Stack Implementations

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Today's Plan



Recap

Stack Implementations:

Array

Vector

Linked Chain

Announcements

Stack ADT

```
#ifndef STACK H
#define STACK H
template<class T>
class Stack
public:
    Stack();
    void push(const T& new entry); // adds an element to top of stack
    void pop(); // removes element from top of stack
    T top() const; // returns a copy of element at top of stack
    int size() const; // returns the number of elements in the stack
    bool isEmpty() const; // returns true if no elements on stack false otherwise
private:
          //implementation details here
     //end Stack
};
#include "Stack.cpp"
```

#endif // STACK H `

Choose a Data Structure

Array?

Vector?

Linked chain?

Choose a Data Structure

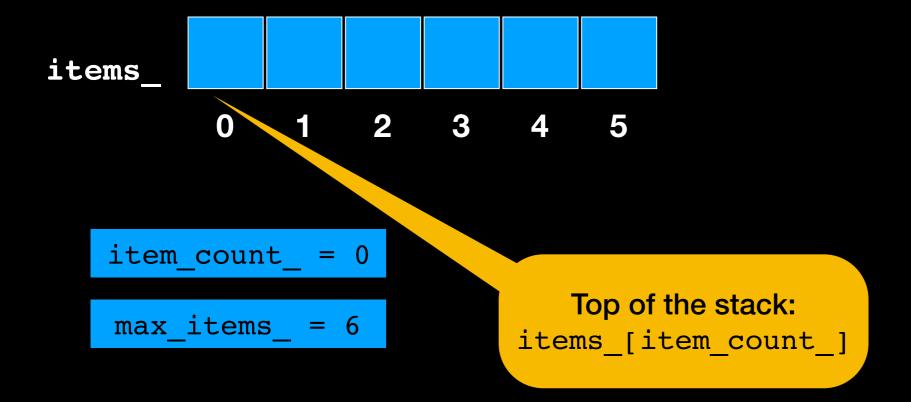
Inserting and removing from same end (LIFO)

Goal: minimize work - Ideally O(1)

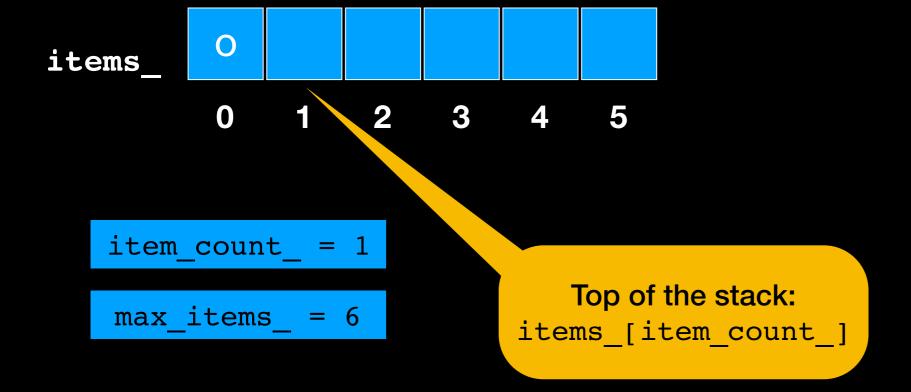
What would you suggest?



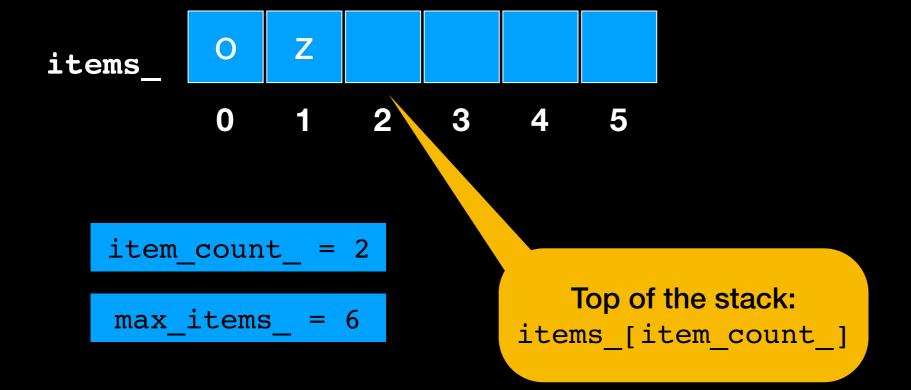
Where is the top of the stack?



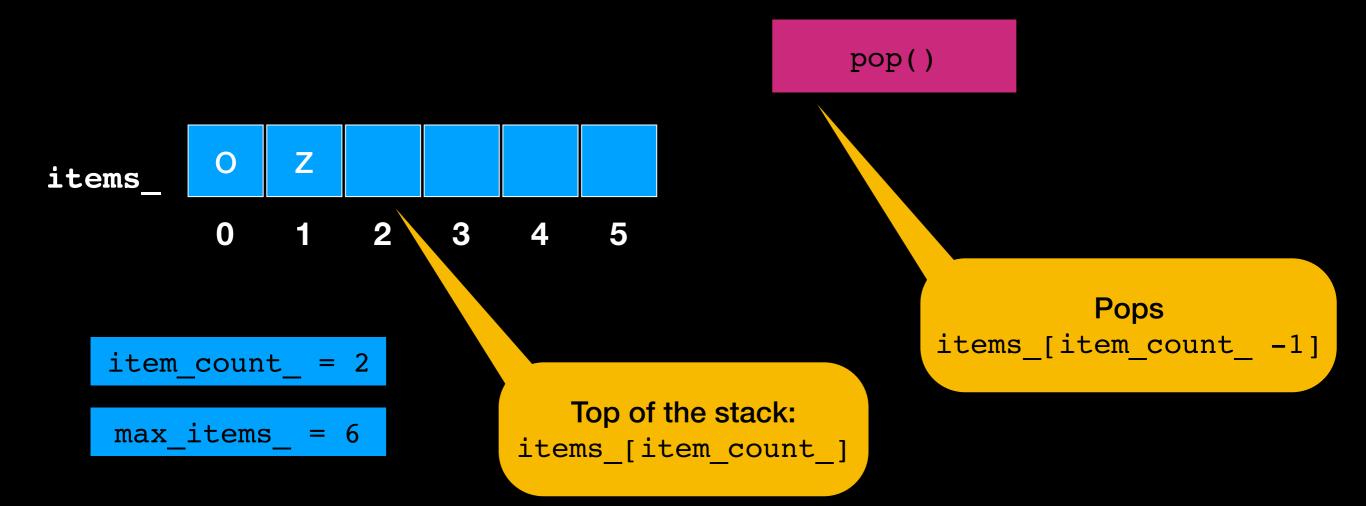
push('0')



push('Z')



push('B')



Array Analysis

```
1 assignment + 1 increment/decrement = O(1)
```

```
size : O(1)
isEmpty: O(1)
push: O(1)
pop : O(1)
top : O(1)
```

GREAT!!!!

Array Analysis

```
1 assignment + 1 increment/decrement = O(1)
```

```
size: O(1)
isEmpty: O(1)
push: O(1)
pop: O(1)
top: O(1)
```

GREAT???

Tilay

push('T')





Sorry Stack is Full!!!

```
item_count_ = 6
```

Top of the stack: items_[item_count_]

```
std::vector<T> some_vector;
```

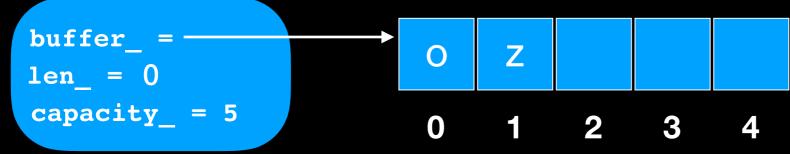
So what is a vector really?

```
std::vector<T> some_vector;
```

So what is a vector really?

Push and pop same as with arrays

Vector (simplified)



```
std::vector<T> some_vector;
```

So what is a vector really?

Stack is Full?

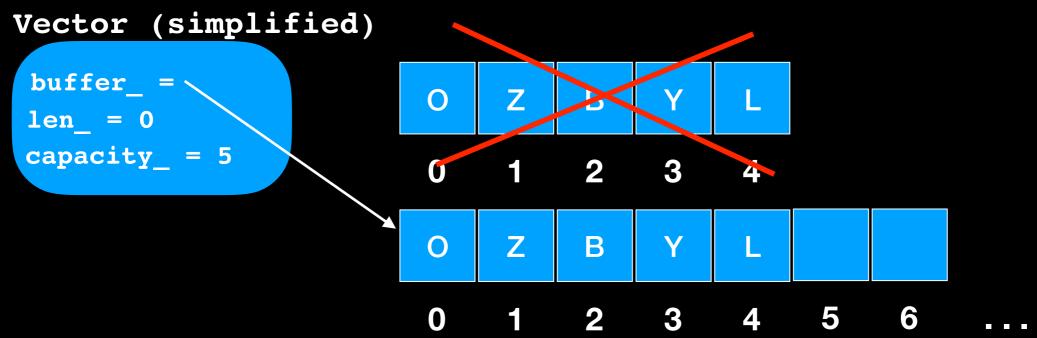
Vector (simplified)

```
std::vector<T> some_vector;
```

So what is a vector really?



No, I'll Grow!!!



Lecture Activity

How much should it grow?

Write a short paragraph arguing the pros and cons of growing by the amount you propose

Vector Analysis

```
1 assignment + 1 increment/decrement = O(1)
```

```
size : O(1)
isEmpty: O(1)
push: O(1)
pop : O(1)
top : O(1)
```

GREAT!!!!

Vector Analysis

```
1 assignment + 1 increment/decrement = O(1)
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```
size : O(1)
isEmpty: O(1)
push: O(1)
pop : O(1)
top : O(1)
```

GREAT???

Except when stack is full must:

- allocate new array
- copy elements in new array
- delete old array

Vector Analysis

```
1 assignment + 1 increment/decrement = O(1)
size: O(1)
isEmpty: O(1)
push: O(1)
pop : O(1)
                 Except when stack is full must:
top: O(1)
                    - allocate new array O(1)
                    - copy elements in new array O(n)
GREAT???
                    - delete old array O(1)
```

How should Vector grow?

Sometimes 1 "step"

Sometimes n "steps"

Consider behavior over several pushes

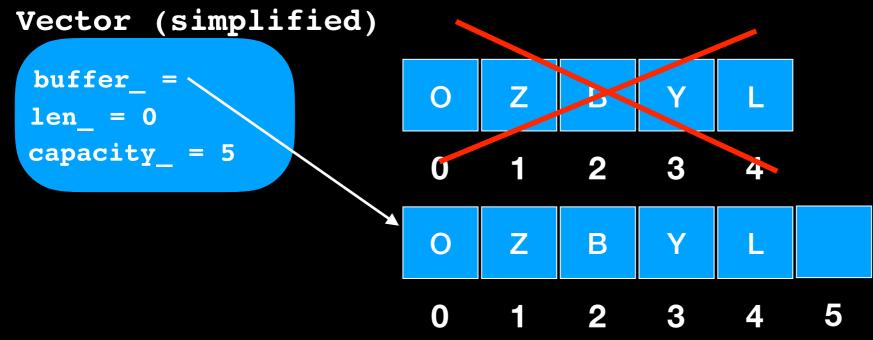
Vector Growth: a naive approach

```
std::vector<T> some_vector;
```

So what is a vector really?



I'll Grow!!!
I will add space for the item to be added



Vector Growth: a naive approach

If vector grows by 1 each time, every push costs n "steps"

```
Cost of pushes:

1 + 2 + 3 + 4 + 5 + ... + n

= n (n+1)/2
```

Vector Growth: a naive approach

If vector grows by 1 each time, every push costs n "steps"

Cost of n pushes:

```
1 + 2 + 3 + 4 + 5 + ... + n
= n (n+1)/2
= n^2/2 + n/2 O(n^2)
```

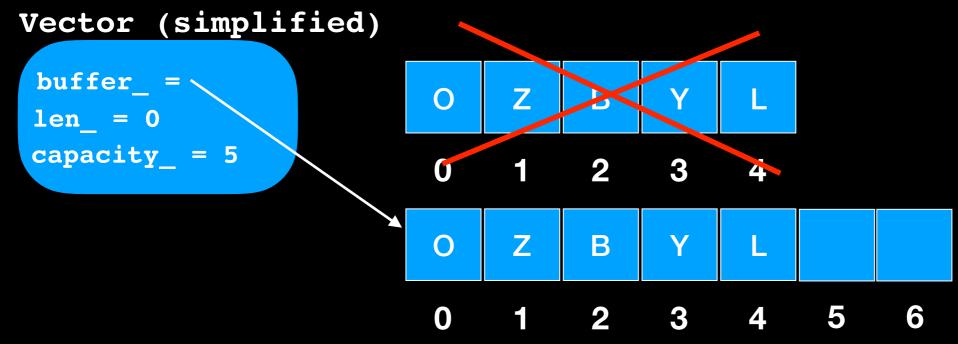
Vector Growth: a better approach

```
std::vector<T> some_vector;
```

So what is a vector really?



l'll Grow!!!
I will add two more slots!



Vector Growth: a better approach

If vector grows by 2 each time,

Let a "hard push" be one where the whole vector needs to be copied

When vector is not copied we have an "easy push"

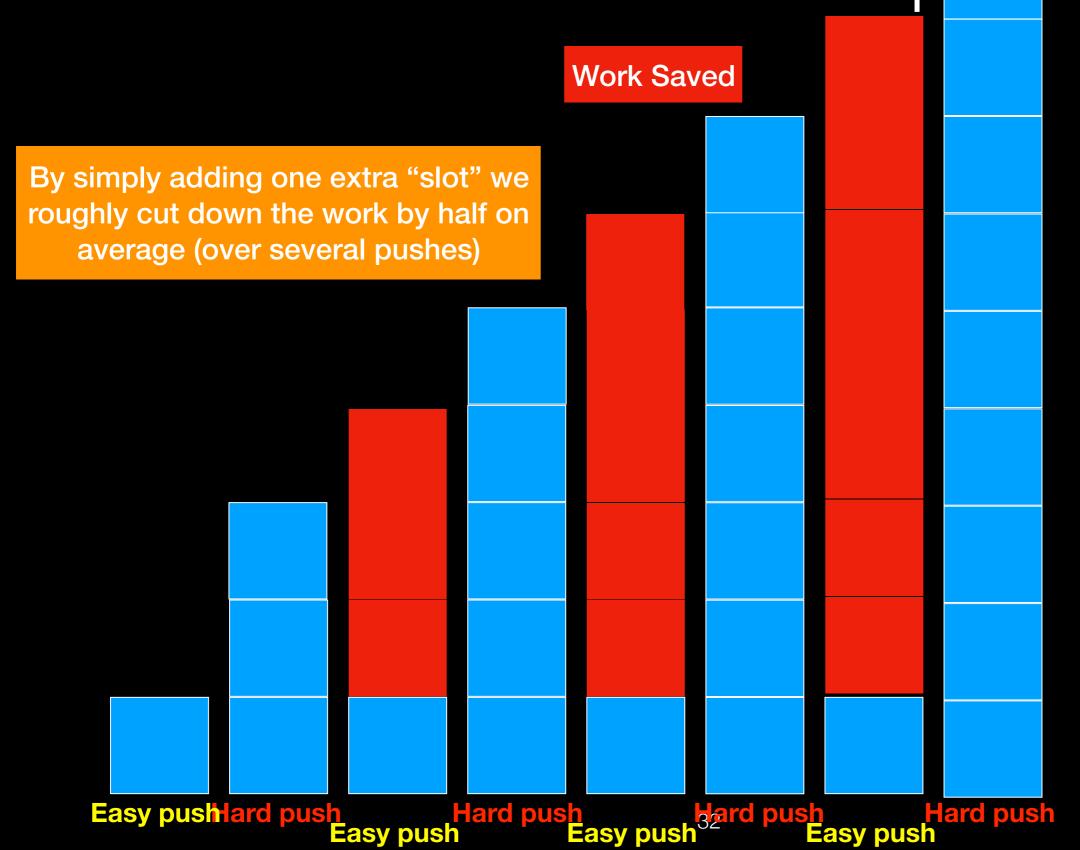
Now half our pushes will be easy (1 step) and half will be hard (n steps)

So if reconsider the work over several pushes?

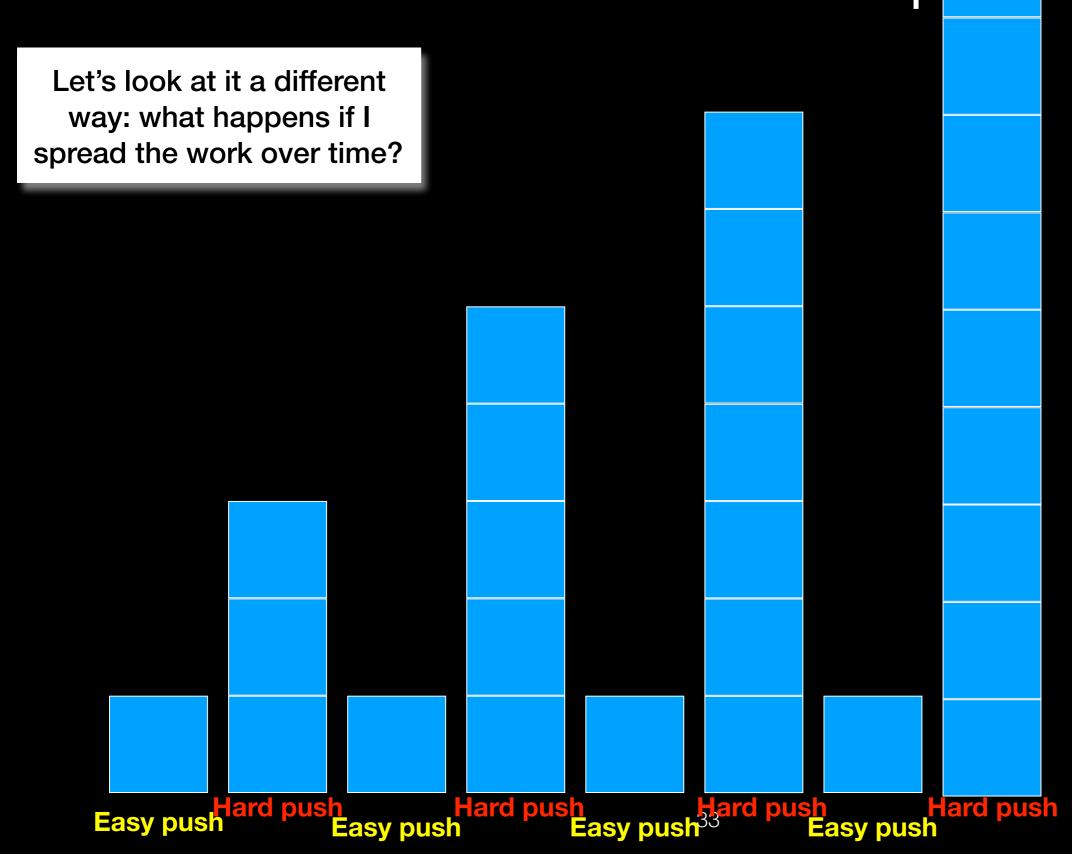
Analysis visualization adapted from Keith Schwarz

Vector Growth: a better ap bach Easy push Hard push Easy push Easy push Easy push Easy push

Vector Growth: a better appach



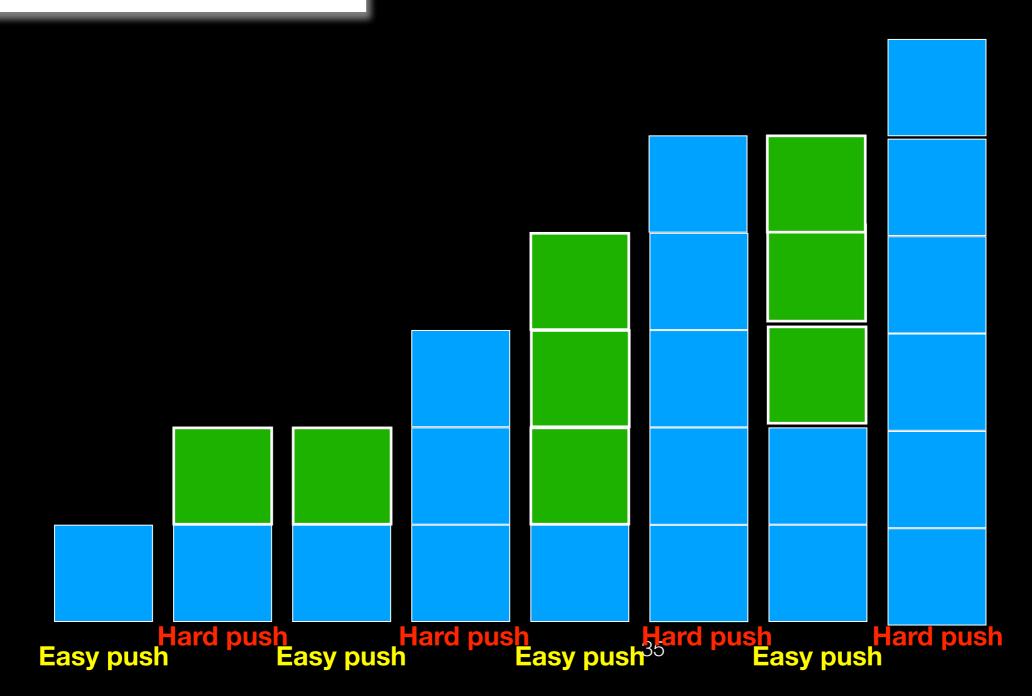
Vector Growth: a better appach



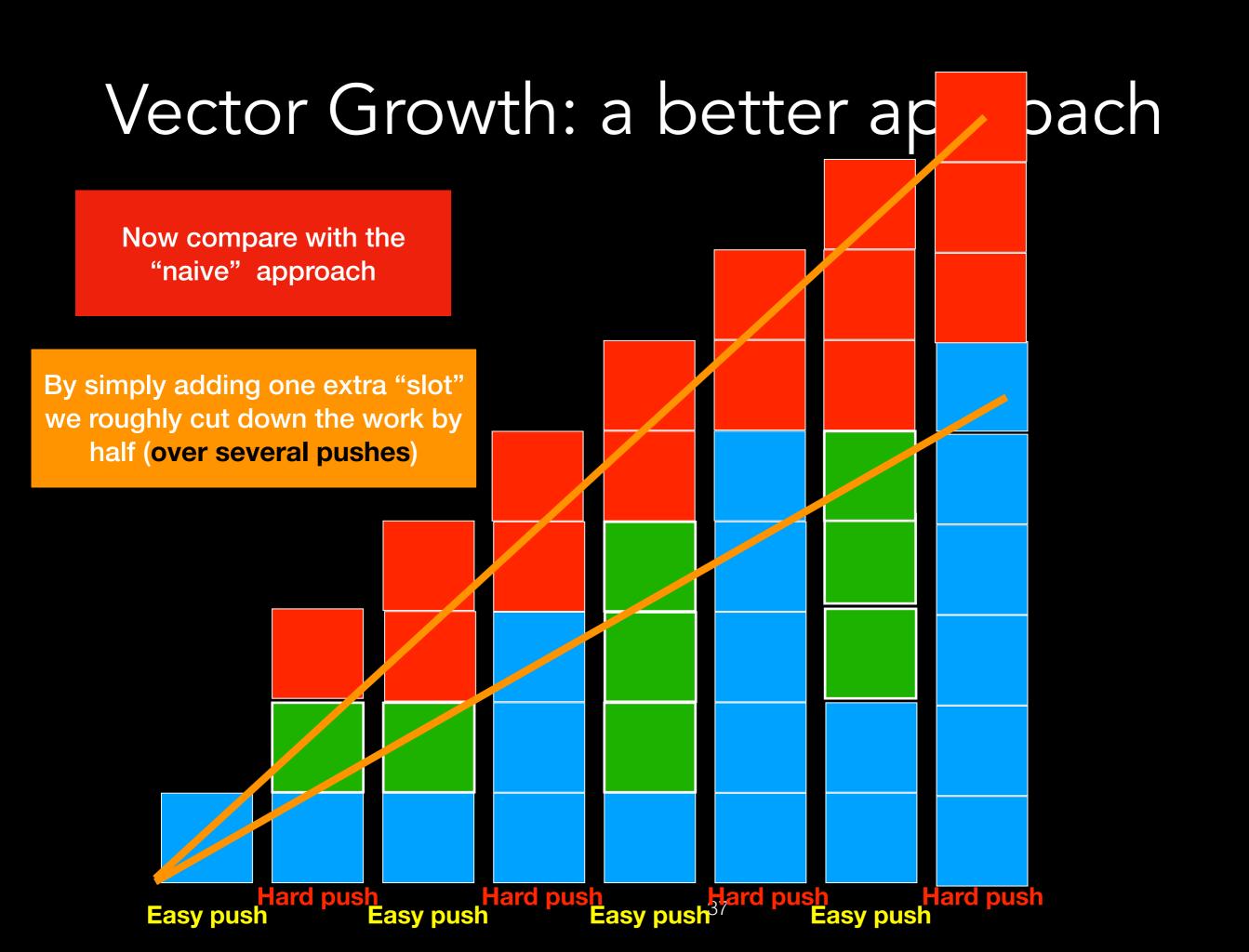
Vector Growth: a better ap bach Let's look at it a different way: what happens if I spread the work over time?

Vector Growth: a better approach

Let's look at it a different way: what happens if I spread the work over time?



Vector Growth: a better ap bach Now compare with the "naive" approach Hard push Easy push Easy push Easy push Easy push Easy push



Can we do better?

Vector Growth: a much better approach

std::vector<T> some vector;

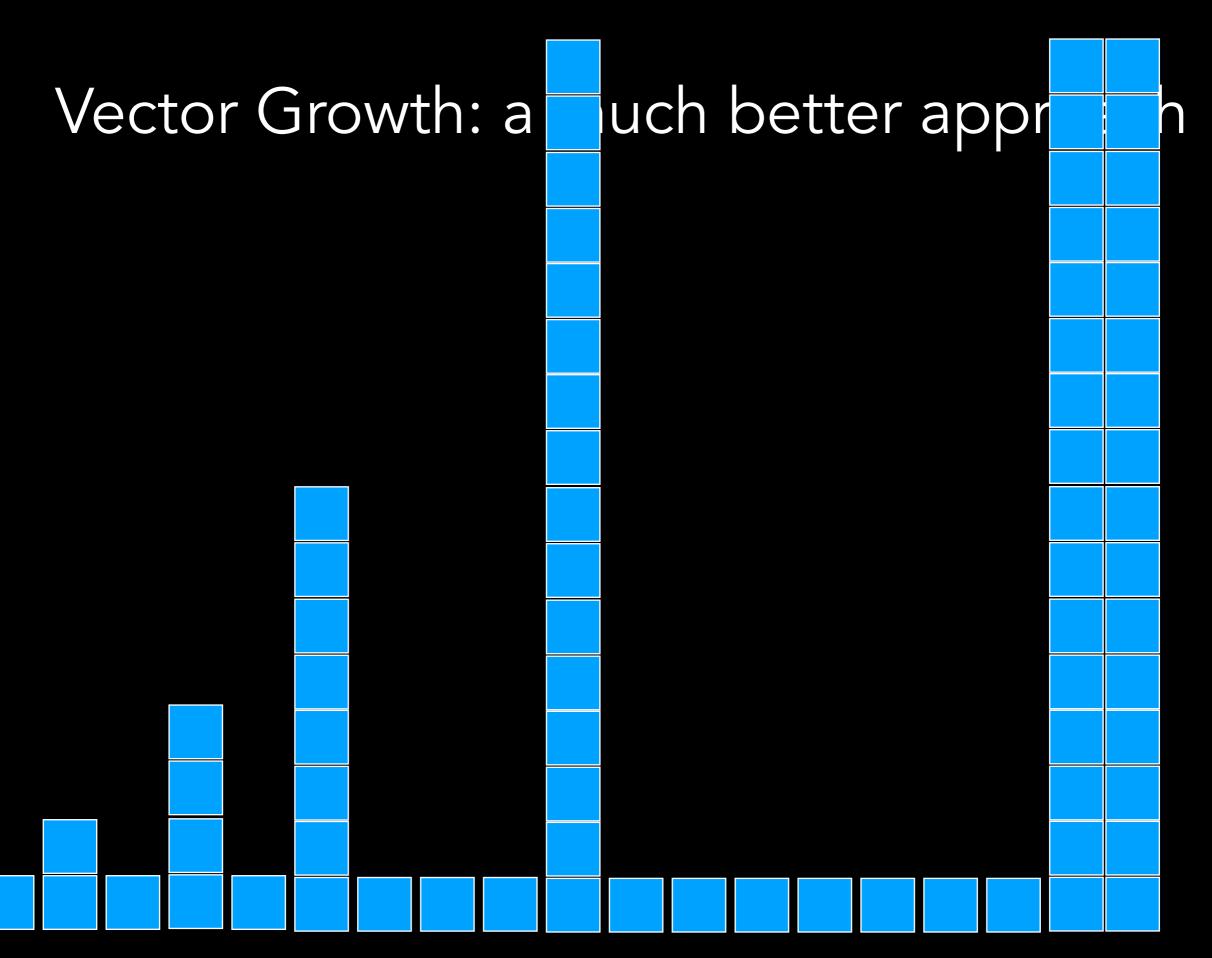
```
So what is a vector really?

Vector (simplified)

buffer = len = 0 capacity = 5

O Z B Y L

O Z B Y L
```



Vector Growth: a much better appr

Let's spread the work over time

Over time I can spread my work so that I have (OVER SEVERAL PUSHES) constant work

Vector Growth: a much better appr

Let's spread the work over time



Over time I can spread my work so that I have (OVER SEVERAL PUSHES) constant work

Vector Growth summarized

If it grows by 1, $O(n^2)$ over time (n pushes - AMORTIZED ANALYSIS)

If it grows by 2, push takes roughly half the "steps" but still O(n²) over time (n pushes - AMORTIZED ANALYSIS)

If it doubles its size, push takes O(1) over time (n pushes - AMORTIZED ANALYSIS)

A steadily shrinking Stack

Let's consider this application:

- Push the 524,288th (2¹⁹)element onto Stack which causes it to double it's size to 1,048,576 (2²⁰)
- Reading an input file
 - pop the elements that match
 - manipulate input record accordingly
 - repeat

A steadily shrinking Stack

Let's consider this application:

- Push the 524,288th (2¹⁹)element onto Stack which causes it to double it's size to 1,048,576 (2²⁰)
- Reading an input file
 - pop the elements that match
 - manipulate input record accordingly
 - repeat

How much I pop will depend on input

A steadily shrinking Stack

Let's consider this application:

Assume a few matches at each iteration -> mostly empty stack but it will be around for a long time!

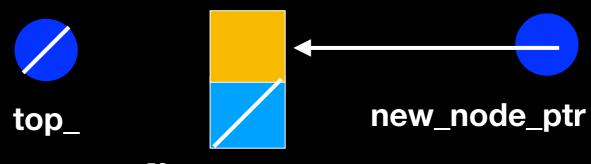
- Push the 524,288th (2¹⁹)element or to Stack which causes it to double it's size to 1,048,576 (2²⁰)
- Reading an input file
 - pop the elements that match
 - manipulate input record accordingly
 - repeat

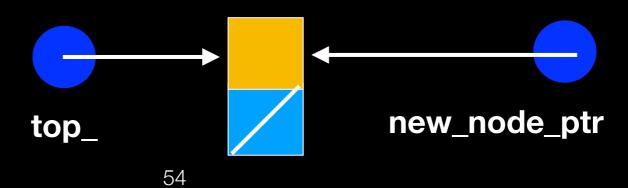


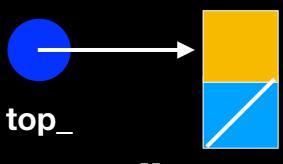
I will not shrink!



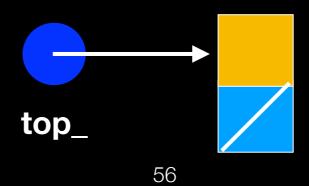


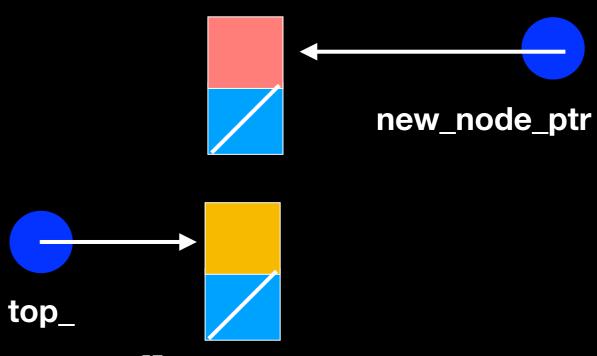


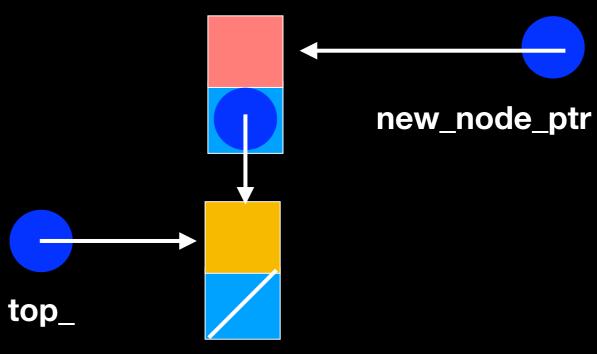


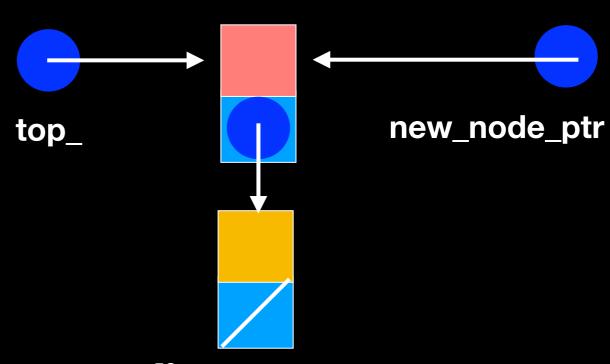


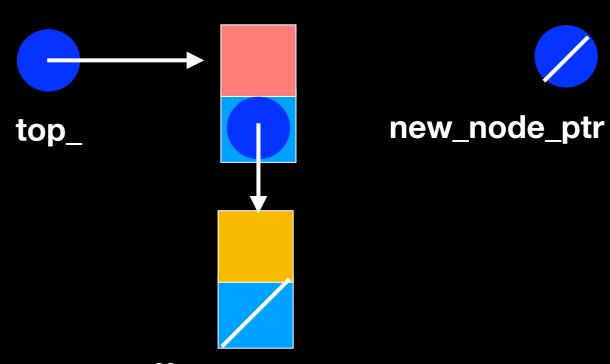


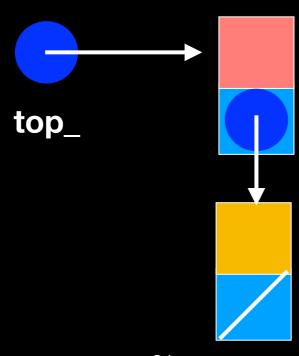


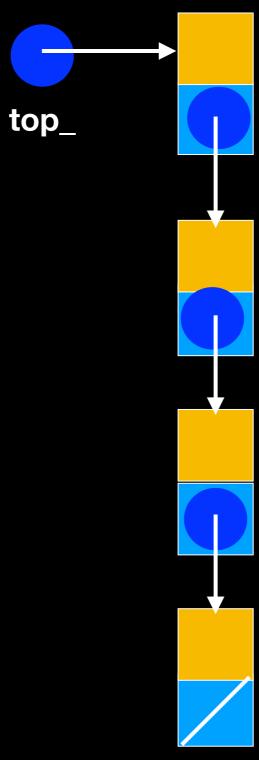








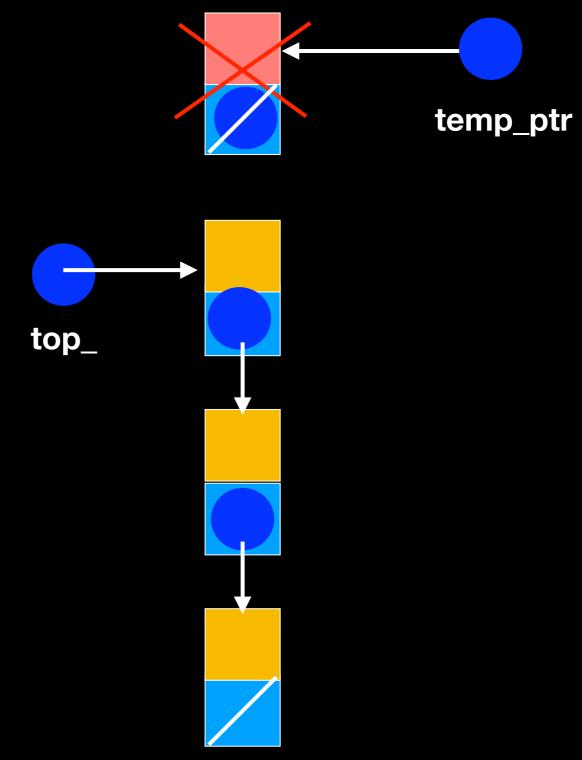




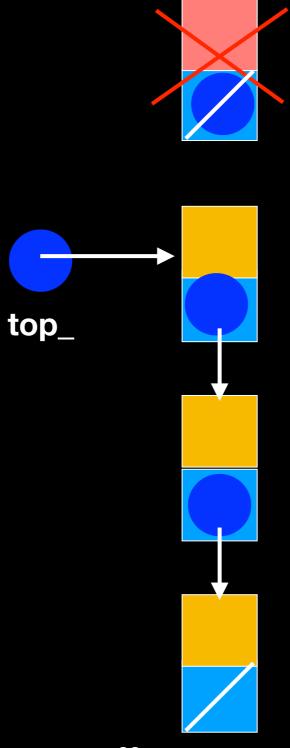
pop top_ temp_ptr

pop temp_ptr top_

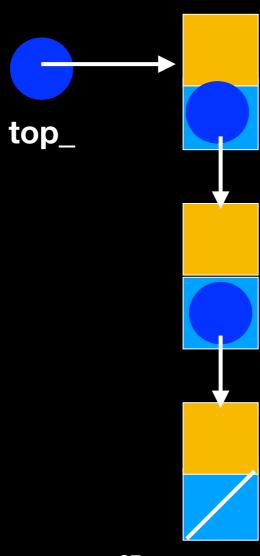
pop



pop







Linked-Chain Analysis

```
1 assignment + 1 increment/decrement = O(1)
```

```
size : O(1)
isEmpty: O(1)
push: O(1)
pop : O(1)
top : O(1)
```

GREAT!!!! And there is no "Except" case here, every operation is O(1)!

To summarize

Array: O(1) for push and pop, but size is bounded

Vector: size is unbounded but

-Some push operations take O(1), others take

 $O(n) \rightarrow O(1)$ over time (AMORTIZED ANALYSIS)

Linked-Chain: O(1) for push and pop and size is unbounded

Implement Stack ADT

```
#ifndef STACK H
#define STACK H
template<class T>
class Stack
public:
   Stack();
   ~Stack(); // destructor
   Stack(const Stack<T>& a stack); //copy constructor
   void push(const T& newEntry); // adds an element to top of stack
   void pop(); // removes element from top of stack
   T top() const; // returns a copy of element at top of stack
   int size() const; // returns the number of elements in the stack
   bool isEmpty() const; // returns true if no elements on stack false otherwise
private:
   Node<T>* top ; // Pointer to top of stack
   //end Stack
#include "Stack.cpp"
#endif // STACK H
```

Problem!

What happens if we call top() on empty stack???

```
T Stack<T>::top() const

if(isEmpty())
    //what do we return???
else
    return top_->getItem();
}
```

Fix!

What happens if we call top() on empty stack???

```
T Stack<T>::top() const
{
    if(isEmpty())
        throw (std::out_of_range("top() called on empty stack"));
    else
        return top_->getItem();
}
```