

-HW 2 tomorrow

-last Wednesday: cubic regression splines  
natural cubic splines

$p=1$ , one  $X$  predictor

overall relationship between  $X$  and  $Y$

### Degrees of Freedom

t-test  $t = \frac{\bar{X} - \mu}{s/\sqrt{n}} \sim t_{n-1}$

Given we have  $\bar{X}$   
we can vary  $n-1$  of  
the samples to get  $\bar{X}$

$$n=4, \bar{X}=10$$

$$X_1 = 5, X_2 = 15, X_3 = 40$$

to make this  $\bar{X}=10$ ,

$$\Rightarrow X_4 = -20$$

degrees of freedom of a model  
 $=$  # of things we estimate

$$Y = \beta_0 + \beta_1 X + \varepsilon \Rightarrow \text{df of model} = 2$$

Cubic spline with  $K$  knots  $\rightarrow \text{df} = K+3$

natural cubic spline  $K$  knots  $\rightarrow \text{df} = K+1$

df  $\approx$  "flexibility" of model

df is a bias/variance trade-off

LS with  $p$  predictors

$$\hookrightarrow p+1 \text{ df}$$

Ridge/LASSO

$$< p+1 \text{ df}$$

shrinkage = reducing df