

Dummy	GPA	GRE	y
1	0.9	1	1
1	0.9	0.875	1
1	0.7	0.75	-1
1	0.6	0.875	-1

$$\vec{w} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{aligned} \nabla_E(\vec{w}) &= -\frac{1}{5} \sum_{k=1}^5 \frac{y_k \vec{x}_k}{1 + e^{y_k \vec{w}^T \vec{x}_k}} \\ &= -\frac{1}{5} \left(\frac{1 \cdot \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}}{1 + e^{1 \cdot (0 \ 0 \ 0) \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}}} + \frac{1 \cdot \begin{bmatrix} 0.9 \\ 0.875 \\ 1 \end{bmatrix}}{1 + e^{1 \cdot (0 \ 0 \ 0) \begin{bmatrix} 0.9 \\ 0.875 \\ 1 \end{bmatrix}}} \right. \\ &\quad \left. + \frac{-1 \cdot \begin{bmatrix} 0.7 \\ 0.75 \\ 1 \end{bmatrix}}{1 + e^{0}} + \frac{-1 \cdot \begin{bmatrix} 0.6 \\ 0.875 \\ 1 \end{bmatrix}}{1 + e^0} \right) \\ &= -\frac{1}{5} \left(\begin{bmatrix} 0.5 \\ 0.5 \\ 0.5 \end{bmatrix} + \begin{bmatrix} 0.5 \\ 0.475 \\ 0.5 \end{bmatrix} + \begin{bmatrix} 0.5 \\ 0.475 \\ 0.4375 \end{bmatrix} - \begin{bmatrix} 0.5 \\ 0.375 \\ 0.375 \end{bmatrix} \right. \\ &\quad \left. - \begin{bmatrix} 0.5 \\ 0.3 \\ 0.4375 \end{bmatrix} \right) \\ &= -\frac{1}{5} \begin{bmatrix} 0.5 \\ 0.75 \\ 0.625 \end{bmatrix} = \begin{bmatrix} -0.1 \\ -0.15 \\ -0.125 \end{bmatrix} \end{aligned}$$

$$\vec{w} \leftarrow \vec{w} - K \nabla_E(\vec{w}) \quad , \quad K = 2$$

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} - 2 \begin{bmatrix} -0.1 \\ -0.15 \\ -0.125 \end{bmatrix} = \begin{bmatrix} 0.2 \\ 0.3 \\ 0.25 \end{bmatrix}$$

After the first iteration,

$$\vec{w} = \begin{bmatrix} 0.2 \\ 0.3 \\ 0.25 \end{bmatrix}$$