Metadynamics

Practical introduction with PLUMED University of Padova

Overview

Morning

- 1. Installing software
- 2. Alanine dipeptide (Ala2) without Metadynamics
- 3. Overview of Metadynamics
- 4. Accelerated sampling with Metadynamics

Afternoon

- 5. Postprocessing
- 6. Metainference (experimental restraints) + Metadynamics on a real-world system

Getting settled

These instructions assume you're using Linux or a Unix-like system like MacOS.

- 1. Install anaconda (if you haven't already): https://www.anaconda.com/products/distribution
- 2. Create a new environment for our simulations:

```
conda create ——name metad—class
conda activate metad—class
```

3. Install GROMACS (MD code) and PLUMED (Plugin for enhanced sampling), this will also install MPI, this means we can run multi-replica simulations:

```
conda install ——strict—channel—priority —c plumed/label/
masterclass—2022 —c conda—forge plumed gromacs
```

4. Test the installation:

```
gmx_mpi mdrun -h 2> /dev/null | grep -q plumed && echo ok
plumed --has-mpi && echo ok
```

Getting settled

Installing python libraries for analysis:

```
conda install jupyter numpy matplotlib
conda install —c conda—forge blas
```

Get the material (including these slides):

```
$ git clone github.com/tlhr/metad-course
```

Archive contents:

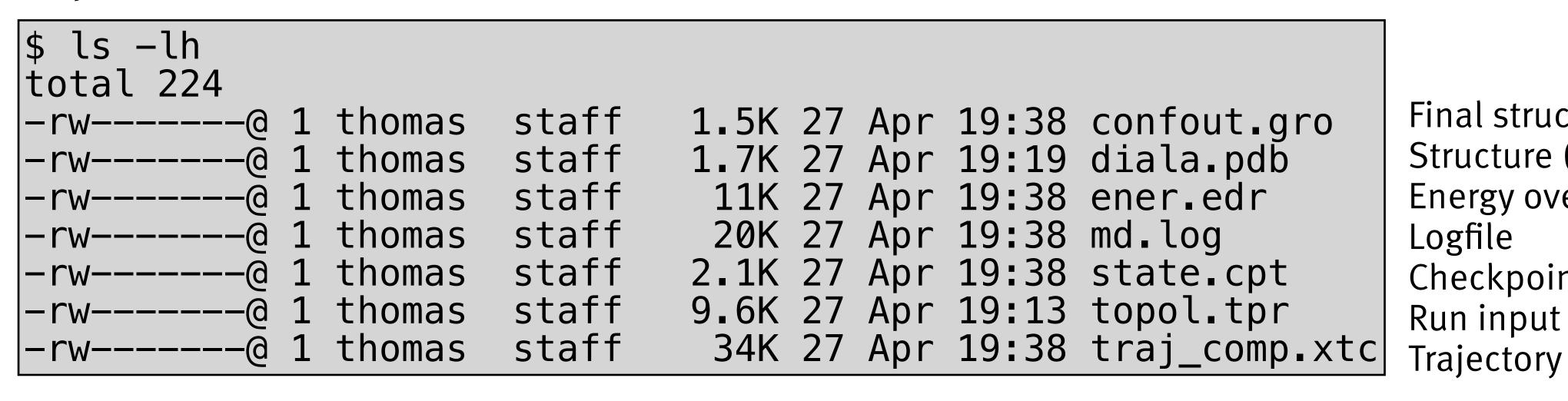
```
(plumed-class) $ ls -lh
total 0
drwxr-xr-x@ 6 thomas staff 192B 28 Apr 15:53 1-aladi-vanilla/
drwxr-xr-x@ 18 thomas staff 576B 28 Apr 15:54 2-aladi-metad/
drwxr-xr-x 8 thomas staff 256B 28 Apr 15:55 3-aladi-metad2d/
drwxr-xr-x@ 29 thomas staff 928B 28 Apr 18:25 4-egaw-mm/
```

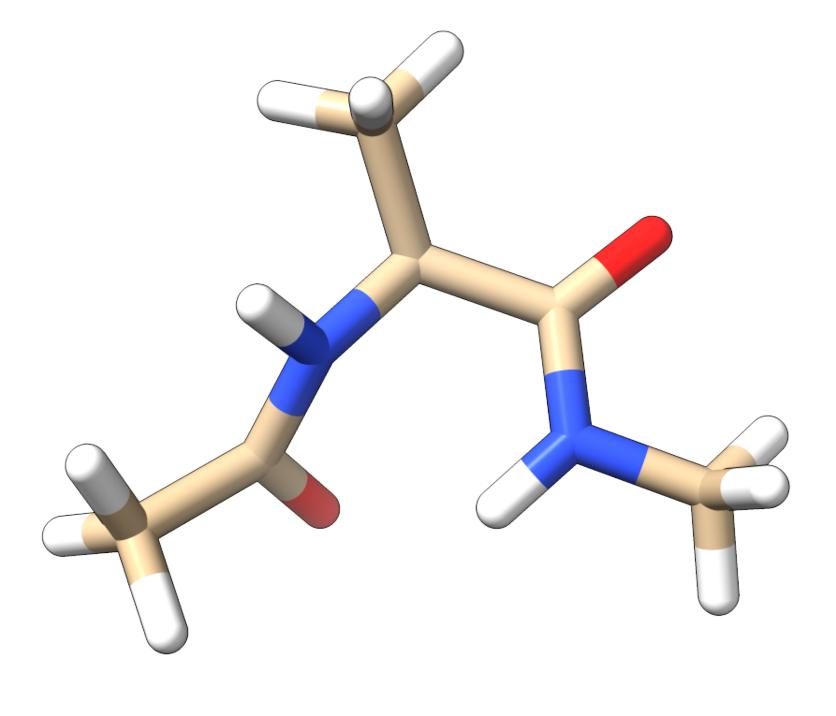
No metadynamics (1-aladi-vanilla)

Running:

```
gmx_mpi mdrun -s topol.tpr -v -nsteps 5000000
```

Output:

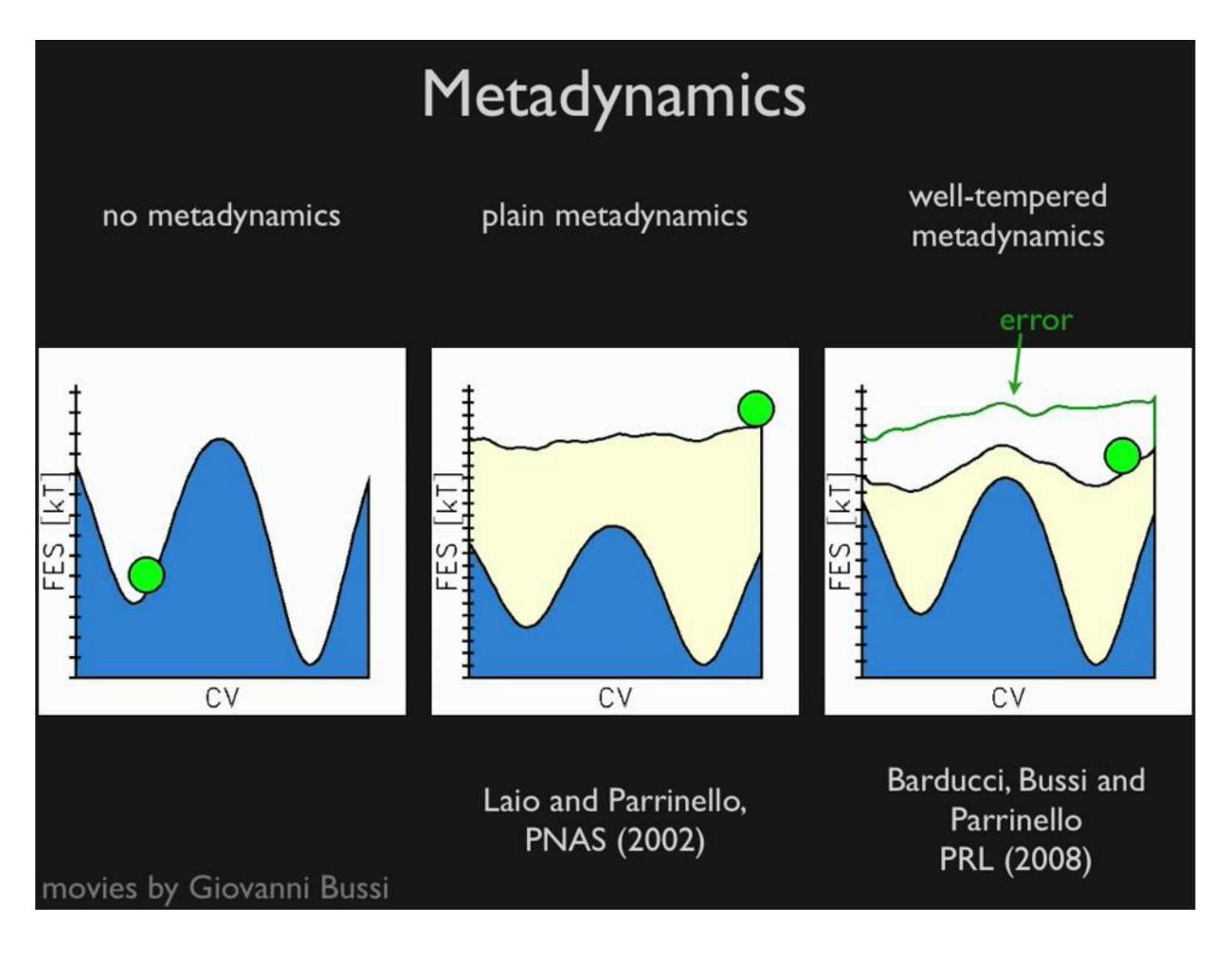




Final structure
Structure (included in tpr)
Energy over time
Logfile
Checkpoint
Run input file
Traiectory

Metadynamics

Conceptual overview



Update potential with Gaussian hill:

$$\dot{V}_{\mathrm{MetaD}}(s,t) = \omega \exp \left[-\sum_{\alpha=1}^{N_{\mathrm{CV}}} \frac{(s_{\alpha} - s_{\alpha}(t))^{2}}{2\sigma_{\alpha}^{2}} \right]$$

$$\dot{V}_{\mathrm{WTMetaD}}(s,t) = \omega \exp \left[-\frac{V(s(t),t)}{k_{\mathrm{B}}\Delta T} \right] \exp \left[-\sum_{\alpha=1}^{N_{\mathrm{CV}}} \frac{(s_{\alpha} - s_{\alpha}(t))^{2}}{2\sigma_{\alpha}^{2}} \right]$$

No metadynamics

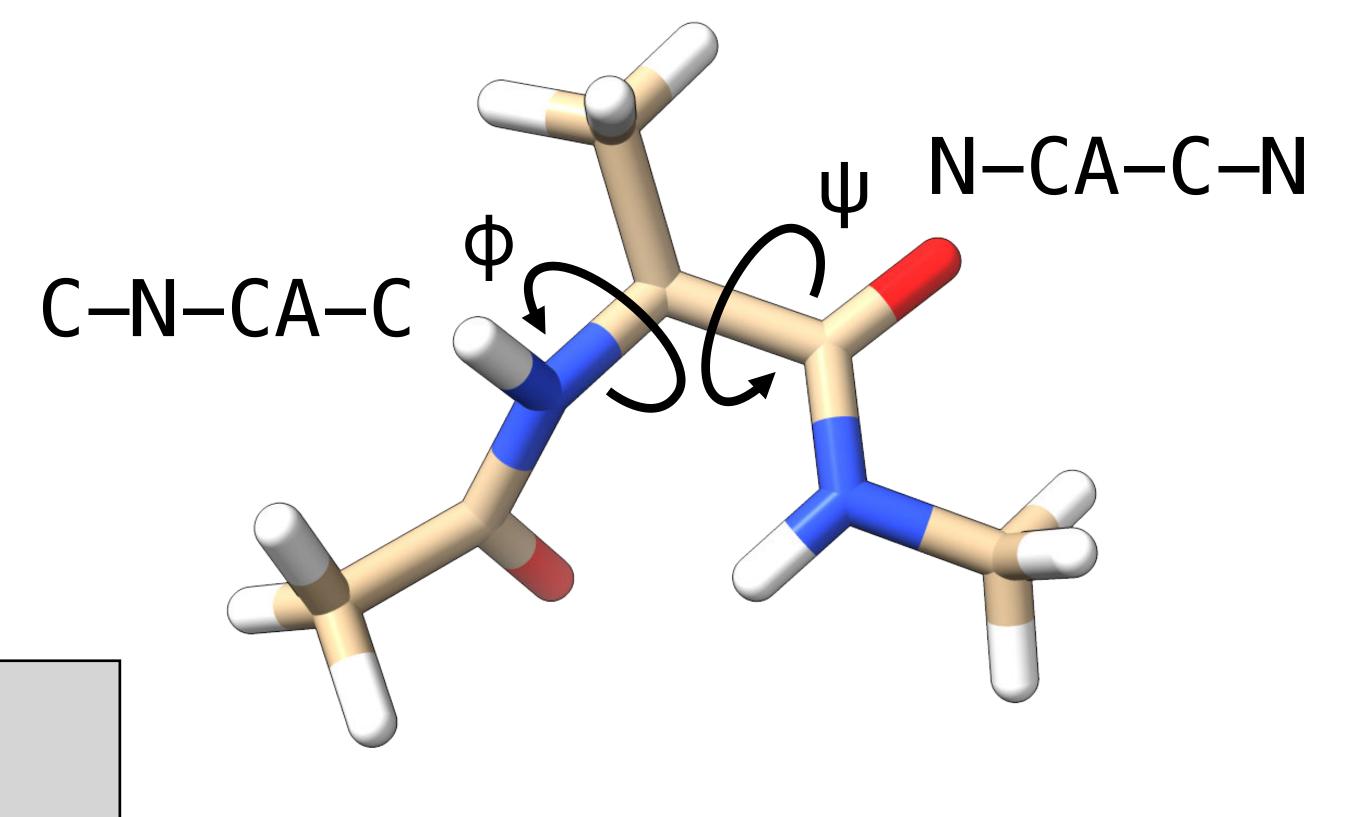
PLUMED syntax:

label: ACTION F00=3.14 BAR=blah

PLUMED input (plumed.dat):

phi: TORSION ATOMS=????
psi: TORSION ATOMS=????

PRINT ARG=phi,psi FILE=COLVAR STRIDE=1



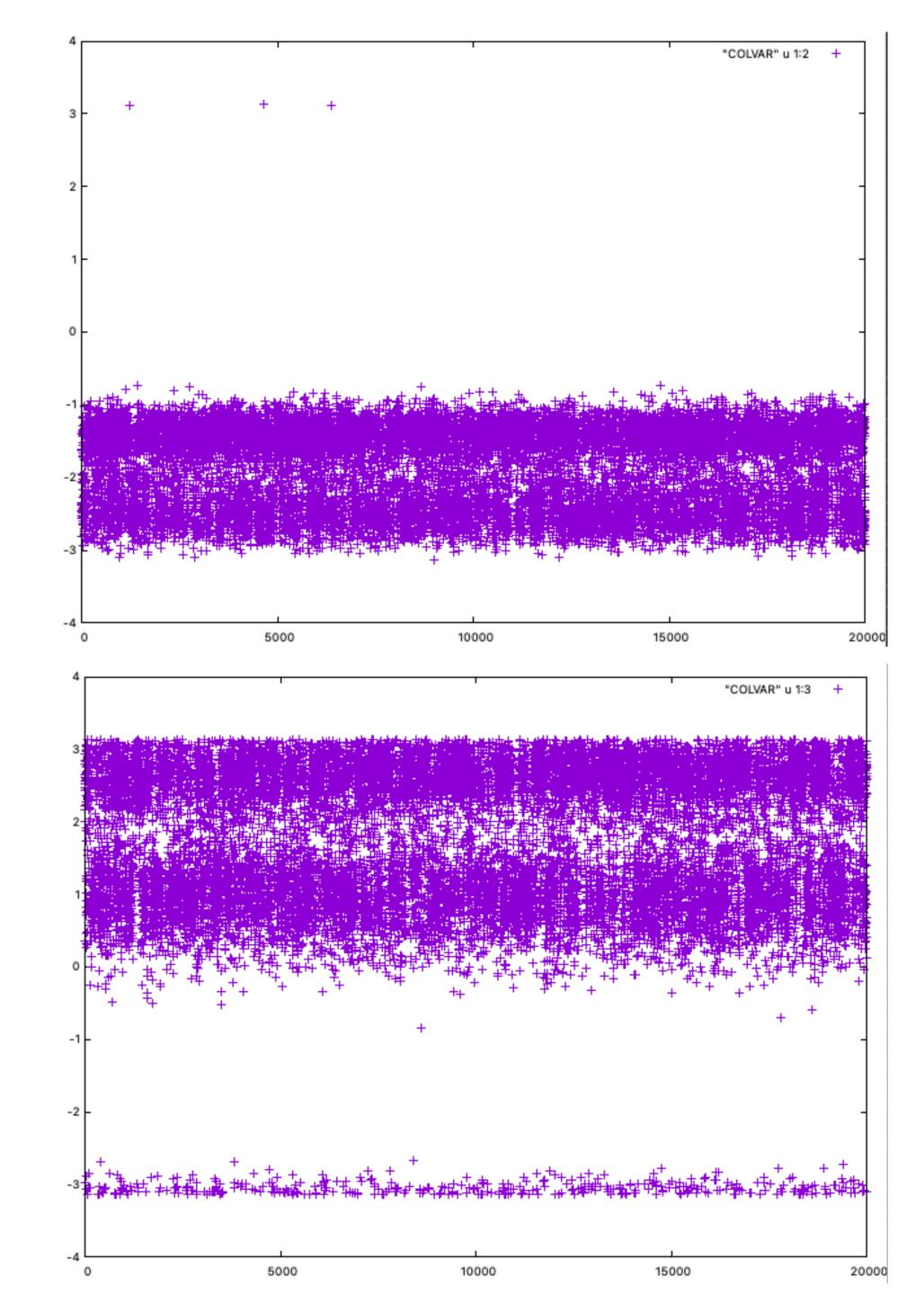
Analysis:

plumed driver --plumed plumed.dat --mf_xtc traj_comp.xtc

Alanine dipeptide No metadynamics

Plotting CV over time:

```
gnuplot
plot "COLVAR" u 1:2 w l
replot "COLVAR" u 1:3 w l
```



Metadynamics (2-aladi-metad)

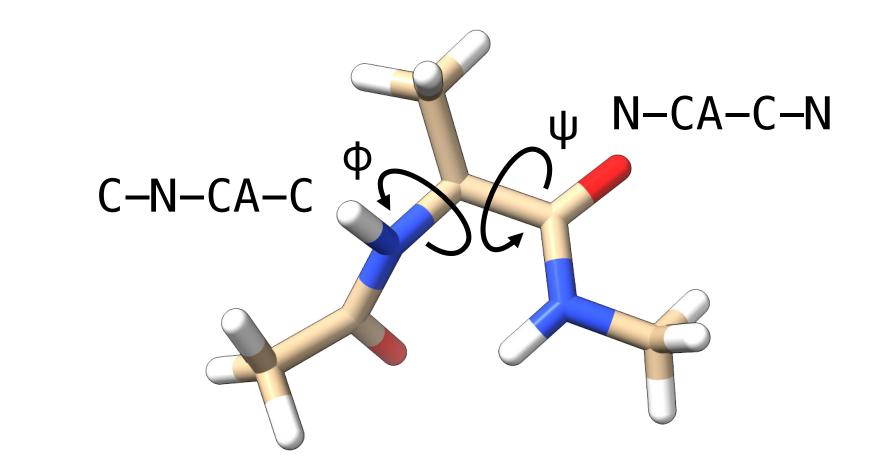
PLUMED input (plumed.dat):

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

metad: METAD ...
   ARG=phi
   PACE=500 HEIGHT=1.2 BIASFACTOR=8
    # Choose sigma based on fluctuations in unbiased run (1/2 or 1/3)
   SIGMA=????
   FILE=HILLS GRID_MIN=-pi GRID_MAX=pi
...
PRINT ARG=phi,psi,metad.bias FILE=COLVAR STRIDE=100
```

Running:

```
gmx_mpi mdrun -s topol.tpr -v -nsteps 5000000 -plumed plumed.dat
```



Detour: Parallel-bias metadynamics

Biasing many collective variables at once

Problem: Depositing a high-dimensional Gaussian falls victim to the curse of dimensionality

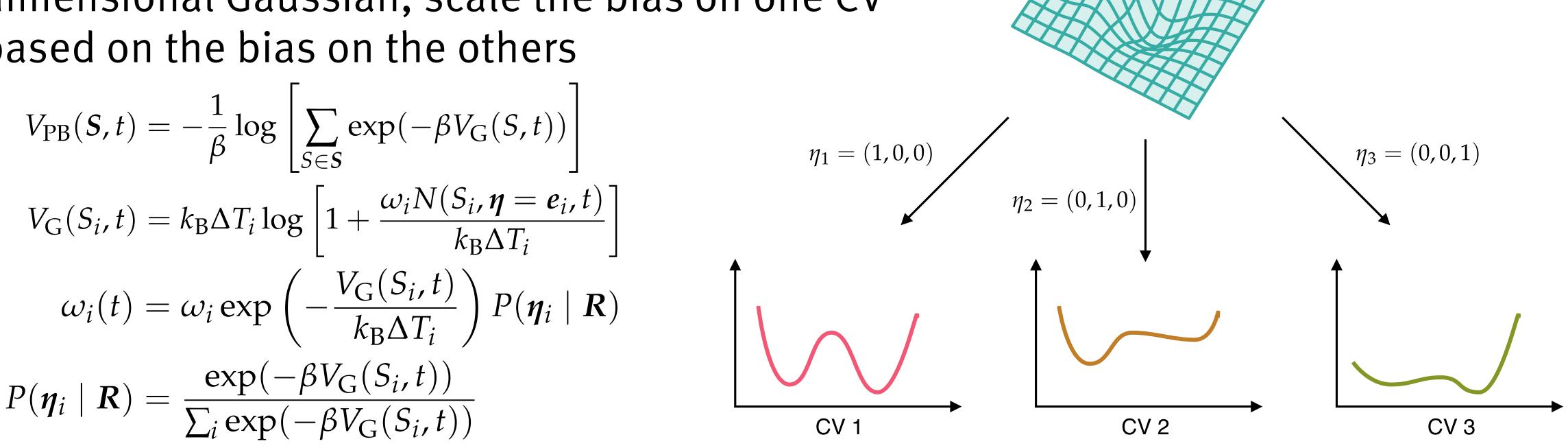
Idea: deposit many 1D-Gaussians instead of a highdimensional Gaussian, scale the bias on one CV based on the bias on the others

$$V_{PB}(S,t) = -\frac{1}{\beta} \log \left[\sum_{S \in S} \exp(-\beta V_{G}(S,t)) \right]$$

$$V_{G}(S_{i},t) = k_{B}\Delta T_{i} \log \left[1 + \frac{\omega_{i}N(S_{i}, \eta = e_{i}, t)}{k_{B}\Delta T_{i}} \right]$$

$$\omega_{i}(t) = \omega_{i} \exp \left(-\frac{V_{G}(S_{i},t)}{k_{B}\Delta T_{i}} \right) P(\eta_{i} \mid \mathbf{R})$$

$$P(\eta_{i} \mid \mathbf{R}) = \frac{\exp(-\beta V_{G}(S_{i},t))}{\sum_{i} \exp(-\beta V_{G}(S_{i},t))}$$



Metadynamics postprocessing

Plotting CV over time:

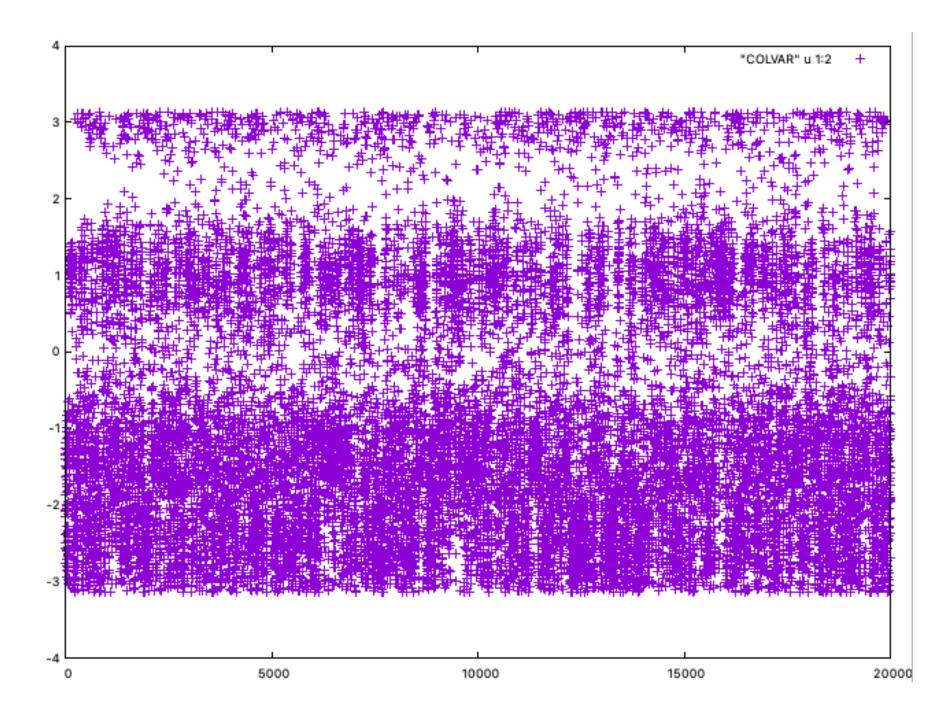
```
gnuplot
plot "COLVAR" u 1:2
replot "COLVAR" u 1:3
```

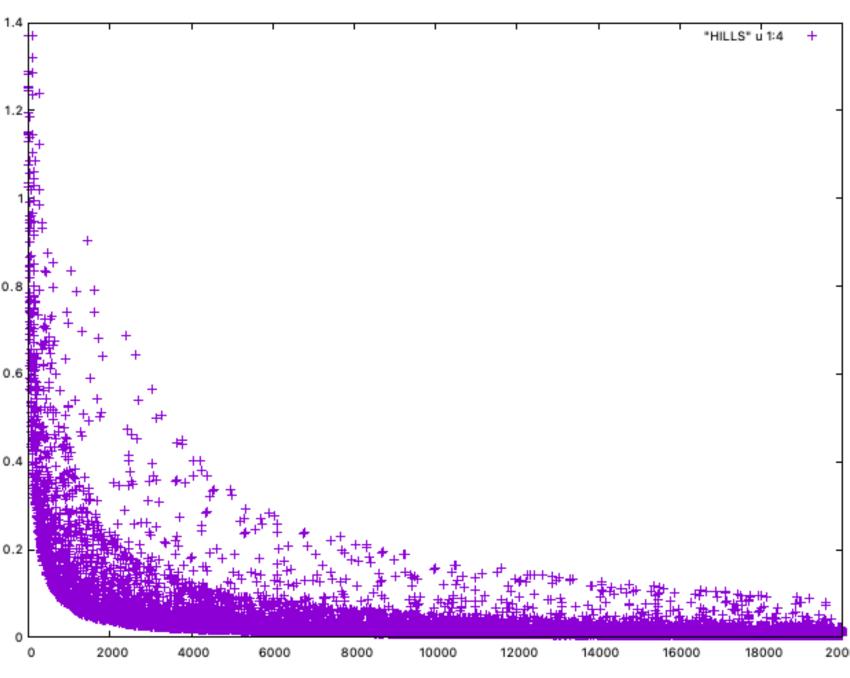
HILLS file content:

```
#! FIELDS time phi sigma_phi height biasf
#! SET multivariate false
#! SET kerneltype stretched-gaussian
#! SET min_phi -pi
#! SET max_phi pi
```

Plot the gaussian height over time:

```
gnuplot
plot "HILLS" u 1:4
```





Metadynamics postprocessing

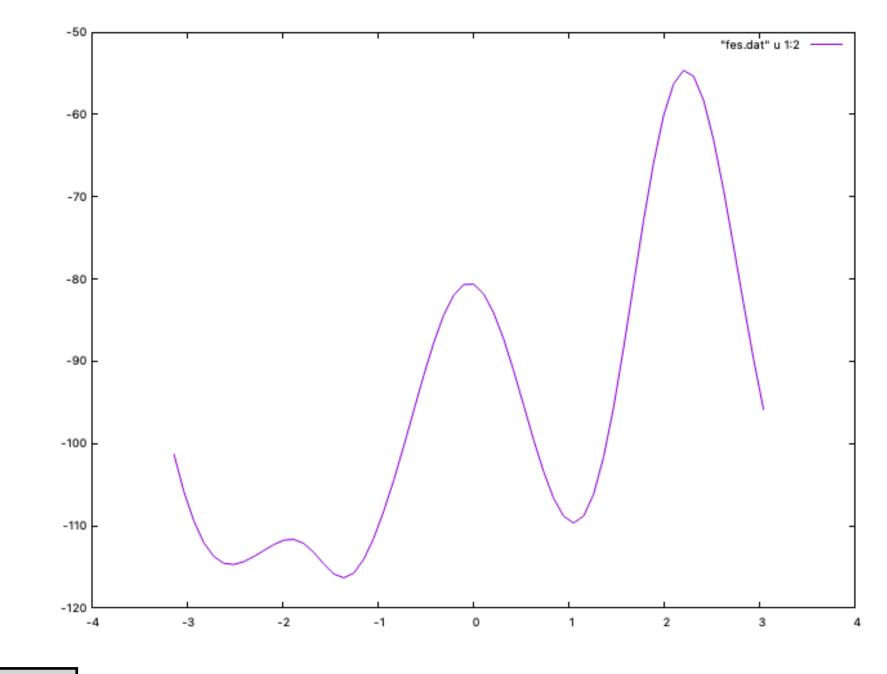
Estimate the free energy surface:

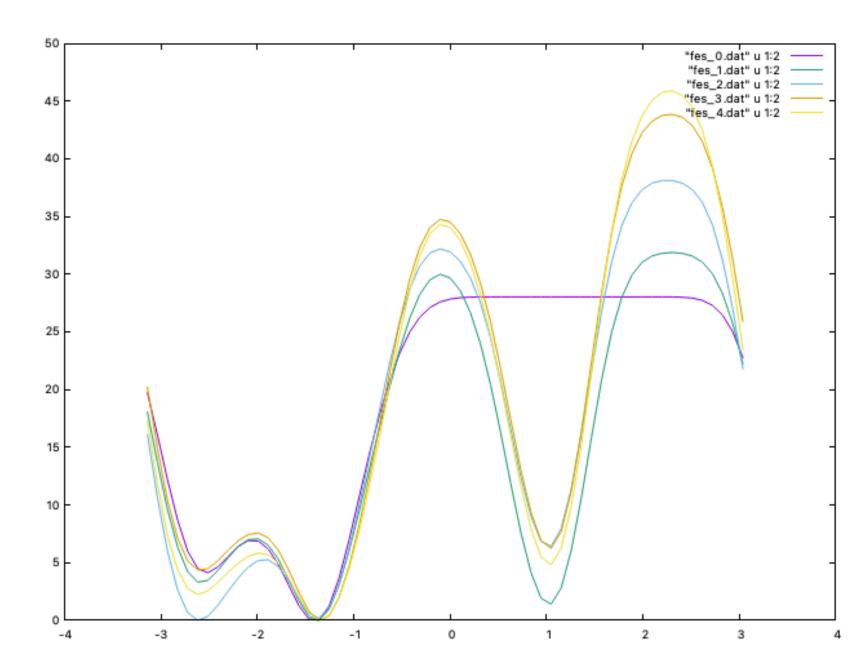
```
plumed sum_hills --hills HILLS
```

Estimate the free energy surface over time:

```
plumed sum_hills ——hills HILLS ——stride 100 —mintozero # Plot the first few fes.dat files
```

Is it converged?





Metadynamics postprocessing

Un-biasing the simulation:

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

metad: METAD ...
    ARG=phi
    PACE=100000000 HEIGHT=0.0 BIASFACTOR=8
    SIGMA=???? # Use your value here!
    FILE=HILLS GRID_MIN=-pi GRID_MAX=pi
    RESTART=YES
...
PRINT ARG=phi,psi,metad.bias FILE=COLVAR_RW STRIDE=1
```

Run on the trajectory:

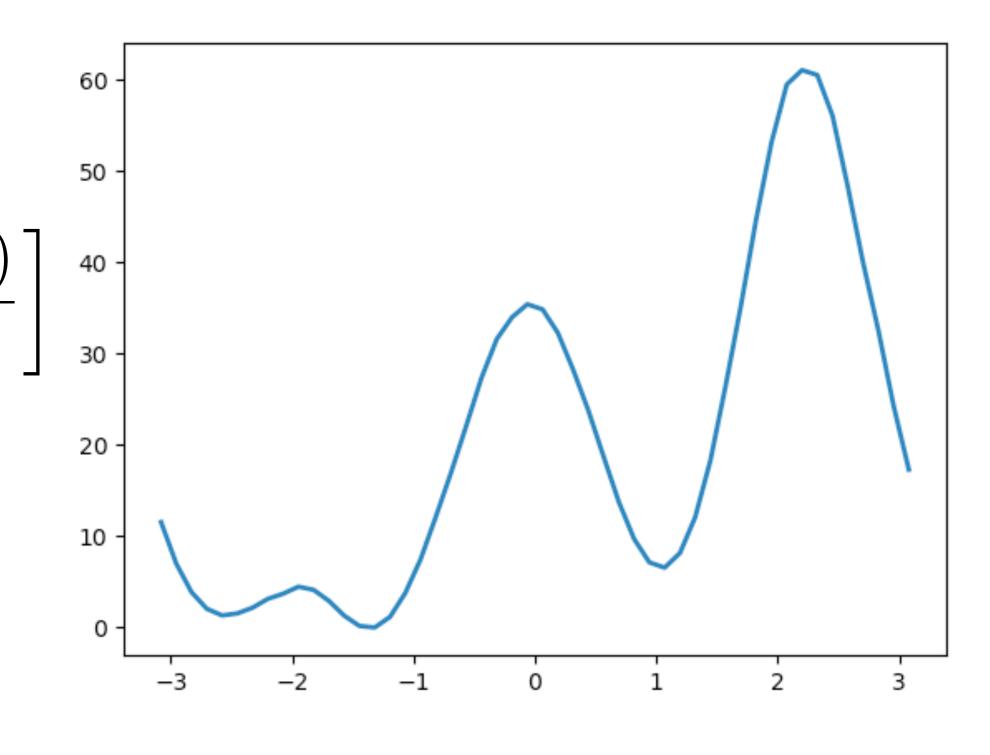
```
plumed driver --plumed plumed-rw.dat --mf_xtc traj_comp.xtc --kt 2.494339
```

Metadynamics postprocessing

Calculating weights:

import numpy as np

```
bias = np.loadtxt("COLVAR_RW")[:, -1]
weights = np.exp(bias / 2.494339)
```



Creating a 1D free energy surface:

weights /= weights.sum()

```
import matplotlib.pyplot as plt
phi, psi = np.loadtxt("COLVAR_RW")[:, [1, 2]].T
hist, edges = np.histogram(phi, bins=50, range=(-np.pi, np.pi),
                           density=True, weights=weights)
x = 0.5 * (edges[:-1] + edges[1:])
F = -2.494339 * np.log(hist)
|F| -= F_min()
plt.plot(x, F); plt.show()
```

2D Metadynamics (3-aladi-metad2d)

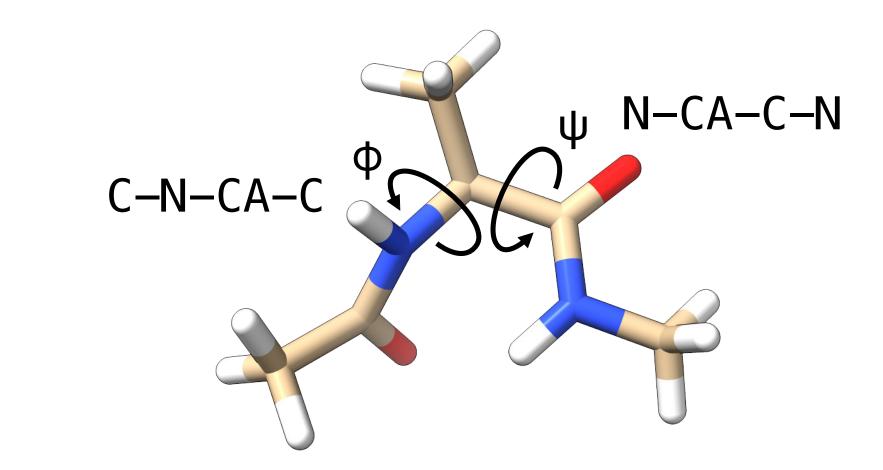
PLUMED input (plumed.dat):

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

metad: METAD ...
    ARG=phi,psi
    PACE=500 HEIGHT=1.2 BIASFACTOR=14
    # Choose sigma based on fluctuations in unbiased run (1/2 or 1/3)
    SIGMA=????,???
    FILE=HILLS GRID_MIN=-pi,-pi GRID_MAX=pi,pi
...
PRINT ARG=phi,psi,metad.bias FILE=COLVAR STRIDE=100
```

Running:

```
gmx_mpi mdrun -s topol.tpr -v -nsteps 5000000 -plumed plumed.dat
```



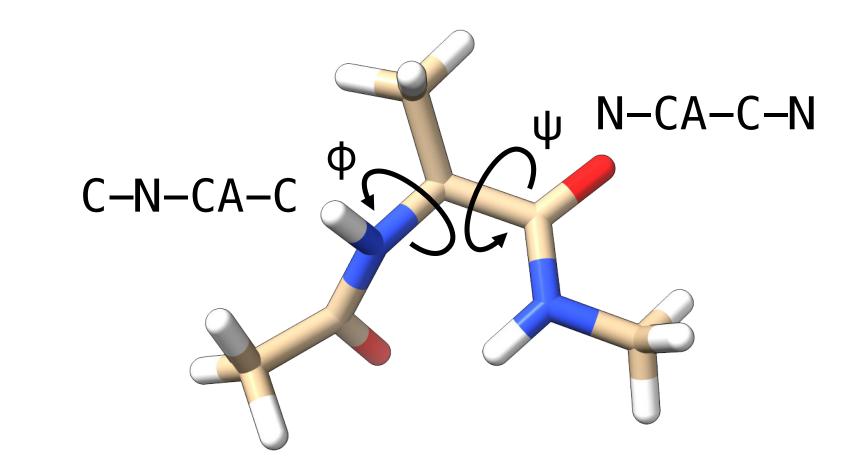
2D Metadynamics postprocessing

PLUMED input (plumed.dat):

```
phi: TORSION ATOMS=5,7,9,15
psi: TORSION ATOMS=7,9,15,17

metad: METAD ...
   ARG=phi,psi
   PACE=10000000 HEIGHT=0.0 BIASFACTOR=14
   # Choose previous values
   SIGMA=????,????
   FILE=HILLS GRID_MIN=-pi,-pi GRID_MAX=pi,-pi
   RESTART=YES
...

PRINT ARG=phi,psi,metad.bias FILE=COLVAR STRIDE=100
```



Running:

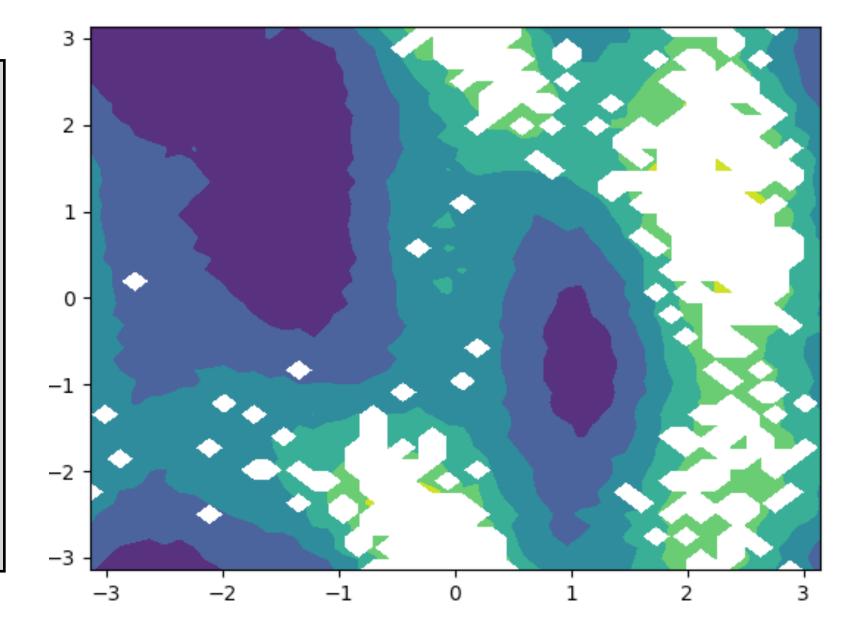
plumed driver ——plumed plumed—rw.dat ——mf_xtc traj_comp.xtc ——kt 2.494339

2D Metadynamics postprocessing

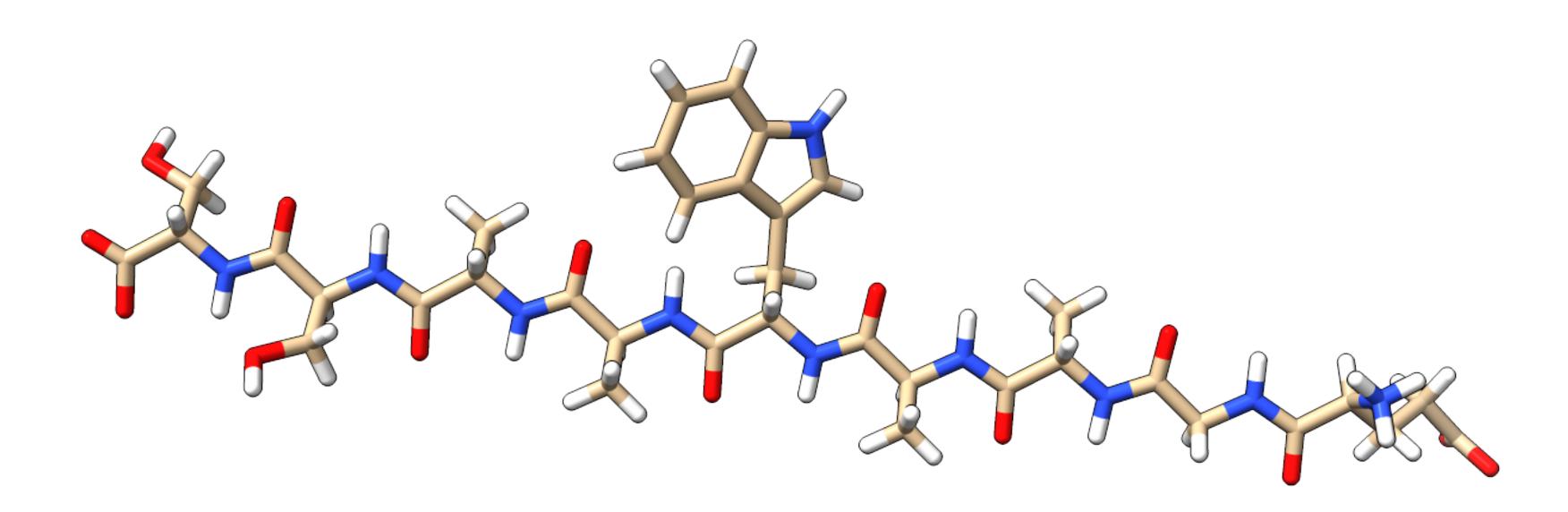
Calculate weights as before $w \propto \exp\left[\frac{v \, \text{MetaD}(s)}{k_{\text{B}} T}\right]$. Create a 2D free energy surface:

```
import matplotlib.pyplot as plt

phi, psi = np.loadtxt("COLVAR_RW")[:, [1, 2]].T
hist, edges = np.histogram2d(
    phi, psi, bins=50, density=True, weights=weights,
    range=((-np.pi, np.pi), (-np.pi, np.pi)))
xx, yy = np.mgrid[-np.pi:np.pi:50j, -np.pi:np.pi:50j]
F = -2.494339 * np.log(hist)
F -= F.min()
plt.contourf(xx, yy, F); plt.show()
```



Metadynamics + experimental restraints (4-egaw-mm)



Enhance sampling with metadynamics, and add experimental restraints (from NMR) to improve accuracy

Metadynamics + experimental restraints

To apply restraints we need a *forward model* mapping from our structure (XYZ coordinates) to our experimental observable (typically a scalar):

$$f:$$
 Structure $\to \mathbb{R}$

Use the *Karplus* relation to go from dihedral angles to J-coupling:

$$^{3}J(\theta) = A\cos^{2}(\theta + \Delta\theta) + B\cos(\theta + \Delta\theta) + C$$

Then apply a restraint in form of a harmonic potential:

$$V(X, \sigma \mid d) \propto \frac{(f(X) - d)^2}{\sigma^2}$$

Metainference

$$V_{\text{MI}}(X, \sigma \mid d) = \sum_{r=1}^{N_{\text{r}}} \left\{ V_{\text{FF}}(X_r) + k_{\text{B}}T \sum_{i=1}^{N_{\text{d}}} \left[\frac{(\langle f_i(X) \rangle - d_i)^2}{2\sigma_{r,i}^2} + \frac{1}{2} \ln(2\pi\sigma_{r,i}^2) + \frac{1}{2} \ln\left(\frac{\sigma_{r,i}^2}{2}\right) \right] \right\}$$

 $X = [X_r]$ Ensemble of conformations

 $\sigma = [\sigma_{r,i}]$ Errors

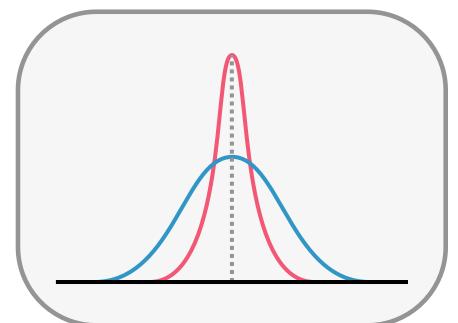
 $d = [d_i]$ Datapoints

f(X) Forward model

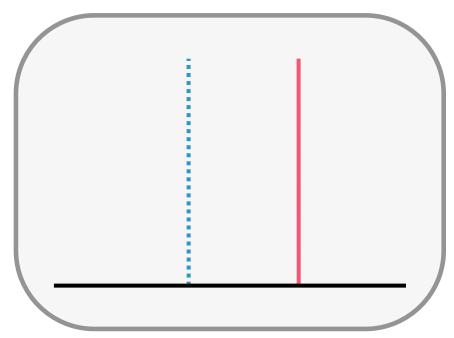
 $N_{\rm d}$ Number of datapoints

 $N_{\rm r}$ Number of replicas

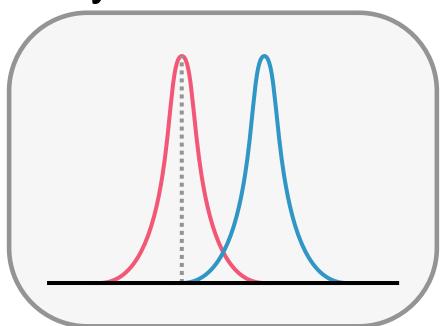
Random error



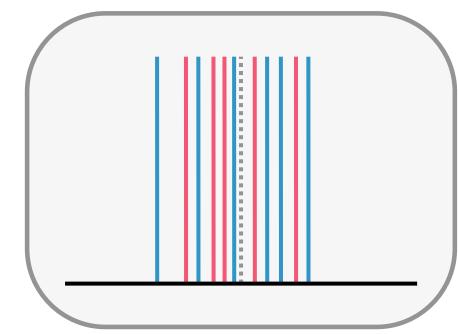
Forward model error



Systematic error



Ensemble error



Metadynamics + experimental restraints

Forward model in PLUMED (H^{α} –N, based on Ψ dihedrals):

```
TYPE=HAN

ATOMS1=@psi-2 COUPLING1=-0.49

ATOMS2=@psi-4 COUPLING2=-0.54

ATOMS3=@psi-5 COUPLING3=-0.53

ATOMS4=@psi-7 COUPLING4=-0.39

ATOMS5=@psi-8 COUPLING5=-0.39

LABEL=jhan
```

$$^{3}J(\theta) = A\cos^{2}(\theta + \Delta\theta) + B\cos(\theta + \Delta\theta) + C$$

Metadynamics + experimental restraints

Ensemble-averaged statistics:

```
ENSEMBLE ...
    ARG=(jhan\.j-.*),pb.bias REWEIGHT
    LABEL=ens
... ENSEMBLE

STATS ...
    ARG=(ens\.jhan\.j-.*) PARARG=(jhan\.exp-.*)
    LABEL=jhanst
... STATS

PRINT ARG=jhanst.* STRIDE=2000 FILE=../STATS.J
```

Weighted instantaneous ensemble average

$$w(s_r, t) = \exp\left(\frac{V(s_r, t)}{k_B T}\right) \left[\sum_{j=1}^{N_{\text{replica}}} \exp\left(\frac{V(s_j, t)}{k_B T}\right)\right]^{-1}$$

Statistics (e.g. correlation of forward model with experimental value)

Print to file

Metadynamics + experimental restraints

Ensemble-averaged restraints with error-accounting:

```
METAINFERENCE ...
ARG=(jhan\.j-.*),(jhahn\.j-.*),pb.bias
PARARG=(jhan\.exp-.*),(jhahn\.exp-.*)
NOISETYPE=MGAUSS REWEIGHT OPTSIGMAMEAN=SEM AVERAGING=200
SIGMA0=5.0 SIGMA_MIN=0.0001 SIGMA_MAX=15.0 DSIGMA=0.1
WRITE_STRIDE=10000
LABEL=byj
...
```

$$V_{\text{MI}}(X, \sigma \mid d) = \sum_{r=1}^{N_{\text{r}}} \left\{ V_{\text{FF}}(X_r) + k_{\text{B}}T \sum_{i=1}^{N_{\text{d}}} \left[\frac{(\langle f_i(X) \rangle - d_i)^2}{2\sigma_{r,i}^2} + \frac{1}{2} \ln(2\pi\sigma_{r,i}^2) + \frac{1}{2} \ln\left(\frac{\sigma_{r,i}^2}{2}\right) \right] \right\}$$

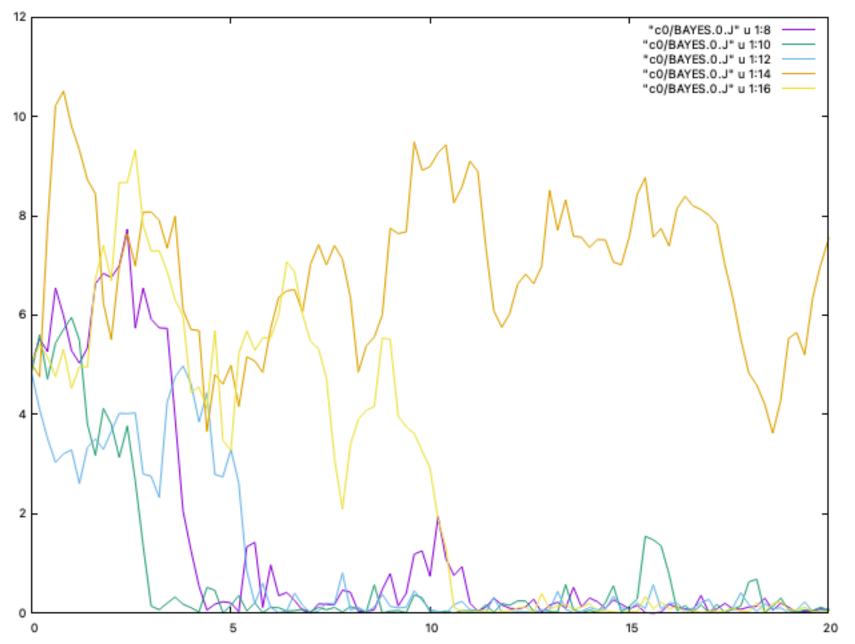
$$\sigma_{r,i}^2 = (\sigma_{r,i}^{\rm B})^2 + (\sigma_i^{\rm SEM})^2$$
 Sampled by Monte Carlo
 Estimated based on windowed average (AVERAGING)

Metadynamics + experimental restraints

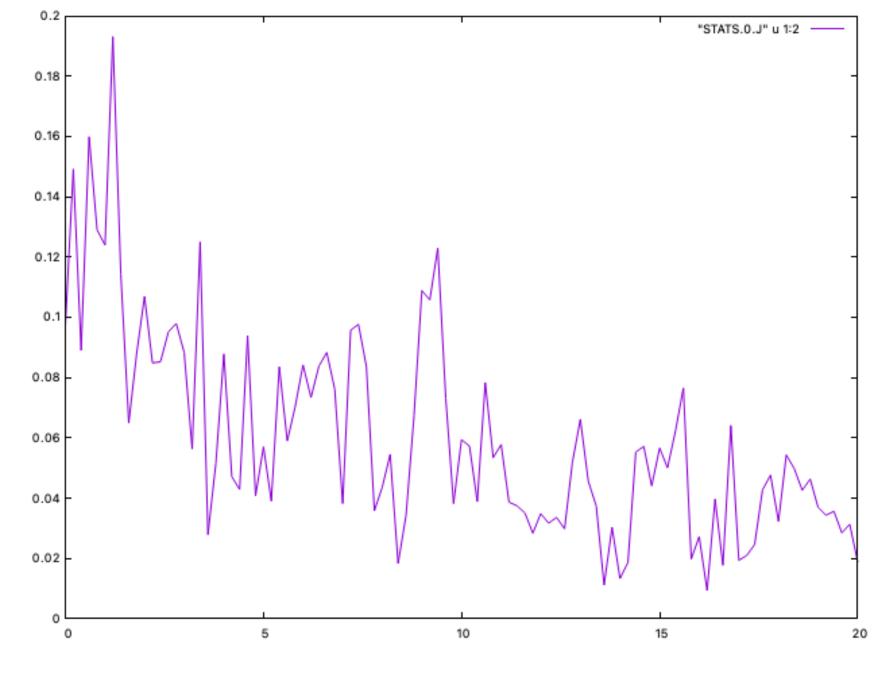
Running in multi-replica mode (requires at least 4 cores):

```
mpirun —np 4 gmx_mpi mdrun —s topol —plumed ../plumed.dat —multidir c? —v —nsteps 10000
```

Per-datapoint sigma over time



Squared deviation over time



Useful resources

- GROMACS
 - Simple tutorial: http://www.mdtutorials.com/gmx/lysozyme/
 - User guide: https://manual.gromacs.org/documentation/current/user-guide/index.html
- PLUMED
 - Brief intro: https://www.plumed.org/doc-v2.8/user-doc/html/master- i s d d-1.html
 - Metadynamics: https://www.plumed.org/doc-v2.8/user-doc/html/master- i s d d-2.html
 - Metainference: https://www.plumed.org/doc-v2.8/user-doc/html/isdb-1.html
 - Reference: https://www.plumed.org/doc-v2.8/user-doc/html/index.html
- Python
 - Standard library: https://docs.python.org/3/
 - Numpy: https://numpy.org/doc/stable/

Relevant papers / books

- Metadynamics
 - How-to guide <u>Bussi & Branduardi</u>
 - Well-tempered metadynamics <u>Barducci 2008</u>
 - Parallel-bias metadynamics <u>Pfaendtner & Bonomi 2015</u>
 - Adaptive gaussians <u>Branduardi 2012</u>
- Forward models
 - J-couplings <u>Karplus 1963</u>
 - 3-J coupling *A*, *B*, *C* parameters <u>Pérez 2001</u>
- Metainference
 - Original method <u>Bonomi & Camilloni 2015</u>
 - With metadynamics <u>Bonomi & Camilloni 2016</u>
 - Practical guide on the EGAAWAASS peptide