# **k-Nearest Neighbors**

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In this lesson we'll learn the theory behind using k-nearest neighbors (kNN) as a supervised classification technique. We'll then use kNN to classify the UCI wine dataset in R.

### Additional packages needed

To run the code you may need additional packages.

• If necessary install the followings packages.

```
install.packages("ggplot2");
install.packages("class");
library(ggplot2)
library(class)
```

#### **Data**

We will be using the UCI Machine Learning Repository: Wine Data Set. These data are the results of a chemical analysis of wines grown in the same region in Italy but derived from three different cultivars. The analysis determined the quantities of 13 constituents found in each of the three types of wines.

The attributes are:

- 1) Alcohol
- 2) Malic acid
- 3) Ash
- 4) Alcalinity of ash
- 5) Magnesium
- 6) Total phenols
- 7) Flavanoids
- 8) Nonflavanoid phenols
- 9) Proanthocyanins
- 10) Color intensity
- 11) Hue
- 12) OD280/OD315 of diluted wines
- 13) Proline

Feel free to tweet questions to [@NikBearBrown](https://twitter.com/NikBearBrown)

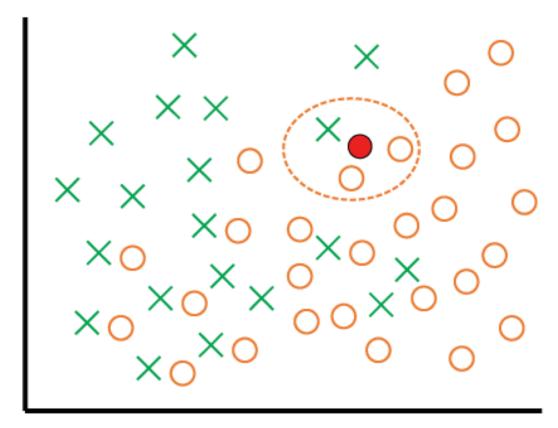
```
# Load our data
data url <-
'http://nikbearbrown.com/YouTube/MachineLearning/M07/wine.csv'
wn <- read.csv(url(data url))</pre>
head(wn)
##
     Cultivar Alcohol Malic.acid Ash Alcalinity.ash Magnesium
Total.phenols
## 1
                14.23
                             1.71 2.43
                                                  15.6
            1
                                                              127
2.80
## 2
                13.20
                             1.78 2.14
                                                  11.2
                                                              100
            1
2.65
## 3
            1
                13.16
                             2.36 2.67
                                                  18.6
                                                              101
2.80
                                                  16.8
## 4
            1
                14.37
                             1.95 2.50
                                                              113
3.85
## 5
            1
                13.24
                             2.59 2.87
                                                  21.0
                                                              118
2.80
## 6
            1
                14.20
                             1.76 2.45
                                                  15.2
                                                              112
3.27
     Flavanoids Nonflavanoid.phenols Proanthocyanins Color.intensity
##
Hue
## 1
           3.06
                                 0.28
                                                  2.29
                                                                   5.64
1.04
           2.76
## 2
                                 0.26
                                                  1.28
                                                                   4.38
1.05
           3.24
                                 0.30
## 3
                                                  2.81
                                                                   5.68
1.03
## 4
           3.49
                                 0.24
                                                  2.18
                                                                   7.80
0.86
## 5
           2.69
                                 0.39
                                                  1.82
                                                                   4.32
1.04
## 6
           3.39
                                 0.34
                                                  1.97
                                                                   6.75
1.05
##
     OD280.OD315 Proline
## 1
            3.92
                     1065
## 2
            3.40
                     1050
## 3
            3.17
                     1185
## 4
            3.45
                     1480
## 5
                      735
            2.93
## 6
            2.85
                     1450
```

## k-Nearest Neighbors (kNN)

A simple supervised learning algorithm is k-Nearest Neighbors algorithm (k-NN). KNN is a non-parametric method used for classification and regression.

In both cases, the input consists of the k closest training examples in the feature space. The output depends on whether k-NN is used for classification or regression:

In k-NN classification, the output is a class membership. An object is classified by a majority vote of its neighbors, with the object being assigned to the class most common among its k nearest neighbors (k is a positive integer, typically small). If k = 1, then the object is simply assigned to the class of that single nearest neighbor.



k-nearest neighbor voting

k-nearest neighbor voting

In k-NN regression, the output is the property value for the object. This value is the average of the values of its k nearest neighbors.

k-NN has the nice property that a labled subset of a data set could be used to label the whole data set. This is especially important in the analysis of "big-data." Most big-data sets are only partially labled, as labeling often librarys human annotation. While many are looking to unsupervised learning the 'future' of big-data, k-Nearest Neighbors is an instance of a supervised learning algorithm that can be used with big-data.

The kNN classification problem is to find the k nearest data points in a data set to a given query data point. The point is then assigned to the group by a majority "vote." For this reason, pick an odd k is prefered as the odd vote can break ties. This operation is also known as a kNN join, and can be defined as: given two data sets *R* and *S*, find the k nearest Neighbor from *S* for every object in *R*. *S* refers to data that

has already been classified, the training set. *R* refers to data that is needs to be classified.

The kNN algorithm can be fairly expensive, especially if one chooses a large k, as the k-nearest neighbors in *S* for every point in *R* needs to be calculated.

### **Nearest neighbor search**

A simple solution to finding nearest neighbors is to compute the distance from the each point in S to every point in R and keeping track of the "best so far". This algorithm, sometimes referred to as the naive approach, has a running time of O(|R||S|).

One can speed up the search to retrieve a "good guess" of the nearest neighbor. This is often done be limiting the search to a preset radius around a point culling out most of the points in *S*. If k neighbors aren't not found in the radius then the bound can be iteratively expanded until k are found. Althernatively, the vote could be made using fewer points when k points aren't found within a radius r.

## k-Nearest Neighbors is nonparametric "lazy learning"

K-Nearest Neighbors algorithm (kNN) is a nonparametric method for classifying objects based on the closest training examples in the feature space. kNN is nonparametric becuase it does not involve any estimation of parameters. This is sometimes called "lazy learning" or instance-based learning, as the mapping is approximated locally and all computation is deferred until classification.

#### **kNN Classification and Distance Metrics**

Neighbors are defined by a distance or dissimilarity measure. In essence, the only thing that kNN librarys is some measure of "closeness" of the points in S and R. Any distance metric or dissimilarity measure can be used. The most common being the Euclidean distance between the points  $x = (x_1, x_2, ..., x_n)$  and  $y = (y_1, y_2, ..., y_n)$  is given by the pythagorean formula:

$$d(\mathbf{p}, \mathbf{q}) = d(\mathbf{q}, \mathbf{p}) = \sqrt{(q_1 - p_1)^2 + (q_2 - p_2)^2 + \dots + (q_n - p_n)^2}$$
$$= \sqrt{\sum_{i=1}^{n} (q_i - p_i)^2}.$$

Any measure of "closeness", distance or dissimilarity measure can be used. For example,

• Chebyshev distance - measures distance assuming only the most significant dimension is relevant.

- Hamming distance identifies the difference bit by bit of two strings
- Mahalanobis distance normalizes based on a covariance matrix to make the distance metric scale-invariant.
- Manhattan distance measures distance following only axis-aligned directions.
- Minkowski distance is a generalization that unifies Euclidean distance, Manhattan distance, and Chebyshev distance

.. and many more.

## **kNN** Algorithm

#### **Distance function**

The distance function depends on your needs, but in general choosing features and distance metrics in which being "close" makes some sense in your domain are the distance metrics and features to choose. The type of variable, categorical, ordinal or nominal should be considered when choosing a sensible measure of closeness.

### k nearest neighbors

Given an data point p, a training data set S, and an integer k, the k nearest neighbors of p from S, denoted as kNN(p, S), are a set of k objects from S such that:

$$\forall o \in kNN(q, S), \forall s \in S-kNN(q, S), |o, p| \leq |s, p|$$

## kNN join

Given two data sets R and S (where S is a training data set) and an integer k, the kNN join of R and S is defined as:

$$kNNjoin(R, S) = \{(r, s) | \forall r \in R, \forall s \in kNN(r, S)\}$$

Basically, this combines each object  $r \in R$  with its k nearest neighbors from S.

# **Steps in kNN Classification**

The kNN algorithm can be summarized in the following simple steps:

- Determine k (the selection of k depends on your data and project libraryments; there is no magic formula for k).
- Calculate the distances between the new input and all the training data (as with k, the selection of a distance function also depends on the type of data).

- Sort the distance and determine the k nearest neighbors based on the kth minimum distance.
- Gather the categories of those neighbors.
- Determine the category based on majority vote.

# k-Nearest Neighbors (kNN) in R

k-Nearest Neighbors (kNN) in R

head(wn)							
##		lcohol	Malic.acid	Ash	Alcalinity.ash	Magnesium	
Total.phenols							
## 1		14.23	1./1	2.43	15.6	127	
2.80		42.00	4 70	2 4 4	44.2	100	
## 2		13.20	1.78	2.14	11.2	100	
2.65		12 16	2.26	2 67	10.6	101	
## 3		13.16	2.36	2.67	18.6	101	
2.80		14 27	1 05	2 50	16.0	112	
## 4 3.85		14.37	1.95	2.50	16.8	113	
## 5		13.24	2 50	2.87	21.0	118	
2.80		13.24	2.59	2.0/	21.0	110	
## 6		14.20	1 76	2.45	15.2	112	
3.27		14.20	1.70	2.43	13.2	112	
##		Nonfl:	avanoid nhei	nols F	Proanthocyanins	Color inte	nsitv
Hue	Tavanoras	140111 1	avanora.pnc	.015 .	1 ounchocy uniins	color finec	
## 1	3.06		(	2.28	2.29		5.64
1.04							
## 2			(	ð.26	1.28		4.38
1.05							
## 3	3.24		(	0.30	2.81		5.68
1.03							
## 4	3.49	1	(	ð.24	2.18		7.80
0.86							
## 5	2.69	1	(	0.39	1.82		4.32
1.04							
## 6		1	(	ð.34	1.97		6.75
1.05							
##	OD280.OD31						
## 1			<b>265</b>				
## 2			<b>050</b>				
## 3			185				
## 4			480				
## 5			735				
## 6	2.8	5 14	450				

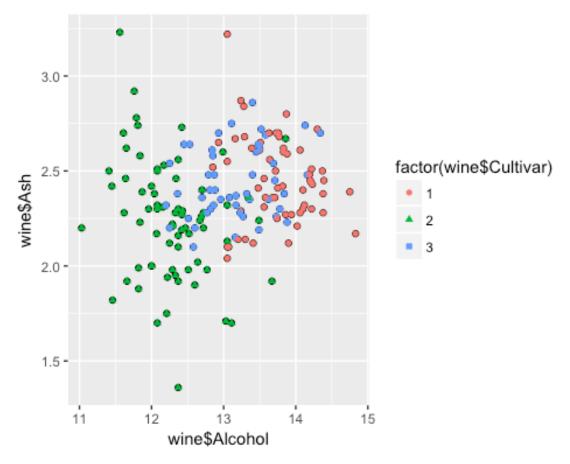
```
summary(wn)
##
       Cultivar
                      Alcohol
                                     Malic.acid
                                                        Ash
##
   Min. :1.000
                   Min.
                         :11.03
                                   Min. :0.740
                                                   Min.
                                                          :1.360
                                                   1st Qu.:2.210
##
   1st Qu.:1.000
                   1st Qu.:12.36
                                   1st Qu.:1.603
   Median :2.000
                   Median :13.05
                                   Median :1.865
                                                   Median :2.360
##
   Mean
          :1.938
                   Mean
                          :13.00
                                   Mean
                                          :2.336
                                                   Mean
                                                          :2.367
##
   3rd Qu.:3.000
                   3rd Qu.:13.68
                                   3rd Qu.:3.083
                                                   3rd Qu.:2.558
   Max.
          :3.000
                   Max.
                         :14.83
                                   Max. :5.800
                                                   Max. :3.230
##
##
   Alcalinity.ash
                     Magnesium
                                    Total.phenols
                                                      Flavanoids
                                                    Min.
##
   Min.
          :10.60
                   Min. : 70.00
                                    Min.
                                          :0.980
                                                           :0.340
##
   1st Qu.:17.20
                   1st Qu.: 88.00
                                    1st Qu.:1.742
                                                    1st Qu.:1.205
   Median :19.50
                   Median : 98.00
                                    Median :2.355
                                                    Median :2.135
##
   Mean
          :19.49
                   Mean
                         : 99.74
                                    Mean
                                           :2.295
                                                    Mean
                                                           :2.029
                                                    3rd Qu.:2.875
##
   3rd Ou.:21.50
                   3rd Qu.:107.00
                                    3rd Qu.:2.800
           :30.00
                          :162.00
                                           :3.880
                                                    Max.
                                                           :5.080
##
   Max.
                   Max.
                                    Max.
   Nonflavanoid.phenols Proanthocyanins Color.intensity
                                                              Hue
          :0.1300
                               :0.410
                                        Min. : 1.280
## Min.
                        Min.
                                                         Min.
:0.4800
## 1st Qu.:0.2700
                        1st Qu.:1.250
                                        1st Qu.: 3.220
                                                         1st
Ou.:0.7825
## Median :0.3400
                        Median :1.555
                                        Median : 4.690
                                                         Median
:0.9650
          :0.3619
## Mean
                        Mean
                               :1.591
                                        Mean : 5.058
                                                         Mean
:0.9574
## 3rd Qu.:0.4375
                        3rd Qu.:1.950
                                        3rd Qu.: 6.200
                                                         3rd
Ou.:1.1200
## Max.
          :0.6600
                        Max.
                               :3.580
                                        Max.
                                               :13.000
                                                         Max.
:1.7100
    OD280.OD315
                      Proline
##
##
   Min.
         :1.270
                   Min. : 278.0
                   1st Ou.: 500.5
   1st Ou.:1.938
##
   Median :2.780
                   Median : 673.5
##
          :2.612
                         : 746.9
   Mean
                   Mean
##
##
   3rd Ou.:3.170
                   3rd Ou.: 985.0
## Max.
         :4.000
                   Max. :1680.0
length(wn)
## [1] 14
names(wn)
## [1] "Cultivar"
                              "Alcohol"
                                                     "Malic.acid"
## [4] "Ash"
                              "Alcalinity.ash"
                                                     "Magnesium"
## [7] "Total.phenols"
                              "Flavanoids"
"Nonflavanoid.phenols"
## [10] "Proanthocyanins"
                              "Color.intensity"
                                                     "Hue"
## [13] "OD280.OD315"
                              "Proline"
table(wn$Cultivar)
```

```
##
## 1 2 3
## 59 71 48
wn$Cultivar
##
 1 1 1 1
2 2 2 2
2 2 2 2
3 3 3 3
3 3 3 3
## [176] 3 3 3
length(wn$Cultivar)
## [1] 178
```

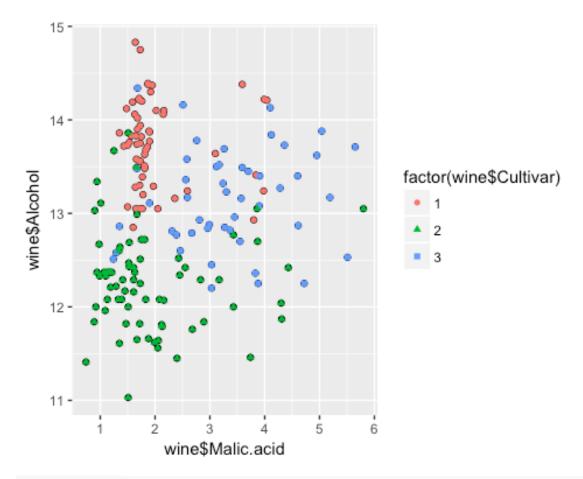
```
shuff<-runif(nrow(wn))</pre>
shuff
##
     [1] 0.879416736 0.465057831 0.203559469 0.857664812 0.446806759
##
     [6] 0.993477742 0.357465548 0.431790816 0.601351195 0.299737555
    [11] 0.065804084 0.950887116 0.072150465 0.090625413 0.893852573
##
    [16] 0.762482274 0.574194463 0.144995949 0.767682299 0.141855116
    [21] 0.339898303 0.417410148 0.072240409 0.639542649 0.452636903
    [26] 0.644134149 0.766408274 0.332183770 0.199284510 0.843122139
##
    [31] 0.848746219 0.930845051 0.159976850 0.469081585 0.364277273
##
    [36] 0.305499332 0.725547439 0.585616025 0.428702026 0.401016329
    [41] 0.228177729 0.563623512 0.698064011 0.299441274 0.415499139
    [46] 0.520055889 0.153109725 0.739615300 0.214080374 0.162166949
##
    [51] 0.082340735 0.375922605 0.539000284 0.056279513 0.429294613
##
    [56] 0.129012763 0.134195874 0.257771960 0.311076509 0.578258805
##
    [61] 0.719523014 0.801622628 0.483144780 0.911315740 0.160058855
##
    [66] 0.858762778 0.490823320 0.893487326 0.208629933 0.896674890
##
    [71] 0.425024987 0.862942249 0.753033714 0.882109831 0.149832761
##
##
    [76] 0.360869391 0.552097062 0.216466527 0.924754099 0.523228708
    [81] 0.753214470 0.167602310 0.941527774 0.883650711 0.263295079
##
    [86] 0.502849103 0.072817653 0.355810725 0.803872135 0.904544791
    [91] 0.592107939 0.701228071 0.590443582 0.227611112 0.502662175
## [96] 0.036936287 0.529074259 0.250616603 0.262424937 0.105996758
## [101] 0.699227039 0.362480839 0.108325217 0.355212895 0.496549245
## [106] 0.118456276 0.557677326 0.085181800 0.963453403 0.152147554
## [111] 0.635562747 0.676331046 0.721586145 0.080935735 0.387654620
## [116] 0.098254921 0.466039377 0.530348545 0.454439861 0.057937427
```

```
## [121] 0.280140246 0.502869837 0.988537036 0.808908303 0.244104668
## [126] 0.518662793 0.820486286 0.164370501 0.698453487 0.260842148
## [131] 0.960960730 0.416402775 0.449777470 0.226571414 0.532649183
## [136] 0.895524792 0.026771151 0.845000878 0.549343386 0.006257911
## [141] 0.789321971 0.071647472 0.927306648 0.445342876 0.876622166
## [146] 0.097234364 0.329052628 0.832512605 0.267979169 0.042547621
## [151] 0.635819976 0.773744501 0.858690942 0.494700995 0.019334461
## [156] 0.828572836 0.709275471 0.661391530 0.914107190 0.710001386
## [161] 0.453391860 0.868659350 0.823411378 0.920017180 0.135356334
## [166] 0.305071812 0.655010787 0.261217887 0.459005100 0.818608793
## [171] 0.955147237 0.794117657 0.337661183 0.099180498 0.934245064
## [176] 0.510923482 0.433632229 0.539134596
wine<-wn[order(shuff),]</pre>
wine$Cultivar
    2 1 2 2
1 1 2 1
3 1 3 3
## [106] 2 2 1 1 2 1 2 2 1 2 3 1 1 3 3 2 1 2 2 2 3 3 2 2 1 1 2 2 1 1 1
3 3 3 2
## [141] 2 2 3 2 3 3 3 1 3 1 1 3 2 2 3 3 1 2 2 2 1 3 2 2 2 3 3 2 3 1 3
2 1 3 3
## [176] 2 2 1
```

```
qplot(wine$Alcohol,wine$Ash,data=wine)+geom_point(aes(colour =
factor(wine$Cultivar),shape = factor(wine$Cultivar)))
```



qplot(wine\$Malic.acid,wine\$Alcohol,data=wine)+geom\_point(aes(colour =
factor(wine\$Cultivar),shape = factor(wine\$Cultivar)))



```
summary(wine)
##
       Cultivar
                       Alcohol
                                       Malic.acid
                                                           Ash
                                           :0.740
##
    Min.
          :1.000
                    Min.
                          :11.03
                                     Min.
                                                     Min. :1.360
                                     1st Qu.:1.603
    1st Qu.:1.000
                    1st Qu.:12.36
                                                     1st Qu.:2.210
    Median :2.000
##
                    Median :13.05
                                     Median :1.865
                                                     Median :2.360
##
   Mean
          :1.938
                          :13.00
                                          :2.336
                                                            :2.367
                    Mean
                                     Mean
                                                     Mean
##
    3rd Qu.:3.000
                    3rd Qu.:13.68
                                     3rd Qu.:3.083
                                                     3rd Qu.:2.558
          :3.000
                           :14.83
                                          :5.800
##
    Max.
                    Max.
                                     Max.
                                                     Max.
                                                             :3.230
##
    Alcalinity.ash
                      Magnesium
                                      Total.phenols
                                                        Flavanoids
##
    Min.
           :10.60
                    Min.
                           : 70.00
                                      Min.
                                             :0.980
                                                      Min.
                                                              :0.340
    1st Qu.:17.20
                    1st Qu.: 88.00
                                      1st Qu.:1.742
                                                      1st Qu.:1.205
    Median :19.50
                    Median : 98.00
                                      Median :2.355
                                                      Median :2.135
    Mean
           :19.49
                    Mean
                           : 99.74
                                      Mean
                                             :2.295
                                                      Mean
                                                             :2.029
##
    3rd Qu.:21.50
                    3rd Qu.:107.00
                                      3rd Qu.:2.800
                                                      3rd Qu.:2.875
##
##
    Max.
           :30.00
                    Max.
                            :162.00
                                      Max.
                                             :3.880
                                                      Max.
                                                             :5.080
##
    Nonflavanoid.phenols Proanthocyanins Color.intensity
                                                                 Hue
##
   Min.
           :0.1300
                         Min.
                                 :0.410
                                          Min. : 1.280
                                                            Min.
:0.4800
   1st Qu.:0.2700
                         1st Qu.:1.250
                                          1st Qu.: 3.220
                                                            1st
Qu.:0.7825
                                          Median : 4.690
## Median :0.3400
                         Median :1.555
                                                            Median
:0.9650
```

```
## Mean
           :0.3619
                         Mean
                                :1.591
                                         Mean : 5.058
                                                          Mean
:0.9574
## 3rd Qu.:0.4375
                         3rd Qu.:1.950
                                         3rd Qu.: 6.200
                                                          3rd
Ou.:1.1200
## Max.
           :0.6600
                         Max.
                                :3.580
                                         Max.
                                                :13.000
                                                          Max.
:1.7100
                       Proline
##
     OD280.OD315
           :1.270
                           : 278.0
##
   Min.
                    Min.
##
                    1st Qu.: 500.5
   1st Qu.:1.938
   Median :2.780
                    Median : 673.5
##
                         : 746.9
##
   Mean
           :2.612
                    Mean
   3rd Qu.:3.170
                    3rd Qu.: 985.0
##
                    Max. :1680.0
##
   Max. :4.000
```

```
wine.scaled<-as.data.frame(lapply(wine[,c(2:14)], scale))</pre>
head(wine.scaled)
        Alcohol Malic.acid
                                   Ash Alcalinity.ash
                                                        Magnesium
## 1 -0.1978477 0.5582544 0.88751034
                                            1.3489954
                                                       0.08810981
## 2 -0.5181131 -0.9366262 -0.97146956
                                            0.1512342
                                                       0.22814148
## 3 -0.9246039
                2.1336974 0.63235624
                                            0.4506745 -0.75208020
## 4 -0.6536100 -0.7307445 -0.60696370
                                           -0.1482061
                                                       4.35907571
     0.0977820 1.3996841 -0.02375431
                                            0.6003946
## 5
                                                       0.92829983
                                           -0.7171427
## 6 0.9477173 -0.3905920 1.14266445
                                                       1.06833150
##
     Total.phenols Flavanoids Nonflavanoid.phenols Proanthocyanins
## 1
        0.03976608 -1.4309028
                                         1.3510772
                                                        -1.3643519
## 2
       -1.30240632 -1.4509256
                                         1.3510772
                                                        -0.3335300
## 3
       -1.46218874 -1.5610513
                                         1.3510772
                                                        -1.3818234
## 4
       0.32737445 0.2410054
                                        -0.3363022
                                                         2.9511225
## 5
       -1.41425402 -0.6400001
                                        -0.1755994
                                                        -0.7877905
## 6
        1.12628658 0.7615996
                                         0.2261576
                                                         0.1556735
##
     Color.intensity
                            Hue OD280.OD315
                                                Proline
## 1
         -0.05956551 -0.2950911 -0.65026988 -0.49822018
## 2
          1.09646103 -1.6513403 -1.49535170 -0.33944338
## 3
         -0.52111342 -0.9075907 -1.88972321 -0.08540051
## 4
         -1.06030491 0.8861582 0.02579557 0.60369079
## 5
          1.87289677 -1.6950903 -1.80521503 -0.62524162
## 6
          0.53570189 0.7549083 0.44833648 1.99457553
summary(wine.scaled)
##
       Alcohol
                         Malic.acid
                                              Ash
          :-2.42739
   Min.
                       Min.
                             :-1.4290
                                         Min.
                                                :-3.66881
   1st Qu.:-0.78603
                       1st Qu.:-0.6569
                                         1st Qu.:-0.57051
##
##
   Median : 0.06083
                       Median :-0.4219
                                         Median :-0.02375
##
   Mean
          : 0.00000
                       Mean
                              : 0.0000
                                         Mean
                                                : 0.00000
##
    3rd Qu.: 0.83378
                       3rd Qu.: 0.6679
                                         3rd Qu.: 0.69615
##
   Max.
           : 2.25341
                              : 3.1004
                                         Max.
                                                : 3.14745
                       Max.
## Alcalinity.ash
                          Magnesium Total.phenols
```

```
Min. :-2.663505
                       Min. :-2.0824
                                        Min. :-2.10132
                                        1st Qu.:-0.88298
   1st Qu.:-0.687199
                       1st Qu.:-0.8221
                       Median :-0.1219
                                        Median : 0.09569
##
   Median : 0.001514
##
   Mean
         : 0.000000
                              : 0.0000
                                              : 0.00000
                       Mean
                                        Mean
##
   3rd Qu.: 0.600395
                       3rd Qu.: 0.5082
                                         3rd Qu.: 0.80672
          : 3.145637
                              : 4.3591
                                               : 2.53237
##
   Max.
                       Max.
                                        Max.
##
     Flavanoids
                     Nonflavanoid.phenols Proanthocyanins
## Min.
          :-1.6912
                     Min.
                            :-1.8630
                                         Min.
                                                :-2.06321
   1st Qu.:-0.8252
                     1st Qu.:-0.7381
                                         1st Qu.:-0.59560
##
   Median : 0.1059
                     Median :-0.1756
                                         Median :-0.06272
##
                                         Mean : 0.00000
   Mean
         : 0.0000
                     Mean : 0.0000
   3rd Qu.: 0.8467
                     3rd Qu.: 0.6078
                                         3rd Qu.: 0.62741
##
##
   Max.
          : 3.0542
                     Max.
                            : 2.3956
                                         Max.
                                               : 3.47527
## Color.intensity
                          Hue
                                         OD280.OD315
                                                            Proline
## Min.
         :-1.6297
                           :-2.08884
                                       Min. :-1.8897
                     Min.
                                                         Min.
                                                                : -
1.4890
## 1st Qu.:-0.7929
                     1st Qu.:-0.76540
                                       1st Qu.:-0.9496
                                                         1st Qu.:-
0.7824
## Median :-0.1588
                     Median : 0.03303
                                       Median : 0.2371
                                                         Median :-
0.2331
## Mean
          : 0.0000
                     Mean
                            : 0.00000
                                       Mean : 0.0000
                                                                :
                                                         Mean
0.0000
## 3rd Qu.: 0.4926
                     3rd Qu.: 0.71116
                                       3rd Qu.: 0.7864
                                                         3rd Qu.:
0.7561
## Max.
          : 3.4258
                     Max.
                            : 3.29241
                                       Max.
                                              : 1.9554
                                                         Max.
2.9631
```

```
normalize<- function(x) {</pre>
  return((x-min(x))/(max(x)-min(x)))
}
wine.normalized<-as.data.frame(lapply(wine[,c(2:14)],normalize))
head(wine.normalized)
       Alcohol Malic.acid
                               Ash Alcalinity.ash Magnesium
Total.phenols
## 1 0.4763158 0.4387352 0.6684492
                                         0.6907216 0.3369565
0.4620690
## 2 0.4078947 0.1086957 0.3957219
                                         0.4845361 0.3586957
0.1724138
## 3 0.3210526 0.7865613 0.6310160
                                         0.5360825 0.2065217
0.1379310
## 4 0.3789474 0.1541502 0.4491979
                                         0.4329897 1.0000000
0.5241379
## 5 0.5394737 0.6245059 0.5347594
                                         0.5618557 0.4673913
0.1482759
## 6 0.7210526 0.2292490 0.7058824
                                         0.3350515 0.4891304
0.6965517
     Flavanoids Nonflavanoid.phenols Proanthocyanins Color.intensity
```

```
## 1 0.05485232
                            0.7547170
                                              0.1261830
                                                               0.3105802
## 2 0.05063291
                            0.7547170
                                              0.3123028
                                                               0.5392491
## 3 0.02742616
                            0.7547170
                                              0.1230284
                                                               0.2192833
## 4 0.40717300
                            0.3584906
                                             0.9053628
                                                               0.1126280
## 5 0.22151899
                            0.3962264
                                             0.2302839
                                                               0.6928328
## 6 0.51687764
                            0.4905660
                                             0.4006309
                                                               0.4283276
##
            Hue OD280.OD315
                                Proline
## 1 0.33333333
                  0.32234432 0.2225392
## 2 0.08130081
                  0.10256410 0.2582026
## 3 0.21951220
                  0.00000000 0.3152639
## 4 0.55284553
                  0.49816850 0.4700428
## 5 0.07317073
                  0.02197802 0.1940086
## 6 0.52845528 0.60805861 0.7824536
summary(wine.normalized)
##
       Alcohol
                        Malic.acid
                                              Ash
                                                          Alcalinity.ash
##
   Min.
           :0.0000
                      Min.
                              :0.0000
                                        Min.
                                                :0.0000
                                                          Min.
                                                                  :0.0000
##
    1st Qu.:0.3507
                      1st Qu.:0.1705
                                        1st Qu.:0.4545
                                                          1st Qu.:0.3402
##
   Median :0.5316
                      Median :0.2223
                                        Median :0.5348
                                                          Median :0.4588
##
   Mean
           :0.5186
                      Mean
                              :0.3155
                                        Mean
                                                :0.5382
                                                          Mean
                                                                  :0.4585
##
    3rd Qu.:0.6967
                      3rd Qu.:0.4629
                                        3rd Qu.:0.6404
                                                          3rd Qu.:0.5619
##
    Max.
           :1.0000
                      Max.
                              :1.0000
                                                :1.0000
                                                          Max.
                                                                  :1.0000
##
                      Total.phenols
                                           Flavanoids
      Magnesium
Nonflavanoid.phenols
##
   Min.
           :0.0000
                      Min.
                              :0.0000
                                        Min.
                                                :0.0000
                                                          Min.
                                                                  :0.0000
##
                                                          1st Qu.:0.2642
    1st Qu.:0.1957
                      1st Qu.:0.2629
                                        1st Qu.:0.1825
##
   Median :0.3043
                      Median :0.4741
                                        Median :0.3787
                                                          Median :0.3962
##
    Mean
           :0.3233
                      Mean
                              :0.4535
                                        Mean
                                                :0.3564
                                                          Mean
                                                                  :0.4375
##
    3rd Qu.:0.4022
                      3rd Qu.:0.6276
                                        3rd Qu.:0.5348
                                                           3rd Qu.:0.5802
##
    Max.
           :1.0000
                      Max.
                              :1.0000
                                        Max.
                                                :1.0000
                                                          Max.
                                                                  :1.0000
##
    Proanthocyanins
                      Color.intensity
                                             Hue
                                                           OD280.OD315
                                                :0.0000
##
           :0.0000
                              :0.0000
                                        Min.
                                                                  :0.0000
   Min.
                      Min.
                                                          Min.
                                        1st Qu.:0.2459
##
    1st Qu.:0.2650
                      1st Qu.:0.1655
                                                          1st Qu.:0.2445
                      Median :0.2910
                                        Median :0.3943
##
   Median :0.3612
                                                          Median :0.5531
                                                :0.3882
##
           :0.3725
                      Mean
                              :0.3224
                                                          Mean
                                                                  :0.4915
    Mean
                                        Mean
##
    3rd Qu.:0.4858
                      3rd Qu.:0.4198
                                        3rd Qu.:0.5203
                                                          3rd Qu.:0.6960
##
           :1.0000
                              :1.0000
    Max.
                      Max.
                                        Max.
                                                :1.0000
                                                          Max.
                                                                  :1.0000
##
       Proline
##
    Min.
           :0.0000
##
    1st Qu.:0.1587
##
   Median :0.2821
##
   Mean
           :0.3344
##
    3rd Qu.:0.5043
##
    Max.
           :1.0000
nrow(wine)
## [1] 178
```

```
wine.normalized.train<-wine.normalized[1:150,]</pre>
wine.normalized.test<-wine.normalized[151:178,]</pre>
wine.normalized.train.target<-wine[1:150,c(1)]</pre>
wine.normalized.test.target<-wine[151:178,c(1)]</pre>
wine.normalized.test.target
   [1] 1 3 2 2 3 3 1 2 2 2 1 3 2 2 2 3 3 2 3 1 3 2 1 3 3 2 2 1
k<-5
knn.m1<-knn(train = wine.normalized.train, test =</pre>
wine.normalized.test,wine.normalized.train.target,k)
knn.m1
## [1] 1 3 2 1 3 3 1 1 3 2 1 3 2 2 2 3 3 2 3 1 3 2 1 3 3 2 2 1
## Levels: 1 2 3
length(knn.m1)
## [1] 28
cm<-table(wine.normalized.test.target,knn.m1)</pre>
cm
##
                               knn.m1
## wine.normalized.test.target 1 2 3
                              1 6 0 0
                              2 2 9 1
##
##
                              3 0 0 10
```

#### Resources

- Using R For k-Nearest Neighbors (KNN)
- Using the k-Nearest Neighbors Algorithm in R
- kNN PSU