
CS 400 Lecture 3:

AVL Review,
Nested Classes,
Red-Black Trees

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Agenda for Tonight

5:30	Discuss Homework 0 ...
5:40	Review of AVL Trees: Balancing and Upkeep
6:10	X-Team activity
6:20	Break
6:35	Notes: Red-Black Trees
7:36	Break
7:40	Nested Classes
7:50	Putting it all together: AVLTree.java
8:00	Starting Program 2a: AVLTree.java
8:30	Adjourn

Homework 0:
answers should be available on Canvas
tomorrow morning

Review of AVL Trees

[Visualizer Web Site](#)

[Worksheet](#)

Notes about AVL Trees

Named after George Adelson-Velsky and Evgenii Landis

Complexity Analysis:

Insert, Delete, Lookup all are $O(\text{Height})$

They proved that the height worst-case is about
 $1.44 * \log_2(N)$

There must be Balance in the Force

```
private int getBalance(Node n){  
    return n.getRight().getHeight() - n.getLeft().getHeight();  
}  
  
private int getHeight(Node n) {  
    return recursiveHeight(n);  
    // OR have an instance variable for height for each node  
    // and constantly update this on every rotation/insert/delete  
}  
  
private int recursiveHeight(Node n){  
    if (n == null)  
        return 0;  
    return 1 + Math.max(recursiveHeight(n.getLeft())  
                        + recursiveHeight(n.getRight()));  
}  
}
```

Algorithm for AVL Insert

- 1.) use the recursive insert code from a Binary Search Tree
- 2.) update the height of this node by looking at height of left and right
- 3.) calculate the balance factor of this node
- 4.) check the four cases for rebalancing
 - if (getBalance() >=2 && just inserted a value to right of this node)
 // Right-Right case
 - if (getBalance() >= 2 && just inserted a value to the left of this node)
 // Right-Left case
 - if (getBalance() <=-2 && just inserted a value to right of this node)
 // Left-Right case
 - if (getBalance() <=- 2 && just inserted a value to the left of this node)
 // Left-Left case

AVL Tree Delete?

0. Try some examples based on the Worksheet
1. Perform a BST Delete (see code from previous lecture)
2. Update the heights and balances.
3. Determine what rotations are needed.
4. There may be cascading rotations that need to be checked.

X-Team Activity

We will FORM teams tonight for in-class and out-of-class assignments during the semester.

These will not be your final project teams. You will choose your team members for the final project.

Break until:
6:35

Notes: Red-Black Trees

Red-Black Trees: Reference

Visualizer:

[CS department's summary page](#)

Break Until:
7:40

Nested Class:

A class that is defined within another class.

Both the nested and outer classes have access to the other's private methods and fields.

Increases Encapsulation (hiding details)

Inner (Nested) Classes

Reading: [Oracle's Java Tutorial: Nested Classes](#)

Example: [AVLTree with an inner class](#)