Queue ADT

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Today's Plan



Recap

Queue ADT

Applications

Announcements

A data structure representing a waiting line

Objects can be enqueued to the back of the line

or dequeued from the front of the line

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Objects can be enqueued to the back of the line

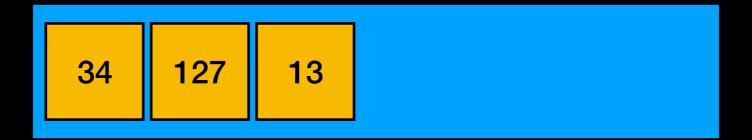
or dequeued from the front of the line

34 127 13

A data structure representing a waiting line

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or dequeued from the front of the line



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A data structure representing a waiting line

Objects can be enqueued to the back of the line

or dequeued from the front of the line

FIFO: First In First Out

Only front of queue is accessible (front), no other objects in the queue are visible

Queue Applications

Generating all substrings

Recognizing Palindromes

Any waiting queue

- Print jobs
- OS scheduling processes with equal priority
- Messages between asynchronous processes

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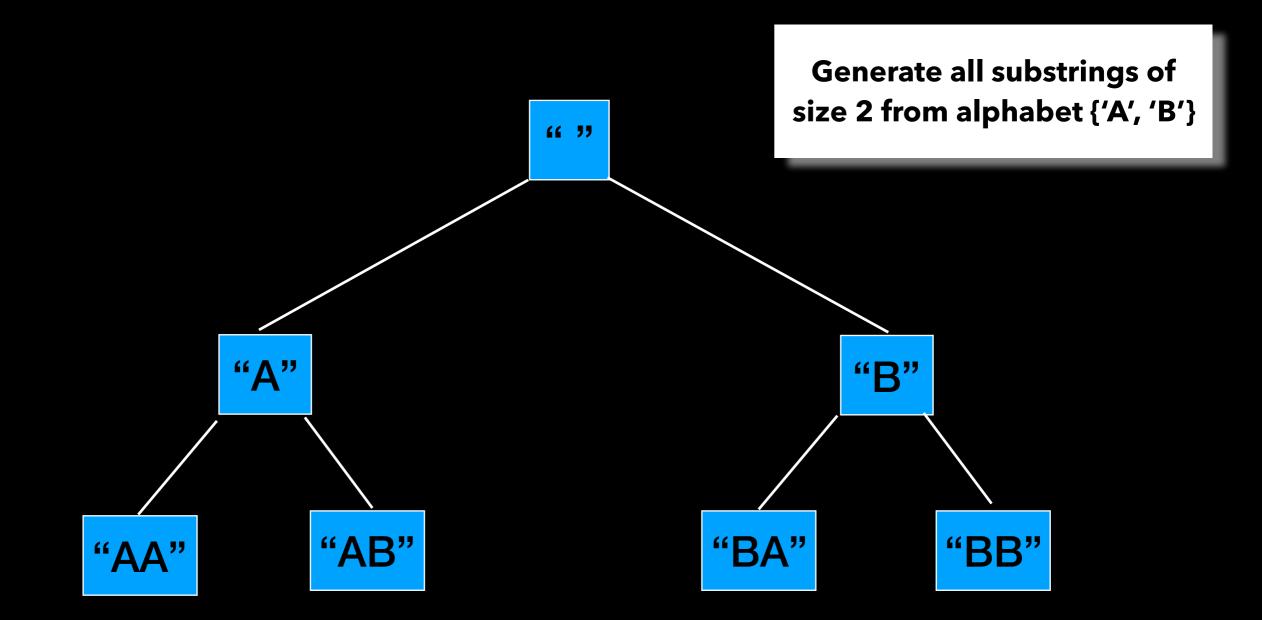
Generating all substrings

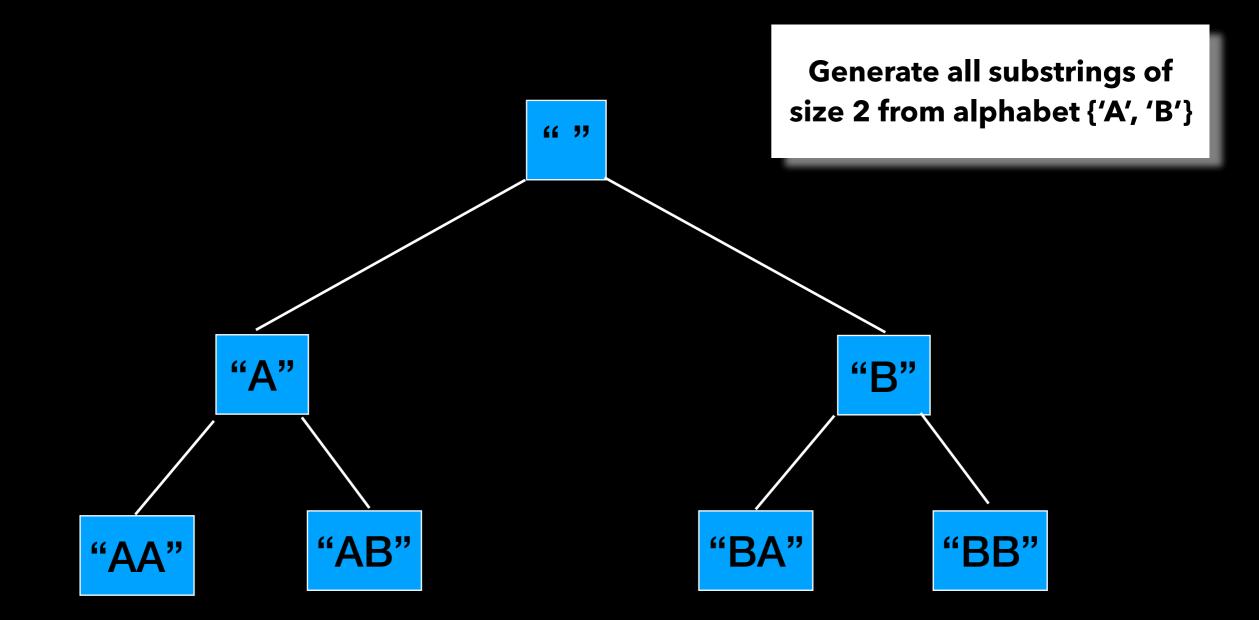
Generate all possible strings up to some fixed length n with repetition (same character included multiple times)

We saw how to do something similar recursively (generate permutations of fixed size n no repetition)

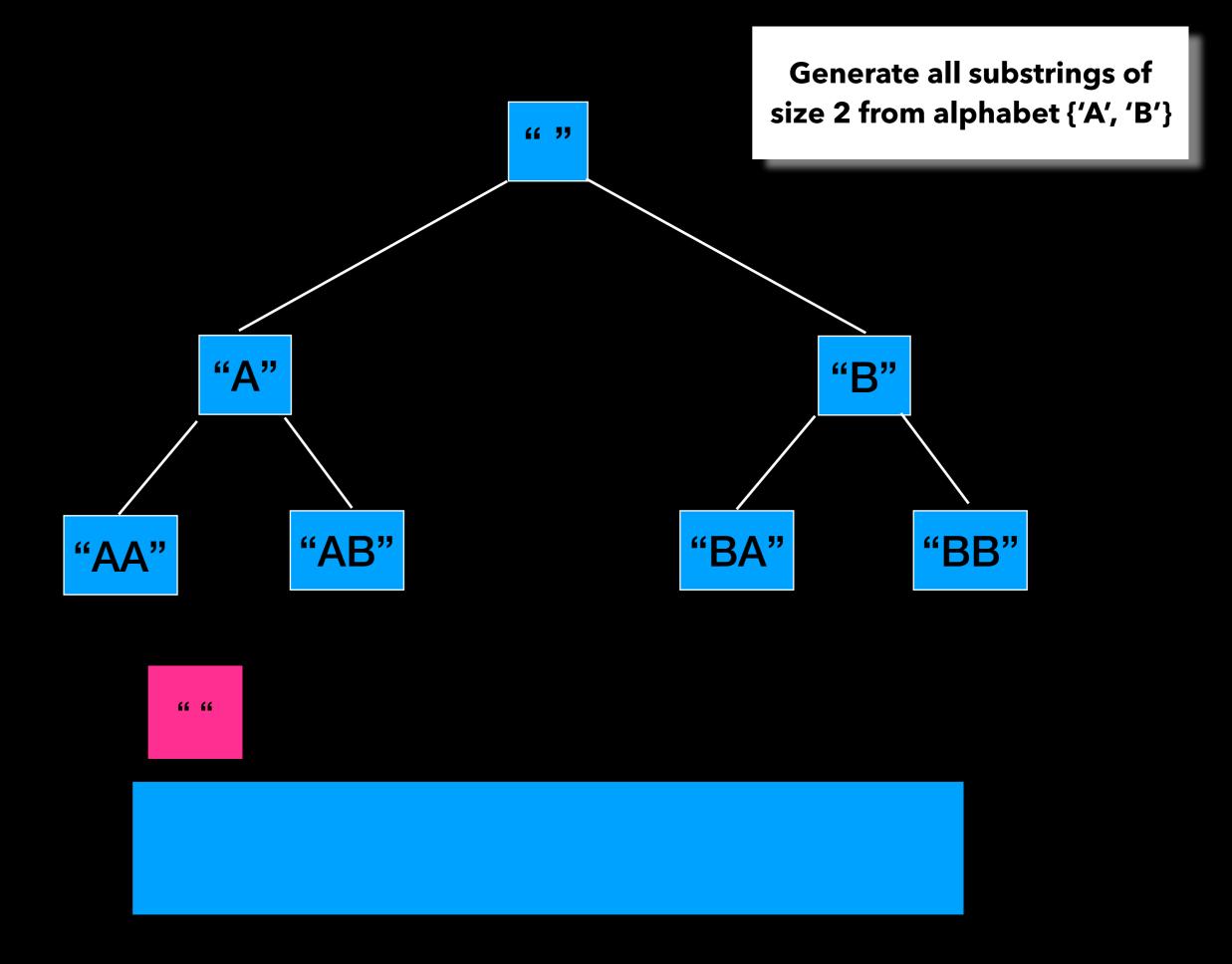
How might we do it with a queue?

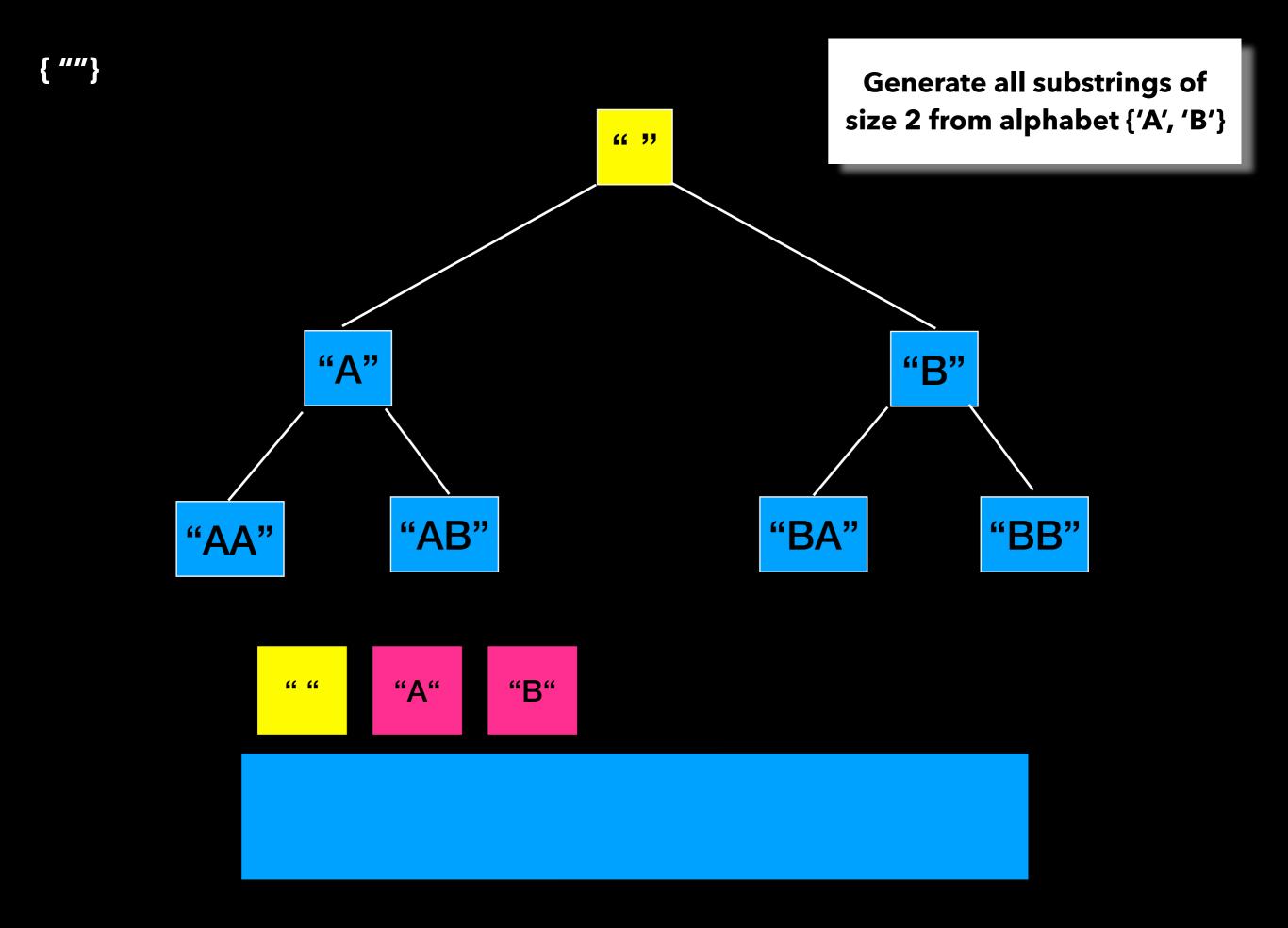
Example simplified to n = 2 and only letters A and B

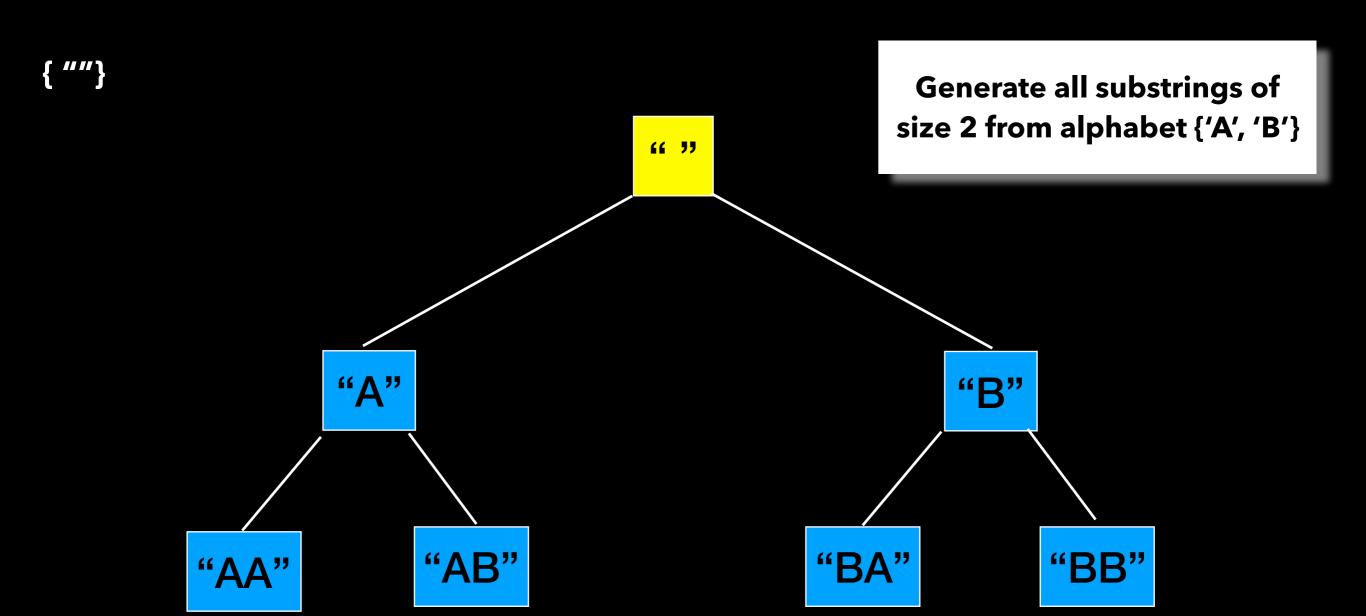




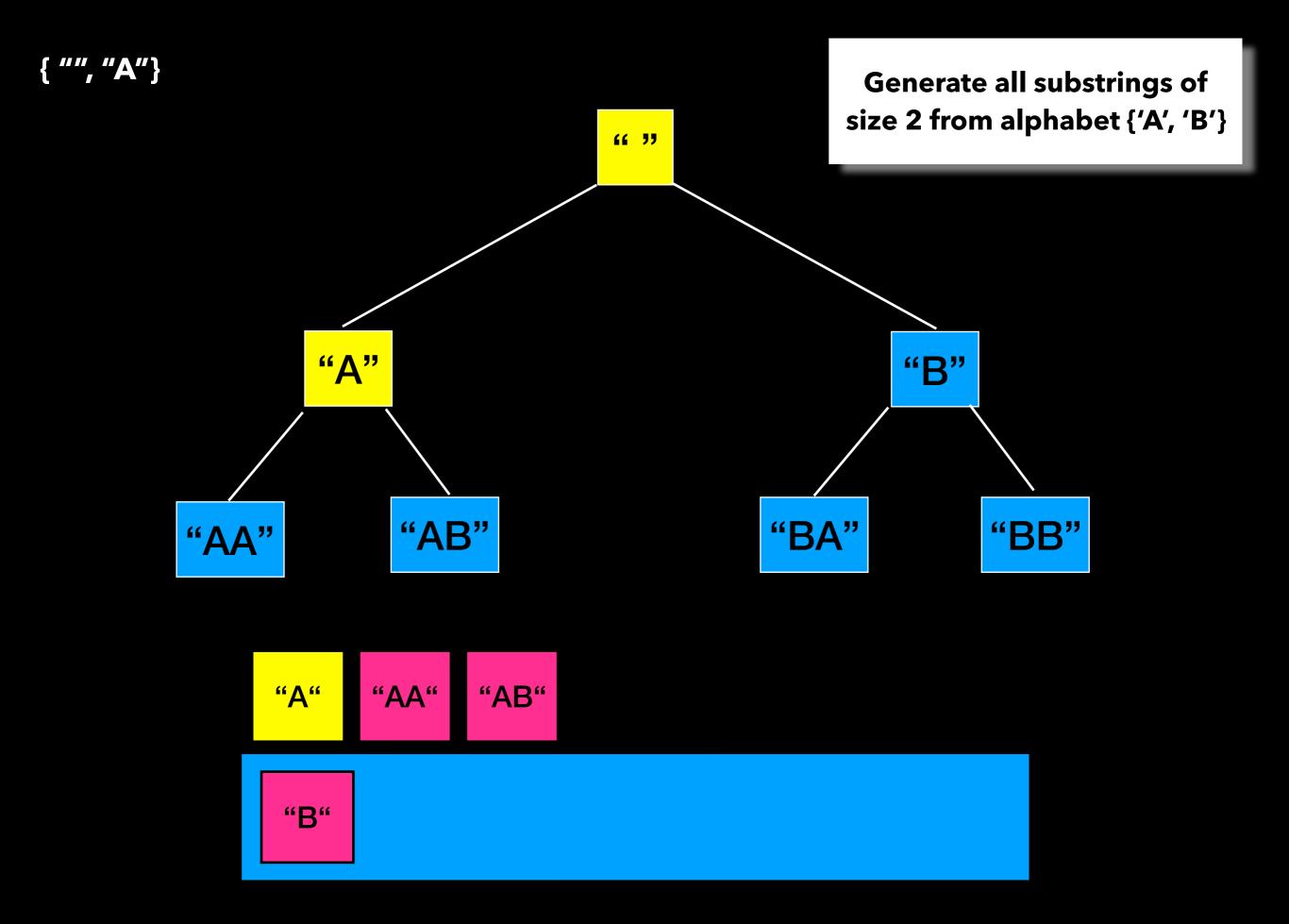


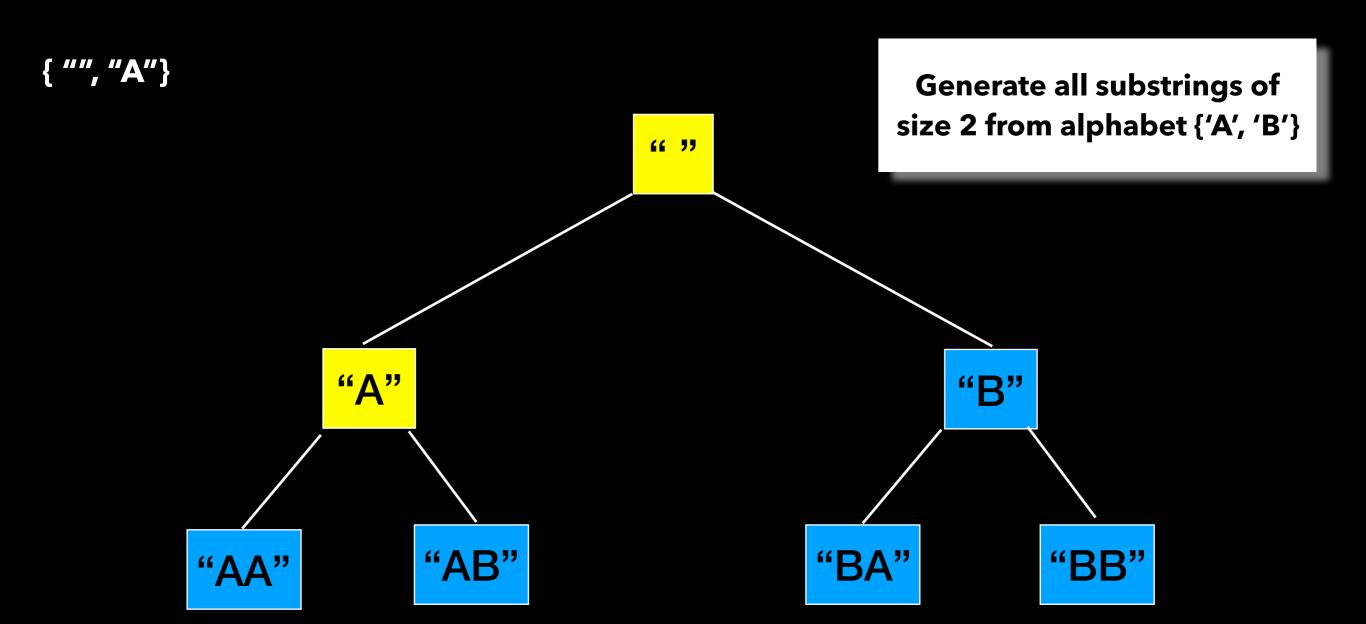


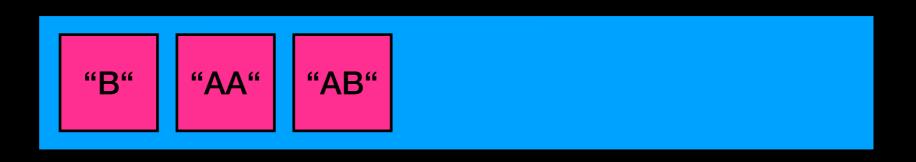


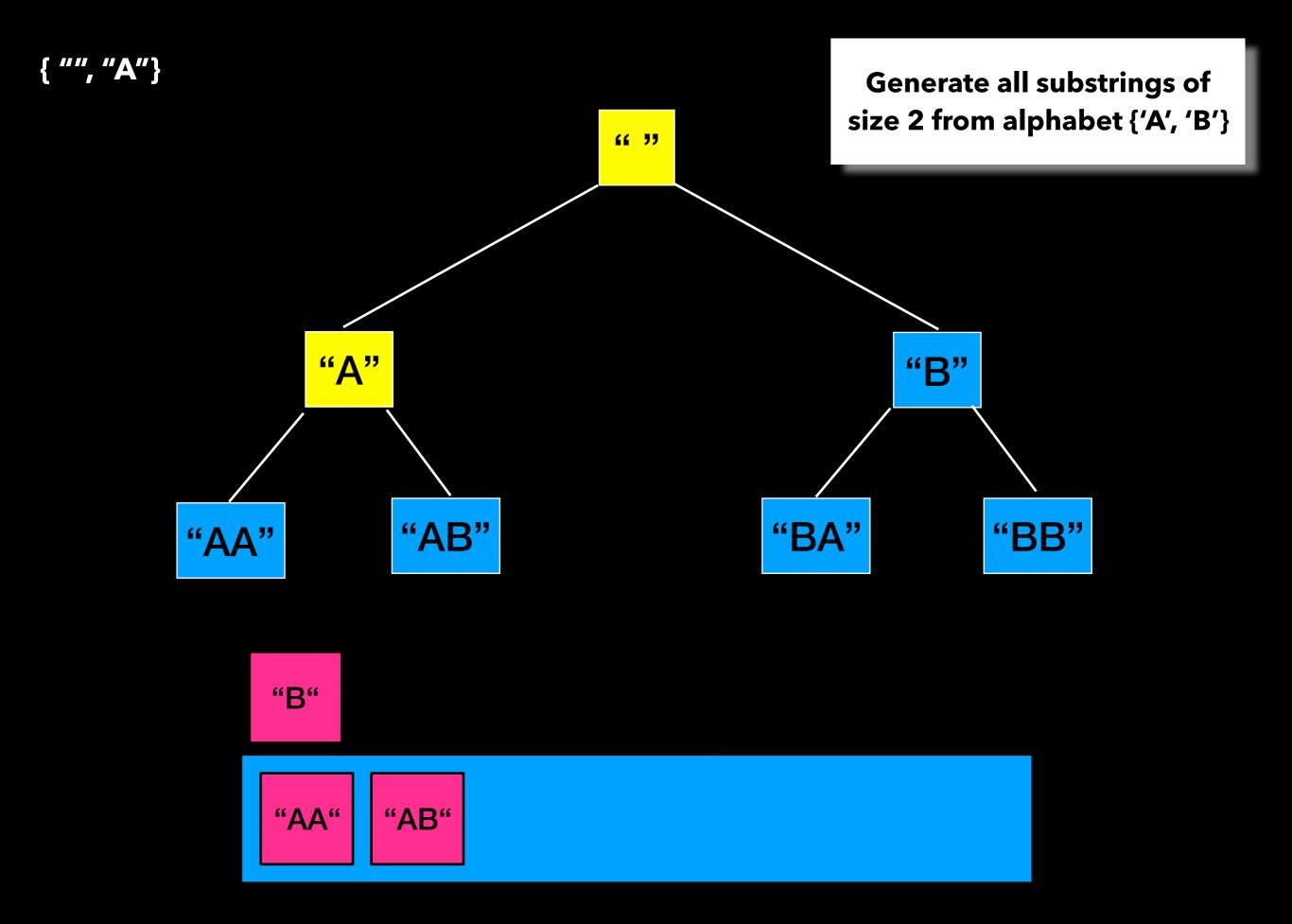


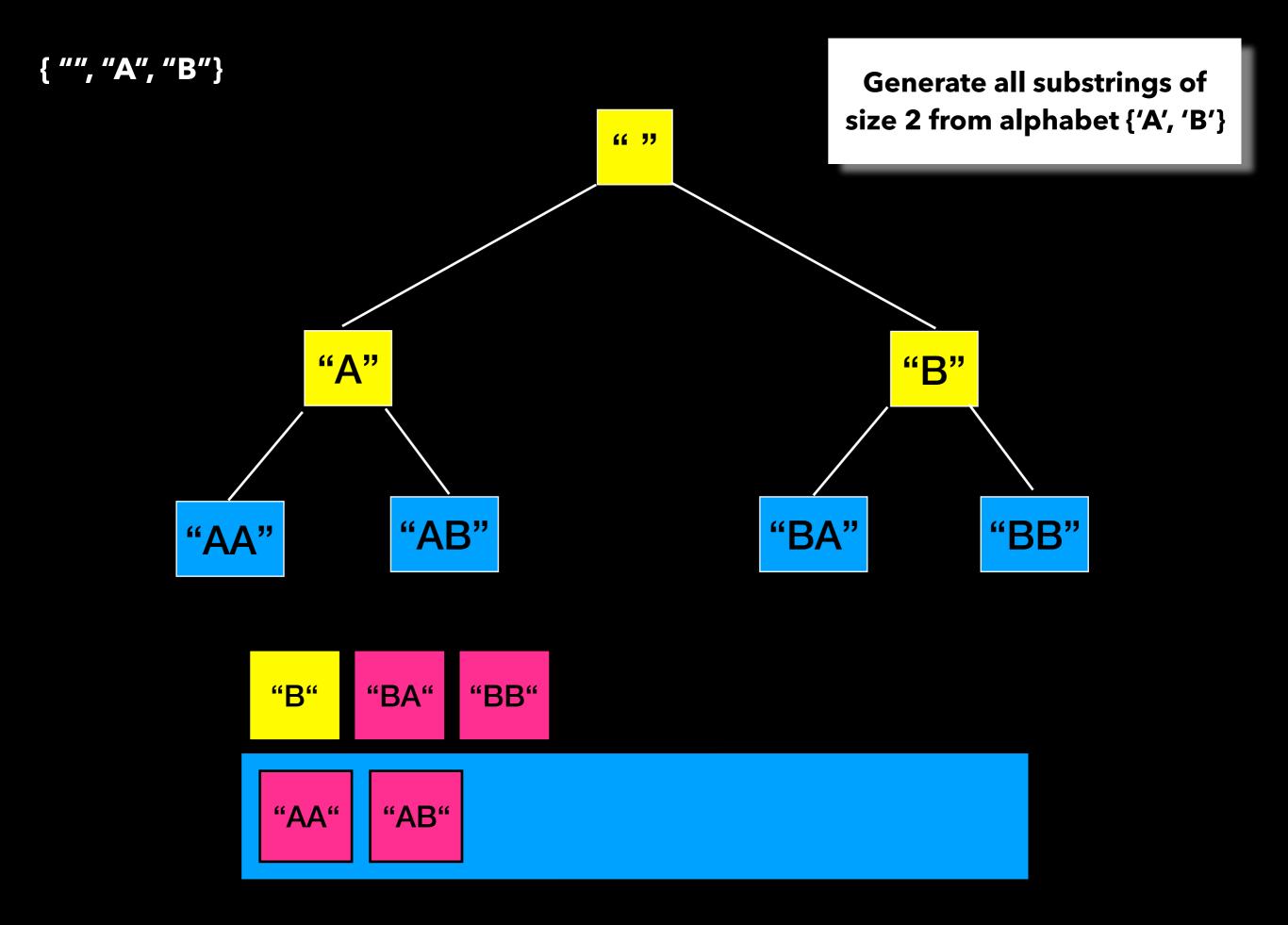


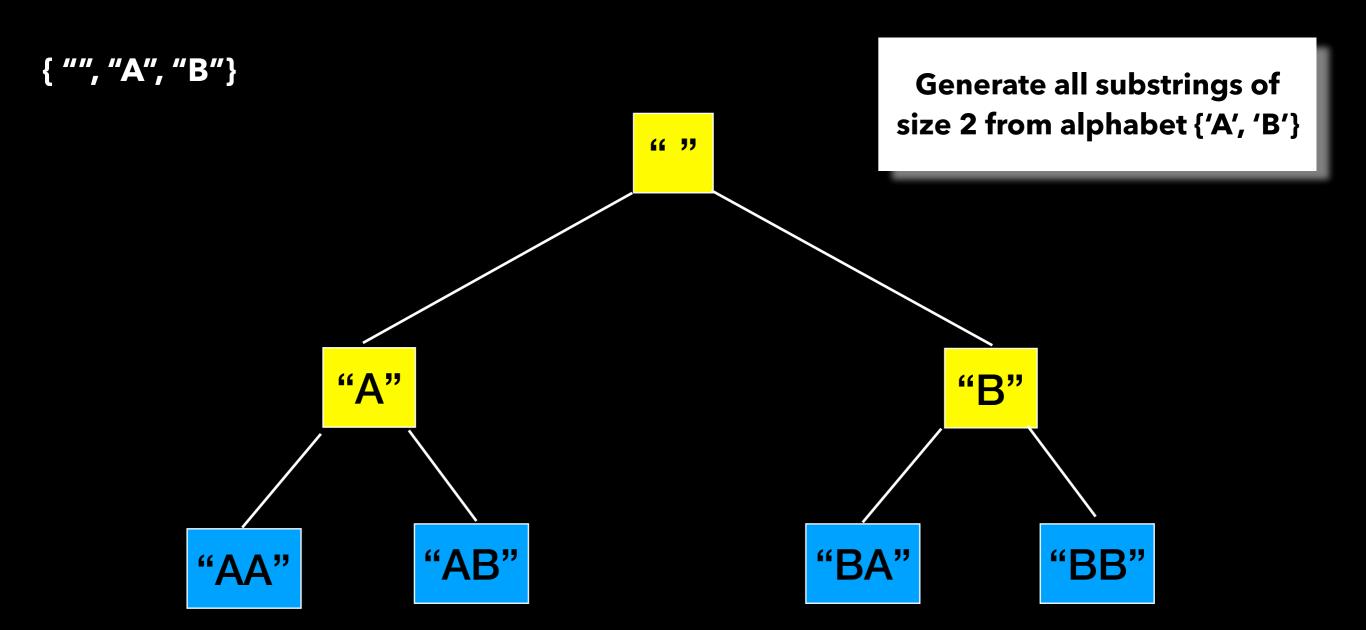


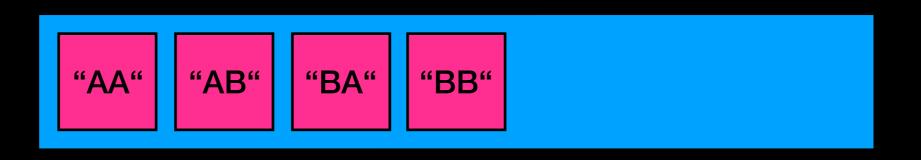


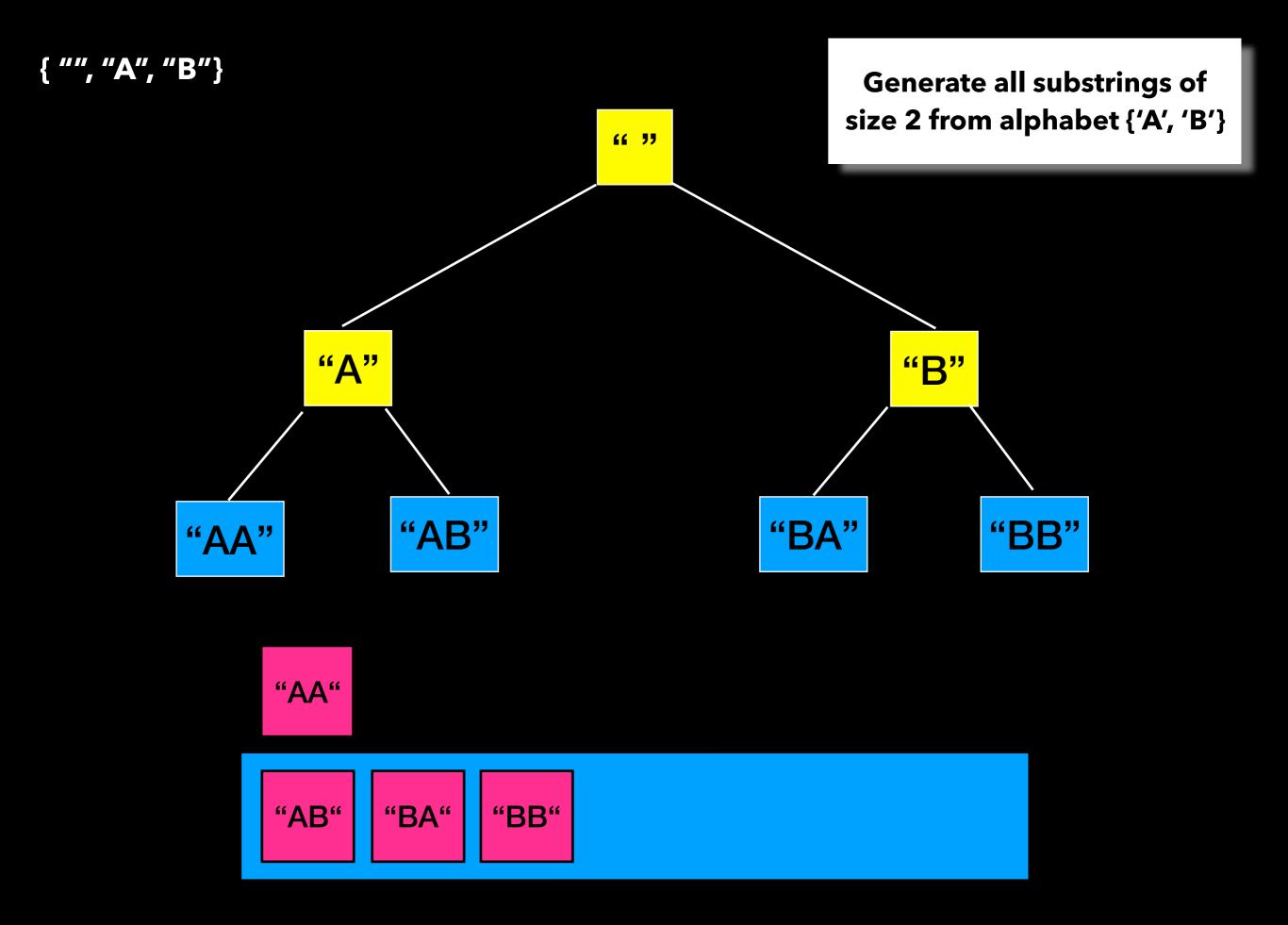


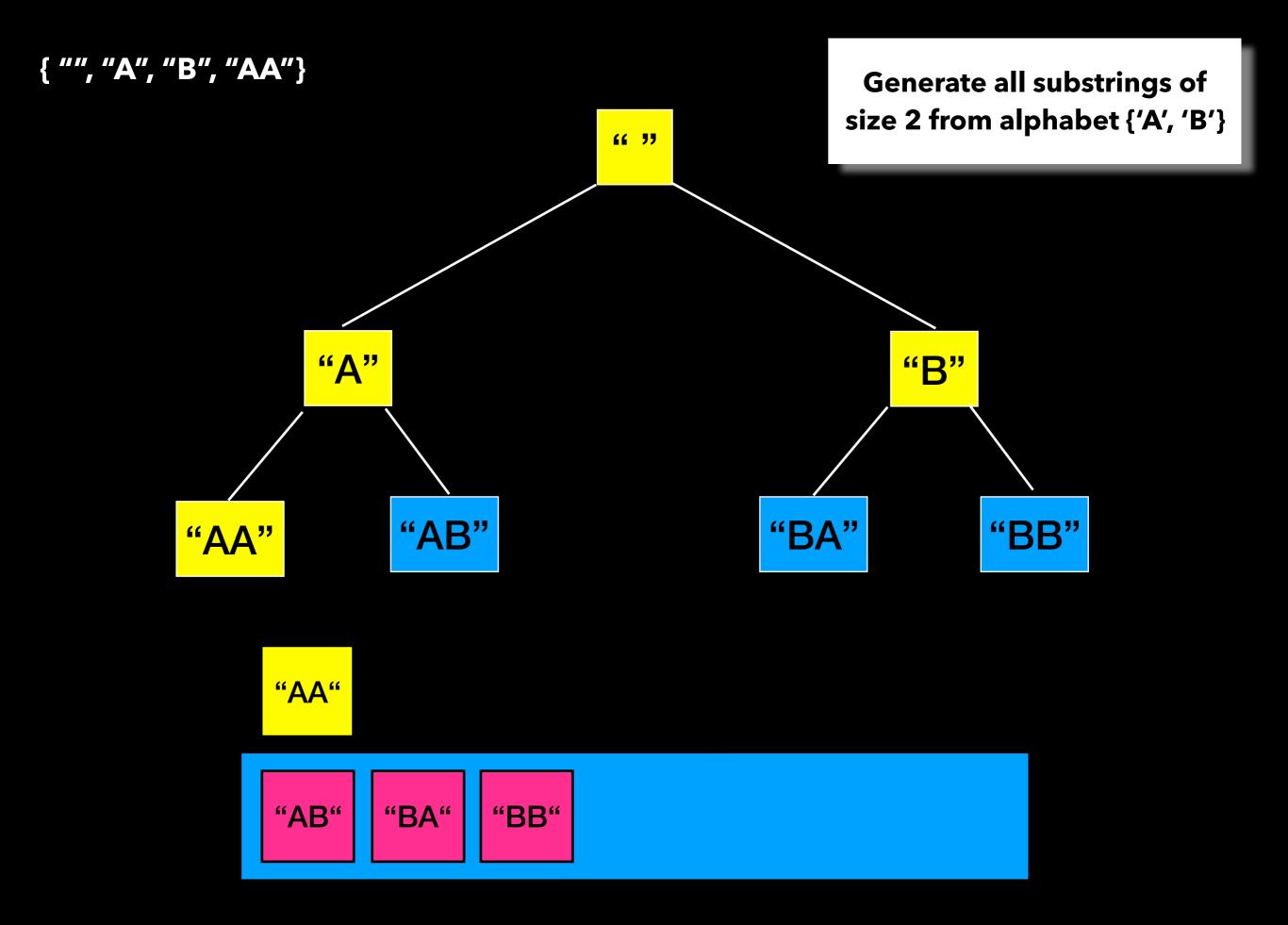


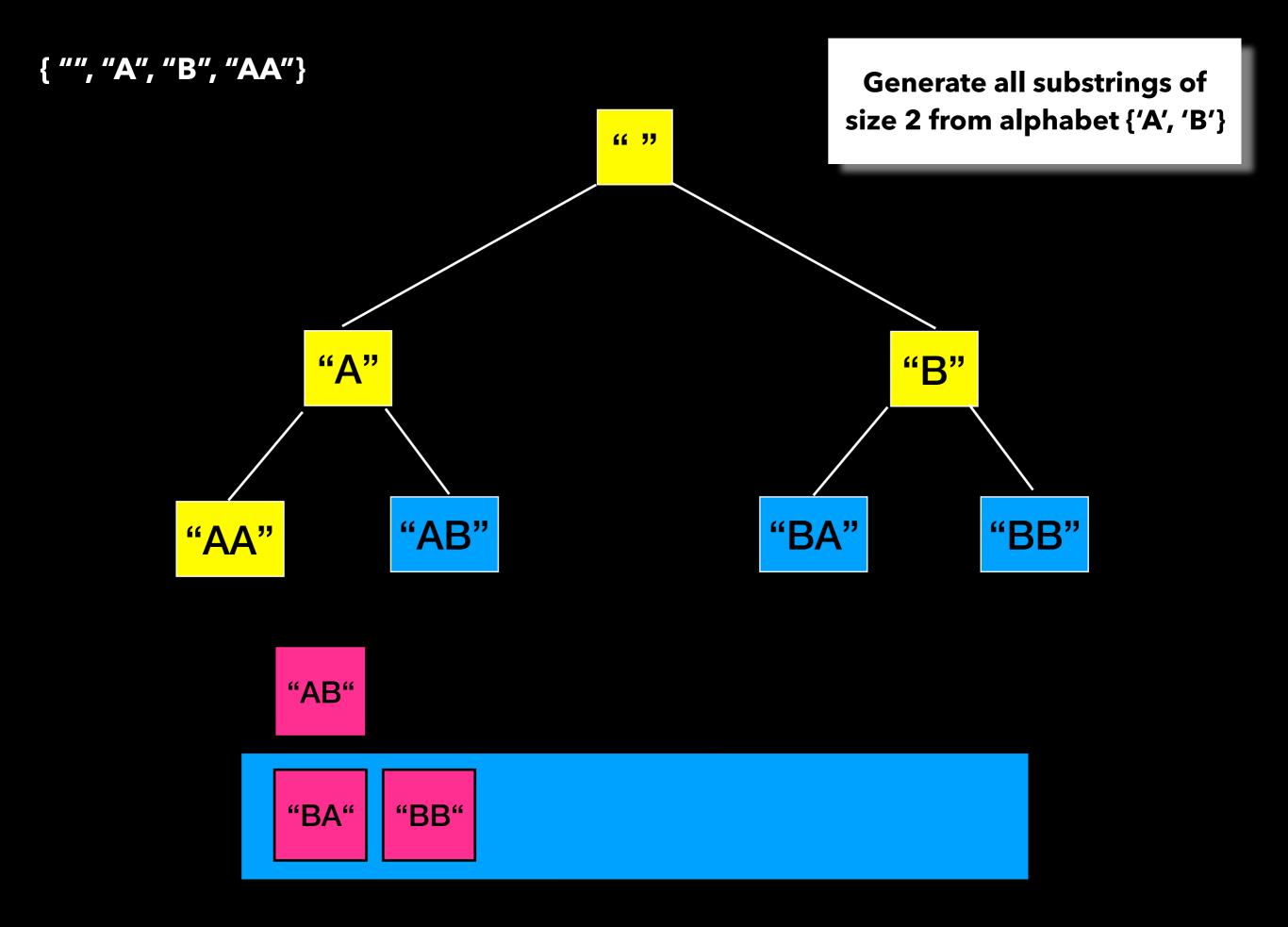


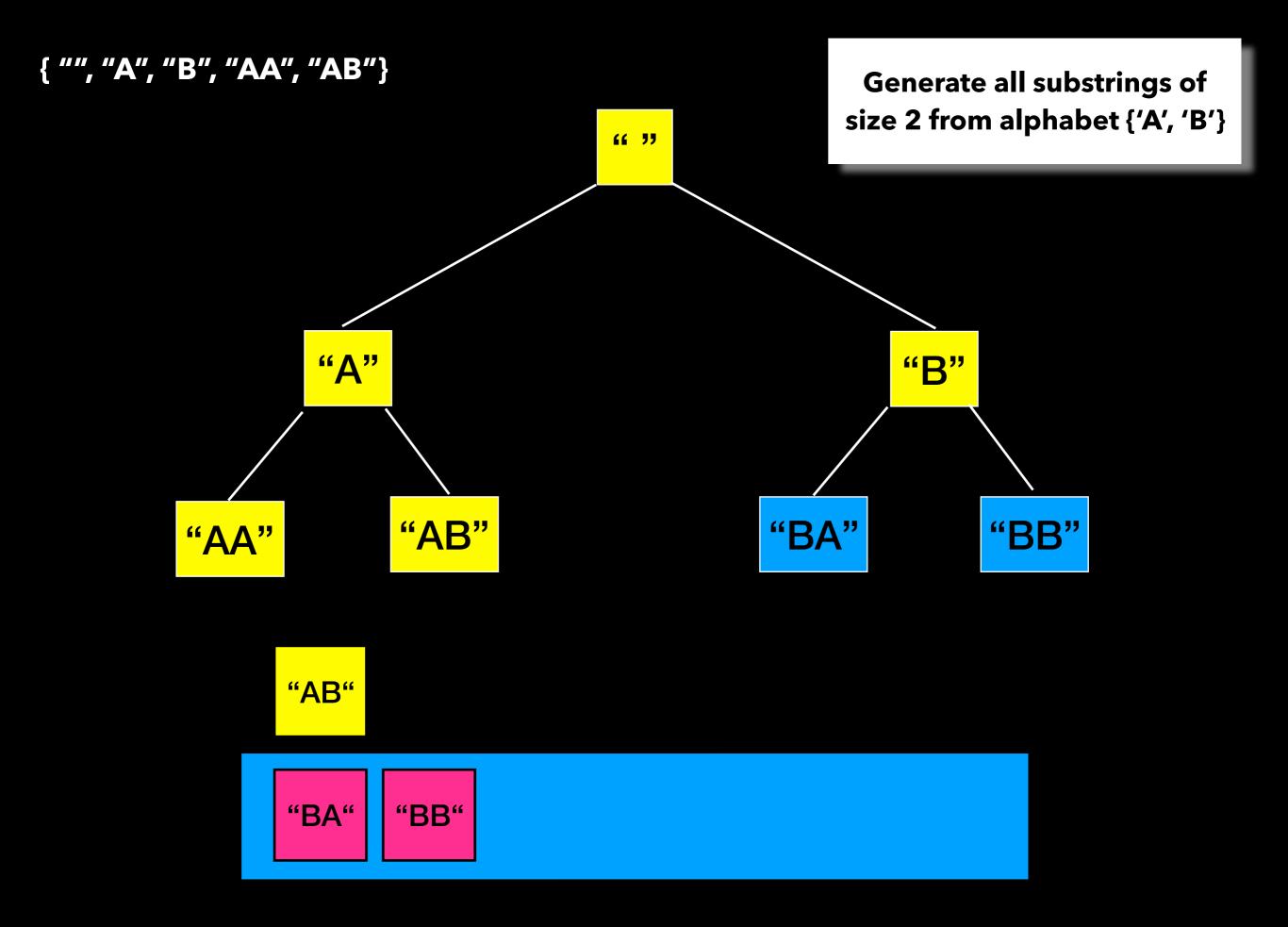


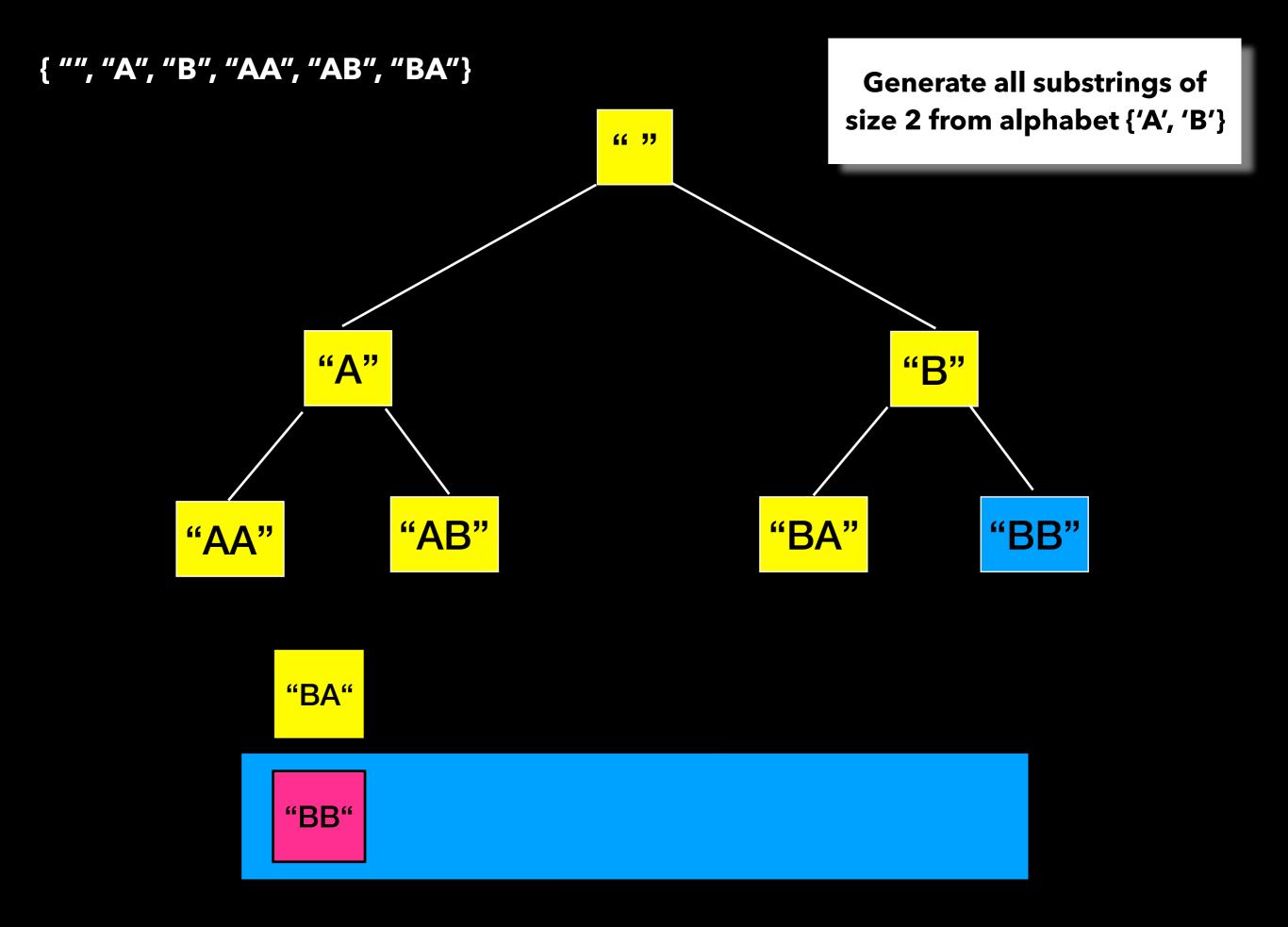


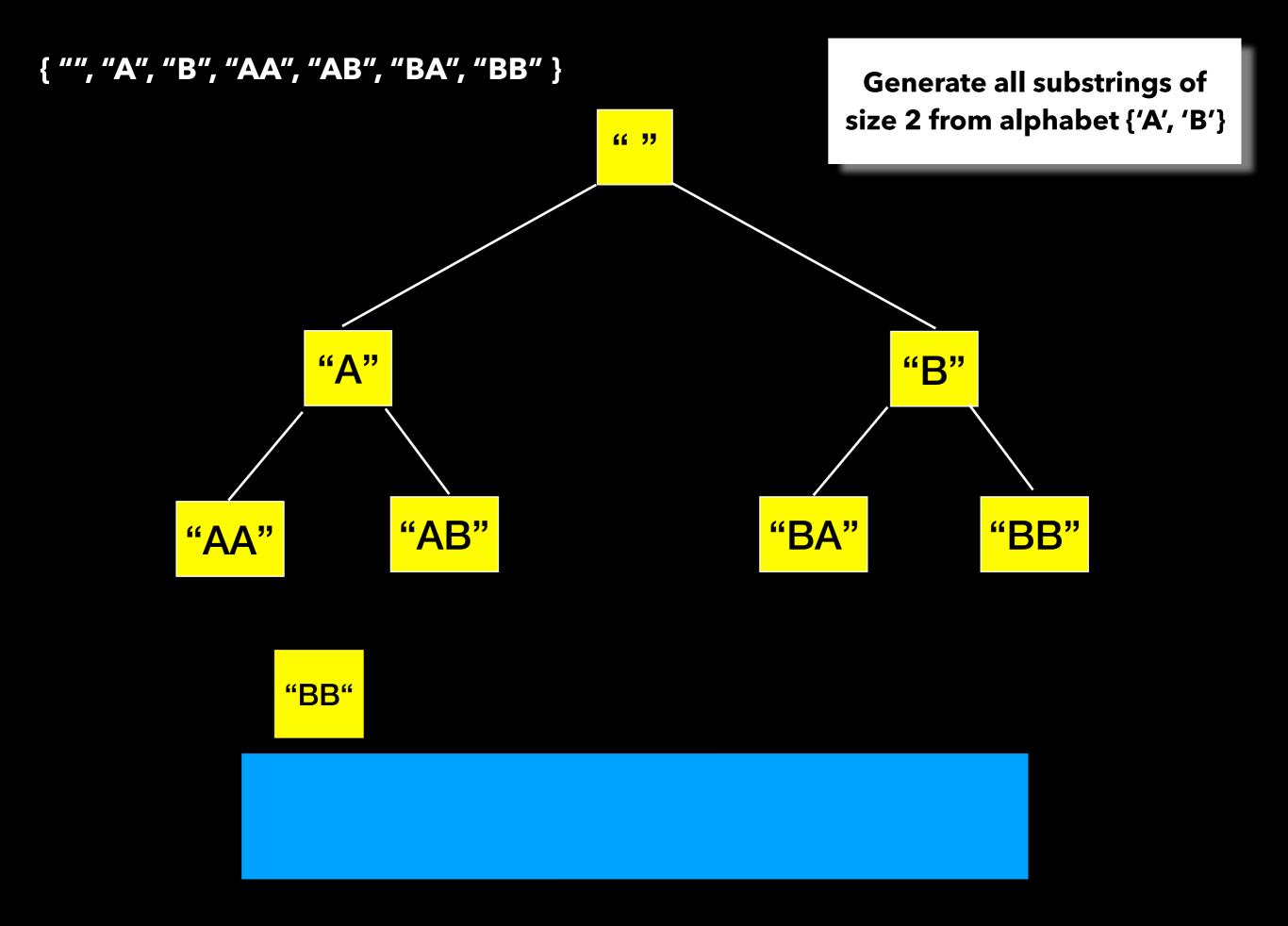


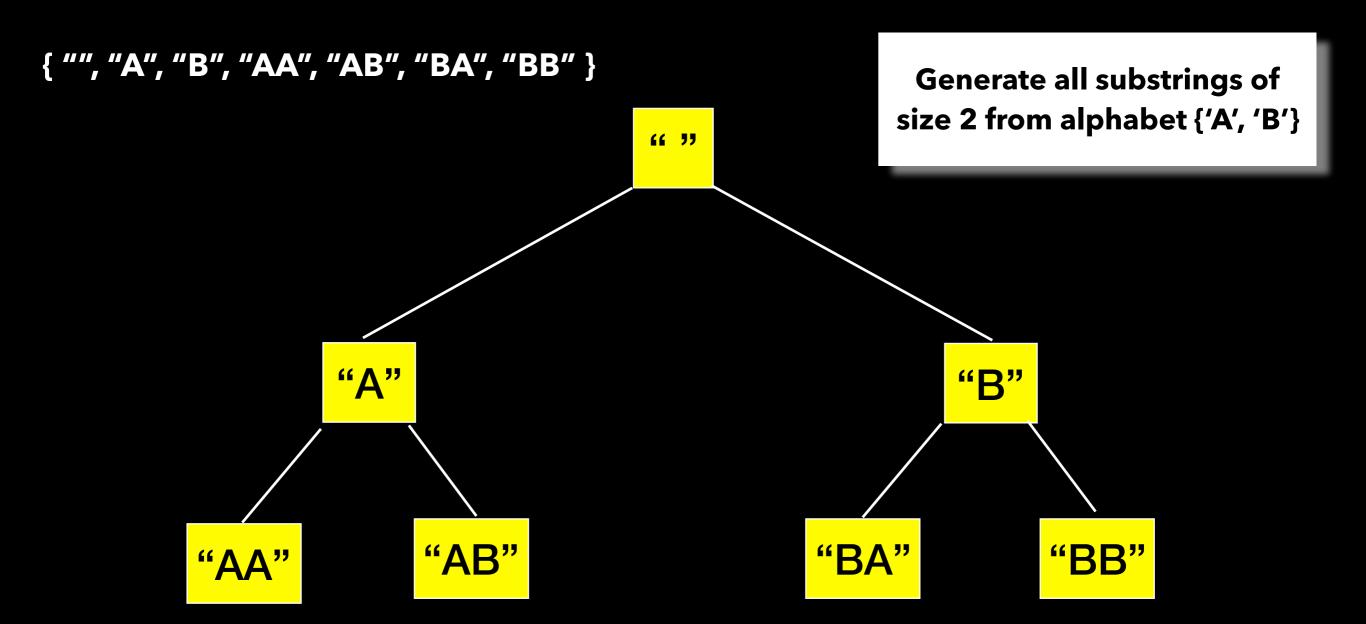












Breadth-First Search

```
Applications
Find shortest path in graph
GPS navigation systems
Crawlers in search engines
```

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Generally good when looking for the "shortest" or "best" way to do something => lists things in increasing order of "size" stopping at the "shortest" solution

Size of Substring

Analysis

Finding all substrings (with repetition) of size up to n

Assume alphabet (A, B, ..., Z) of size 26

The empty string = 1

All strings of size $1 = 26^{1}$

All strings of size $2 = 26^2$

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All strings of size $n = 26^n$

With repetition: I have 26 options for each of the n characters

Lecture Activity

```
Size of Substring
```

```
findAllSubstrings(int n)
{
    put empty string on the queue
```

Analyze the worst-case time complexity of this algorithm assuming alphabet of size 26 and up to strings of length n

```
T(n) = ?
O(?)
```

```
while(queue is not empty){
    let current_string = dequeue and add to result
    if(size of current_string < n){
        for(each character ch)//every character in alphabet
            append ch to current_string and enqueue it
    }
}
return result;
}</pre>
```

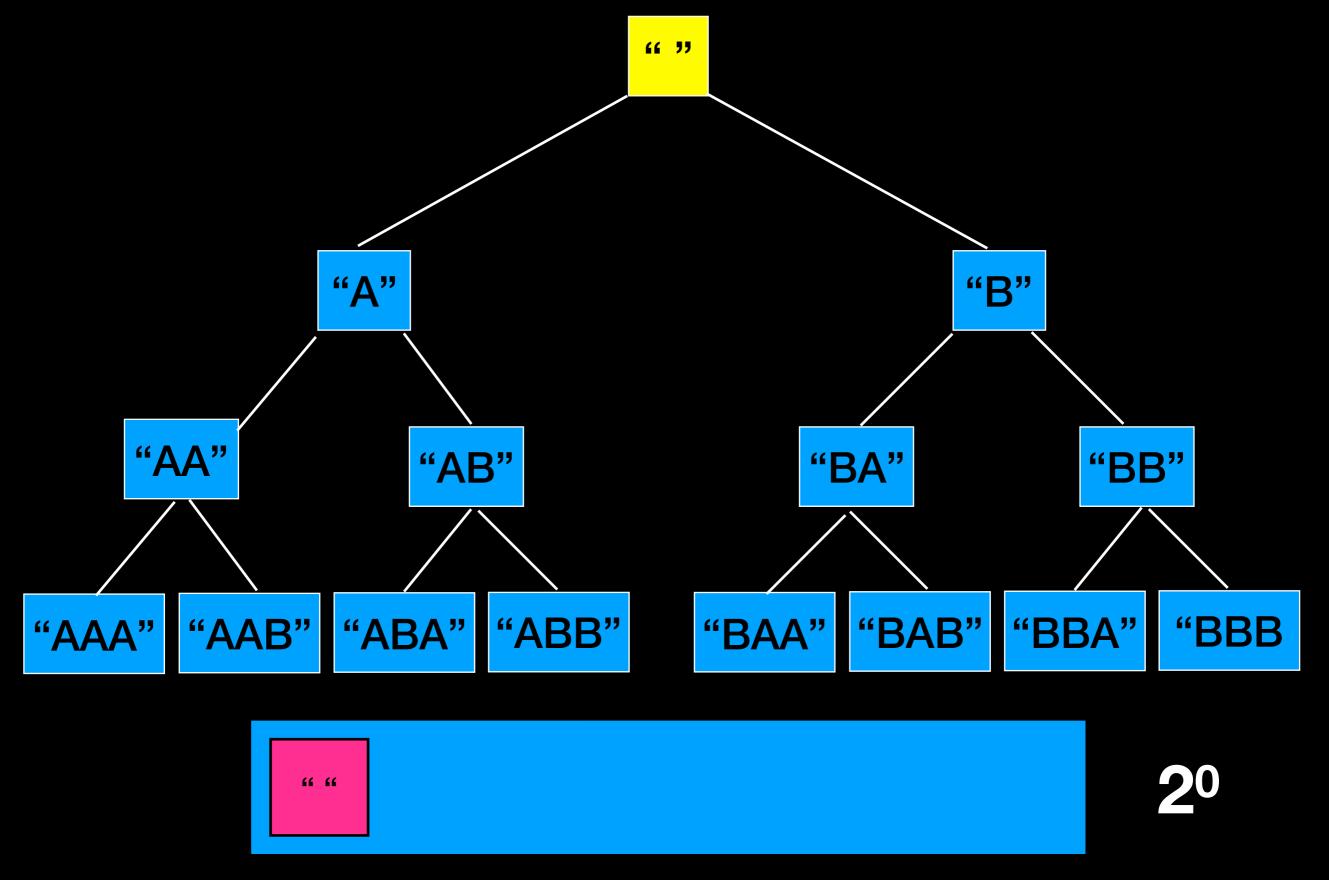
$$T(n) = 26^0 + 26^1 + 26^2 + \dots 26^n$$

Removes 1 string from the queue

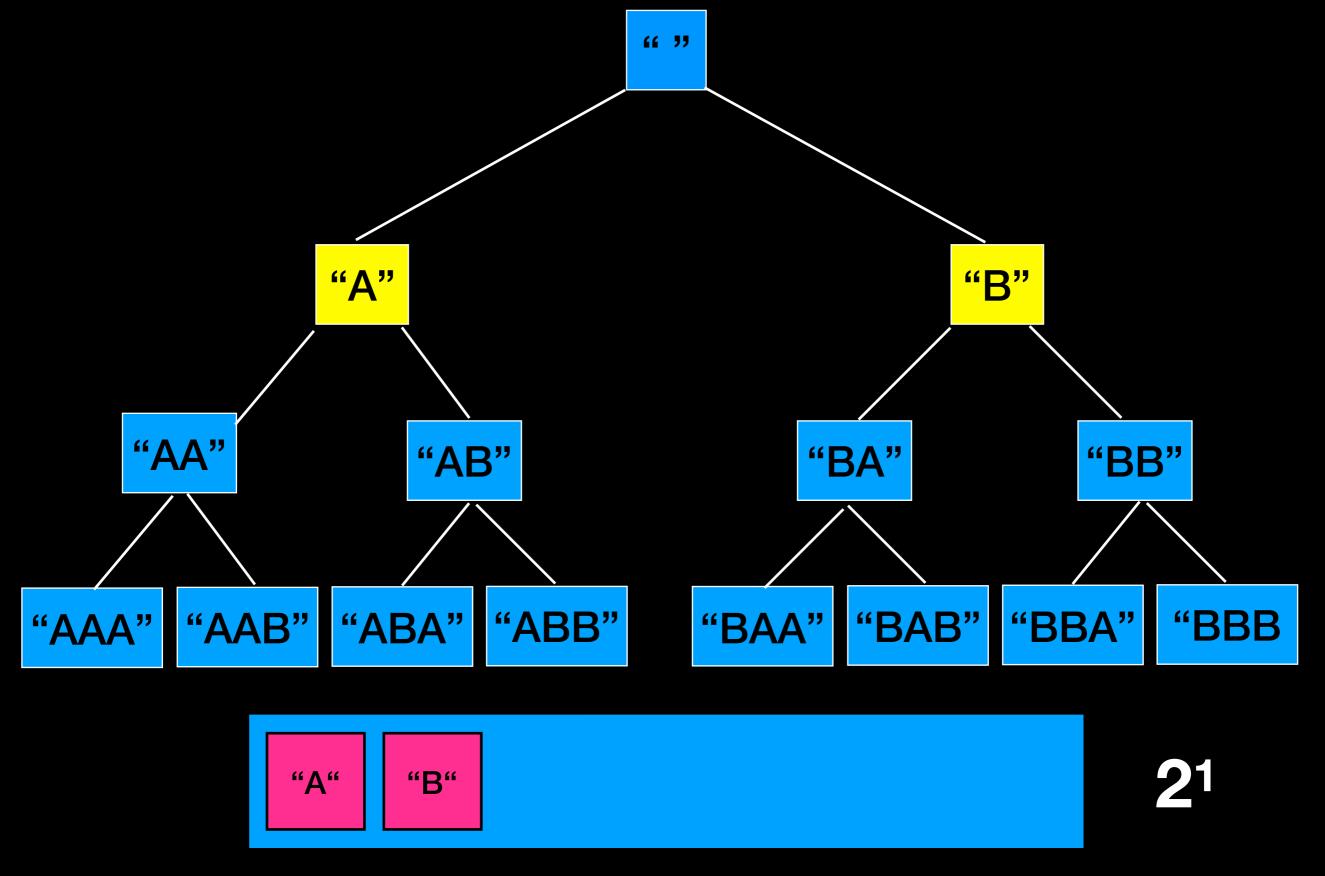
Removes 1 string from the queue

 $T(n) = 26^0 + 26^1 + 26^2 + \dots 26^n$

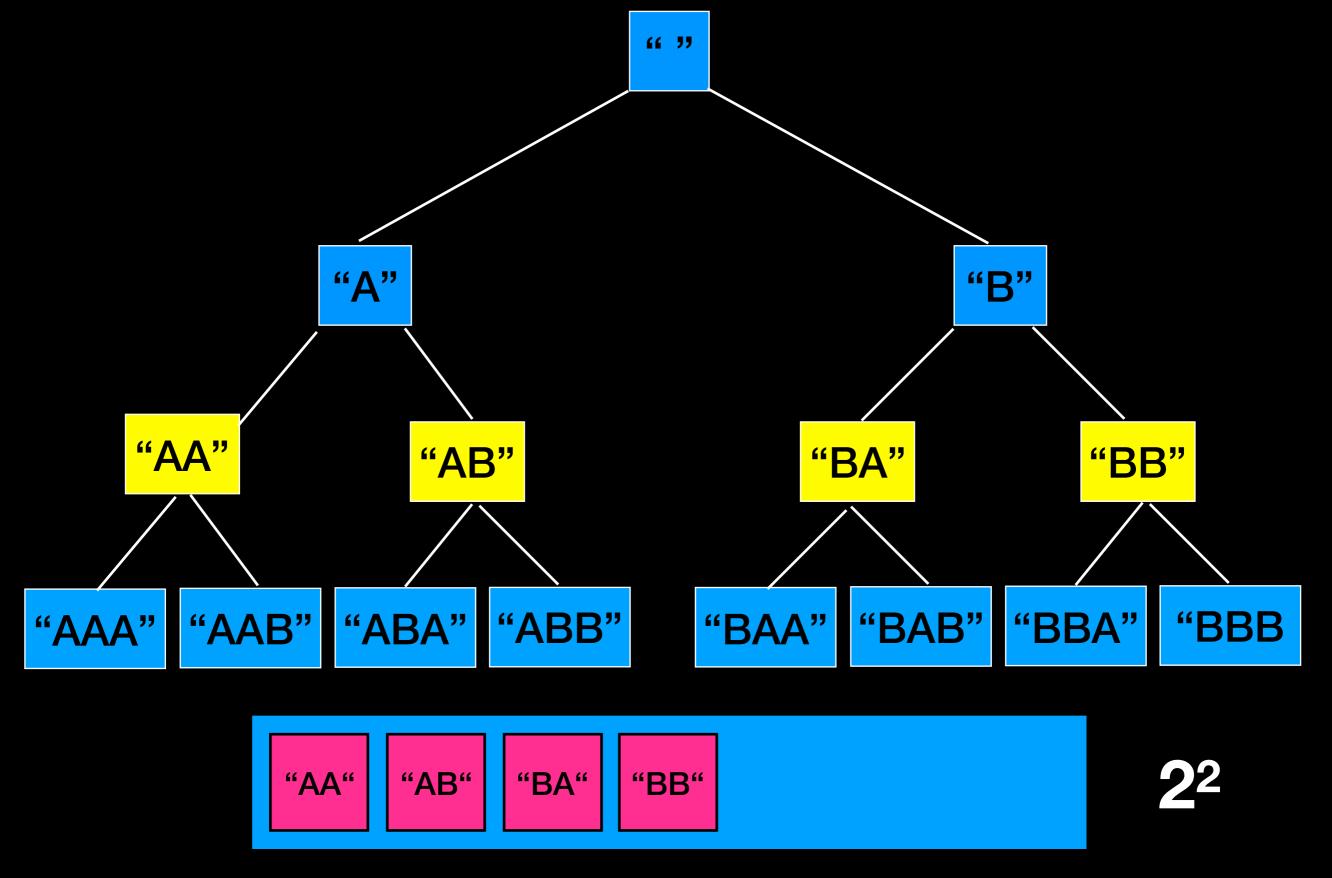
Let n = 3, alphabet still {'A','B'}



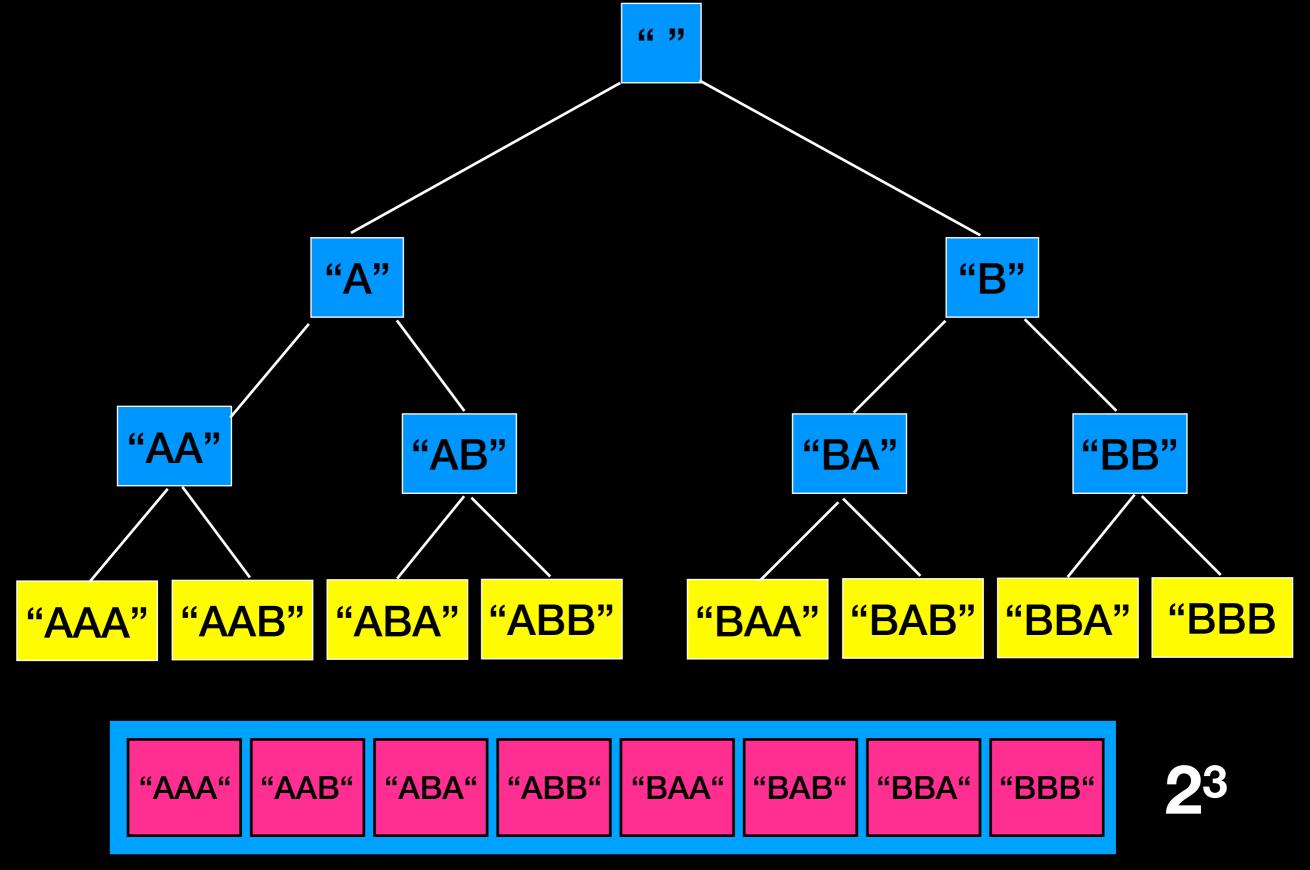
Let n = 3, alphabet still {'A', 'B'}



Let n = 3, alphabet still {'A', 'B'}



Let n = 3, alphabet still {'A','B'}



Memory Usage

With alphabet $\{'A', 'B', ..., 'Z'\}$, at some point we end up with 26^n strings in memory

Size of string on my machine = 24 bytes

Running this algorithm for n = 7 ($\approx 193GB$) is the maximum that can be handled by a standard personal computer

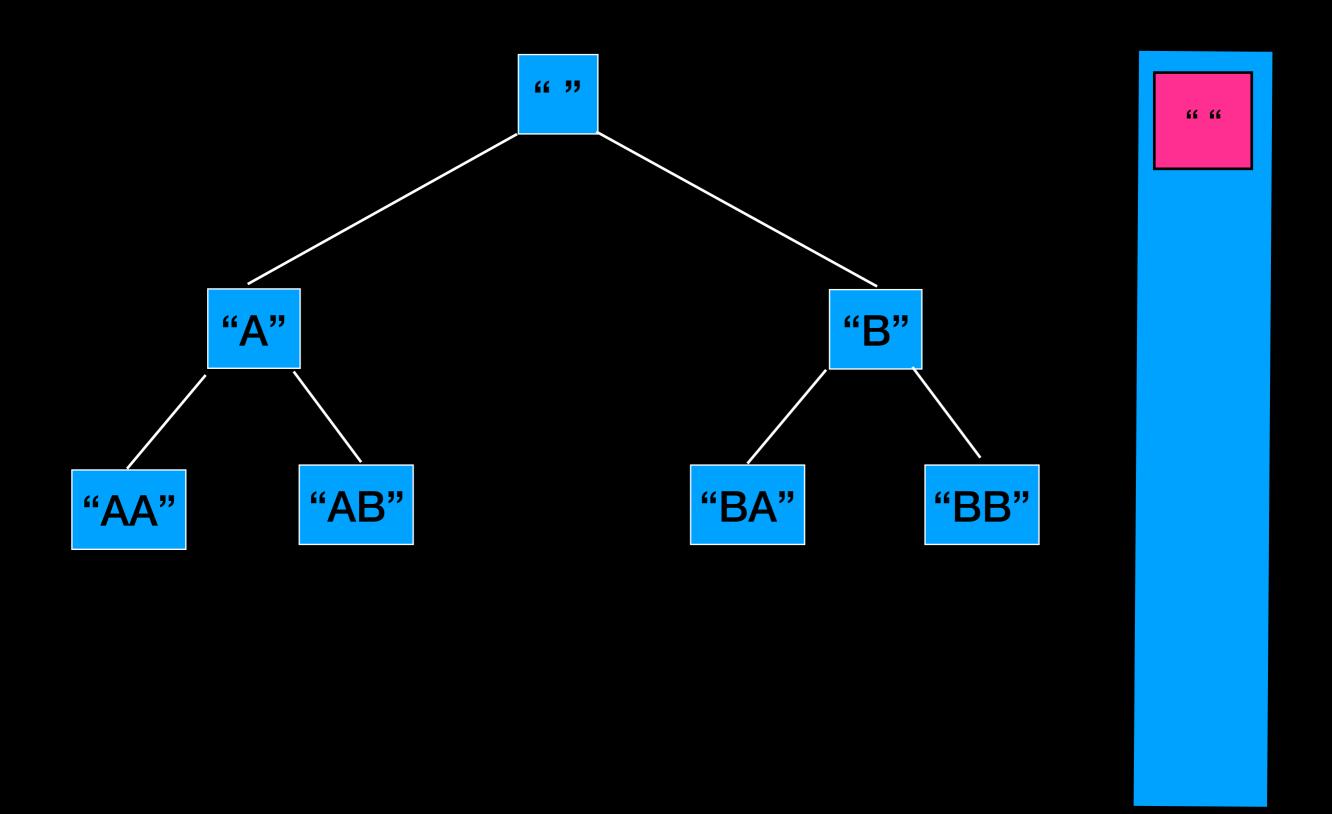
Massive

requirement

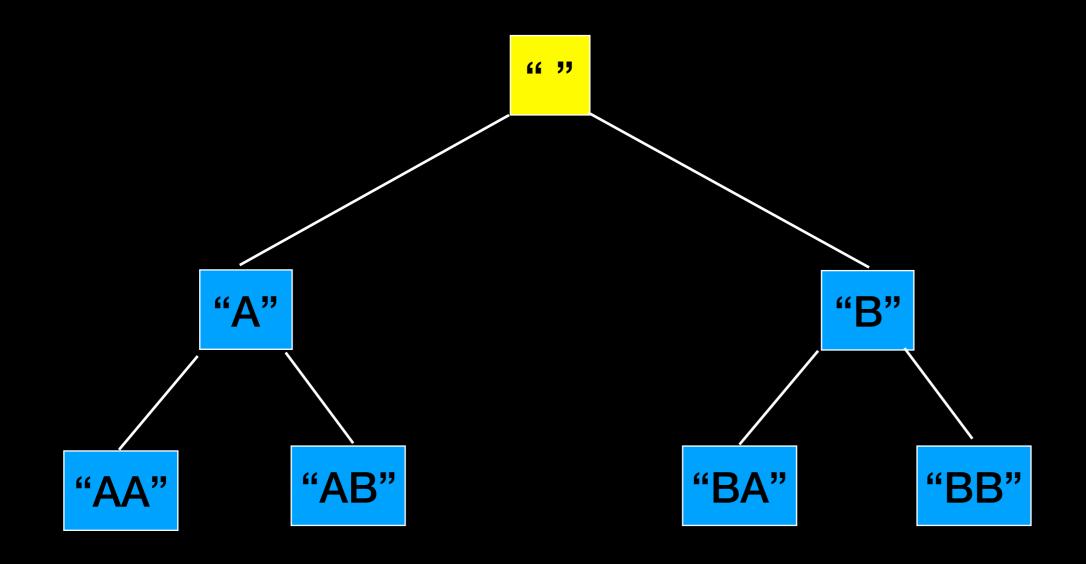
For $n = 8 \approx 5TB$

What if we use a stack?

O(26ⁿ)



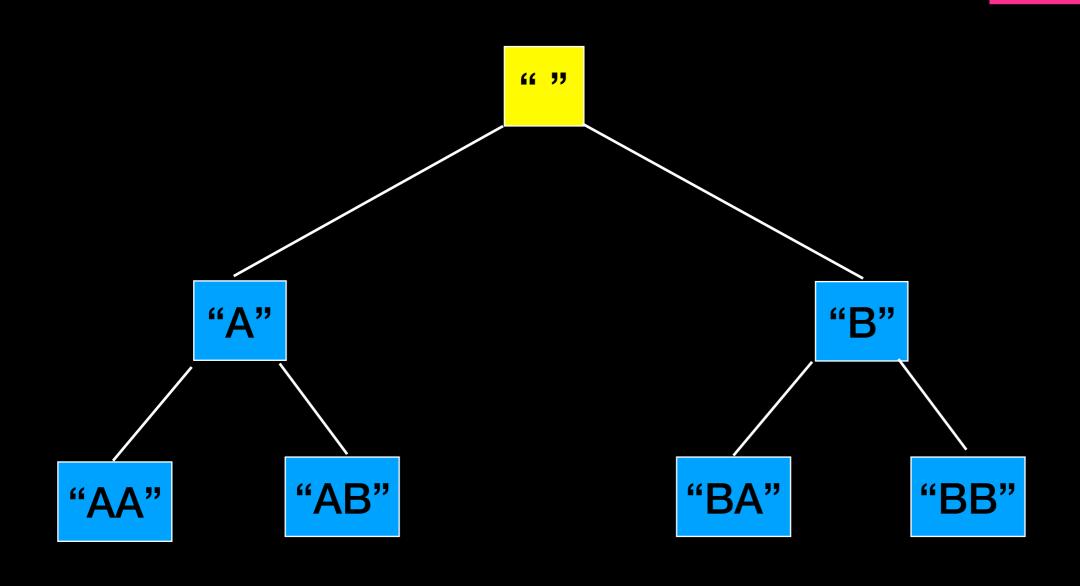
66 66

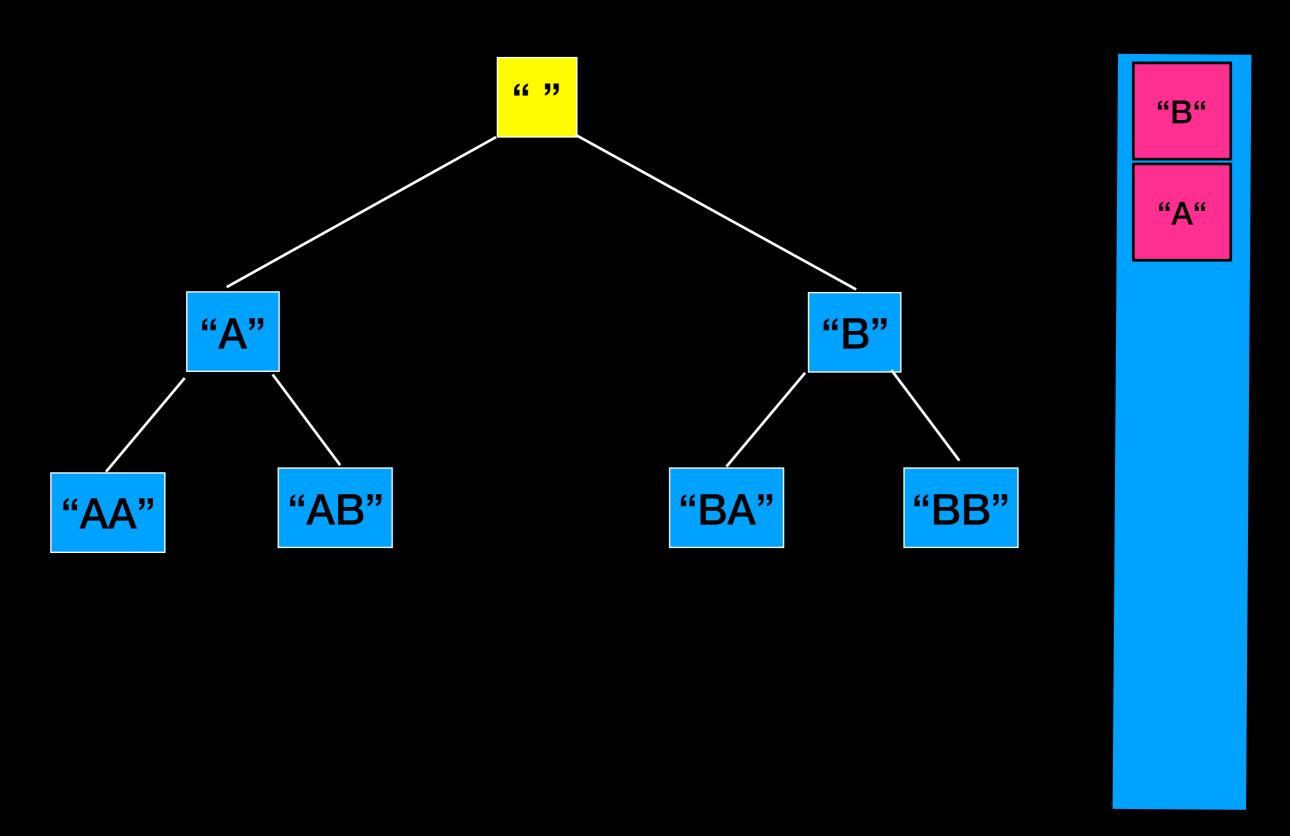


66 66

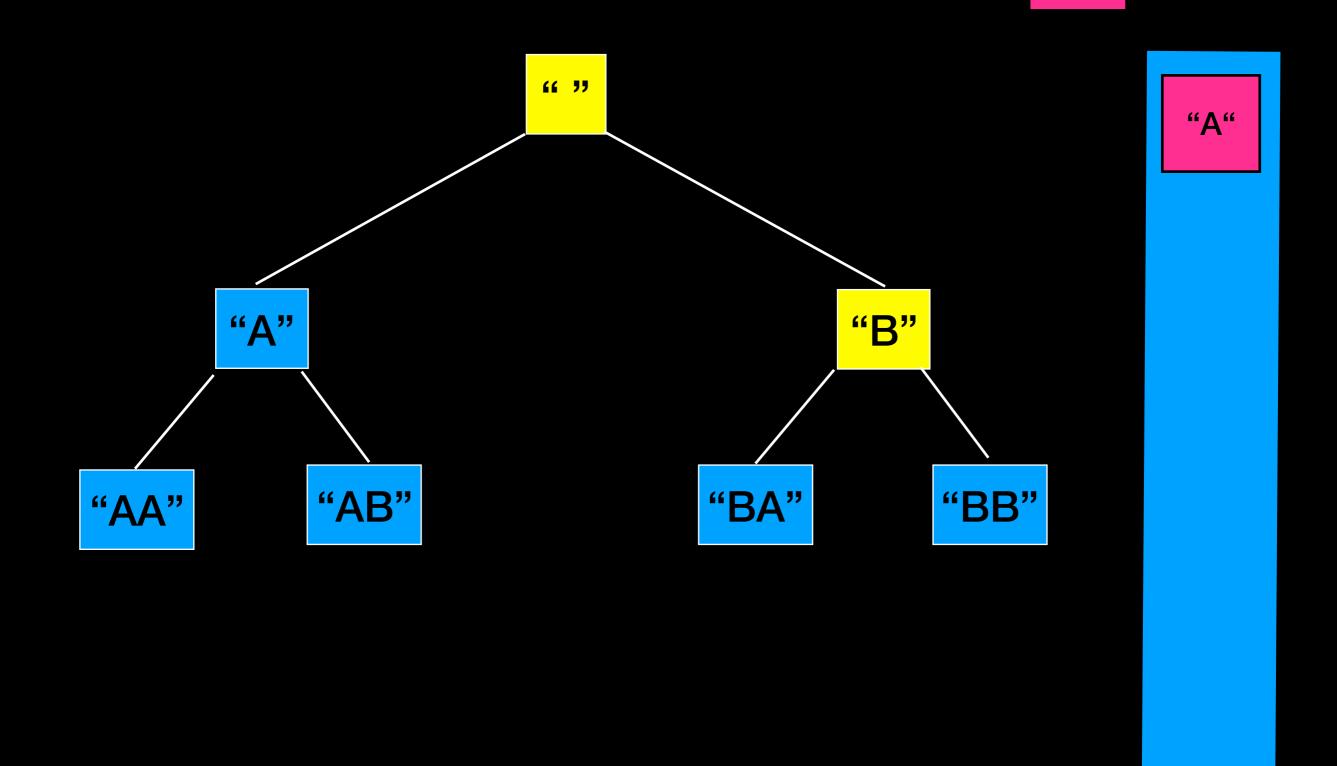
"A"

"B"





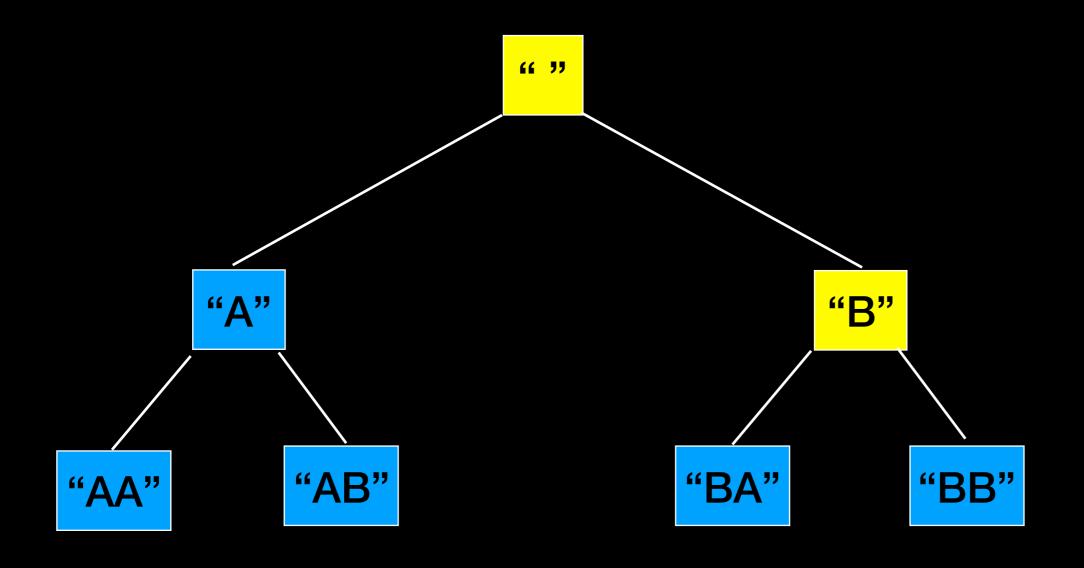
"B"



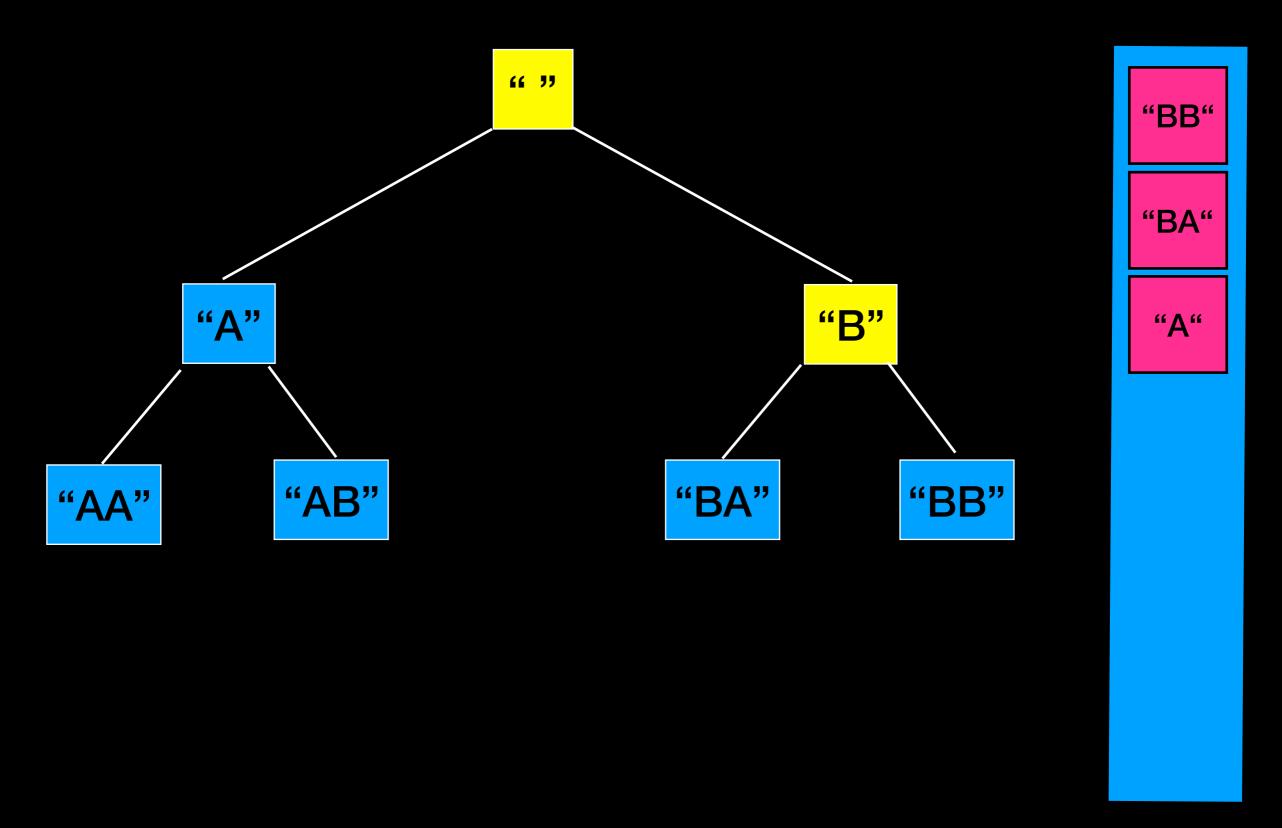
{ "","B"}

"B" "BA" "BB"

"**A**"

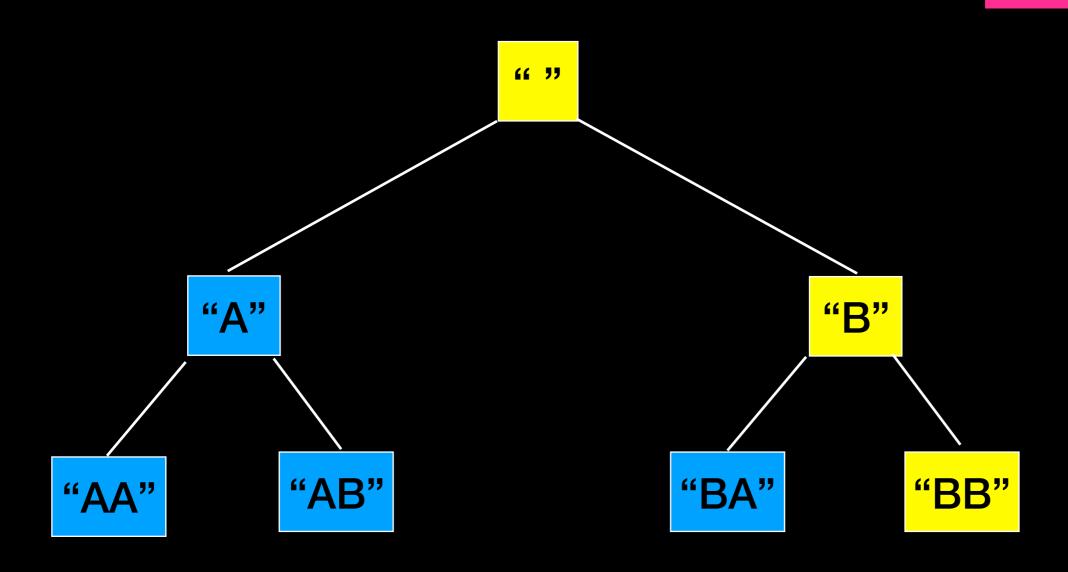


{ "","B"}



{ "","B","BB"}



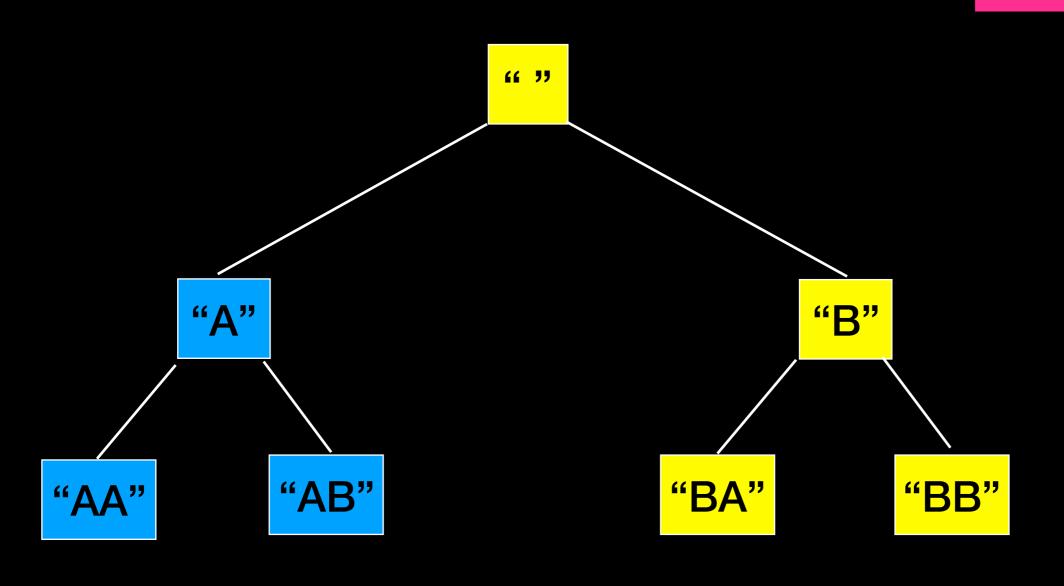




"A"

{ "","B","BB","BA"}

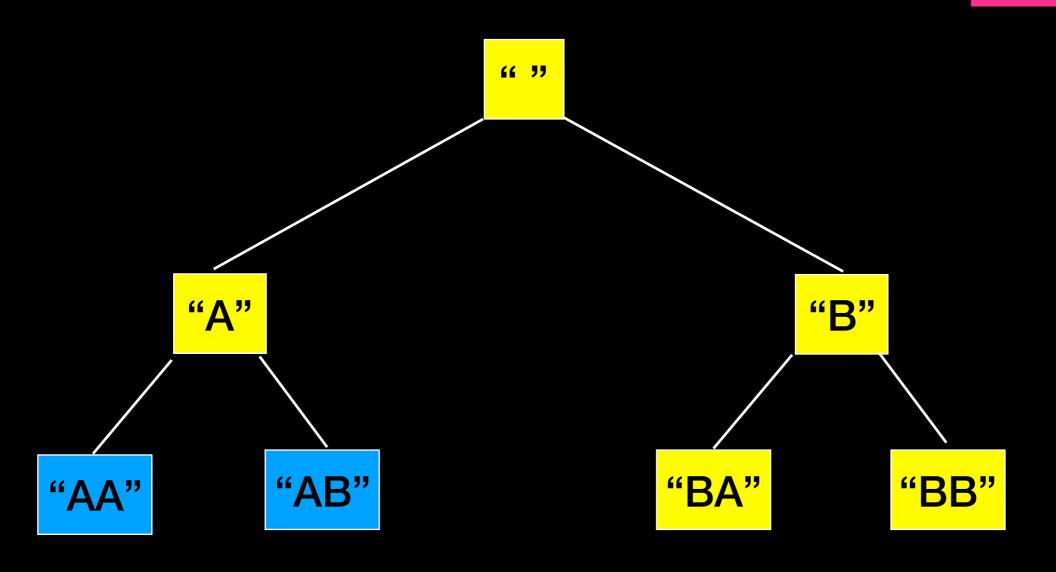




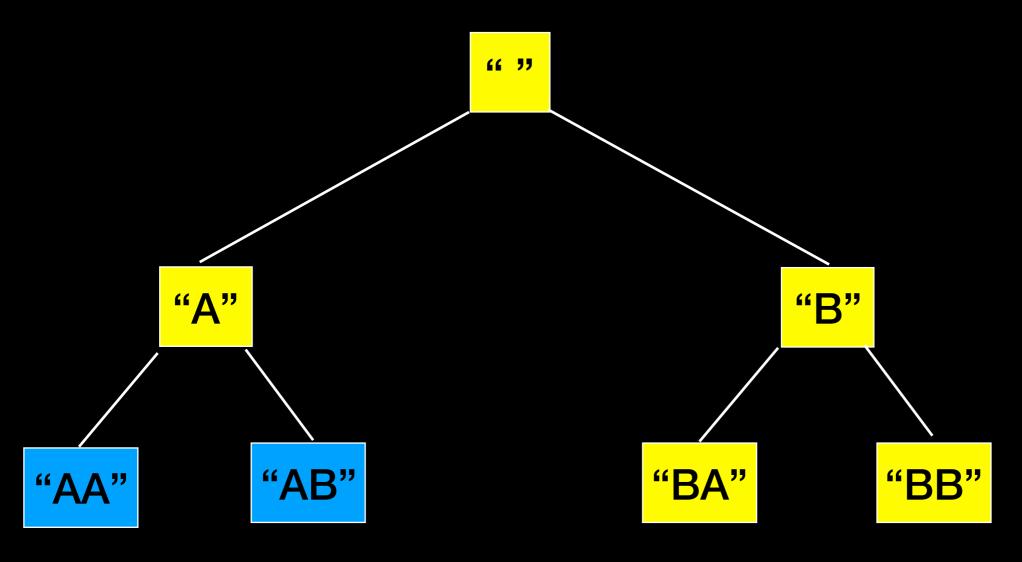


{ "","B","BB","BA","A"}

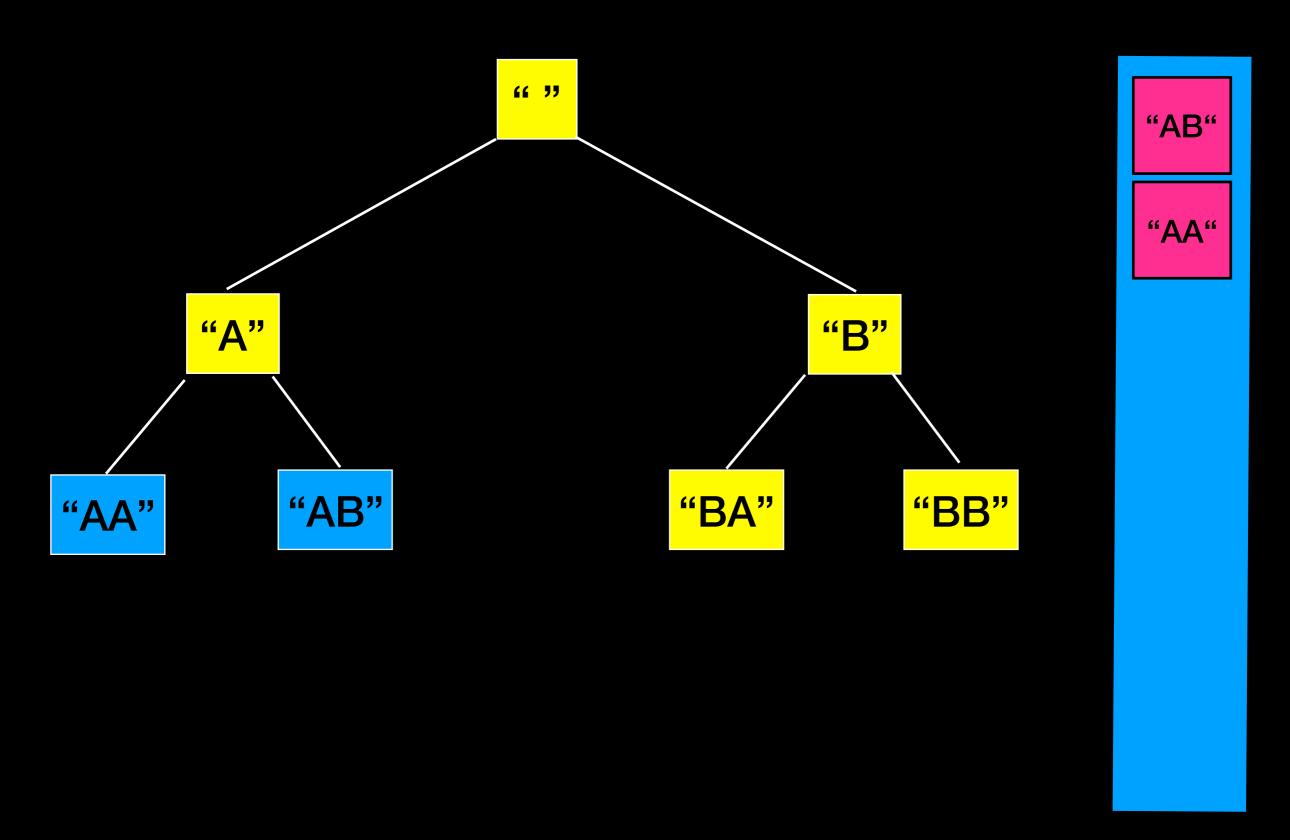






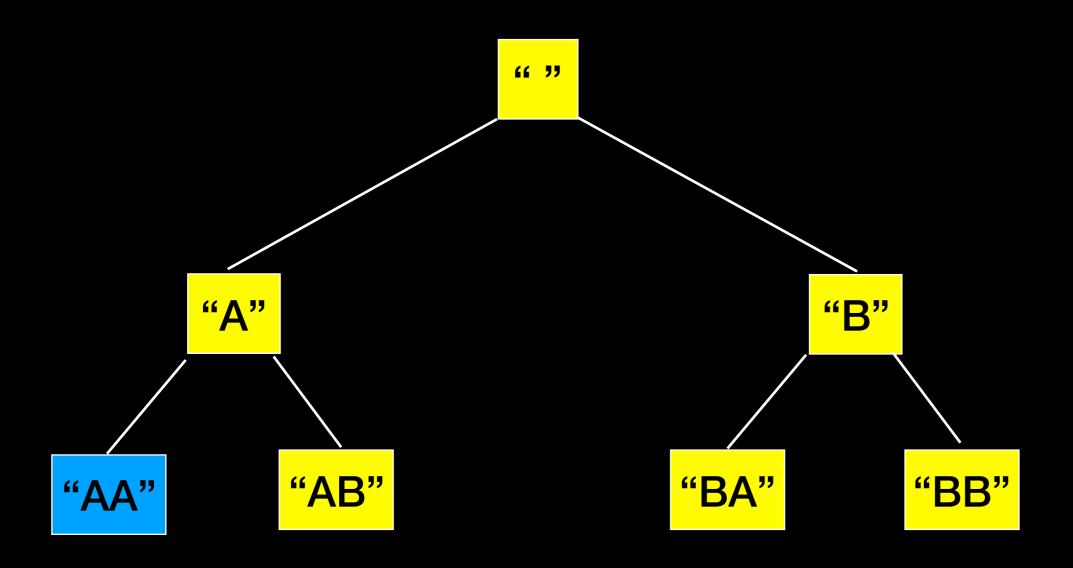


{ "","B","BB","BA","A"}



{ "","B","BB","BA","A","AB"}

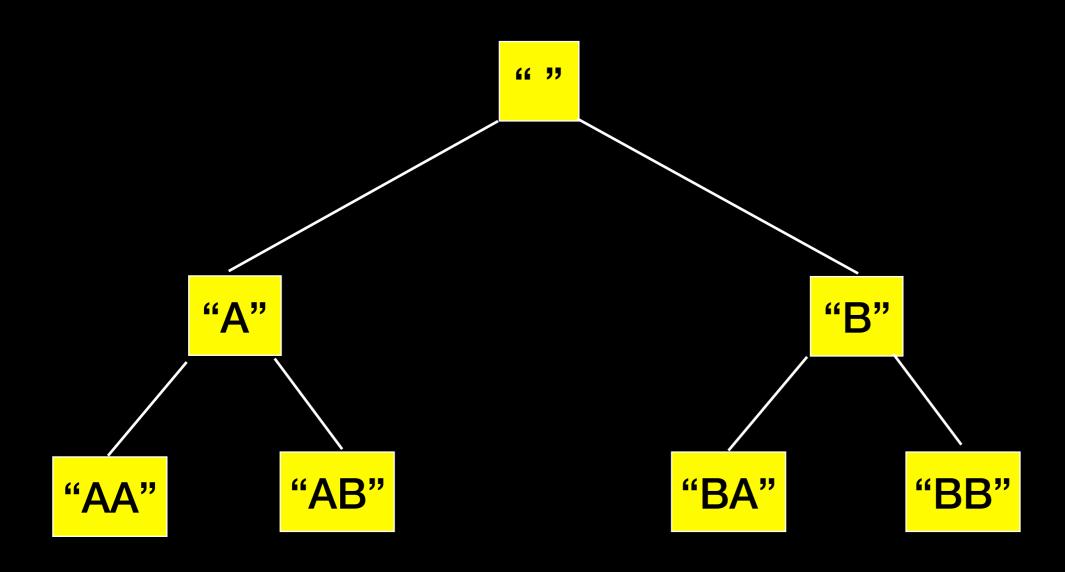




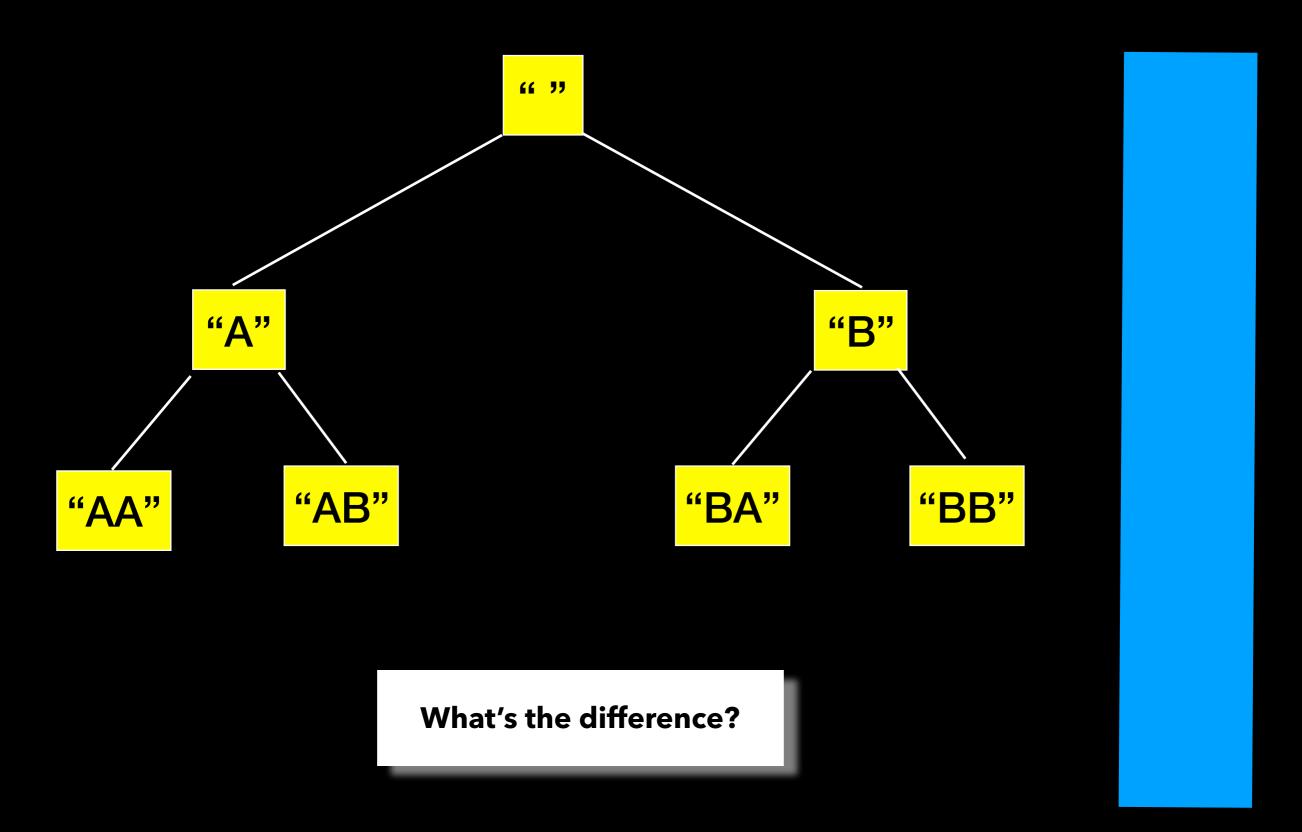


{ "","B","BB","BA","A","AB","AA"}





{ "","B","BB","BA","A","AB","AA"}



Depth-First Search

```
Applications
Detecting cycles in graphs
Path finding
Finding strongly connected components in graph
```

Same worst-case runtime analysis

More space efficient than previous approach

Does not explore options in increasing order of size

Comparison

Breadth-First Search (using a queue)

Time $O(26^n)$

Space O(26n)

Good for exploring options in increasing order of size when expecting to find "shallow" or "short" solution

Memory inefficient when must keep each "level" in memory

Depth-First Search (using a stack)

Time $O(26^n)$

Space O(n)

Explores each option individually to max size - does NOT list options by increasing size

More memory efficient

Recognizing Palindromes

Palindrome: a string that reads the same in reverse order

Anna

Civic

Kayak

Noon

Radar

Lecture Activity

```
Write C++ for
bool isPalindrome(string s)
```

```
bool isPalindrome(string const& word, int first, int last)
{
    //base case: a string with 0 or 1 character is a palindrome
    if(last - first <= 1)
        return true;
    // first and last are different, it is not a palindrome
    if(word[first] != word[last])
        return false;
    // first == last so check if smaller word is a palindrome
    return isPalindrome(word, first+1, last-1);
}</pre>
```

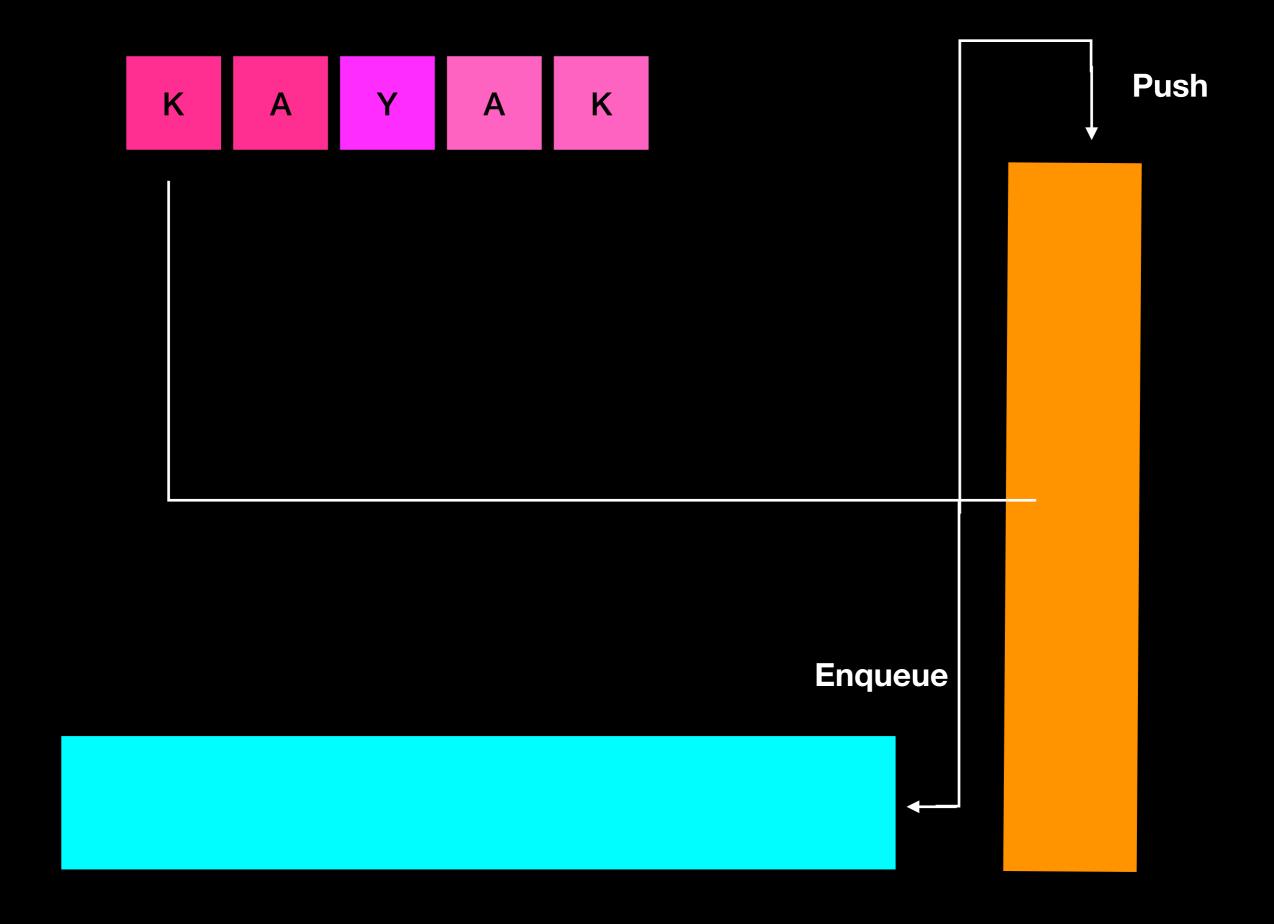
What if you have an incoming stream of characters, one at a time?

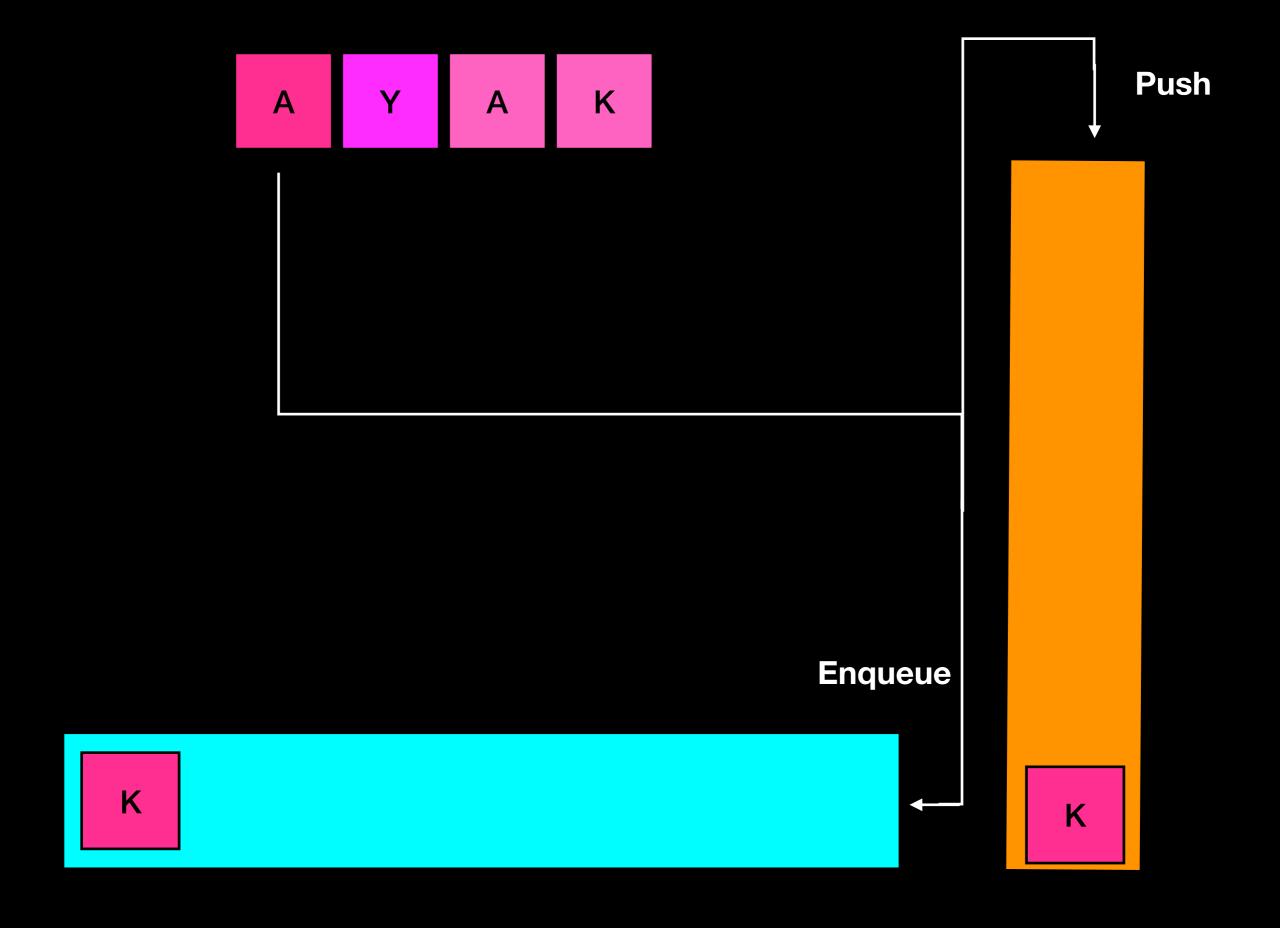
Notice

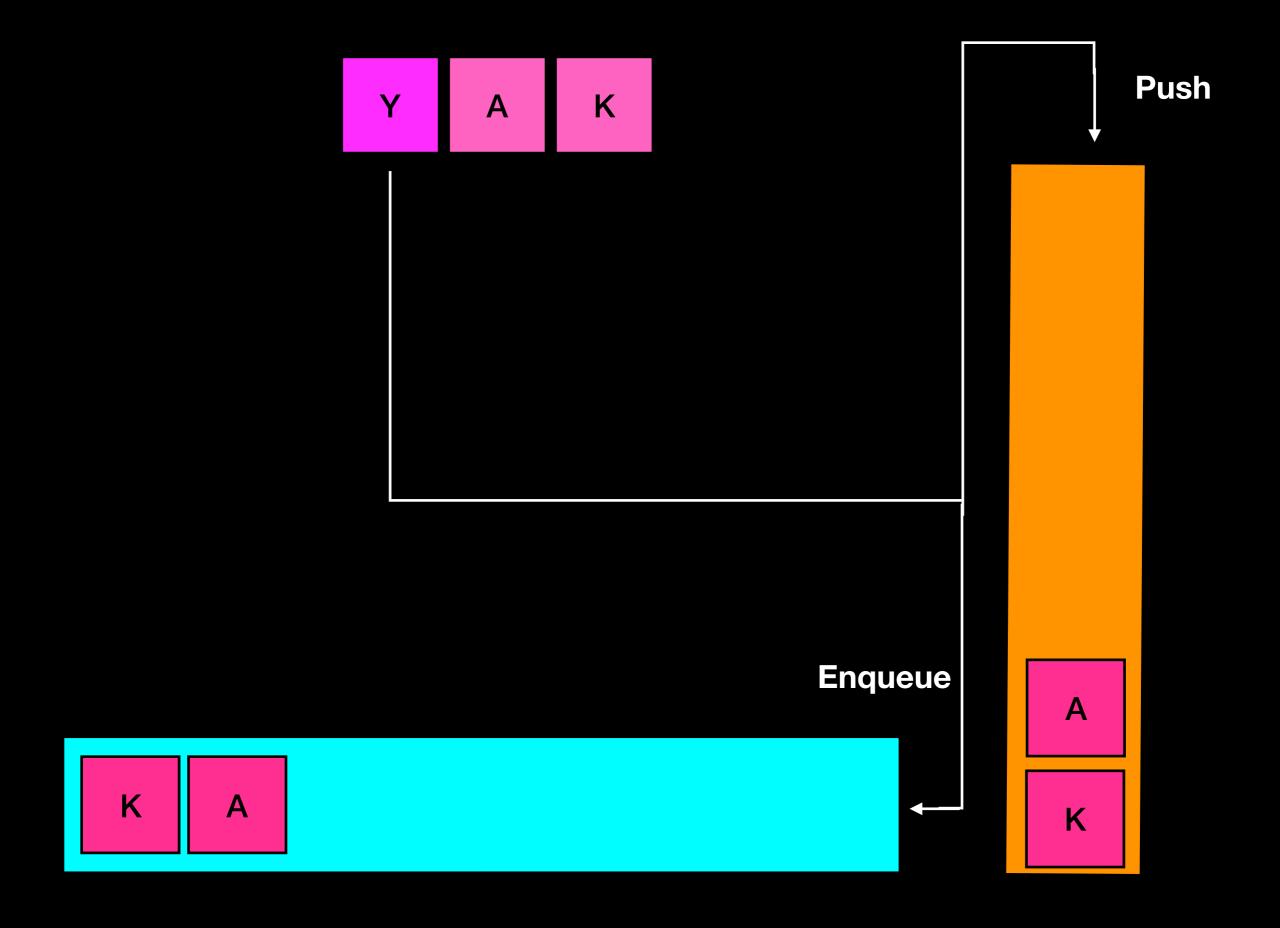
A stack can be used to reverse a string (LIFO)

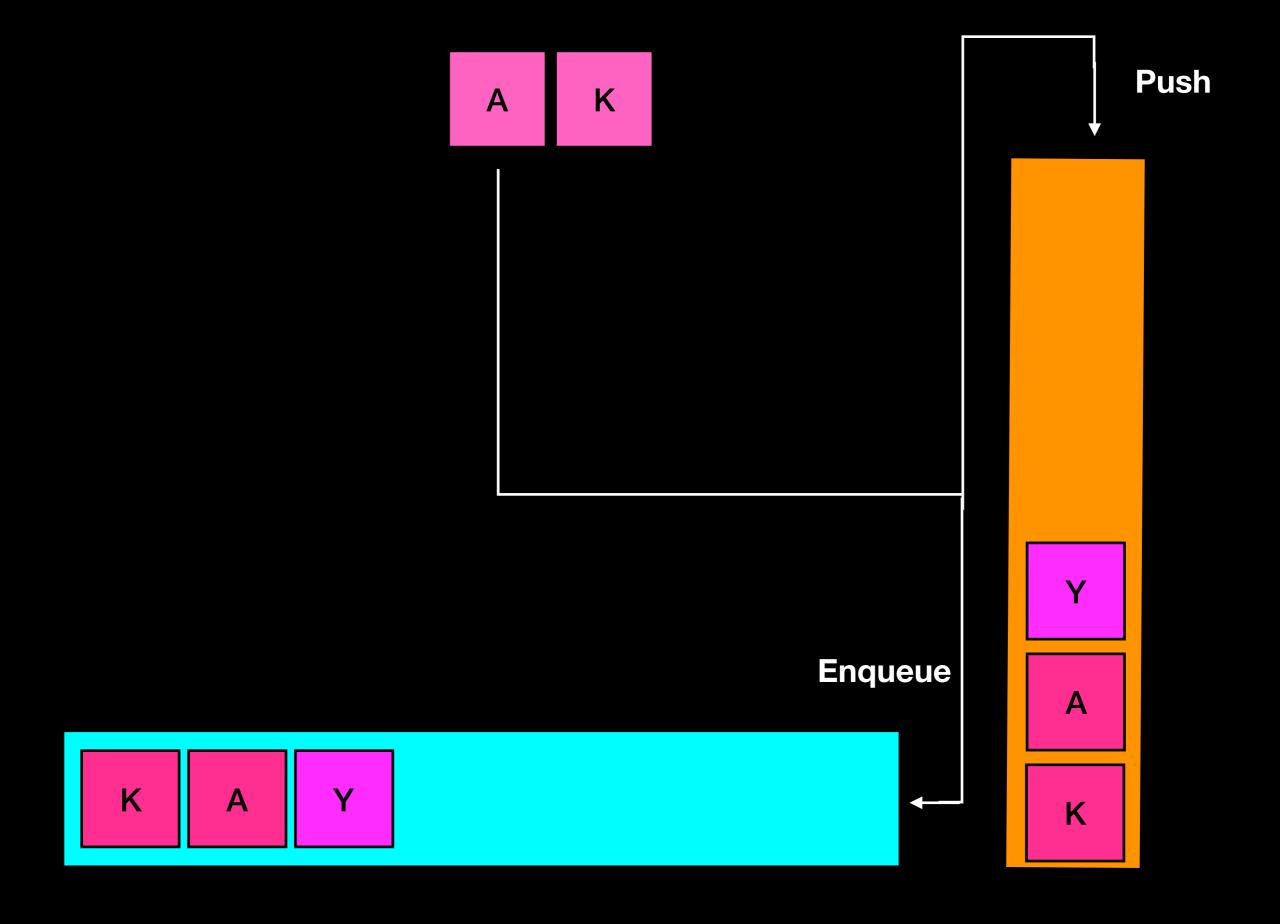
A queue can be used to preserve the original order of a string (FIFO)

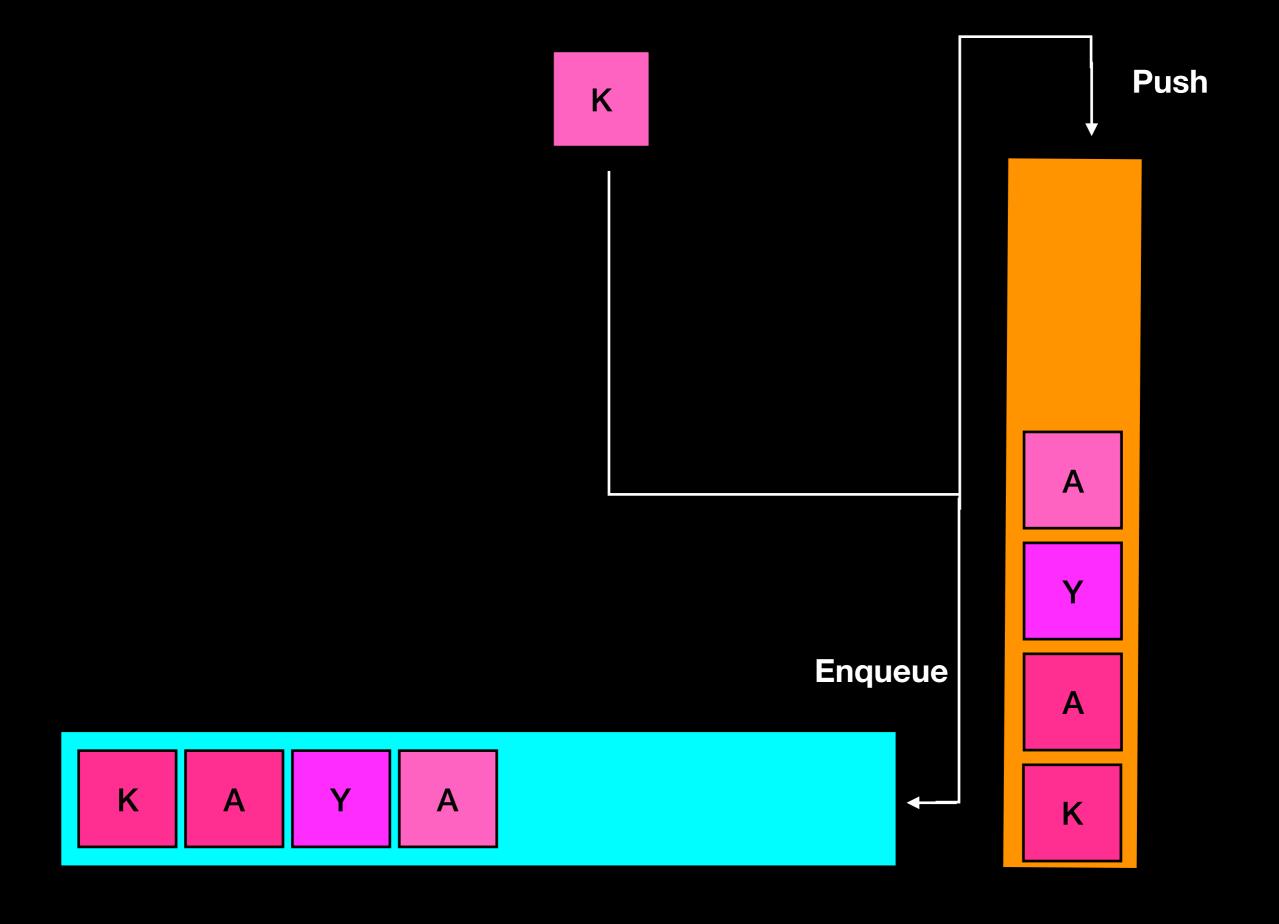
Algorithm: add incoming characters to both stack and queue and then compare to check if they are the same (palindrome!)

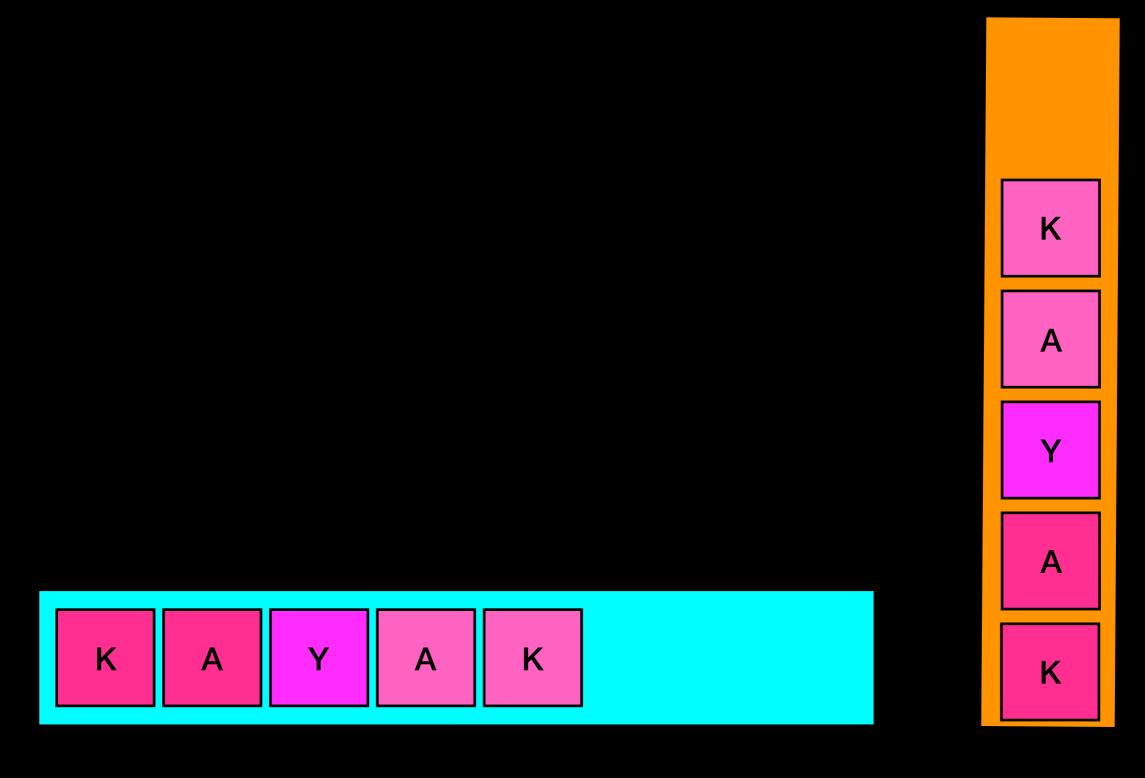


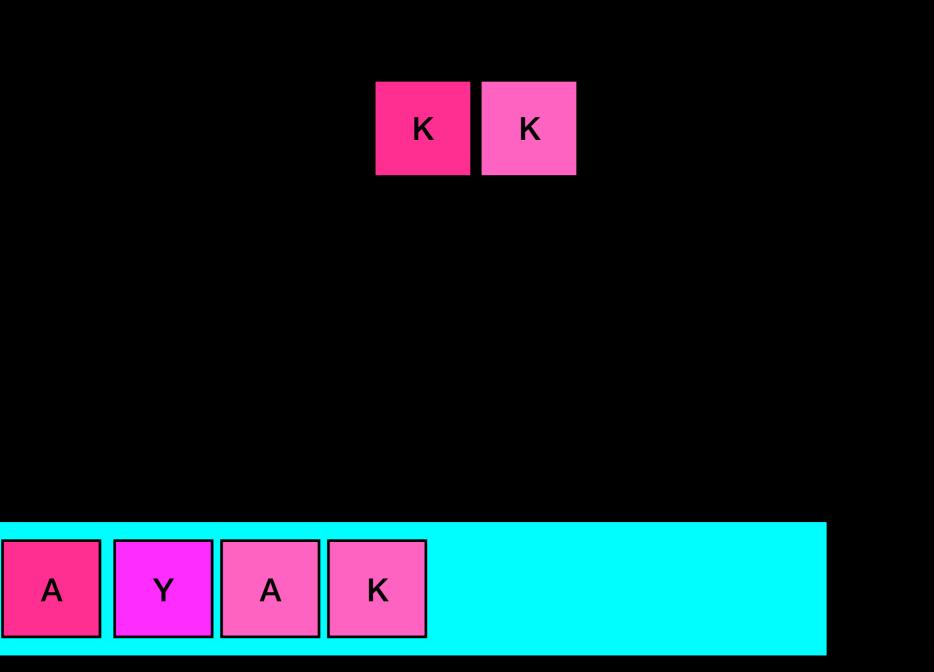


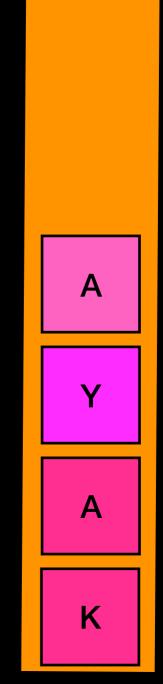


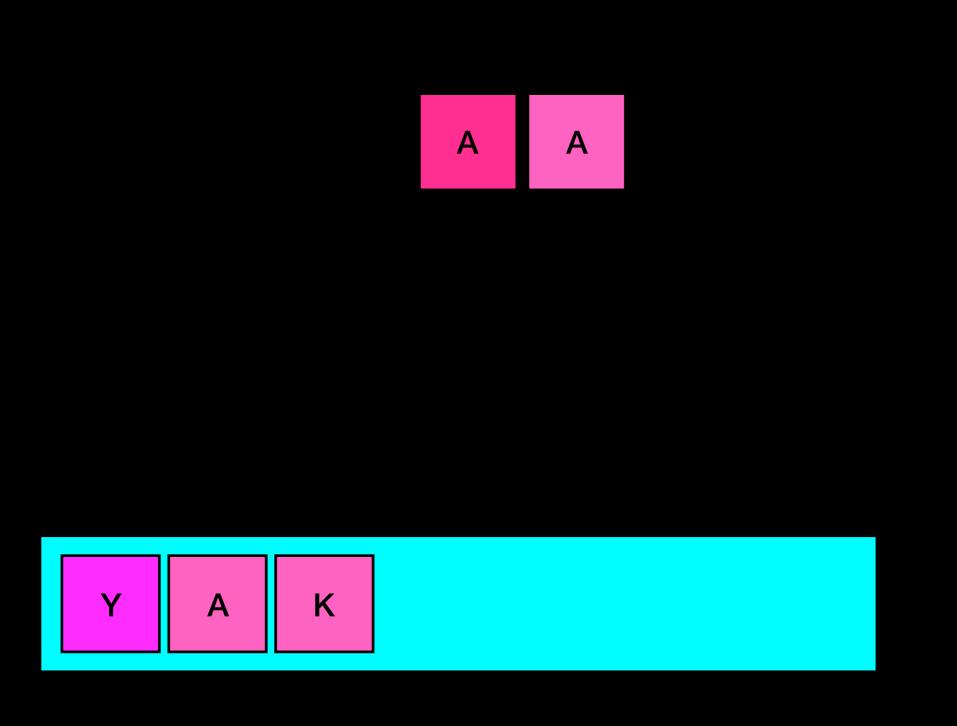


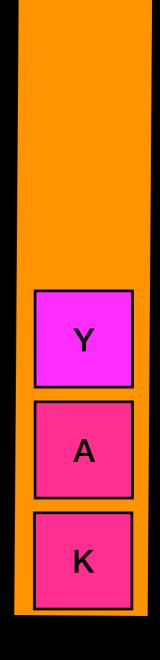


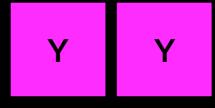




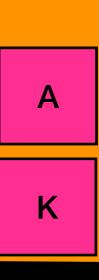








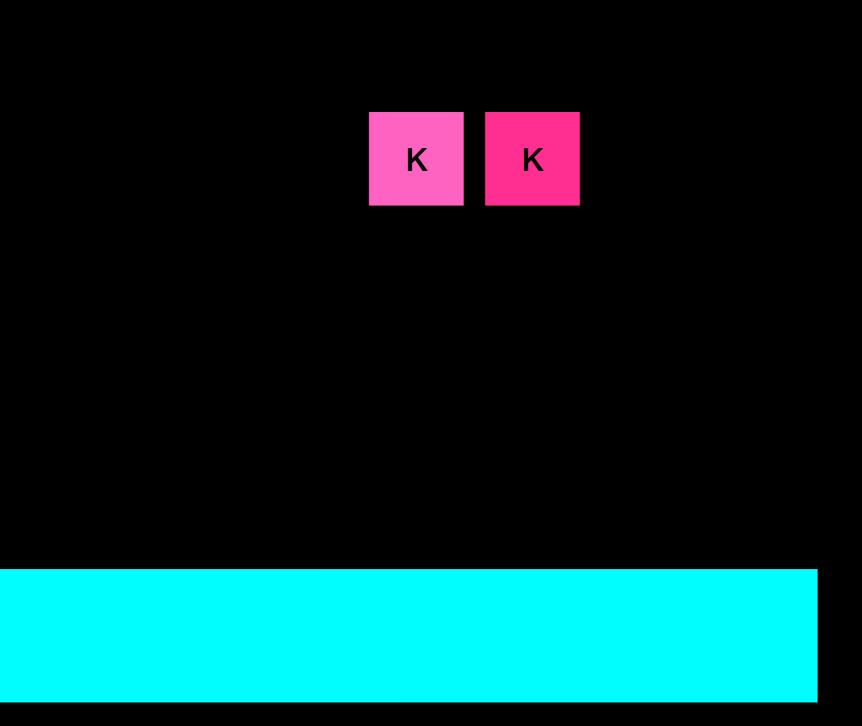
A K

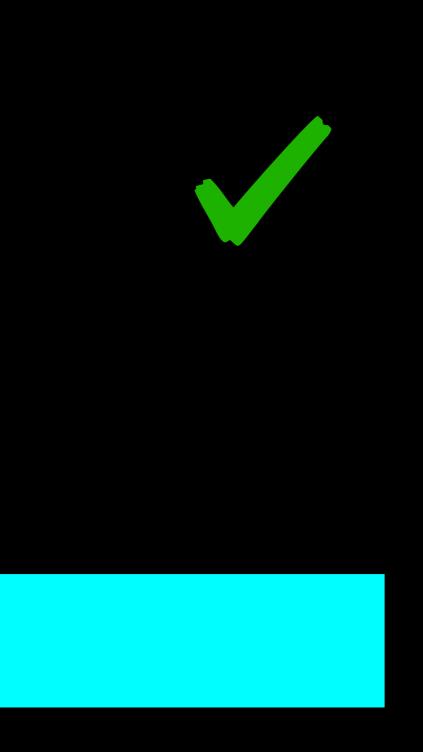


A

K

K





```
bool isPalidrome()
   while(there are incoming characters)
        add character to both stack and queue
    caractersAreEqual = true
   while(queue is not empty and charactersAreEqual)
   {
        if(queue front() == stack top()){
            queue.dequeue()
            stack.pop()
        else
            charactersAreEqual = false
    }
    return charactersAreEqual
```

Analyze the worst-case time complexity of this algorithm T(n) = ?

```
O(?)
bool isPalidrome()
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           queue.dequeue()
            stack.pop()
        }
        else
            charactersAreEqual = false
    }
    return charactersAreEqual
            T(n) = K_1n + K_2n + K_3
```

Double ended queue (deque)

Can add and remove to/from front and back

Double ended queue (deque)

Can add and remove to/from front and back

Double ended queue (deque)

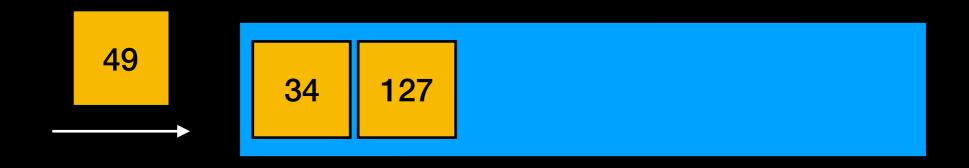
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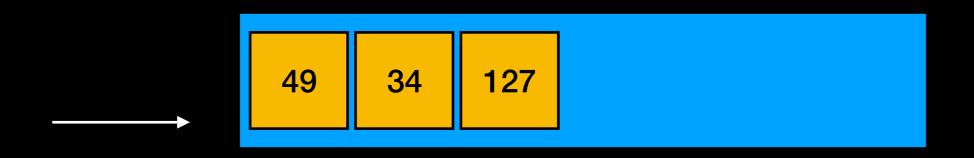
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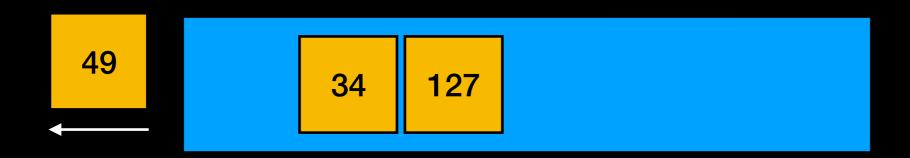
Double ended queue (deque)

Can add and remove to/from front and back



Double ended queue (deque)

Can add and remove to/from front and back



Double ended queue (deque)

Can add and remove to/from front and back

Double ended queue (deque)

Can add and remove to/from front and back

Low Priority
High Priority

A queue of items "sorted" by priority

Low Priority
High Priority

Low Priority

High Priority

Low Priority

High Priority

A queue of items "sorted" by priority

If value indicates priority, it amounts to a sorted list that accesses/removes the "highest" items first

Orders elements by priority => removing an element will return the element with highest priority value

Elements with same priority kept in queue order (in some implementations)