# Tree Implementation

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# Today's Plan



Recap

**BST Implementation** 

### Announcements

Last lecture Mock Final Exam

If you take it you must stay for the duration of the exam

```
#ifndef BST H
#define BST H
#include <memory>
template<class T>
class BST
public:
    BST(); // constructor
    BST(const BST<T>& tree); // copy constructor
    ~ BST(); // destructor
    bool isEmpty() const;
    size t getHeight() const;
    size t getNumberOfNodes() const;
    void add(const T& new item);
    void remove(const T& new item);
    T find(const T& item) const;
    void clear();
    void preorderTraverse(Visitor<T>& visit) const;
    void inorderTraverse(Visitor<T>& visit) const;
    void postorderTraverse(Visitor<T>& visit) const;
    BST& operator= (const BST<T>& rhs);
private:
    std::shared ptr<BinaryNode<T>> root ptr ;
}; // end BST
#include "BST.cpp"
#endif // BST H
```

We will talk about this at the end of this lecture

Let's try something new and use shared\_ptr:
A bit of extra syntax at declaration but then you use them as regular pointers with less cleaning up

To implement this as a linked structure what do we need to change in our previous implementation ???

# BinaryNode



```
#ifndef BinaryNode H
                                 For shared ptr
#define BinaryNode_H_
#include <memory> _
template<class T>
class BinaryNode
public:
  BinaryNode();
  BinaryNode(const T& an item);
  void setItem(const T& an item);
  T getItem() const;
  bool isLeaf() const;
   auto getLeftChildPtr() const;
   auto getRightChildPtr() const;
  void setLeftChildPtr(std::shared ptr<BinaryNode<T>> left ptr);
  void setRightChildPtr(std::shared ptr<BinaryNode<T>> right ptr);
private:
  T item_; // Data portion
   std::shared ptr<BinaryNode<T>> left; // Pointer to left child
   std::shared ptr<BinaryNode<T>> right; // Pointer to right child
}; // end BST
#include "BinaryNode.cpp"
#endif // BinaryNode H
```

# Lecture Activity

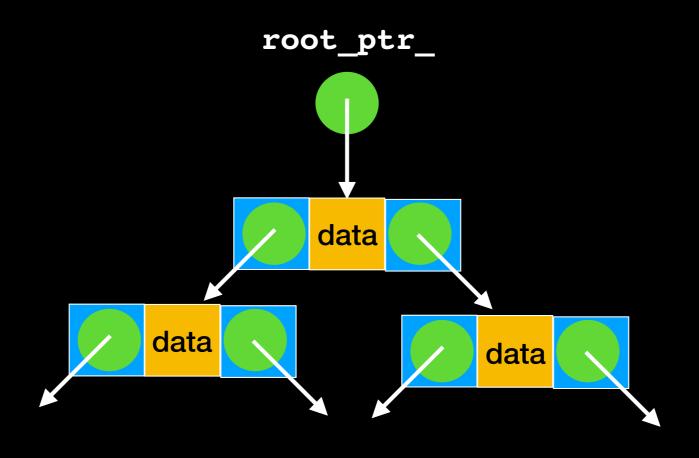
#### Implement:

```
BinaryNode(const T& an_item);
bool isLeaf() const;

void setLeftChildPtr(std::shared_ptr<BinaryNode<T>> left_ptr);
```

```
template<class T>
BinaryNode<T>::BinaryNode(const T& an_item)
      : item_(an_item), left_(nullptr), right_(nullptr)
{ } // end constructor
template<class T>
bool BinaryNode<T>::isLeaf() const
  return ((left_ == nullptr) && (right_ == nullptr));
} // end isLeaf
template<class T>
void BinaryNode<T>::setLeftChildPtr(std::shared_ptr<BinaryNode<T>> left_ptr)
  left_ = left_ptr;
  // end setLeftChildPtr
```

# BST



```
#ifndef BST H
#define BST H
#include <memory>
template<class T>
class BST
public:
    BST(); // constructor
    BST(const BST<T>& tree); // copy constructor
    ~ BST(); // destructor
    bool isEmpty() const;
    size t getHeight() const;
    size t getNumberOfNodes() const;
    void add(const T& new item);
    void remove(const T& new item);
    T find(const T& item) const;
    void clear();
    void preorderTraverse(Visitor<T>& visit) const;
    void inorderTraverse(Visitor<T>& visit) const;
    void postorderTraverse(Visitor<T>& visit) const;
    BST& operator= (const BST<T>& rhs);
private:
    std::shared ptr<BinaryNode<T>> root ptr ;
}; // end BST
#include "BST.cpp"
#endif // BST H
```

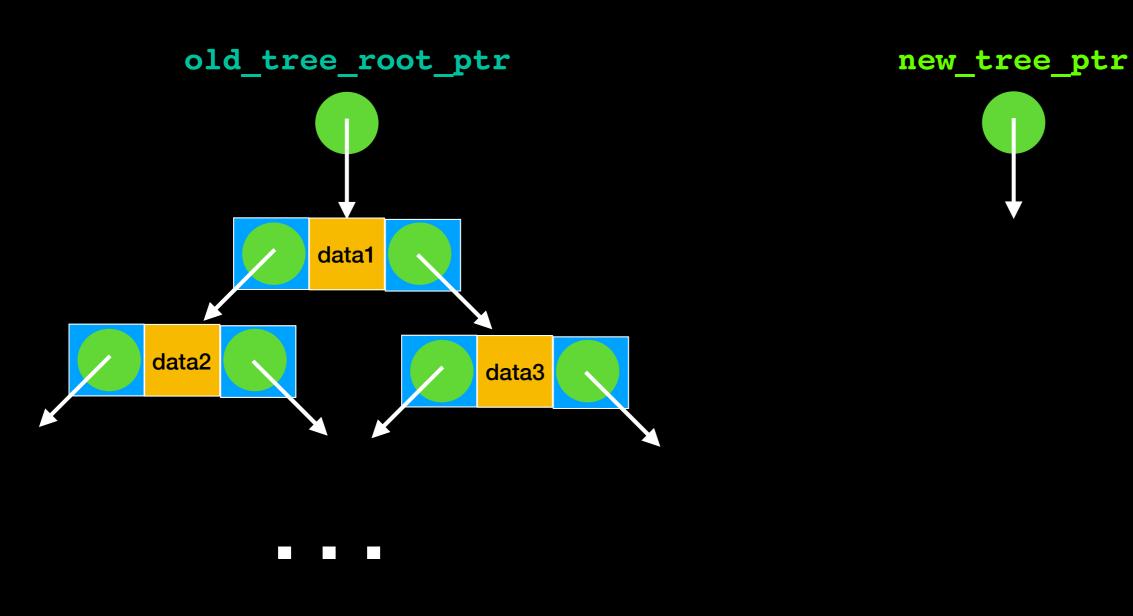
We want our interface to be generic and not tied to implementation. Many of these will therefore use helper functions, which should be private (or protected if you envision inheritance). I do not include them here in the interface for lack of space.

# Copy Constructor

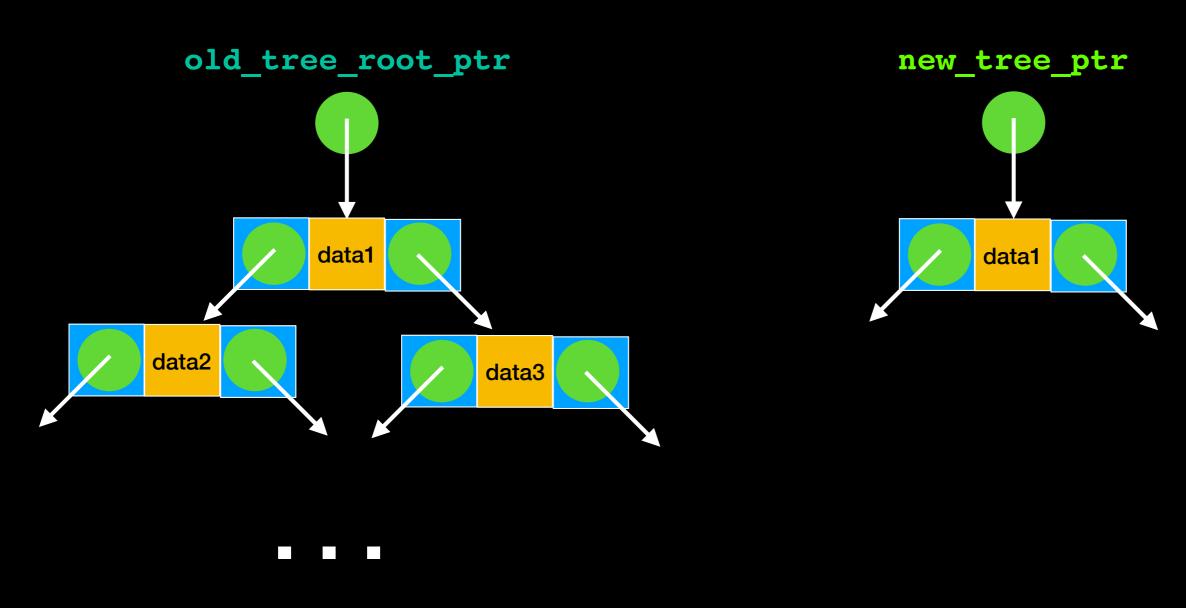
```
template<class T>
BST<T>::BST(const BST<T>& tree)
{
   root_ptr_ = copyTree(tree.root_ptr_); // Call helper function
} // end copy constructor
```

I can use the . operator to access a private member variable because it is s within the class definition.

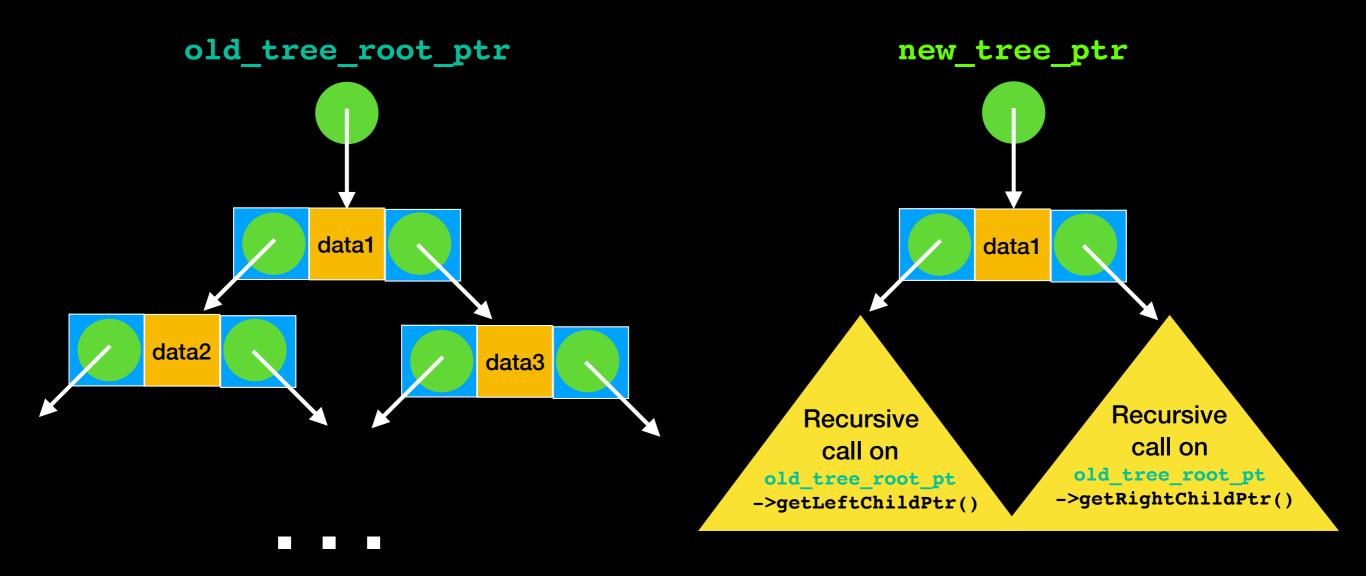
### copyTree(old\_tree\_root\_ptr)



### copyTree(old\_tree\_root\_ptr)



### copyTree(old\_tree\_root\_ptr)



Returning
shared\_ptr,
cleaner to use
auto return type:
-std=c++14

// end copyTree

# Copy Constructor Helper Function

```
template<class T>
auto BST<T>::copyTree(const std::shared ptr<BinaryNode<T>> old tree root ptr) const
                                                               Recall: this is the syntax
   std::shared ptr<BinaryNode<T>> new tree ptr;
                                                                for allocating a "new"
     Copy tree nodes during a preorder traversal
                                                               object with shared ptr
      (old tree root ptr != nullptr)
                                                                    pointing to it
      // Copy node
      new tree ptr = std::make shared<BinaryNode<T>>(old tree root ptr
                                                   ->getItem(), nullptr, nullptr);
     new tree ptr->setLeftChildPtr(copyTree(old tree root ptr->getLeftChildPtr()));
      new tree ptr->setRightChildPtr(copyTree(old tree root ptr
                                                             ->getRightChildPtr());
     // end if
                                Recursive Calls:
   return new tree ptr;
```

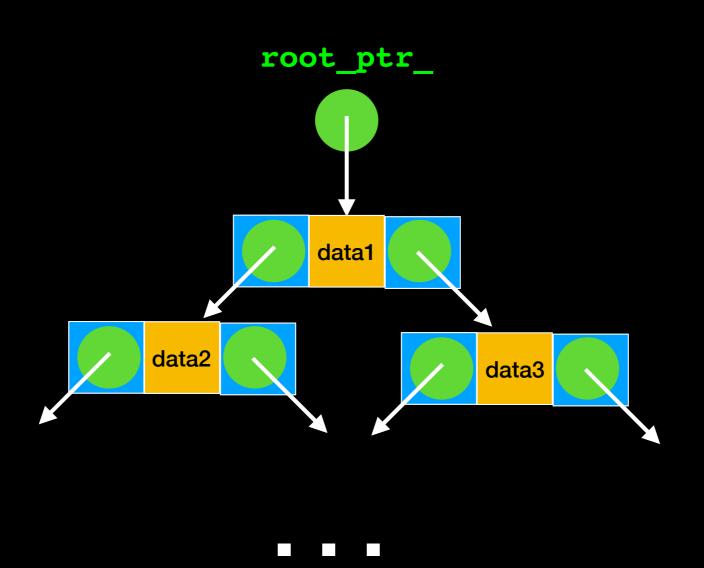
Don't want to tie interface to recursive implementation:

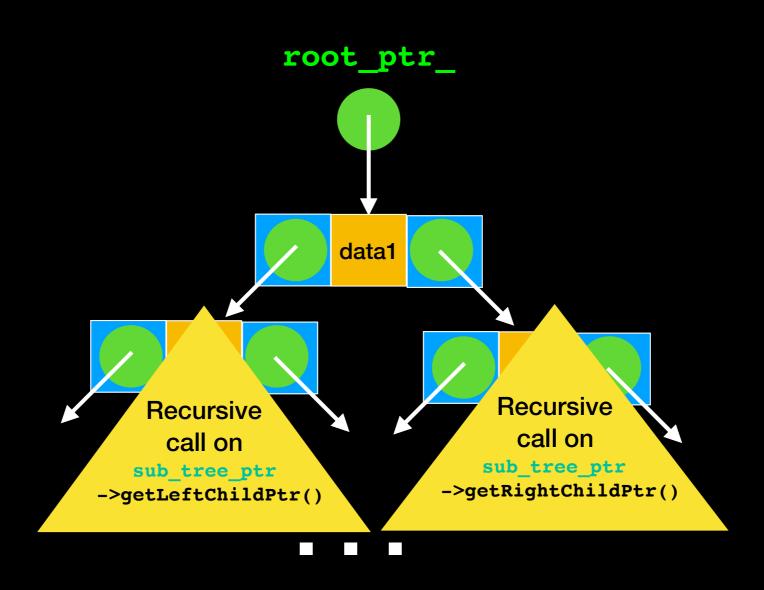
Use helper function

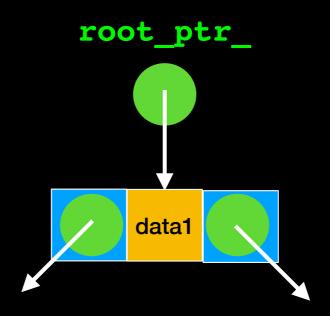
Preorder Traversal Scheme: copy each node as soon as it is visited to make exact copy

### Destructor

```
template < class T>
BST < T > :: ~ BST()
{
    destroyTree(root_ptr_); // Call helper function
} // end destructor
```







root\_ptr\_.reset()

root\_ptr\_

# Destructor Helper Function

Notice: all we have to do is set the shared\_ptr to nullptr with reset() and it will take care of deleting the node.

PostOrder Traversal Scheme:
Delete node only after deleting
both of its subtrees

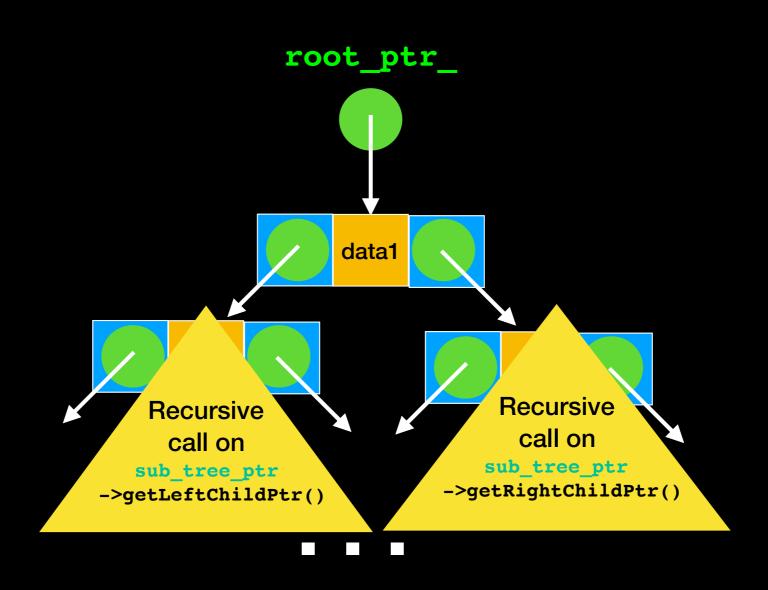
### clear

```
template < class T>
void BST < T > :: clear()
{
    destroyTree(root_ptr_); // Call helper method
} // end clear
```

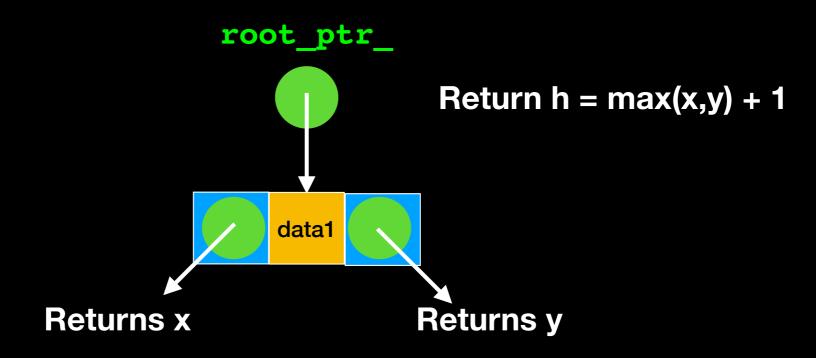
# getHeight

```
template < class T >
int BST < T > :: getHeight() const
{
    return getHeightHelper(root_ptr_);
} // end getHeight
```

## getHeightHelper(sub\_tree\_ptr)



### getHeightHelper(sub\_tree\_ptr)



### getHeightHelper(sub\_tree\_ptr)



#### Similarly: implement these at home!!!

```
int BinaryNodeTree<T>::getNumberOfNodes() const
{    //try it at home!!!!}
int BinaryNodeTree<T>::getNumberOfNodesHelper(std::shared_ptr
<BinaryNode<T>> sub_tree_ptr) {//try it at home!!!!}
```

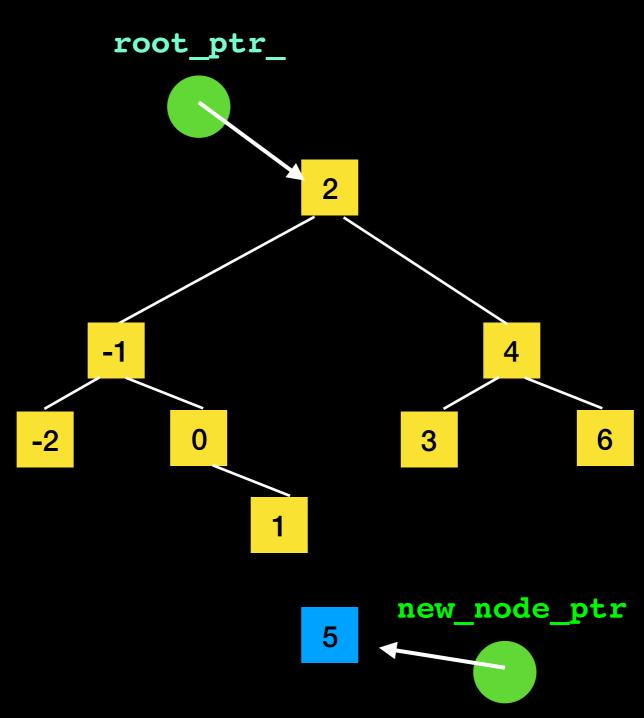
# add and remove

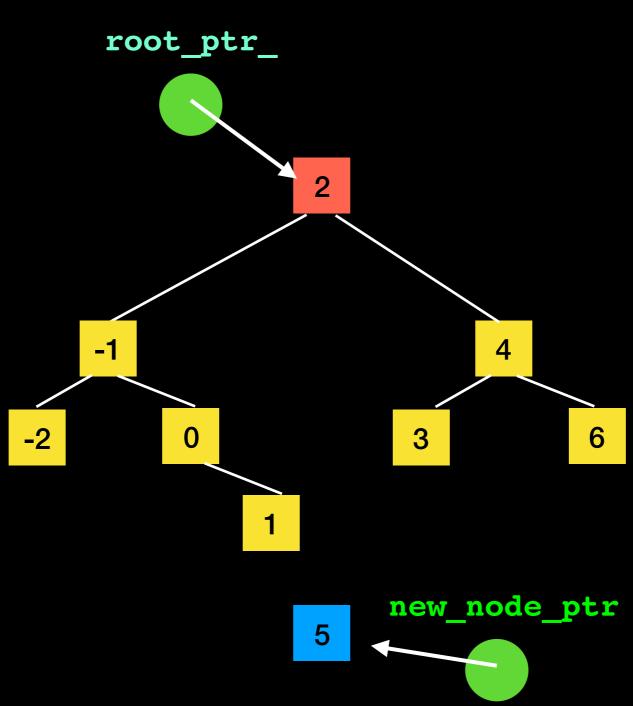
Key methods: determine order of data

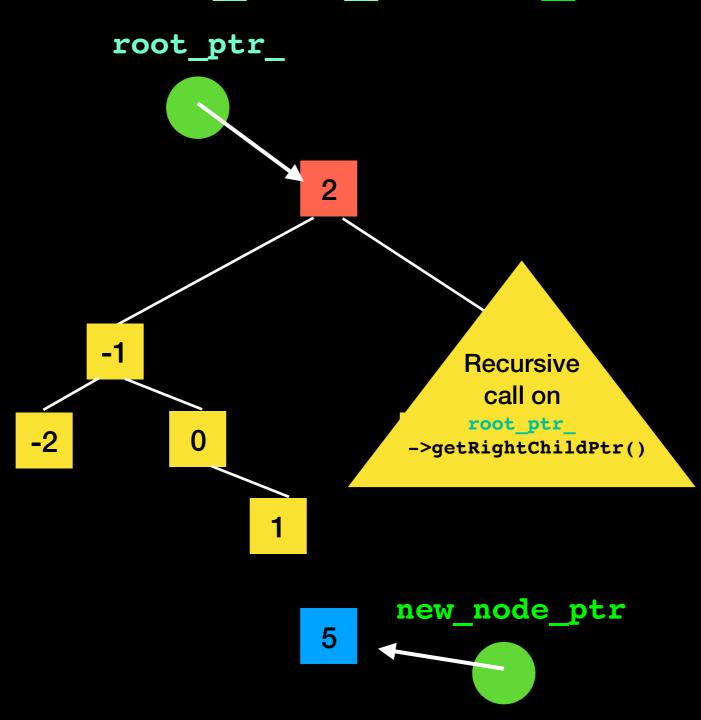
Distinguish between different types of Binary Trees

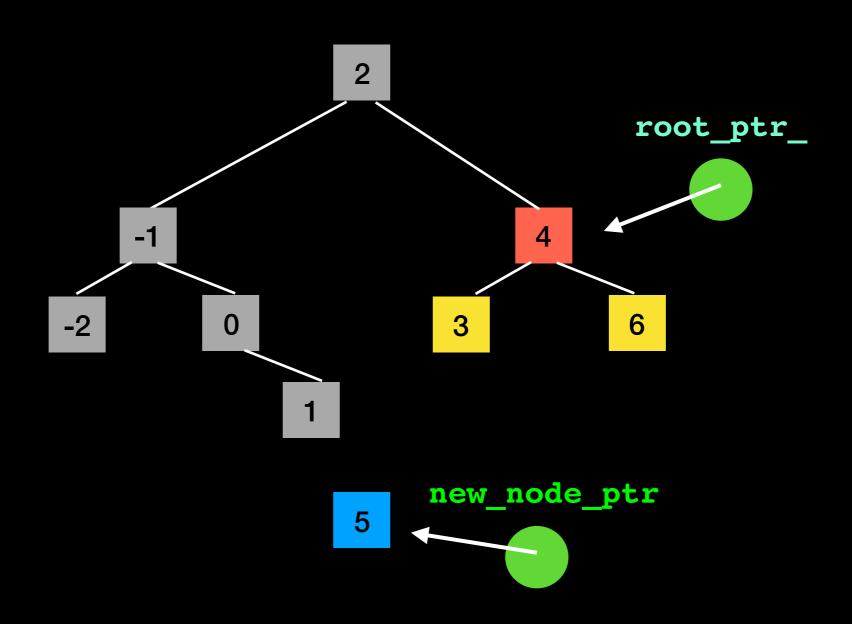
Implement the BST structural property

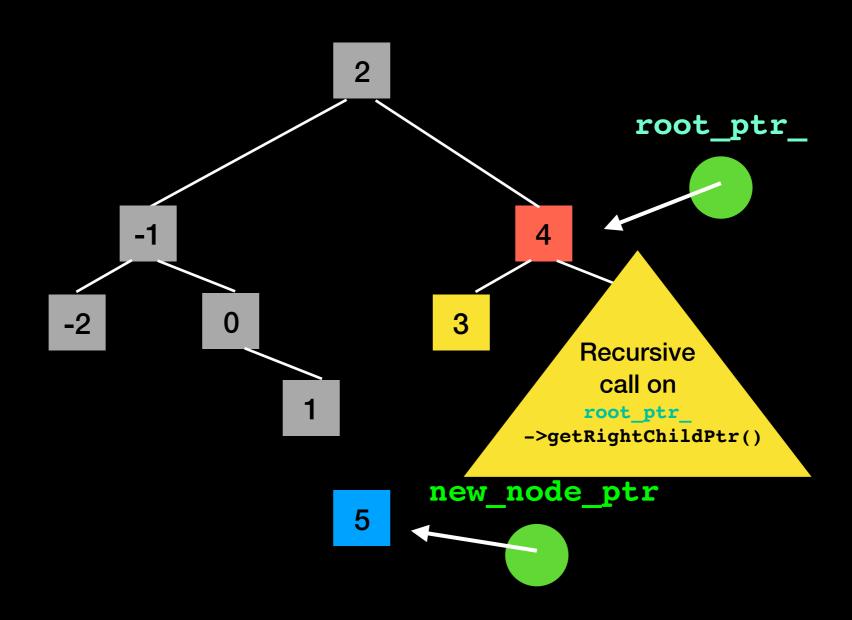
### add

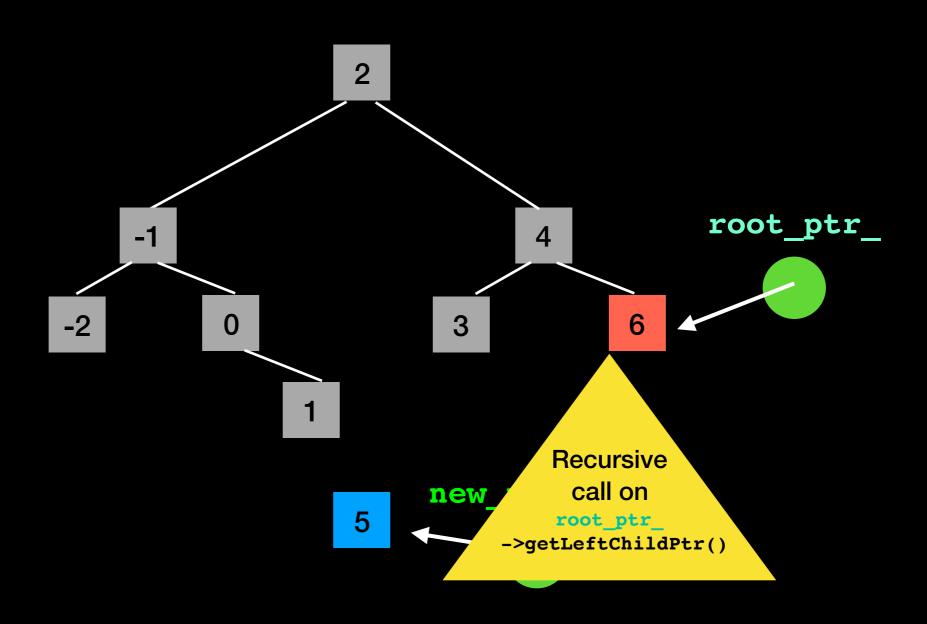




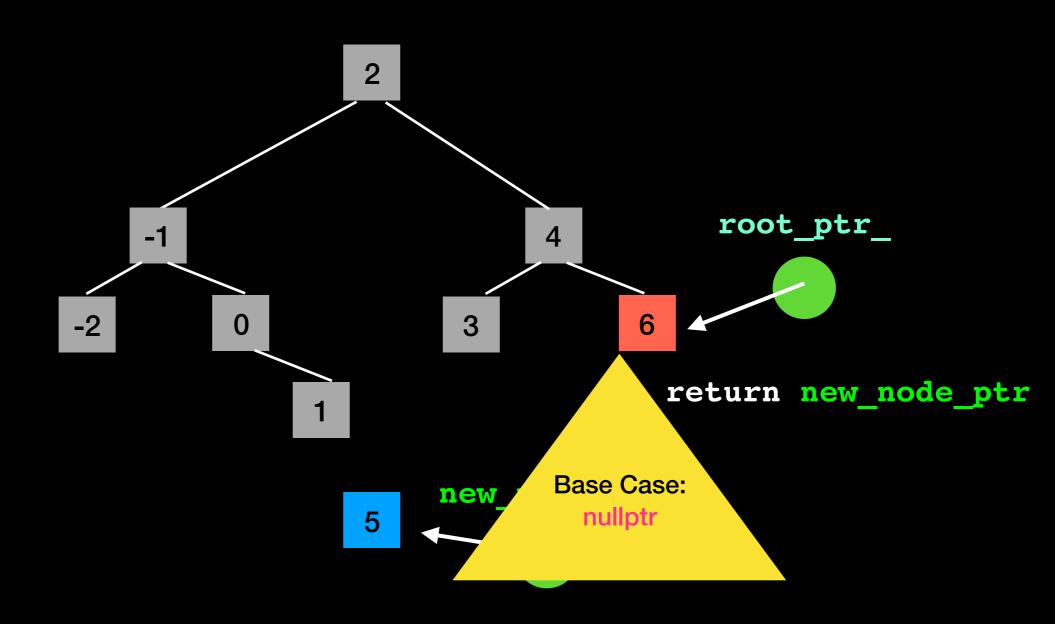




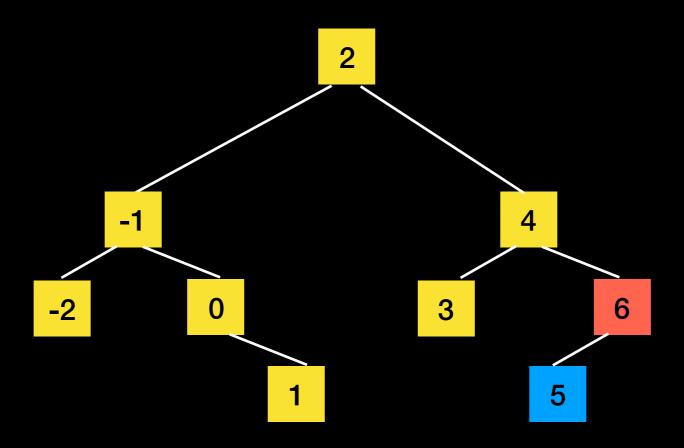




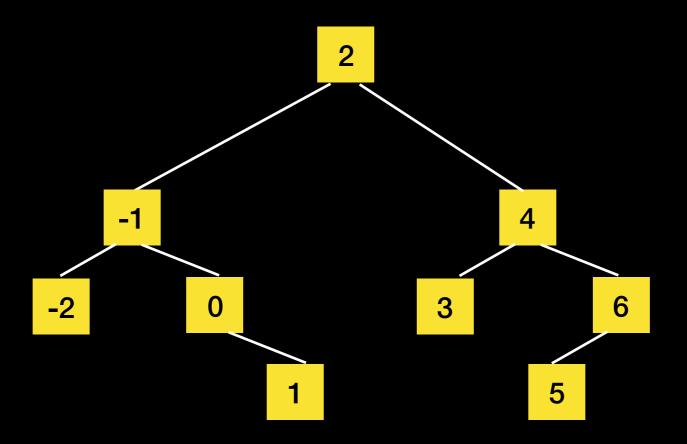
#### placeNode(root\_ptr\_, new\_node\_ptr);



### placeNode(root\_ptr\_, new\_node\_ptr);



### placeNode(root\_ptr\_, new\_node\_ptr);



## add helper function

```
template<class T>
auto BST<T>::placeNode(std::shared ptr<BinaryNode<T>> subtree ptr,
                              std::shared ptr<BinaryNode<T>> new node ptr)
   if (subtree ptr == nullptr)
      return new node ptr; //base case
   else
      if (subtree ptr->getItem() > new node ptr->getItem())
         subtree ptr->setLeftChildPtr(placeNode(subtree ptr->getLeftChildPtr(),
                                                                   new node ptr));
      else
         subtree ptr->setRightChildPtr(placeNode(subtree ptr->getRightChildPtr(),
                                                                  new node ptr));
      return subtree ptr;
      // end if
   // end placeNode
```

#### remove

```
template < class T>
bool BST < T>::remove(const T& target)
{
    bool is_successful = false;
    // call may change is_successful
    root_ptr_ = removeValue(root_ptr_, target, is_successful);
    return is_successful;
} // end remove
```

Safe programming: the public method does not take pointer parameter.
Only protected/private methods have access to pointers and may modify tree structure

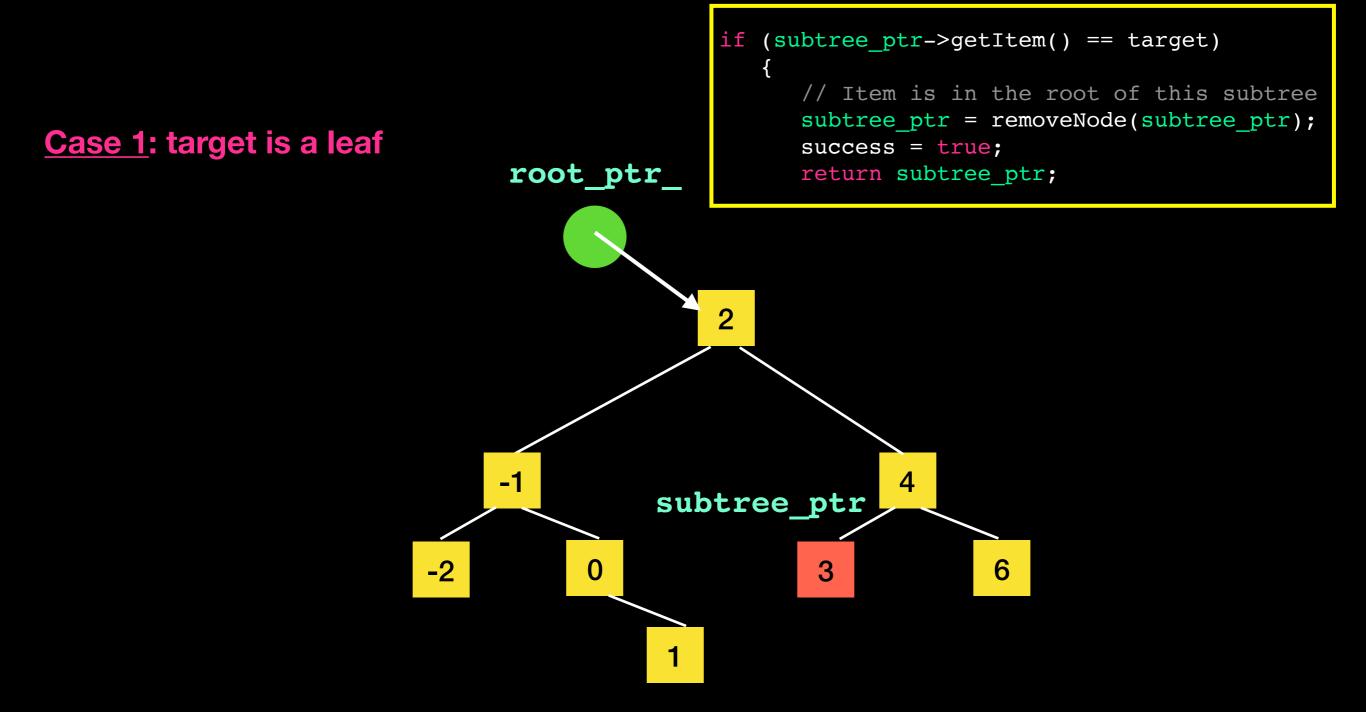
# remove helper function

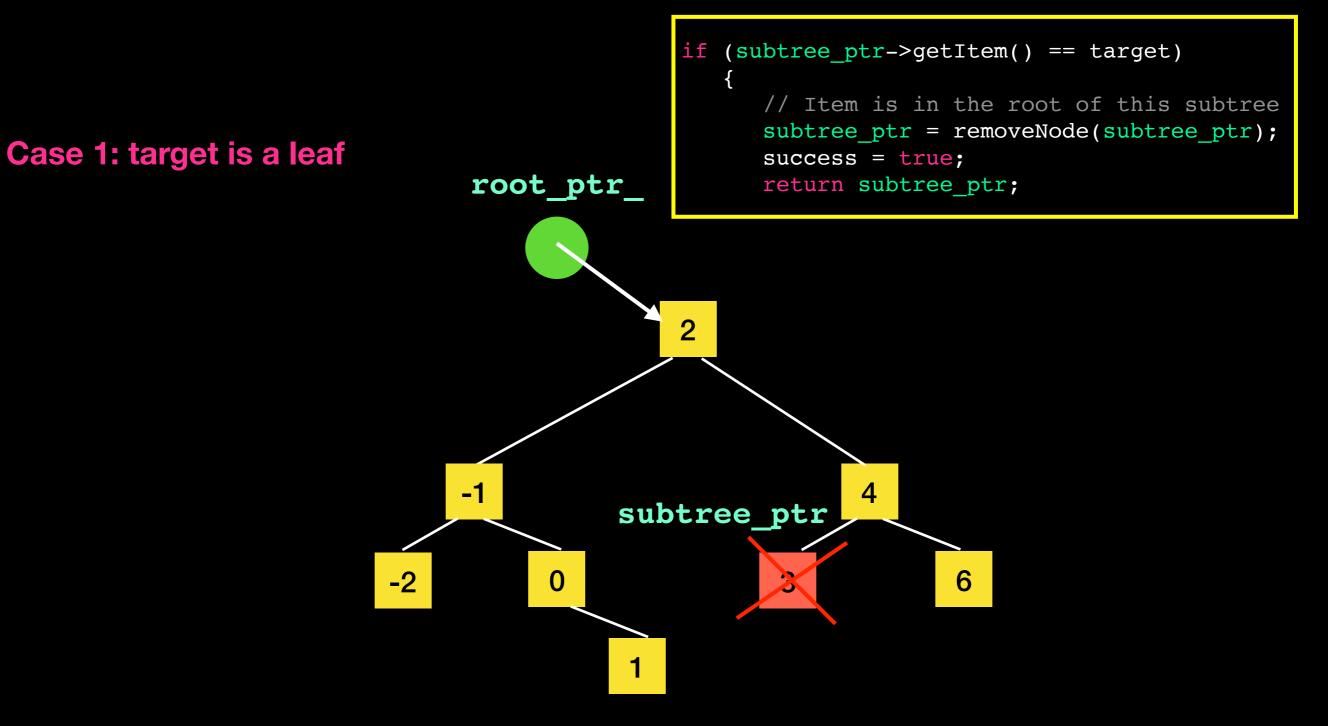
Looks for the value to remove

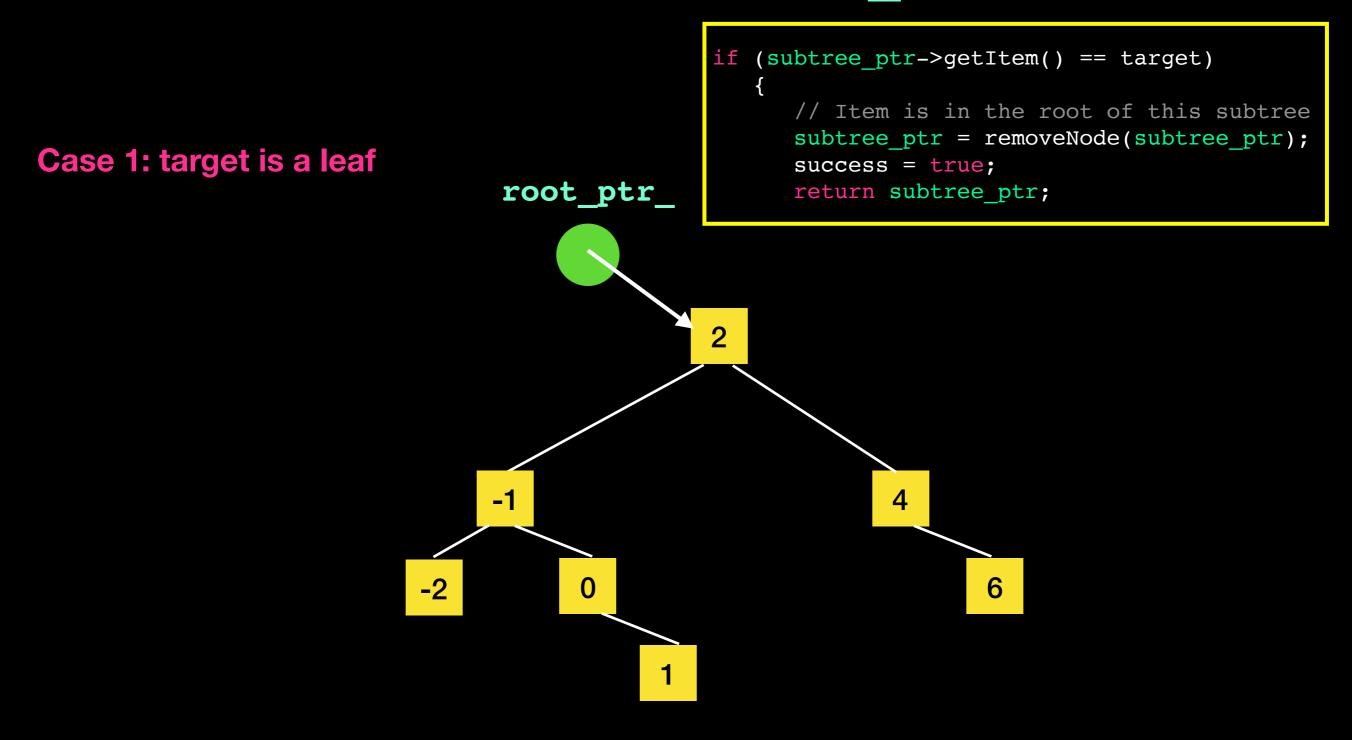
```
template<class T>
auto BST<T>::removeValue(std::shared ptr<BinaryNode<T>>
      subtree ptr, const T target, bool& success)
   if (subtree ptr == nullptr)
                                                target not in tree
      // Not found here
      success = false;
      return subtree ptr;
                                                            Found target now
      (subtree ptr->getItem() == target)
                                                            remove the node
      // Item is in the root of this subtree
      subtree ptr = removeNode(subtree ptr);
      success = true;
      return subtree ptr;
```

## remove helper function cont.ed

```
else
                                                    Search for target in
   if (subtree ptr->getItem() > target)
                                                        left subtree
      // Search the left subtree
      subtree ptr->setLeftChildPtr(removeValue(subtree ptr
                                 ->getLeftChildPtr(), target, success));
                                                      Search for target in
   else
                                                         right subtree
      // Search the right subtree
      subtree ptr->setRightChildPtr(removeValue(subtree ptr
                                 ->getRightChildPtr(), target, success));
   return subtree ptr;
   // end if
   end removeValue
```

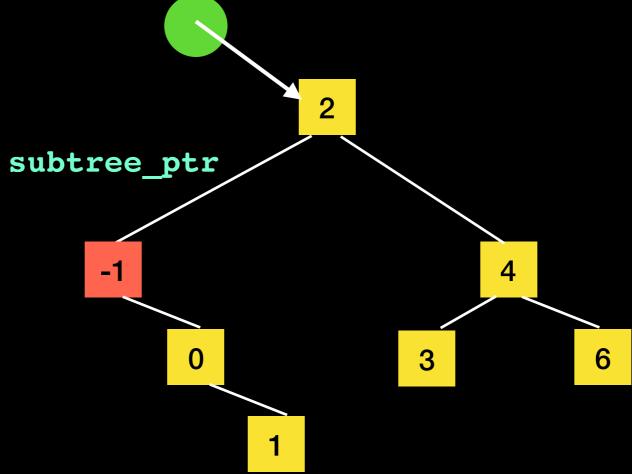






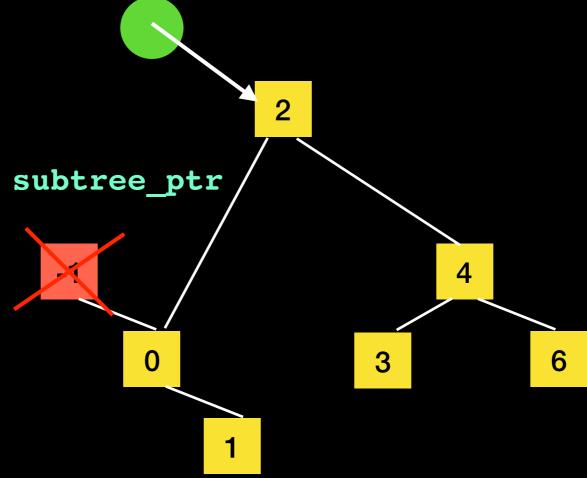
Case 2: target has 1 child Left and right case are symmetric

if (subtree\_ptr->getItem() == target)
{
 // Item is in the root of this subtree
 subtree\_ptr = removeNode(subtree\_ptr);
 success = true;
 return subtree\_ptr;



Case 2: target has 1 child Left and right case are symmetric

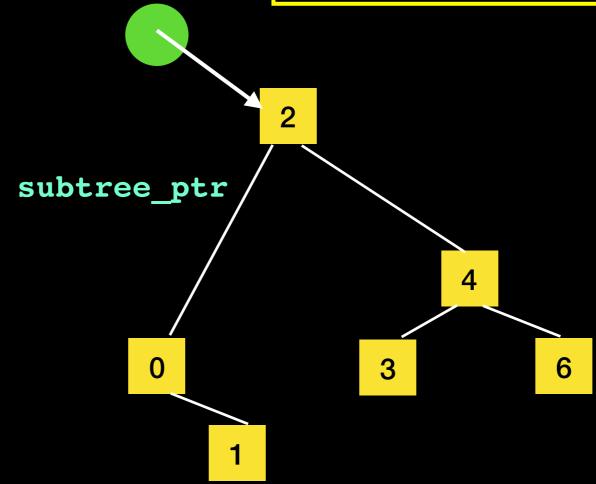
if (subtree\_ptr->getItem() == target)
{
 // Item is in the root of this subtree
 subtree\_ptr = removeNode(subtree\_ptr);
 success = true;
 return subtree\_ptr;



Case 2: target has 1 child Left and right case are symmetric

root\_ptr\_

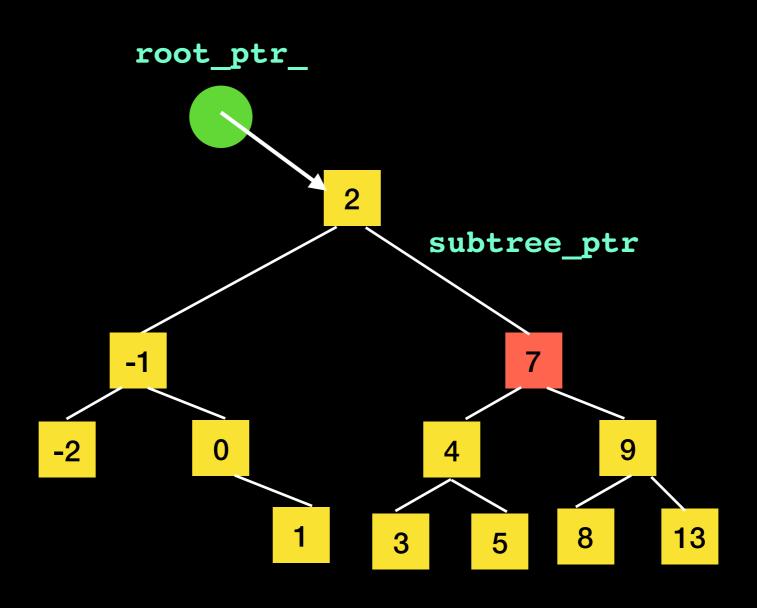
```
if (subtree_ptr->getItem() == target)
{
    // Item is in the root of this subtree
    subtree_ptr = removeNode(subtree_ptr);
    success = true;
    return subtree_ptr;
```

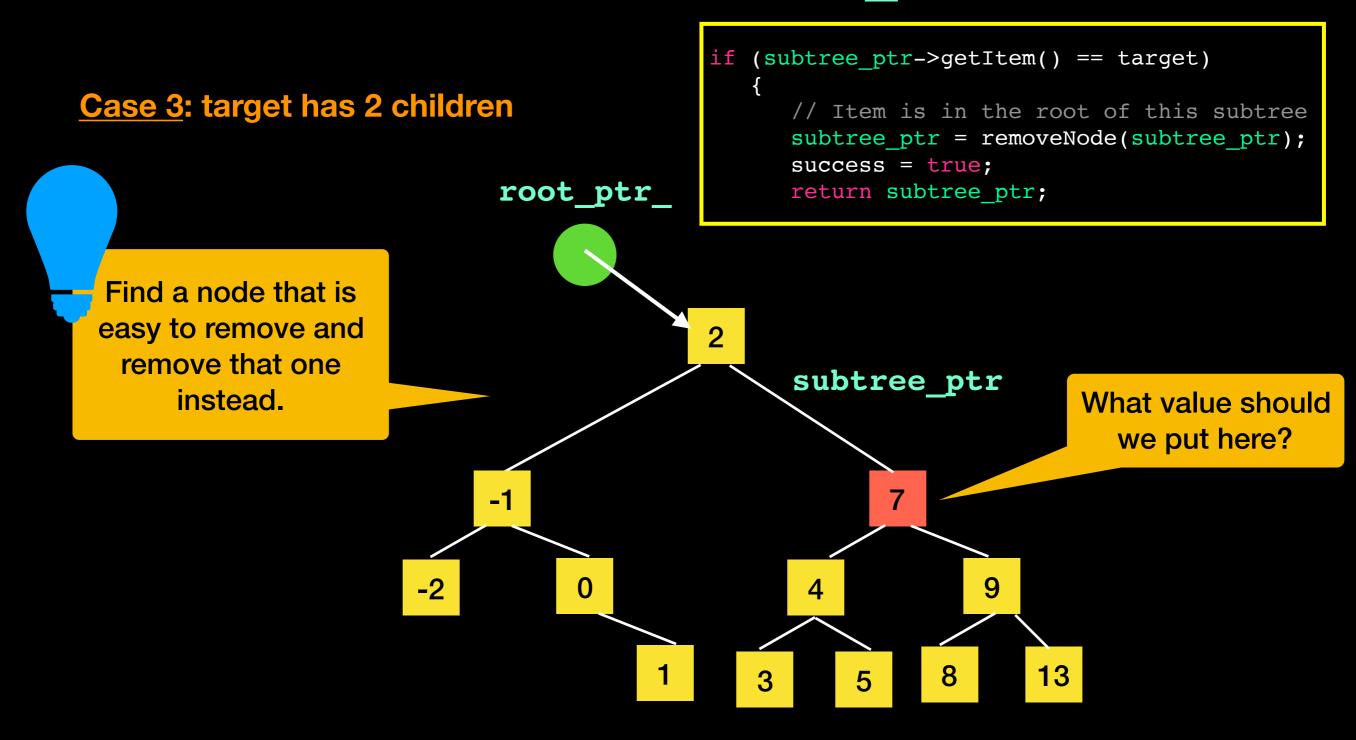


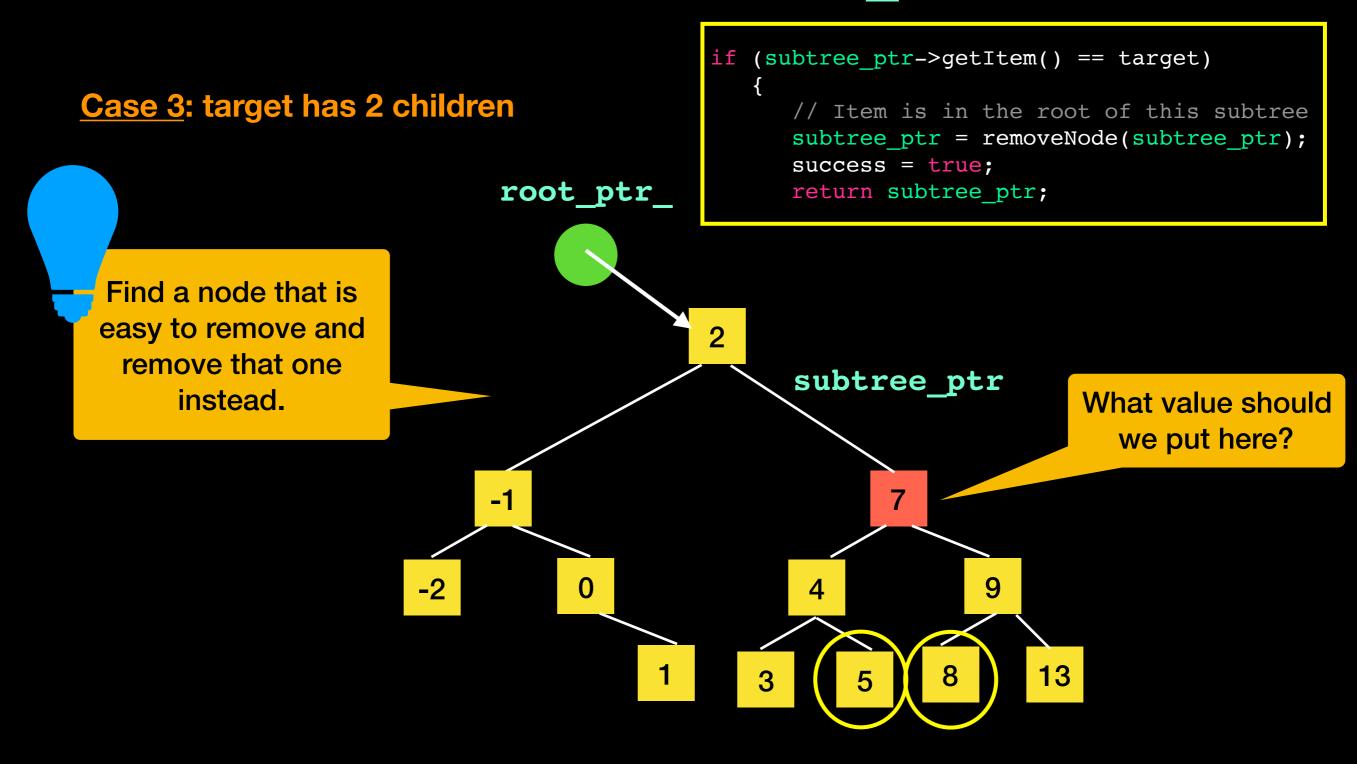
### Lecture Activity

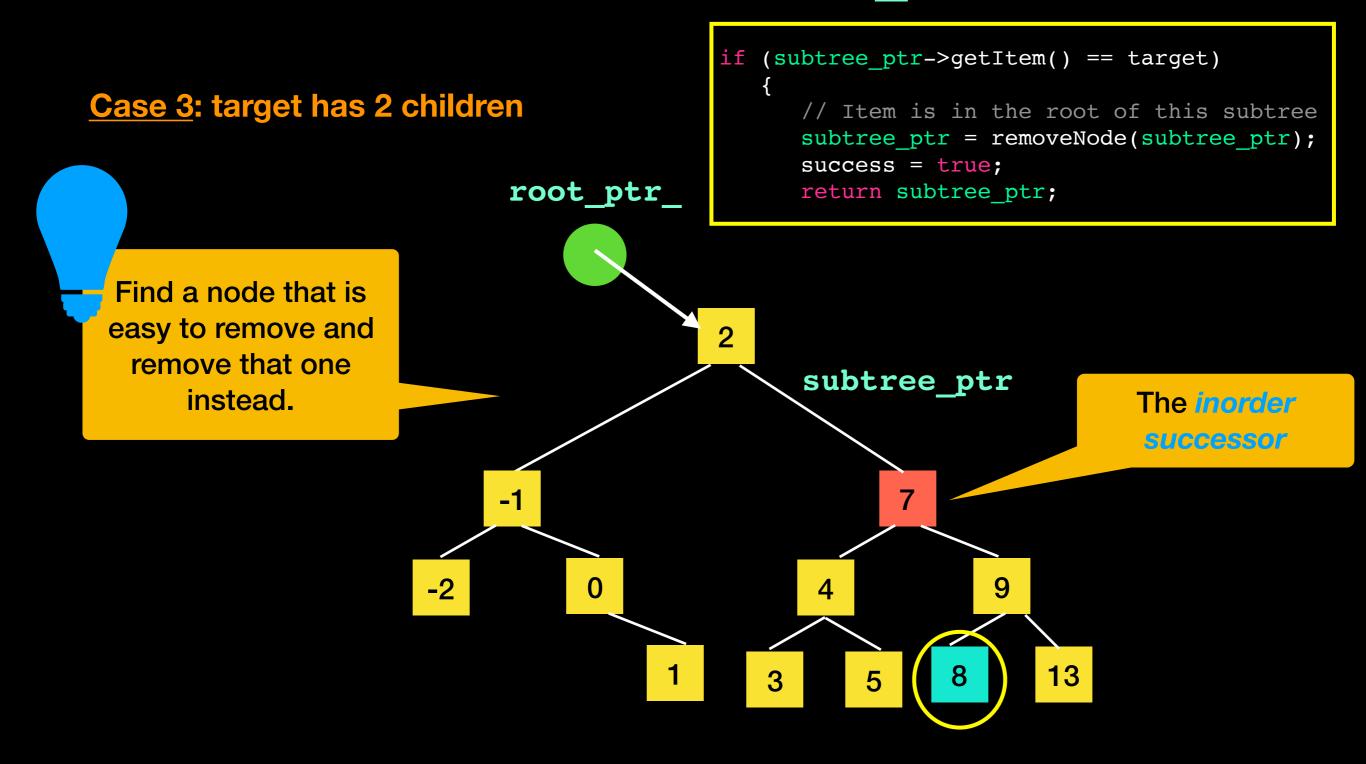
#### How would you remove node 7?

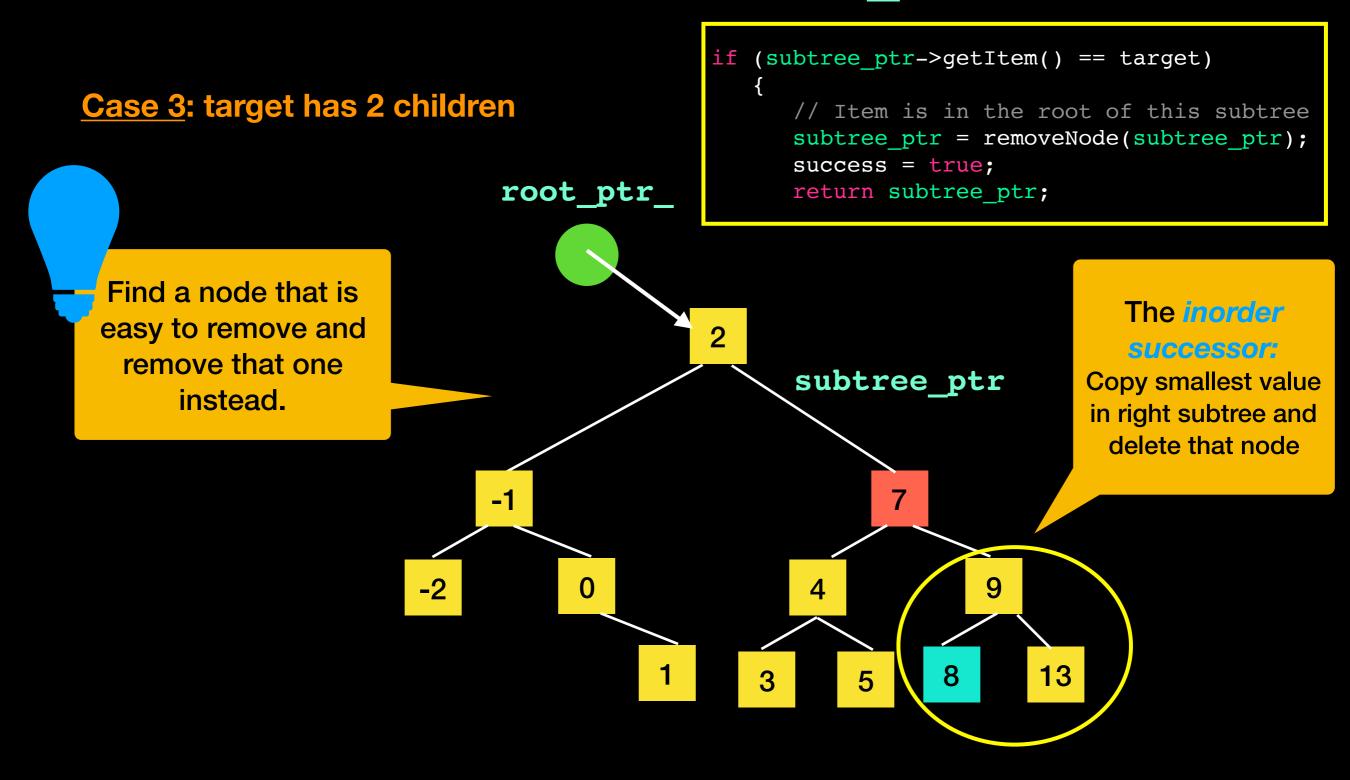
Case 3: target has 2 children

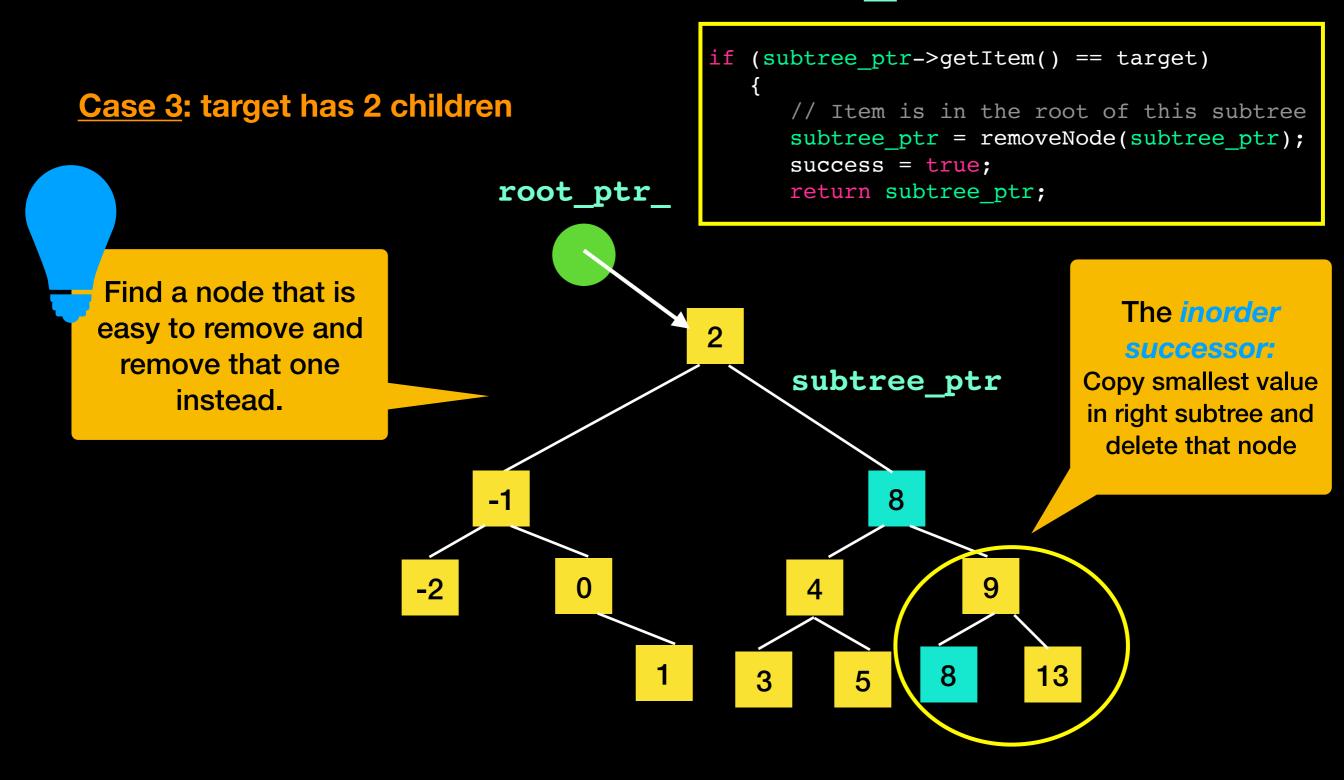


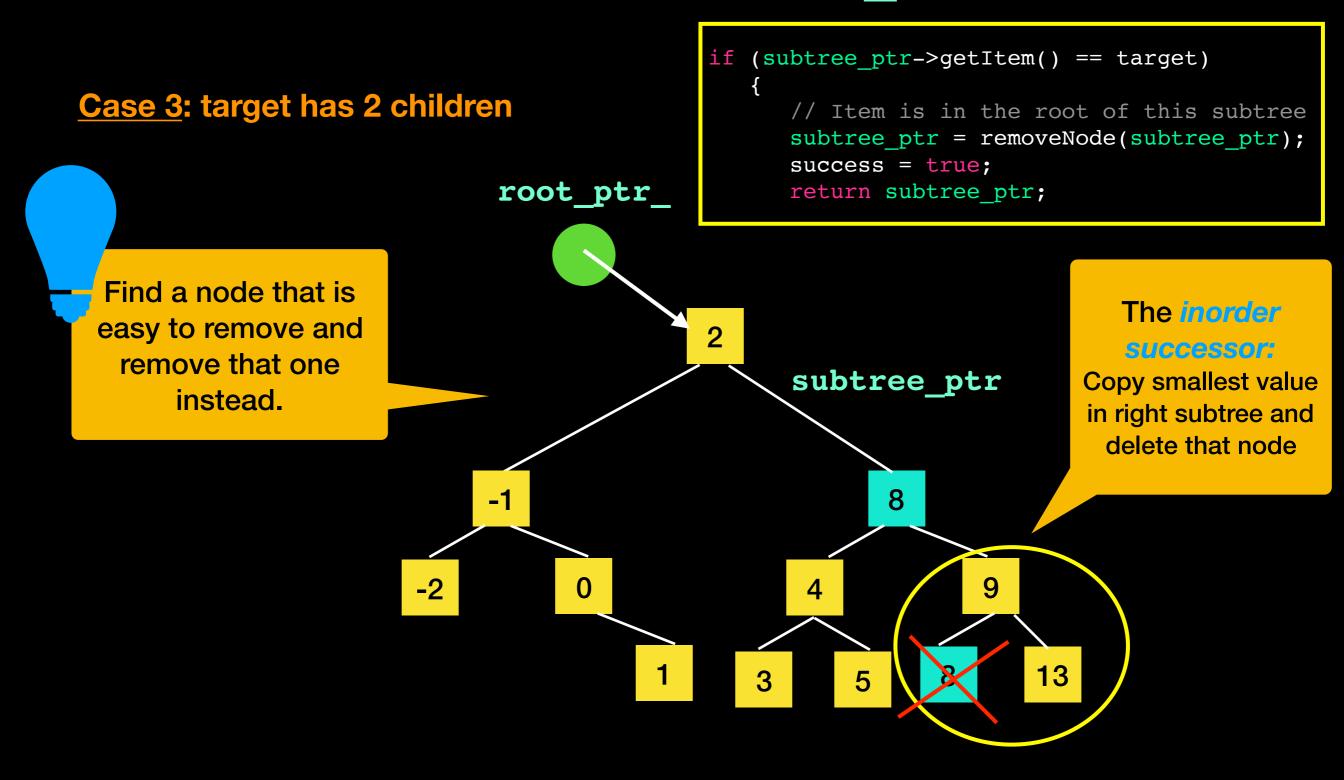










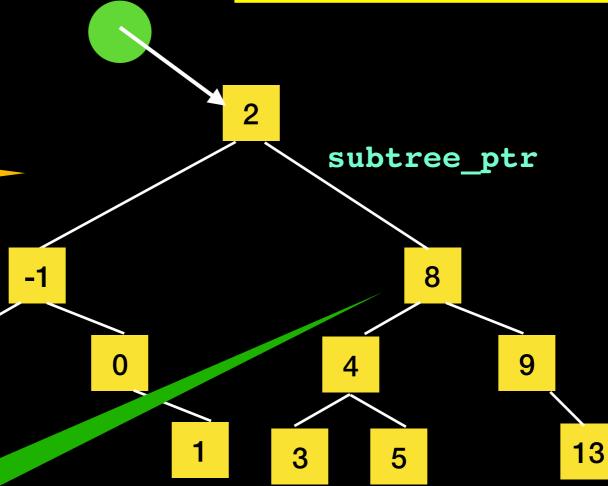


root\_ptr\_

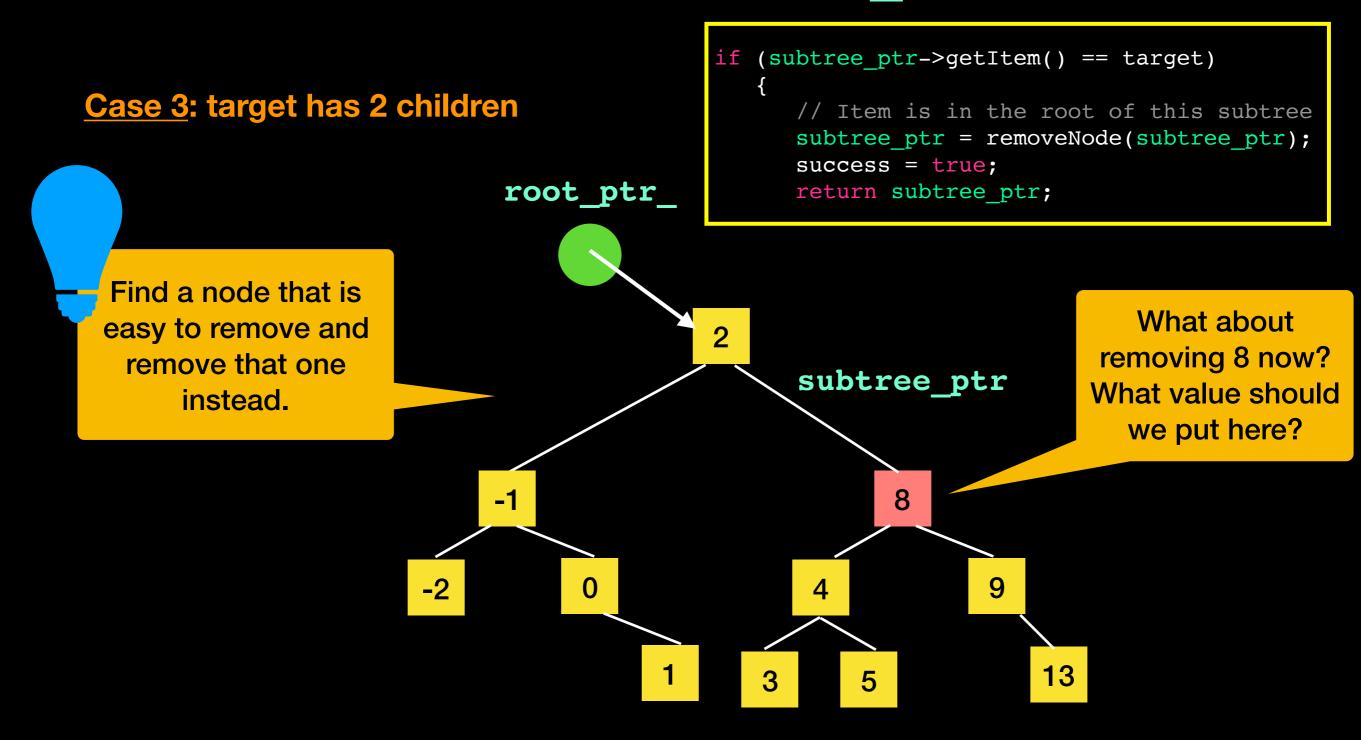
#### Case 3: target has 2 children

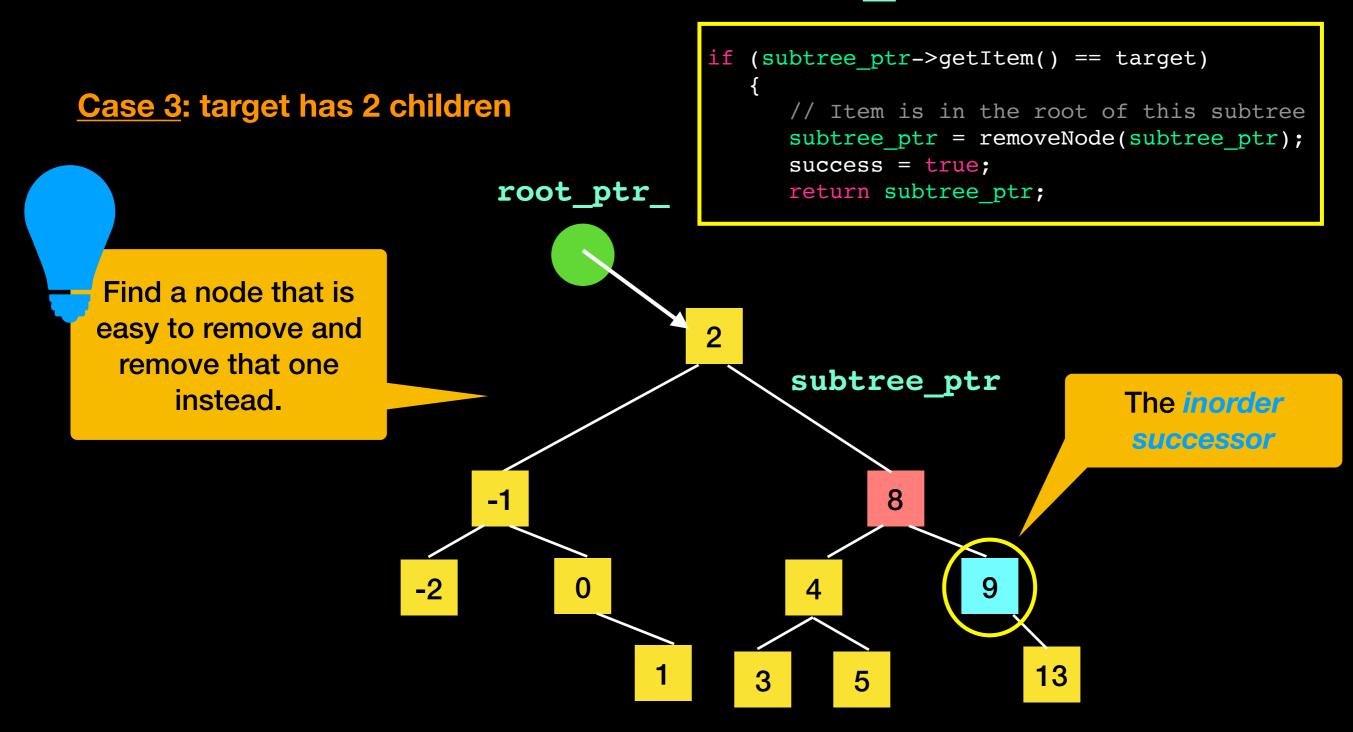
Find a node that is easy to remove and remove that one instead.

if (subtree\_ptr->getItem() == target)
{
 // Item is in the root of this subtree
 subtree\_ptr = removeNode(subtree\_ptr);
 success = true;
 return subtree\_ptr;



This operation will actually "reorganize" the tree





#### removeNode(node\_ptr);

```
template<class T>
auto BST<T>::removeNode(std::shared ptr<BinaryNode<T>> node ptr)
   // Case 1) Node is a leaf - it is deleted
                                                              Node is leaf
   if (node ptr->isLeaf())
      node ptr.reset();
      return node ptr; // delete and return nullptr
                                                                         Node has 1 child
   // Case 2) Node has one child - parent adopts child
   else if (node ptr->getLeftChildPtr() == nullptr) // Has rightChild only
      return node ptr->getRightChildPtr();
   else if (node ptr->getRightChildPtr() == nullptr) // Has left child only
      return node ptr->getLeftChildPtr();
                                                                    Will find leftmost leaf in right
                                                                       subtree, save value in
                                      Node has 2 children
     Case 3) Node has two children:
                                                                   new node value and delete
   else
      T new node value;
      node ptr->setRightChildPtr(removeLeftmostNode(node ptr->getRightChildPtr(),
                                                                        new node value));
      node ptr->setItem(new node value);
      return node ptr;
                                               Safe Programming:
                                           reference parameter is local to
      // end if
                                             the private calling function
   // end removeNode
```



### Implement this at home!!!

```
find(const T& item) const
{
    //try it at home!!!!
}
```

### Traversals

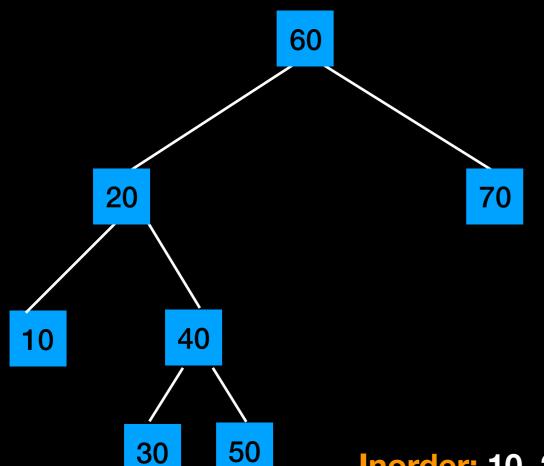
Let's focus on the traversal for now, we will find out what Visitor does next

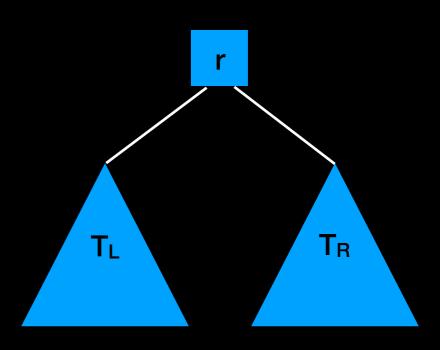
```
template<class T>
void BST<T>::preorderTraverse(Visitor<T>& visit) const
   preorder(visit, root ptr );
   // end preorderTraverse
template<class T>
void BST<T>::inorderTraverse(Visitor<T>& visit) const
   inorder(visit, root ptr );
   // end inorderTraverse
template<class T>
void BST<T>::postorderTraverse(Visitor<T>& visit) const
   postorder(visit, root ptr );
   // end postorderTraverse
```

```
Visit (retrieve, print, modify ...) every node in the tree
Inorder Traversal:

if (T is not empty) //implicit base case
```

```
if (T is not empty) //implicit base case {  traverse \ T_L \\ visit \ the \ root \ r \\ traverse \ T_R \\ \}
```



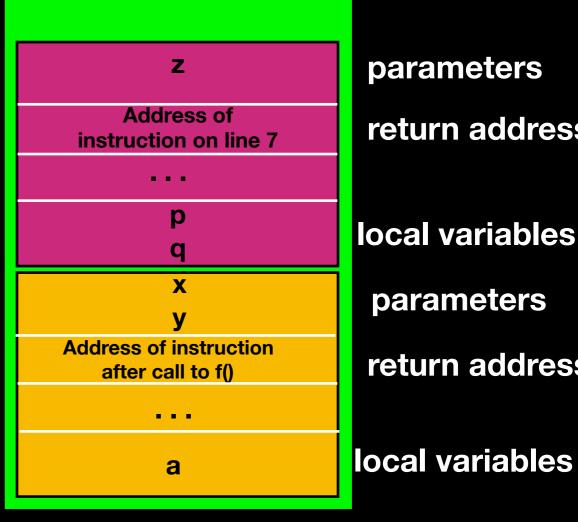


Inorder: 10, 20, 30, 40, 50, 60, 70

### inorderTraverse Helper Function

# Recall: Program Stack

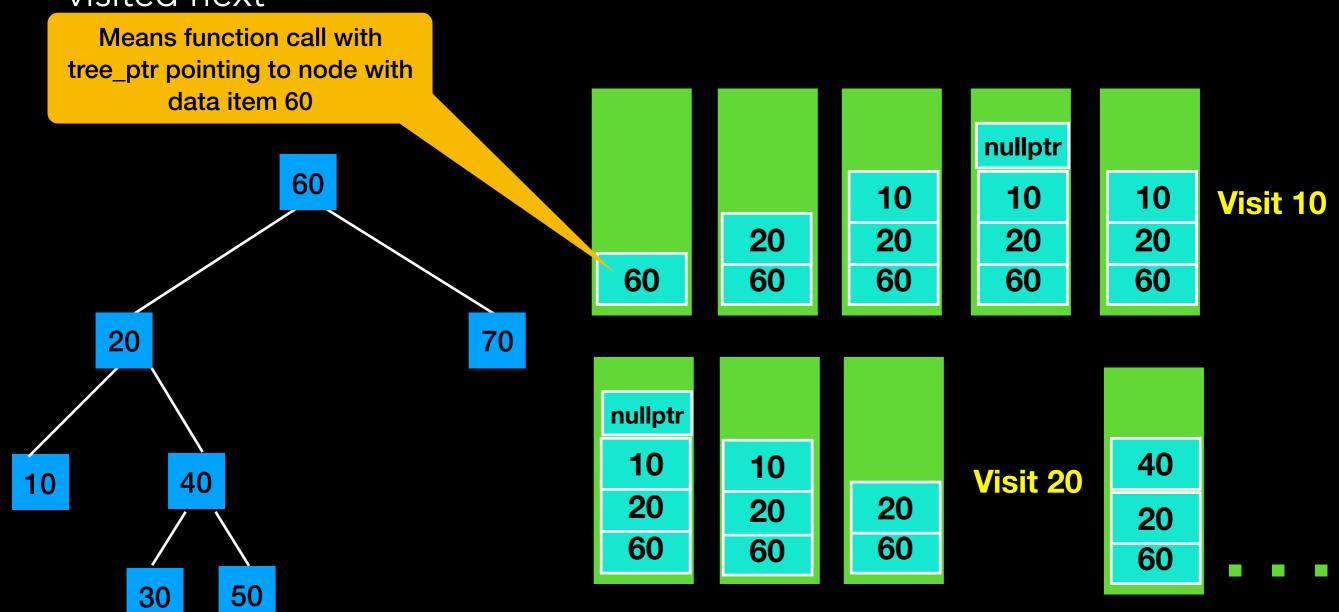
```
1
   void f(int x, int y)
2
3
     int a;
4
    // stuff here
5
   if(a<13)
6
        a = g(a);
7
   // stuff here
                       Stack Frame
8
                          for g()
9
   int g(int z)
10
11
     int p ,q;
                      Stack Frame
12 // stuff here
                         for f()
13 return q;
\overline{14}
```



parameters return address local variables parameters return address

### Recursive Traversal

In recursive solution program stack keeps track of what node must be visited next



## Recursive Traversal

#### With recursion:

- program stack implicitly finds node traversal must visit next
- If traversal backs up to node *d* from right subtree it backs up further to *d*'s parent as a consequence of the recursive program execution

### Non-recursive Traversal

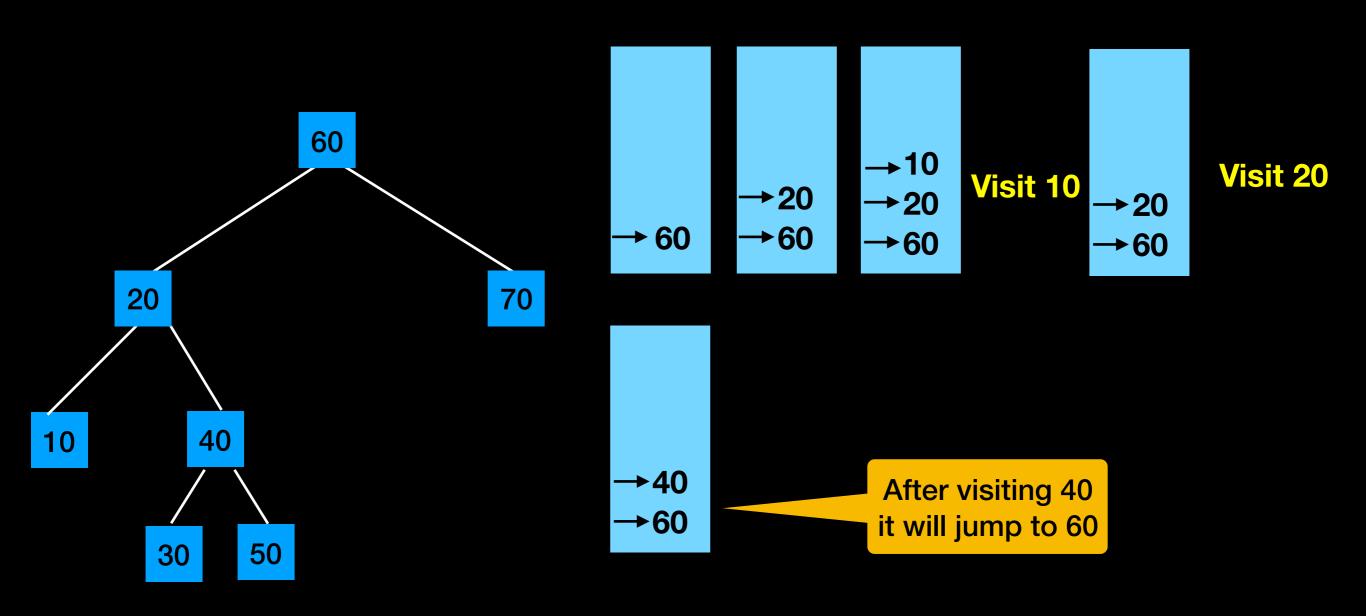
Optimize: Implement iterative approach that maintains an explicit stack to keep track of nodes that must be visited

Place pointer to node on stack **only** before traversing it's left subtree but **NOT** before traversing right subtree

This will also save some "steps" that were unnecessary but implicit in recursive implementation

## Non-recursive Traversal

Iterative solution explicitly maintains a stack of pointers to nodes to keep track of what node must be visited next



## Non-recursive Traversal

```
template<class T>
void BST<T>::inorder(Visitor<T>& visit) const
    std::stack<T> node stack;
    std::shared ptr<BinaryNode<T>> current_ptr = root ptr ;
    bool done = false;
    while(!done)
        if(current ptr != nullptr)
            node stack.push(current_ptr);
            //traverse left subtree
            current ptr = current ptr->getLeftChildPtr();
```

## Non-recursive Traversal cont.

```
//backtrack from empt subtree and visit the node at top of
  //stack, but if stack is empty traversal is completed
  else{
      done = node stack.isEmpty();
       if(!done)
           current_ptr = node stack.top();
           visit(current_ptr->getItem());
           node stack.pop();
           //traverse right subtree of node just visited
           current ptr = current ptr->getRightChildPtr();
end inorder
```

#### Traversals

The last cool trick for you this semester

```
Looking for behavior
```

```
template<class T>
void BST<T>::preorderTraverse(Visitor<T>& visit) const
   preorder(visit, root ptr );
  // end preorderTraverse
template<class T>
void BST<T>::inorderTraverse(Visitor<T>& visit) const
   inorder(visit, root_ptr_);
   // end inorderTraverse
template<class T>
void BST<T>::postorderTraverse(Visitor<T>& visit) const
   postorder(visit, root ptr );
   // end postorderTraverse
```

## Functors

Objects that by overloading operator() can be "called" like a function

```
#ifndef Visitor_hpp
#define Visitor hpp
                                       POLYMORPHISM!
#include <string>
template<class T>
class Visitor
public:
    virtual void operator()(T&) = 0;
    virtual void operator()(T&, T&) = 0;
};
#endif /* Visitor_hpp */
```

```
#ifndef StringPrinter hpp
#define StringPrinter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
class StringPrinter: public Visitor<std::string>
public:
    void operator()(std::string&) override;
    void operator()(std::string&, std::string&) override;
};
#endif /* StringPrinter hpp */
```

```
#include "StringPrinter.hpp"

void StringPrinter::operator()(std::string& x)
{
    std::cout << x << std::endl;
}

void StringPrinter::operator()(std::string& a, std::string& b)
{
    std::cout << a << b << std::endl;
}</pre>
```

```
#ifndef Inverter hpp
#define Inverter hpp
#include "Visitor.hpp"
#include <iostream>
#include <string>
#include <algorithm>
class Inverter: public Visitor<std::string>
public:
    void operator()(std::string&) override;
    void operator()(std::string&, std::string&) override;
};
#endif /* Inverter hpp */
```

```
#include "Inverter.hpp"
void Inverter::operator()(std::string& x)
    std::reverse(x.begin(), x.end());
    std::cout << x << std::endl;</pre>
void Inverter::operator()(std::string& a, std::string& b)
{
    a.swap(b);
    std::cout << a << b << std::endl;</pre>
```

# Traversal with Functor parameter

```
template < class T>
void BST < T>::inorder(Visitor < T>& visit,
    std::shared_ptr < BinaryNode < T>> tree_ptr) const

{
    if (tree_ptr != nullptr)
    {
        inorder(visit, tree_ptr->getLeftChildPtr());
        T the_item = tree_ptr->getItem();
        visit(the_item);
        inorder(visit, tree_ptr->getRightChildPtr());
    } // end if
} // end inorder
```

```
int main() {
    std::string a string = "a string";
    std::string anoter string = "o string";
    BST<std::string> a_tree(a_string);
    a tree.add(anoter string);
    StringPrinter p;
    Inverter i;
    a tree.inorderTraverse(p);
    std::cout << std::endl;</pre>
    a tree.inorderTraverse(i);
    return 0;
```

```
root_ptr_

"a string"

"o string"
```

```
a string
o string
gnirts a
gnirts o
Program ended with exit code: 0
```

```
int main() {
    std::string a string = "a string";
    std::string anoter string = "o string";
    BST<std::string> a_tree(a_string);
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    std::cout << std::endl;</pre>
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```

```
root ptr
      "a string"
                 "o string"
TA-DAH!
```

```
a string
o string
gnirts a
gnirts o
Program ended with exit code: 0
```