

Assignment 3 Naive Bayes

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```
#select, rename and clean the data
bank_data <- bank.df[, c(10, 13, 14)]
bank_data$Online <- as.factor(bank_data$Online)
bank_data$CC <- as.factor(bank_data$CreditCard)
bank_data$Loan <- as.factor(bank_data$Personal.Loan)
bank_data <- bank_data[, c(-1, -3)]

#Data partition with training: validation = 6:4
set.seed(123)
index_train <- createDataPartition(bank_data$Loan,
                                     p = 0.6,
                                     list = FALSE)
train_data <- bank_data[index_train, ]
validate_data <- bank_data[-index_train, ]
```

A. Pivot table of Online, CC and Loan for training data

```
#molted <- melt(train_data, id = c("Online"))
#tibble(molted)
#x.cast <- dcast(molted, Online~variable, fun.aggregate = length)
#x.cast
```

```
xtab <- ftable(xtabs(~CC+Loan+Online, data = train_data))
xtab
```

```
##      Online    0    1
## CC Loan
## 0  0          791 1144
##   1           79  125
## 1  0          310  467
##   1           33   51
```

B. $P(\text{Loan}=1 \mid \text{CC}=1, \text{Online}=1) = 51/(467+51) = 9.85\%$

C. Create two separate pivot tables

```
melt.x1 <- melt(train_data, id = "Loan", variable = "Online")
cast.x1 <- dcast(melt.x1, Loan~Online, fun.aggregate = length)
cast.x1
```

```
##   Loan Online    CC
## 1     0   2712 2712
## 2     1    288  288
```

```
ftable(train_data[, c(3,1)]) #Loan as row vs Online as column
```

```
##      Online    0    1
```

```
## Loan
## 0      1101 1611
## 1      112  176
ftable(train_data[, c(3,2)]) #Loan as row vs CC as column
```

```
##      CC    0    1
## Loan
## 0      1935  777
## 1      204   84
```

D. Compute $P(A | B)$

```
ftable(train_data[, c(2,3)]) #CC | Loan
```

```
##      Loan    0    1
## CC
## 0      1935  204
## 1      777   84
```

```
ftable(train_data[, c(1,3)]) #Online | Loan
```

```
##      Loan    0    1
## Online
## 0      1101  112
## 1      1611  176
```

```
ftable(train_data[, 3]) #Loan distribution
```

```
##      0    1
##
## 2712 288
```

- i. $P(CC = 1 | Loan = 1) = 84 / (204 + 84) = 0.2917$
- ii. $P(Online = 1 | Loan = 1) = 176 / (176 + 112) = 0.6111$
- iii. $P(Loan = 1) = 288 / (288 + 2712) = 0.096$
- iv. $P(CC = 1 | Loan = 0) = 777 / (1935 + 777) = 0.2865$
- v. $P(Online = 1 | Loan = 0) = 1611 / (1611 + 1101) = 0.5940$
- vi. $P(Loan = 0) = 2712 / (2712 + 288) = 0.904$

E. Naive Bayes probability $P(Loan = 1 | CC = 1, Online = 1) = P(CC = 1 | Loan = 1)P(Online = 1 | Loan = 1)P(Loan = 1) / (P(CC = 1 | Loan = 1)P(Online = 1 | Loan = 1)P(Loan = 1) + P(CC = 1 | Loan = 0)P(Online = 1 | Loan = 0)P(Loan = 0)) = 0.2971 \cdot 0.6111 \cdot 0.096 / (0.2971 \cdot 0.6111 \cdot 0.096 + 0.2865 \cdot 0.5940 \cdot 0.904) = 0.1018 = 10.18\%$

F. Naive Bayes result of 10.18% is higher than pivot table calculation of 9.84%

G. Run NB

```
result <- naiveBayes(Loan~Online+CC, data = train_data)
result
```

```
##
## Naive Bayes Classifier for Discrete Predictors
##
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
##
## A-priori probabilities:
## Y
##      0      1
```

```

## 0.904 0.096
##
## Conditional probabilities:
##   Online
## Y      0      1
## 0 0.4059735 0.5940265
## 1 0.3888889 0.6111111
##
##   CC
## Y      0      1
## 0 0.7134956 0.2865044
## 1 0.7083333 0.2916667

```

The entries needed for NB calculation: $P(\text{loan})$ 0.904 and 0.096 $P(\text{Loan} = 0 \mid \text{Online} = 1) = 0.5940$ $P(\text{Loan} = 1 \mid \text{Online} = 1) = 0.6111$ $P(\text{Loan} = 0 \mid \text{CC} = 1) = 0.2865$ $P(\text{Loan} = 1 \mid \text{CC} = 1) = 0.2917$