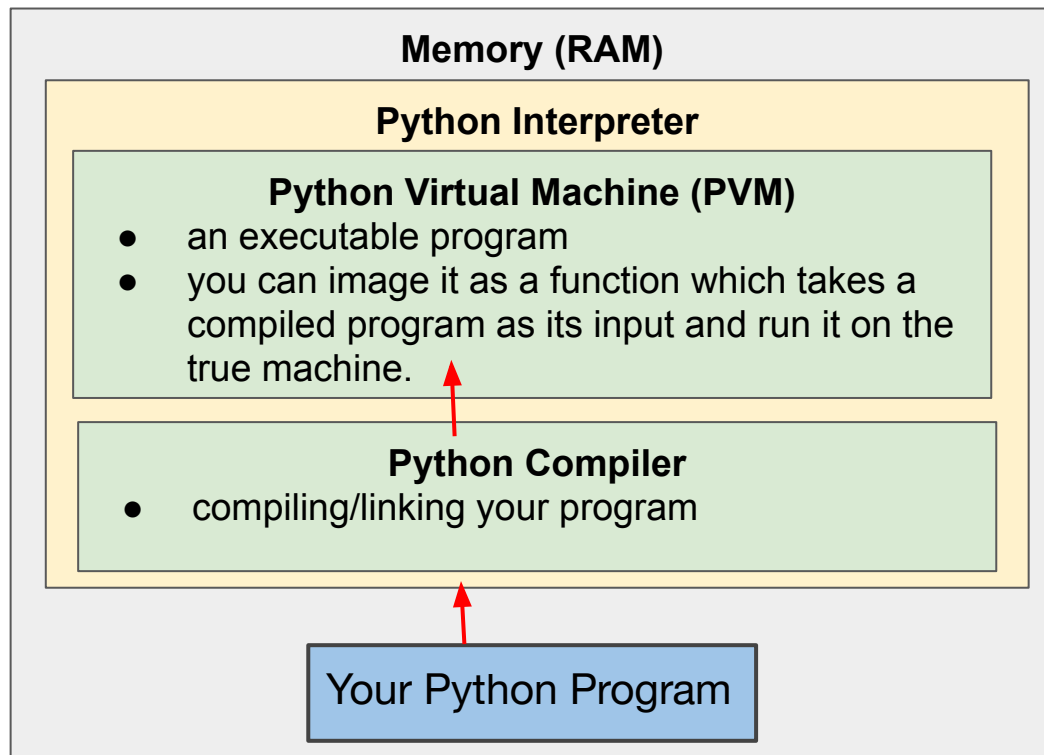


Translating and executing instructions one by one.

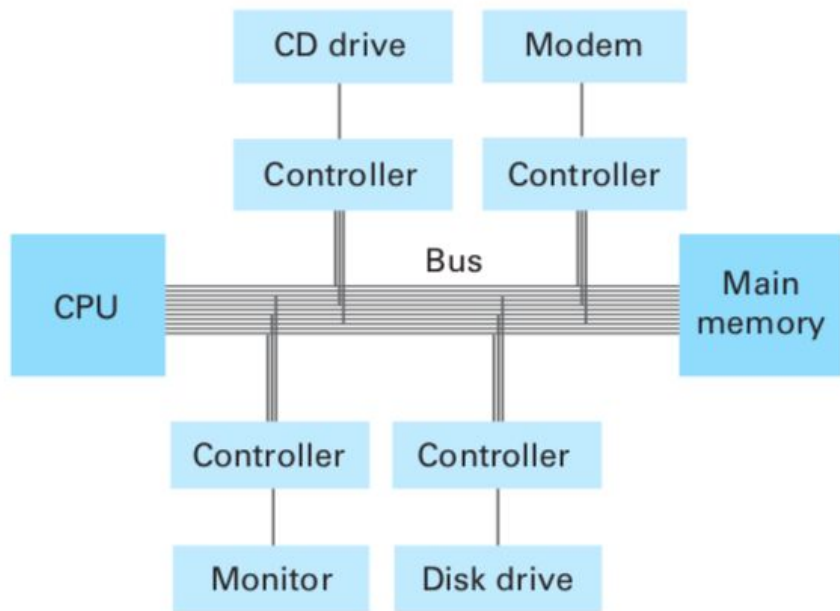
Running Python code

Every statement in your program will be compiled and linked by the compiler, then be executed by the PVM, one by one.

- The compiler translates a statement into the instructions can only be understood by the PVM, called **bytecode**;
- PVM runs the bytecode;
- No need to make an executable file on HDD, then, loading and executing it. (because the PVM is already loaded in memory and can run the code instantly)



Communicating with peripheral devices



CPU and memory communicate with devices such as disk drivers, keyboards through an intermediary apparatus, called **controller**.

A controller translates messages and data back and forth between the computer and the device.

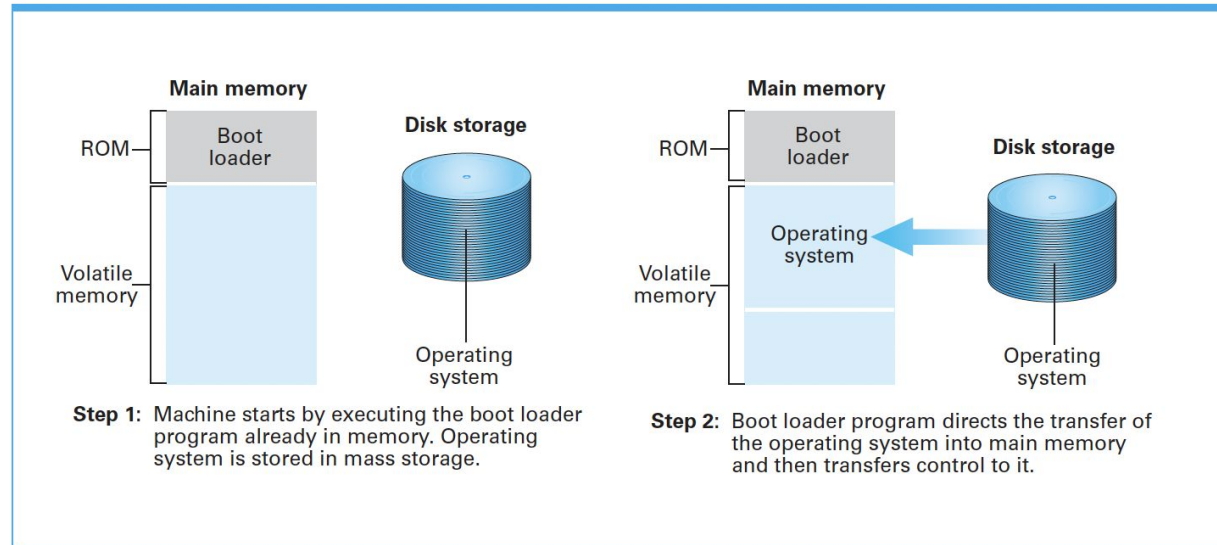
Some communication standards:

- Universal serial bus (usb)
- High definition multimedia interface (HDMI)
- DisplayPort (DP)

To get it started \Rightarrow two steps

1. When you turn on your computer, the program (i.e., boot loader) stored in the ROM is in the main memory and is executed immediately.
2. Boot loader will load the operating system into main memory and transfer control to it.

Figure 3.5 The booting process



Appendix:

- Play with RodRego
- Binary number measurement

Register machine: RodRego

RodRego is a simplified **computer**:

- Only has ten registers (each has an ID, from 0-9)
- Three instructions: INC, DEB, END

You may watch the introduction, then, try the exercises in the following slides

- Introduction to RodRego: https://stream.nyu.edu/media/RodRego/0_a4mklaon
 - Introduction slides: https://docs.google.com/presentation/d/1Gyg6Crp48d5sPz6_NkJqfbQ5yVEbNbwbad0evt4KmSE/edit?usp=sharing
- Go to RodRego: <https://rodrego.it.tufts.edu/>

Now it's your turn.

1. Non-destructive ADD [1] [2] [3]: add Reg 1 and Reg 2, and save the result in Reg [3] (register 1 and 2 stay)
2. MULTIPLY [1] [2] [3]: multiply Reg 1 and Reg 2, and save the result in Reg [3]

Non-destructive add [1] [2] [3]

1. Copy [1] [4]
2. Copy [2] [5]
3. ADD [4] [5]
4. CLEAR [3]
5. MOVE [5] [3]

Question: Can you do better?

RodRego

Step	Operation	Cell 1	Cell 2	Cell 3	Cell 4	Cell 5	Cell 6	Cell 7	Cell 8	Cell 9	Cell 10	Cell 11	Cell 12	Cell 13	Cell 14	Cell 15	Cell 16	Cell 17	Cell 18	Cell 19	Cell 20
1	DEB	4	1	2																	
2	DEB	5	2	3																	
3	DEB	1	4	6																	
4	INC	4	5																		
5	INC	5	3																		
6	DEB	5	7	8																	
7	INC	1	6																		
8	DEB	5	8	9																	
9	DEB	6	9	10																	
10	DEB	2	11	13																	
11	INC	5	12																		
12	INC	6	10																		
13	DEB	6	14	15																	
14	INC	2	13																		
15	DEB	4	16	17																	
16	INC	5	15																		
17	DEB	3	17	18																	
18	DEB	5	19	20																	
19	INC	3	18																		
20	END																				

COPY [1][4]
1 DEB 4 1 2
2 DEB 5 2 3
3 DEB 1 4 6
4 INC 4 5
5 INC 5 3
6 DEB 5 7 8
7 INC 1 6
COPY [2][5]
8 DEB 5 8 9
9 DEB 6 9 10
10 DEB 2 11 13
11 INC 5 12
12 INC 6 10
13 DEB 6 14 15
14 INC 2 13
ADD [4][5]
15 DEB 4 16 17
16 INC 5 15
MOVE [5][3]
17 DEB 3 17 18
18 DEB 5 19 20
19 INC 3 18
20 END

Play Reset Step

Multiply [1][2][3]

Assume:

Reg 1 = N

Reg 2 = M

1. CLEAR [3]
2. LOOP M times:
 - COPY [1][3]

RodRego

0		
1		
2		
3		
4		
5		
6		
7		
8		
9		

1	DEB	3	1	2
2	DEB	4	2	3
3	DEB	2	4	9
4	DEB	1	5	7
5	INC	3	6	
6	INC	4	4	
7	DEB	4	8	3
8	INC	1	7	
9	END			

```

1 DEB 3 1 2
2 DEB 4 2 3
3 DEB 2 4 9
4 DEB 1 5 7
5 INC 3 6
6 INC 4 4
7 DEB 4 8 3
8 INC 1 7
9 END

```

Play

Reset

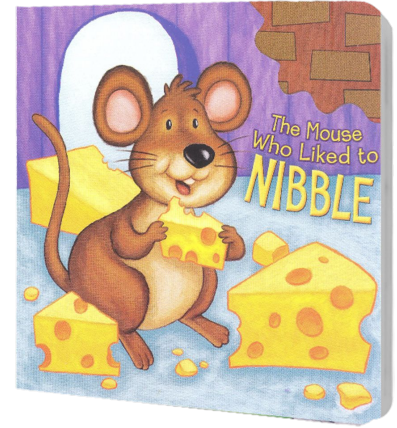
Step

RodRego by [Daniel Dennett](#)
 Web Application by [Ben Tanen](#)

Binary number measurement

Several definitions you should know

- a bit : a binary digit
 - It has two possible values: 0, and 1.
- a byte: a group of eight bits
 - It can represent $2^8 = 256$ possibilities.
- a nibble: a group of four bits (no longer a commonly use)
 - It can represent $2^4 = 16$ possibilities.
- a word: the size of the chunk of data that a microprocessor handling at a time.
 - It depends on the architecture of the microprocessor.
 - a 64-bit microprocessor means it operates on 64-bit word



File size

1 byte = 8 bit

1024 byte = 1 KB

KB = Kilobyte

$$2^{10} = 1024 \approx 10^3$$

1024 KB = 1 MB

MB = Megabyte

$$2^{20} \approx 10^6$$

1024 MB = 1 GB

GB = Gigabyte

$$2^{30} \approx 10^9$$

1024 GB = 1 TB

TB = Terabyte

$$2^{40} \approx 10^{12}$$

1024 TB = 1 PB

PB = Petabyte

$$2^{50} \approx 10^{15}$$